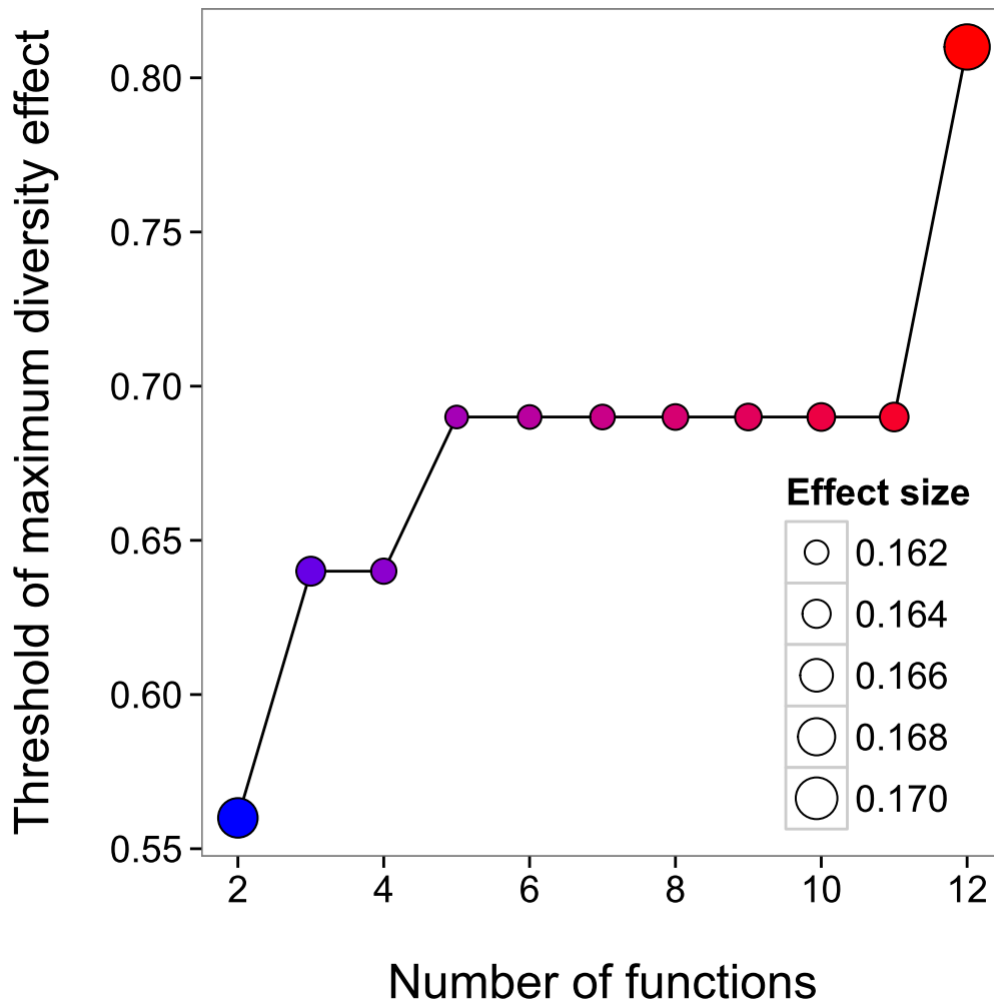
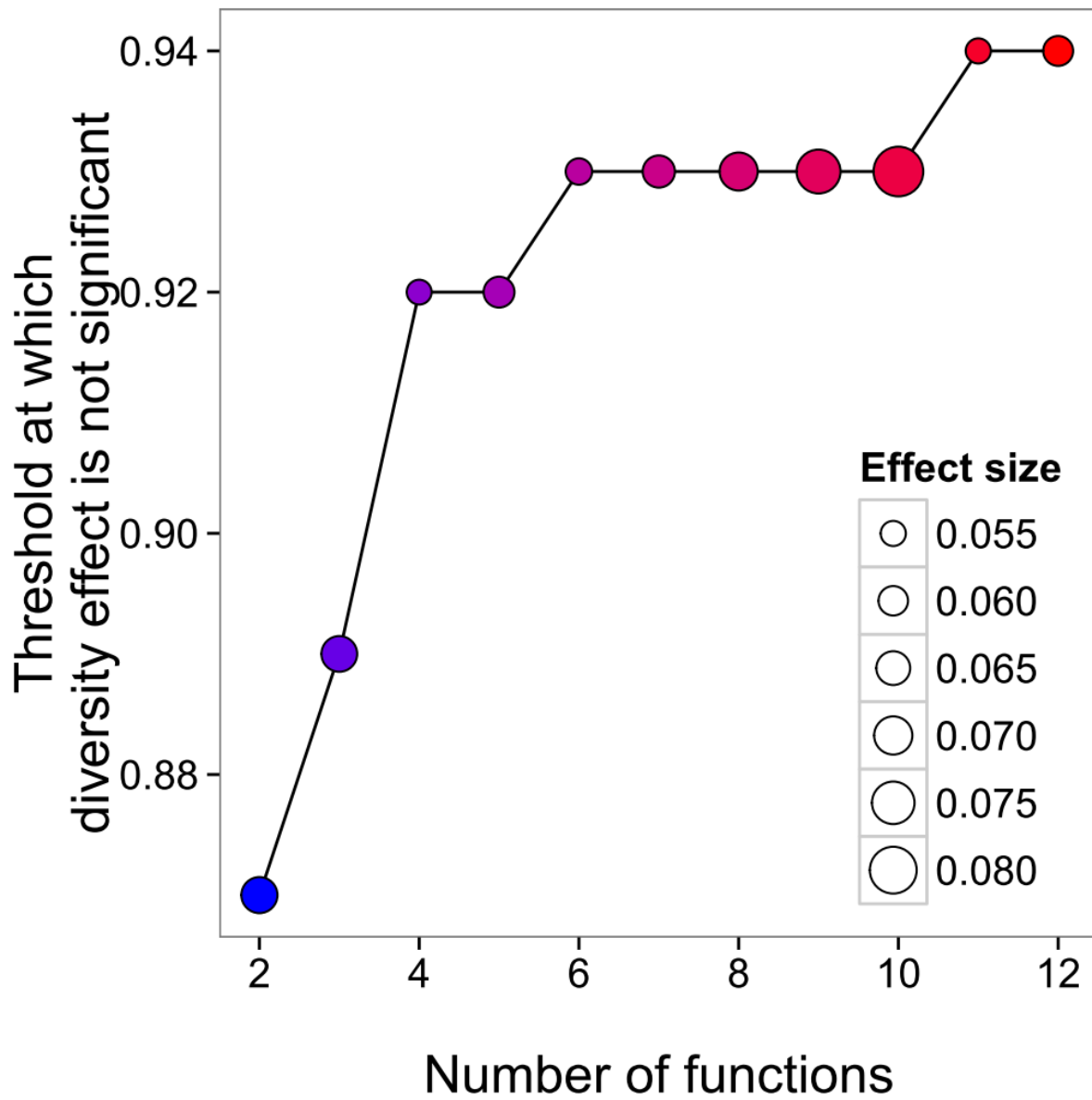


