

# Supplementary Information

## Multi-octave supercontinuum generation from mid-infrared filamentation in a bulk crystal

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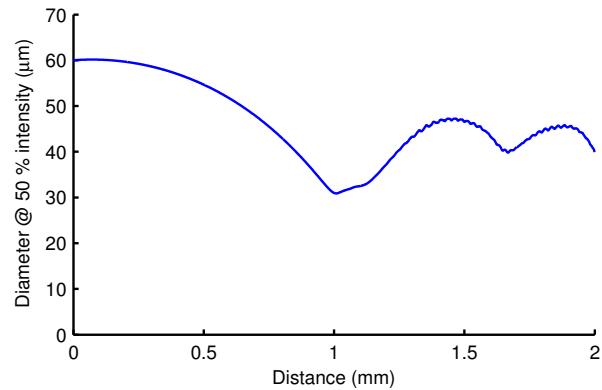
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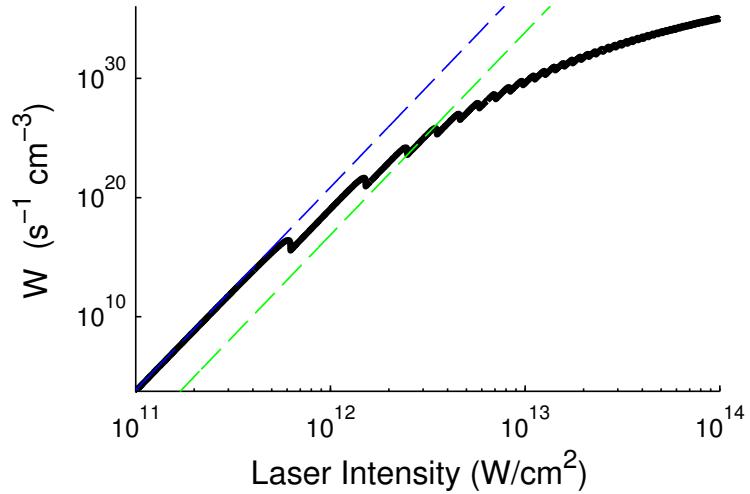
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### Supplementary Figures



Supplementary Figure S1: *Simulated beam diameter.* Simulated beam diameter at 50% intensity limit as function of propagation distance in the YAG plate.



Supplementary Figure S2: *Optical field ionization rate for YAG used in numerical calculations.* Optical field ionization rate for YAG calculated from the Keldysh formulation for a central wavelength of 3.1  $\mu\text{m}$ . The blue dashed lines indicate the low-intensity asymptote describing multiphoton ionization  $W_{MPI} = \sigma_K I^K \rho_{nt}$  where  $K = 17$ ,  $\sigma_{17} = 1 \times 10^{-206} \text{s}^{-1} \text{cm}^{34} \text{W}^{-17}$  and  $\rho_{nt} = 7 \times 10^{22} \text{ cm}^{-3}$ . The green dashed line shows an example of MPI rates (cross section coefficient  $\sigma_{17} = 1 \times 10^{-210} \text{s}^{-1} \text{cm}^{34} \text{W}^{-17}$ ) for which the Fish tail at 550 nm clearly appears in numerically simulated angular spectra.