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Supplemental Data

# Adjusting for Heritable Covariates Can Bias Effect Estimates in Genome-Wide Association Studies

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## Figure S1. Illustrative examples of direct acyclic graphs.

*Y* is the outcome, *C* is a potential covariate, *g* is a predictor of interest, and *U* is an unmeasured variable that can results or depends on *Y*, *C* and *g*.



#### Figure S2. Statistical power in adjusted analysis

Statistical power when the genetic variant is differentially associated with two correlated phenotypes. Two traits *Y* and *C* are simulated with correlation  $\rho_{CY}$  varying from 0 to 0.9. A genetic variant *g* has a positive effect  $\beta_Y$  on *Y* and explains 0.015% (left panel) or 0.04% (right panel) of its variance; we vary the effect of *g* on *C* between  $-\beta_Y$  and  $\beta_Y$ . a) We compared the power at  $5x10^{-8}$  significance level to detect the g/Y association between the marginal model (unadjusted for *C*, red line) to the adjusted model (light grey to black plain line). b) We plotted the power to detect the marginal g/C association (light blue to dark blue plain line) while varying  $\alpha$ , the significance level.



#### Figure S3. Effect of the adjustment on estimate

Upper panel presents  $\hat{\beta}_Y$  the estimated effect of *G* on *Y* in the unadjusted model as a function of  $\hat{\beta}_C$  the estimated effect of *G* on *C* across 1,000 replicates of 100,000 subjects (grey dots) and the regression line (black) when the correlation between *C* and *Y* is 0.5,  $\beta_C = 0$  and  $\beta_Y = 0$  (a) or  $\beta_Y = 0.3$  (b). Upper plots also display  $\Delta_{\hat{\beta}_Y} = \hat{\beta}_Y - \hat{\beta}_{Yadj}$  the change in estimates before and after the adjustment for *C* (blue dots). This change corresponds on average to the deviation of  $\hat{\beta}_Y$  from  $\beta_Y$ . Bottom panel shows the correlation between  $\hat{\beta}_C$  and the *p*-values of  $\hat{\beta}_{Yadj}$ , the estimate of *G* on *Y* after adjustment for *C* for the same replicates.



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# Figure S4. Opposite genetic effects between BMI and WHR/WC

Log<sub>10</sub> p-value of the observed proportion of SNP with effects in opposite direction when assuming a binomial distribution with probability 0.5, when filtering out SNPs based on their *p*-value for association with BMI.



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#### Figure S5. QQplot under the null for three corrections.

We generated 10,000 replicates of 1,000 subjects. For each replicates we simulated normally distributed variables *Y*, *C* and *g*, so that *C* and *Y* display a correlation of 0.5 and *g* explained 1% of the variance of *C* but none of *Y*. We derived the inflation factor  $\lambda$  and plotted the observed distribution of *p*-value for tests of association between *Y* and *g* against its expected distribution. We considered a marginal model in the whole sample (black), a model adjusted for the raw values of *C* (grey) or after removing either the true effect of *g* on *C* (blue) or its estimated effect (green), a *C*-specific strata of the marginal model (*C*≥0, dark red dots, and *C*<0, light red), and a two-step procedure proposed by Vansteelandt et al<sup>1</sup> (orange).



### Figure S6. Bias in covariate stratified analysis.

Outcome values (Y) as a function of a continuous predictor (G) in the total sample and in strata defined by a covariates (C). For simplicity all variables, G, C and Y are normally distributed and generated under model from Figure 1B. The plain lines are the regression lines for the association between G and Y. While there is no correlation between Y and G in the whole sample (a), Y and G display a negative correlation in each C strata (b).