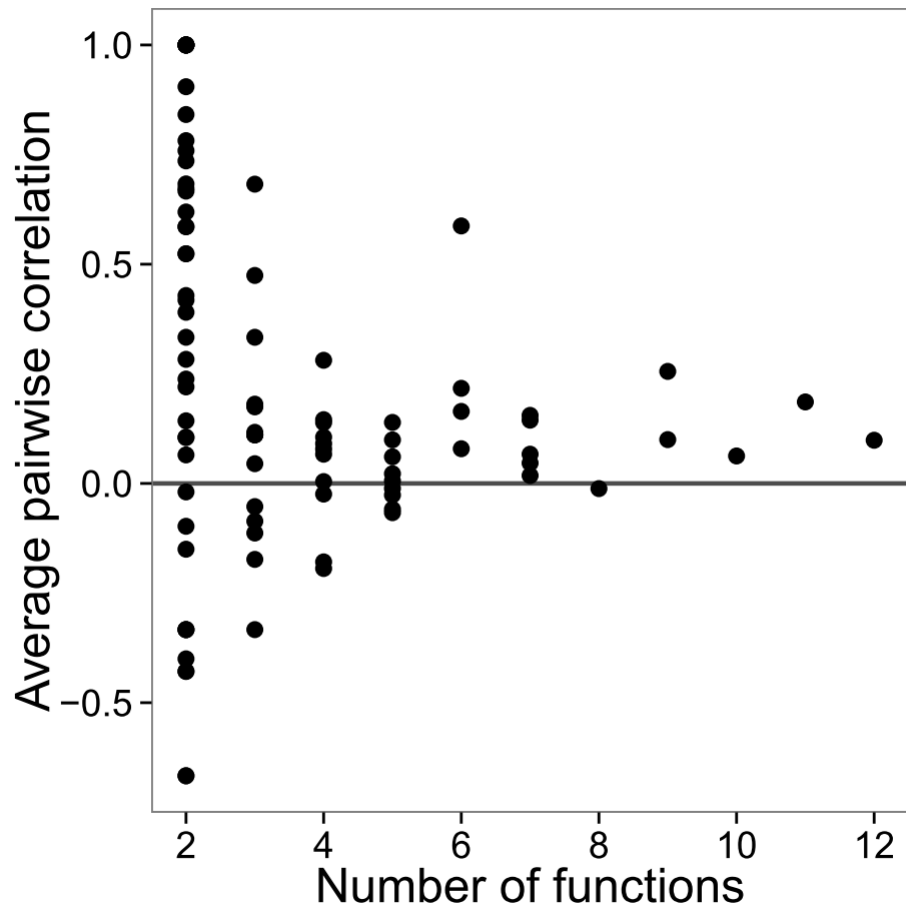
Supplementary Figure 1: The number of functions greater than a threshold against richness, for each level of number of functions (2-12). The raw number of functions greater than a threshold against richness, for thresholds ranging from 1% of the maximum (purple lines) to 99% of the maximum (red lines). Lines are predicted fits from generalized linear mixed effects models that fixed the covariate number of functions at the number indicated in the panel headers.



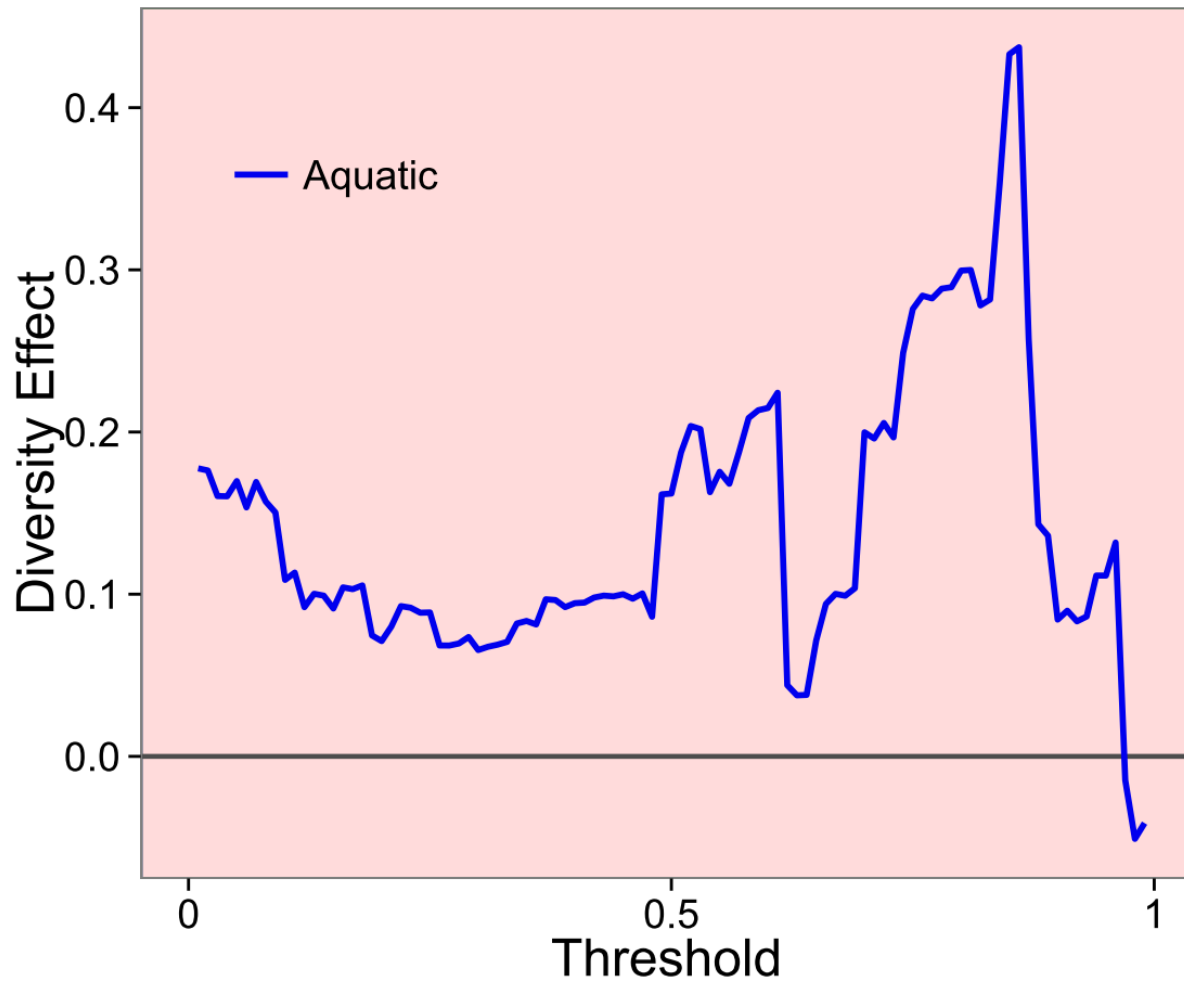
Supplementary Figure 2: The threshold where diversity has its maximum effect increased with the number of functions. The size of the points corresponds to the maximum effect size for each level of number of functions. Shading indicates the gradient from 2 functions (blue) to 12 functions (red).