SNP <sup>a</sup>	Risk Allele	BMI (pval)	T2D (pval)	T2D <sub>adjBMI</sub> (pval)
rs2568958	А	3.77 <i>(1.2x10<sup>-11</sup>)</i>	0.0253 <i>(0.038)</i>	0.0170 (0.15)
rs10913469	С	3.36 <i>(6.2x10<sup>-8</sup>)</i>	-0.0044 (0.87)	-0.0177 (0.27)
rs7561317	G	6.12 <i>(4.2x10<sup>-17</sup>)</i>	0.0212 (0.22)	0.0000 (0.9)
rs7647305	С	4.42 (7.2x10 <sup>-11</sup> )	0.0334 (0.036)	0.0128 (0.35)
rs2844479	Т	1.38 (0.003)	-0.0223 (0.11)	-0.0315 (0.028)
rs6265	G	4.58 (5.1x10 <sup>-10</sup> )	-0.0088 (0.64)	-0.0269 <i>(0.12)</i>
rs925946	Т	3.85 <i>(8.5x10<sup>-10</sup>)</i>	0.0170 (0.15)	0.0043 (0.73)
rs7138803	А	3.28 <i>(1.2x10<sup>-7</sup>)</i>	0.0453 (0.00023)	0.0334 <i>(0.009)</i>
rs7498665	G	3.63 <i>(3.2x10<sup>-10</sup>)</i>	0.0212 (0.069)	0.0128 (0.25)
rs6499640	А	5.26 <i>(4.0x10<sup>-13</sup>)</i>	0.0294 (0.027)	0.0086 (0.48)
rs8050136	А	8.04 <i>(1.1x10<sup>-47</sup>)</i>	0.0531 <i>(1.6x10<sup>-5</sup>)</i>	0.0212 (0.086)
rs12970134	А	4.38 <i>(1.2x10<sup>-12</sup>)</i>	0.0170 (0.18)	0.0000 (0.91)
rs29941	С	4.18 <i>(7.3x10<sup>-12</sup>)</i>	0.0043 (0.7)	0.0000 (0.96)

Table S1. Genetic effect estimates and p-value for association with T2D before and after adjustment for BMI

<sup>a</sup>We extracted SNPs found associated with BMI and/or weight and their estimated effect on BMI and T2D before and after adjustment for BMI from Thorleifsson et al<sup>2</sup>.

SNPs with decreased p-value for association with T2D after the adjustment for BMI are indicated in bold.