Supplementary Figure 3: The threshold after which diversity no longer has a significant effect increased with the number of functions. The size of the points corresponds to the effect size for each level of number of functions. Shading indicates the gradient from 2 functions (blue) to 12 functions (red).

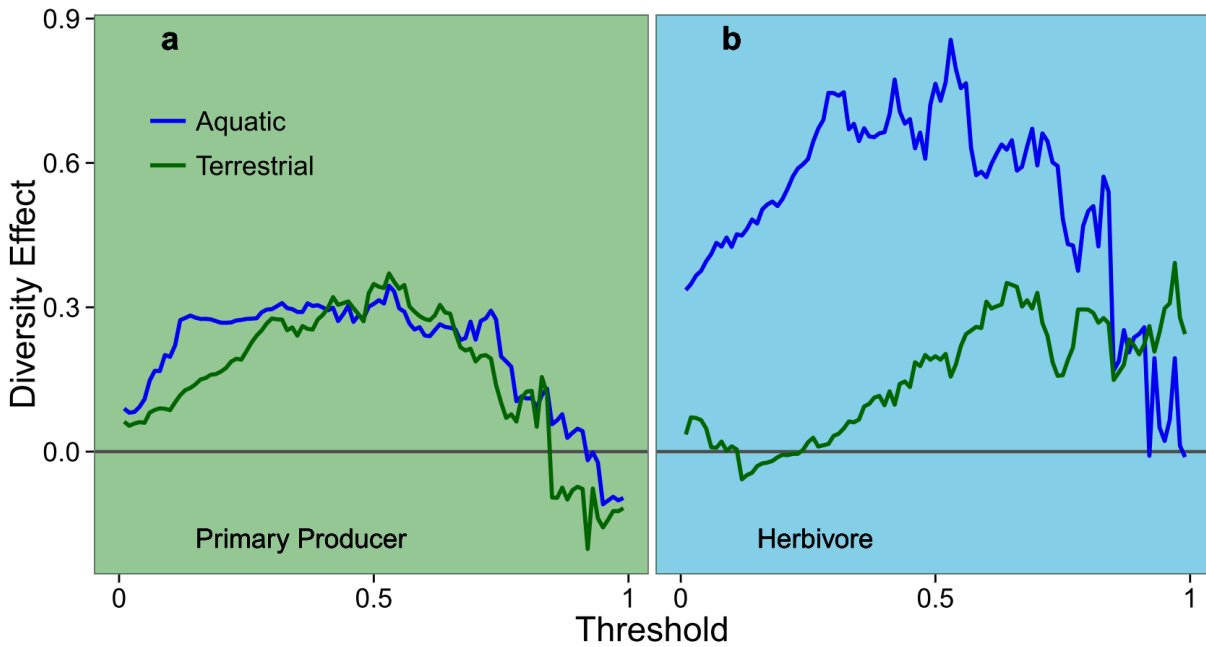


Supplementary Figure 4: The average pairwise correlation among all functions within a given experiment generally decreased with an increasing number of functions. Correlations were calculated as Kendall's rank correlations.

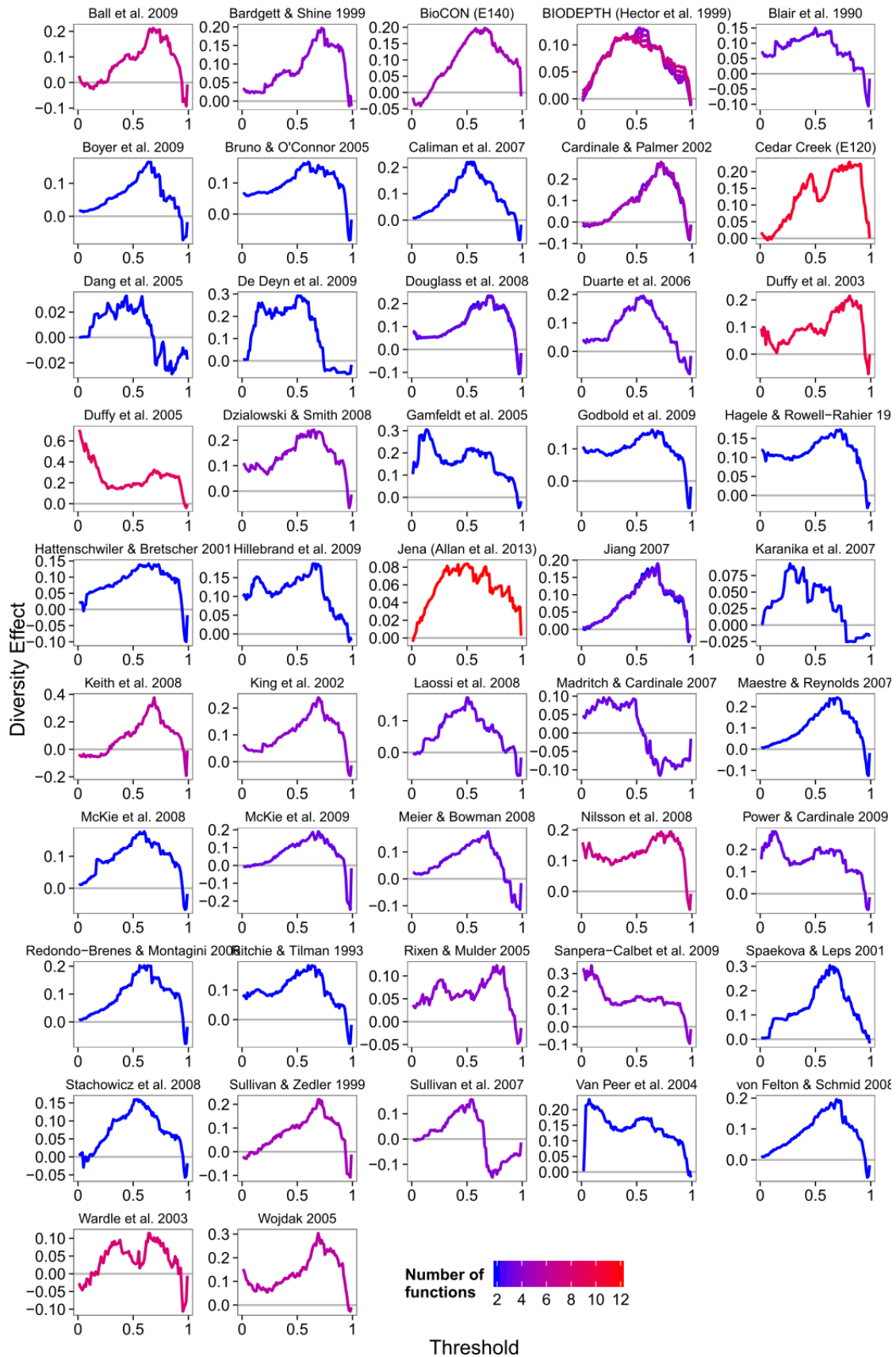


Supplementary Figure 5: The effect of diversity against threshold was highly variable for carnivores.

The effect of biodiversity (linear coefficient regressing the number of functions above a threshold against richness) plotted against the continuum of thresholds from 1-99% of the maximum observed level of functioning. The blue line represents trends from experiments conducted in aquatic systems.