		Effect on the outcome <sup>a</sup>			Effect on covariate <sup>b</sup>				
Outcome	SNP	trait-increasing allele /alt allele	Unadjusted Pvalue <sup>c</sup>	Adjusted Pvalue	trait-increasing allele /alt allele	pValue	opposite effect		
Glycemic tro	Glycemic traits adjusted for BMI (nositive correlation with the outcome) <sup>3</sup>								
	rs2943645	T / C	1.4 x 10 <sup>-7</sup>	2.3 x 10 <sup>-19</sup>	С / Т	0.0069	х		
	rs10195252	Т/С	4.9 x 10 <sup>-10</sup>	1.3 x 10 <sup>-16</sup>	C / T	0.0093	X		
	rs2126259	T / C	1.5 x 10 <sup>-10</sup>	3.3 x 10 <sup>-13</sup>	Τ/Ο	0.60			
	rs4865796	A/G	2.1 x 10 <sup>-8</sup>	2.2 x 10 <sup>-12</sup>	G / A	5.1 x 10 <sup>-5</sup>	х		
	rs17036328	T/C	1.9 x 10 <sup>-5</sup>	3.6 x 10 <sup>-12</sup>	С / Т	0.019	Х		
Fasting	rs731839	G / A	1.7 x 10 <sup>-8</sup>	5.1 x 10 <sup>-12</sup>	A/G	0.0052	х		
Insulin	rs974801	G / A	2.1 x 10 <sup>-10</sup>	3.3 x 10 <sup>-11</sup>	G / A	0.89			
	rs459193	G / A	6.6 x 10 <sup>-8</sup>	1.2 x 10 <sup>-10</sup>	A/G	0.22	х		
	rs6822892	A/G	3.2 x 10 <sup>-5</sup>	2.6 x 10 <sup>-10</sup>	G / A	0.37	X		
	rs4846565	G / A	2.0 x 10 <sup>-8</sup>	1.8 x 10 <sup>-9</sup>	A/G	0.29	х		
	rs3822072	A/G	1.2 x 10 <sup>-4</sup>	1.8 x 10 <sup>-8</sup>	G / A	0.12	х		
	rs6912327	Т/С	2.8 x 10 <sup>-6</sup>	2.3 x 10 <sup>-8</sup>	C / T	0.066	X		
2hGlu	rs7651090	G / A	1.1 x 10+	4.5 x 10 <sup>-8</sup>	A / G	0.026	х		
	rs17762454	Τ/Ο	1.9 x 10 <sup>-7</sup>	9.6 x 10 <sup>-9</sup>	Τ/Ο	0.46			
Fasting	rs7708285	G / A	4.9 x 10 <sup>-6</sup>	1.2 x 10 <sup>-8</sup>	A / G	0.034	х		
Glucose	rs2657879	G / A	5.7 x 10 <sup>-6</sup>	3.9 x 10 <sup>-8</sup>	Á / G	0.24	Х		
Do du mara i	indow a diveted for	n haight (naoiting ag	molation with th	a autoom a)4					
Douy muss i	nuex uujusteu joi					4.00 40.(			
BMI	rs11676272	G/A	6.0 x 10-7	6.0 x 10 <sup>-9</sup>	A/G	1.09 x 10 <sup>-6</sup>	Х		
Forced wital	l agna gity (EVC)	divised for boight (	nogitivo gorrala	tion with the out	10m a) 5				
ronceu vitui									
	rs6923462	17C	na	$5.89 \times 10^{-13}$	C/T	4.86 x 10 <sup>-6</sup>	Х		
	rs1430193	A/T	na	$1.86 \times 10^{-12}$	A/T	6.70 x 10-7			
	rs2863171	C/A	na	$8.97 \times 10^{-10}$	C/A	0.28			
	rs6501431	T/C	na	$2.94 \times 10^{-9}$	T/C	0.23			
	rs1079572	G/A	na	9.95 × 10 <sup>-9</sup>	A/G	0.0098	Х		
	rs4237643	G/T	na	$3.53 \times 10^{-8}$	G/T	0.91	Х		
Ratio of FV(	C over forced exp	iratory Volume in 1 s	second (FEV1) a	djusted for heigh	t (negative correlat	ion with the d	outcome)6		
A	rs1980057	T/C	na	$3.21 \times 10^{-20}$	T/C	0.00073	Х		
Т	rs1032295	G/T	na	$4.37 \times 10^{-15}$	G/T	0.00013	Х		
G	rs2070600	т, Г	na	$3.15 \times 10^{-14}$	T/C	0.41	Х		
Т	rs10947233	Т, G	na	6.66 × 10 <sup>-12</sup>	т́/G	0.52	Х		
Т	rs11168048	C/T	na	$1.08 \times 10^{-11}$	Ć/T	0.0065	х		
Т	rs7735184	T/G	na	6.23 × 10 <sup>-11</sup>	T/G	0.0073	х		
Т	rs2277027	A/C	na	9.93 × 10 <sup>-11</sup>	A/C	0.053	х		
G	rs1422795	T/C	na	$2.62 \times 10^{-10}$	T/C	0.046	х		
G	rs3817928	G/A	na	1.17 × 10 <sup>-9</sup>	A/G	2.0 x 10 <sup>-11</sup>			
č	rs7776375	G/A	na	6.71 × 10 <sup>-9</sup>	A/G	9.4 x 10 <sup>-18</sup>			
G	rs6937121	G/T	na	1.25 × 10 <sup>-8</sup>	T/G	1.2 x 10 <sup>-18</sup>			
<sup>a</sup> We extracte	ed SNPs found asso	ciated with human phe	enotypes at genon	ne-wide significanc	e level in population of	f European an	cestry after		

# Table S2. Additional examples of genetically-associated covariate GWAS

" We extracted SNPs found associated with human phenotypes at genome-wide significance level in population of European ancestry after adjusting for either body mass index or height, for which effect estimates can be extracted from the GIANT consortium database<sup>7</sup>.

<sup>b</sup> For each SNP selected we extracted from the GIANT consortium database<sup>7</sup> their *p*-value for association with BMI or height when relevant, and the trait-increasing allele.