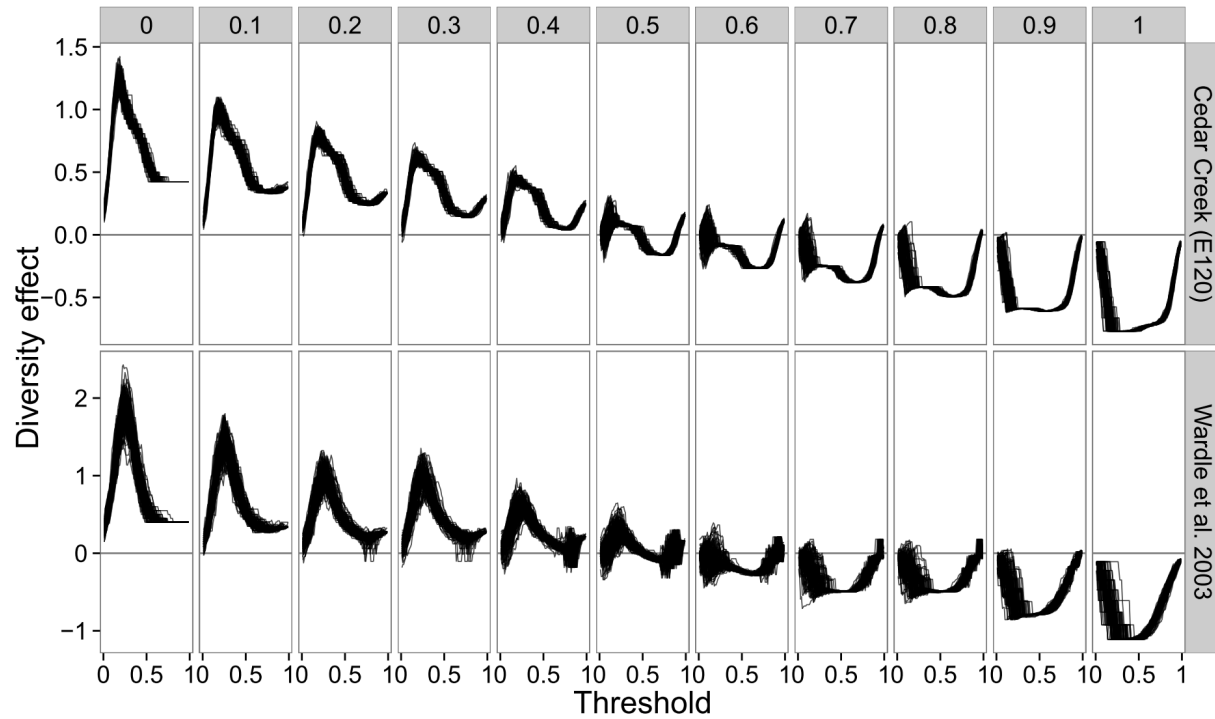


Supplementary Figure 6: Omitting all treatments where the number of species manipulated was $S \leq 6$ revealed stronger effects for herbivores than for plants. The effect of biodiversity (linear coefficient regressing the number of functions above a threshold against richness) plotted against the continuum of thresholds from 1-99% of the maximum observed level of function for **(a)** plants, and **(b)** herbivores. Blue lines represent trends from experiments conducted in aquatic systems, and green lines from terrestrial systems.



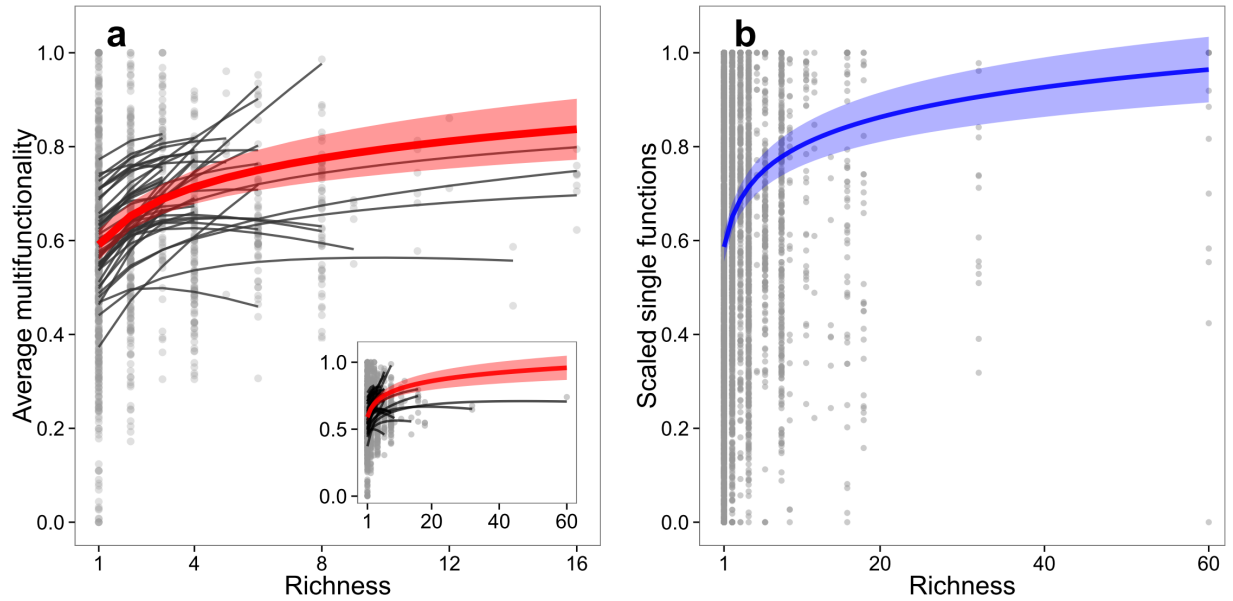
Supplementary Figure 7: Linear coefficients plotted against threshold for each study in the database.

The effect of biodiversity (linear coefficient regressing the number of functions above a threshold against richness) plotted against the continuum of thresholds from 1-99% of the maximum observed level of functioning. Shading indicates the number of functions measured in each study from 2 (blue) to 12 (red). Panel headers correspond to studies used in the main analysis (see Supplementary Table 1).



1

2 **Supplementary Figure 9: Simulations showed that the distribution of diversity effects against**
 3 **threshold changed from concave-up to concave-down with an increasing proportion of negative**
 4 **effects (top panels, in increments of 0.1).** Each line represents one of 100 runs of the simulation. The
 5 top row corresponds to parameters (richness, number of functions measured, diversity treatments)
 6 extracted from¹, and the bottom from².



7

8 **Supplementary Figure 10: Average multifunctionality showed a positive but decelerating relationship**

9 **with richness. (a)** The overall trend extracted from a generalized linear mixed effects model is given by

10 the red line \pm shaded 95% confidence intervals. Individual functions (points) and studies (black lines)

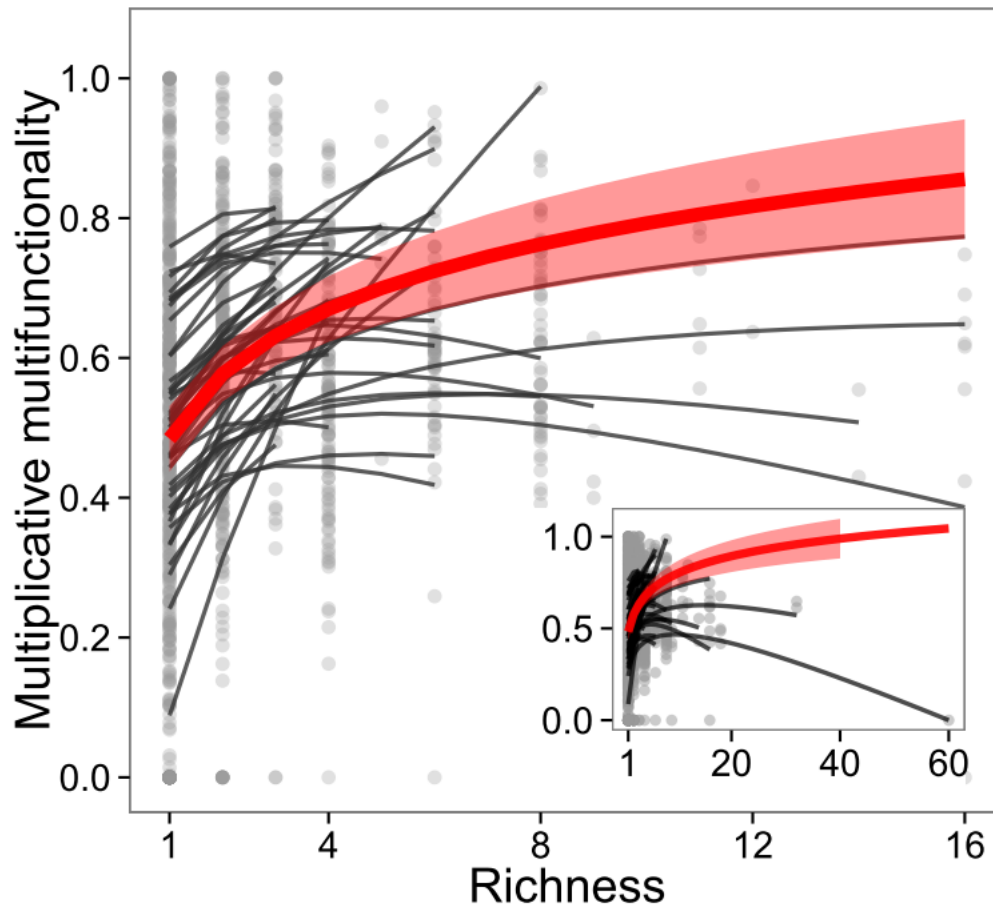
11 varied in their response to increasing richness, but in many cases showed a similar trend. The main

12 graphic shows the predicted trend for experiments that manipulated 16 or fewer species (96% of the

13 dataset), while the inset shows this trend across all experiments in the dataset. **(b)** However, this trend

14 was no different than a pooled analysis of single functions given by the blue line \pm shaded 95%

15 confidence intervals.