<sup>c</sup> GWAS the unadjusted p-value and estimates were not available (noted "na").

Case-scenario	Generative DAG <sup>a</sup>	Mean chi-square for the test of association between G and Y <sup>b</sup>		
		unadjusted	Adjusted for C	
	Figure S1a	989.9	1.0	
C and V share a common cause	Figure S1b	989.9	563.1	
G unu i shure u common cuuse	Figure S1c	278.8	1.0	
	Figure S1d	278.4	1.0	
	Figure S1e	989.7	1.0	
Effect of C on V is modisted through C	Figure S1f	279.0	1.0	
Ejject oj G on T is mediatea through C	Figure S1g	278.8	1.0	
	Figure S1h	989.6	563.3	
	Figure S1i	727.5	676.2	
An unmeasured variable influences both C and Y	Figure S1j	1.0	818.0	
C and Y both influence an unmeasured variable	Figure S1k	1.0	1.0	
	Figure S1l	1.0	2251.7	
C is a descendant of $V$	Figure S1m	1.0	270.8	
	Figure S1n	1.0	2143.4	
	Figure S1o	1.0	444.0	

# Table S3. Mean chi-square for adjusted and unadjusted analysis across 15 null models

<sup>a</sup>DAG: direct acyclic graph. For each DAG from FigureS1 we generated 10,000 replicates of 10,000 individuals. For simplicity all true effects were defined so that independent variables explain 30% of the variance of the dependent variable. All effects were positives.

<sup>b</sup>G, Y and C are the genetic variant, the outcome and the covariate included in the adjusted model, respectively.

## References

- 1. Vansteelandt, S., Goetgeluk, S., Lutz, S., Waldman, I., Lyon, H., Schadt, E.E., Weiss, S.T., and Lange, C. (2009). On the adjustment for covariates in genetic association analysis: a novel, simple principle to infer direct causal effects. Genetic epidemiology 33, 394-405.
- 2. Thorleifsson, G., Walters, G.B., Gudbjartsson, D.F., Steinthorsdottir, V., Sulem, P., Helgadottir, A., Styrkarsdottir, U., Gretarsdottir, S., Thorlacius, S., Jonsdottir, I., et al. (2009). Genome-wide association yields new sequence variants at seven loci that associate with measures of obesity. Nature genetics 41, 18-24.
- 3. Scott, R.A., Lagou, V., Welch, R.P., Wheeler, E., Montasser, M.E., Luan, J., Magi, R., Strawbridge, R.J., Rehnberg, E., Gustafsson, S., et al. (2012). Large-scale association analyses identify new loci influencing glycemic traits and provide insight into the underlying biological pathways. Nature genetics 44, 991-1005.
- 4. Stergiakouli, E., Gaillard, R., Tavare, J.M., Balthasar, N., Loos, R.J., Taal, H.R., Evans, D.M., Rivadeneira, F., St Pourcain, B., Uitterlinden, A.G., et al. (2014). Genome-wide association study of height-adjusted BMI in childhood identifies functional variant in ADCY3. Obesity.
- 5. Loth, D.W., Artigas, M.S., Gharib, S.A., Wain, L.V., Franceschini, N., Koch, B., Pottinger, T.D., Smith, A.V., Duan, Q., Oldmeadow, C., et al. (2014). Genome-wide association analysis identifies six new loci associated with forced vital capacity. Nature genetics 46, 669-677.
- 6. Hancock, D.B., Eijgelsheim, M., Wilk, J.B., Gharib, S.A., Loehr, L.R., Marciante, K.D., Franceschini, N., van Durme, Y.M., Chen, T.H., Barr, R.G., et al. (2010). Meta-analyses of genome-wide association studies identify multiple loci associated with pulmonary function. Nature genetics 42, 45-52.
- 7. Speliotes, E.K., Willer, C.J., Berndt, S.I., Monda, K.L., Thorleifsson, G., Jackson, A.U., Lango Allen, H., Lindgren, C.M., Luan, J., Magi, R., et al. (2010). Association analyses of 249,796 individuals reveal 18 new loci associated with body mass index. Nature genetics 42, 937-948.