16

17 **Supplementary Figure 11: Multiplicative multifunctionality showed a positive but decelerating**

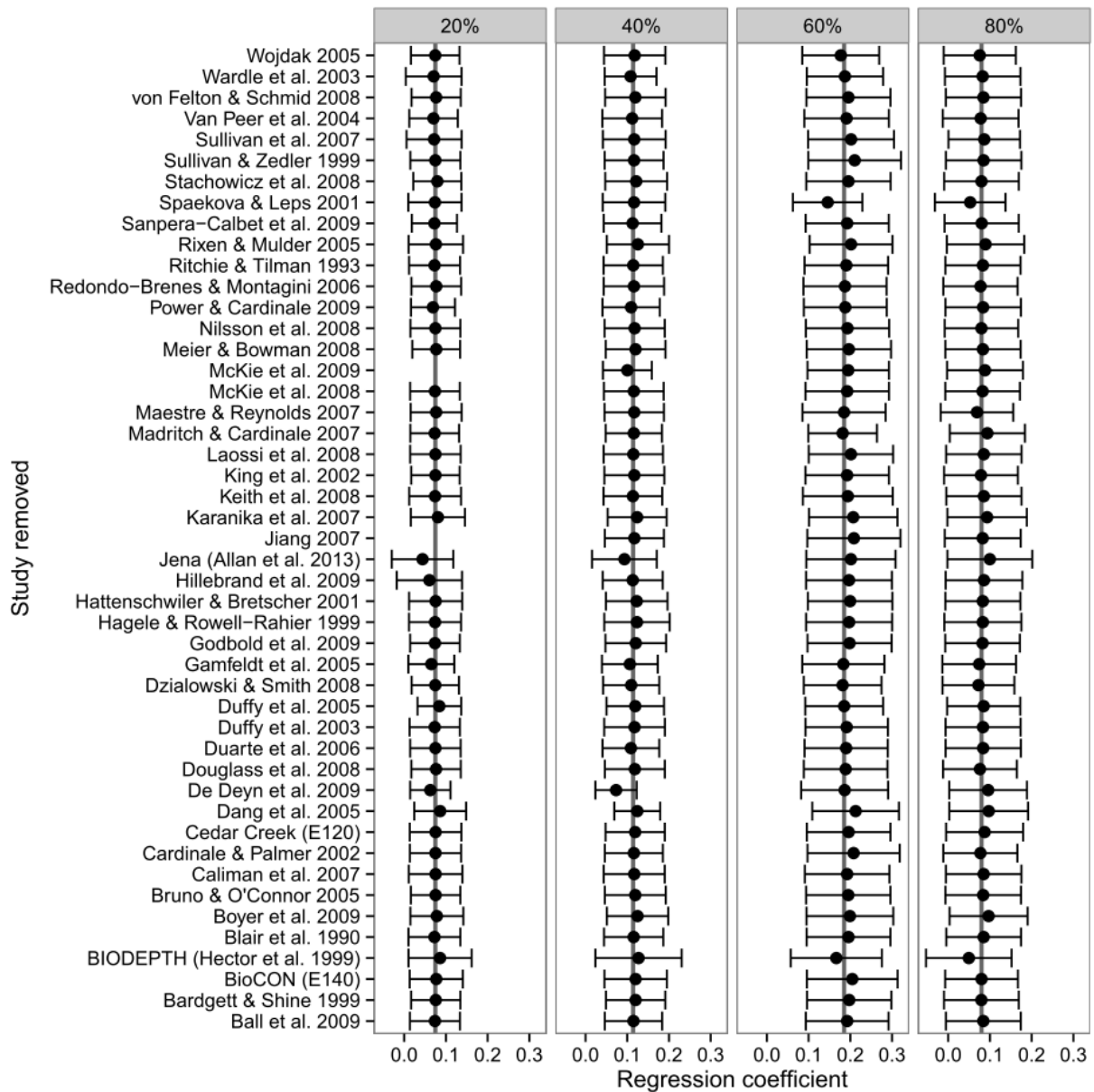
18 **relationship with richness. (a)** The overall trend extracted from a generalized linear mixed effects model

19 is given by the red line \pm shaded 95% confidence intervals. Individual functions (points) and studies

20 (black lines) varied in their response to increasing richness, but in many cases showed a similar trend.

21 The main graphic shows the predicted trend for experiments that manipulated 16 or fewer species (96%

22 of the dataset), while the inset shows this trend across all experiments in the dataset.



23

24 **Supplementary Figure 12: Sensitivity analysis revealed that our results were robust to loss of any**
 25 **given study.** Each point corresponds to the regression coefficient of the richness effect extracted from a
 26 generalized linear mixed effects model run on the reduced dataset missing the single study indicated on
 27 the y-axis. The error bars represent 95% confidence intervals, and the solid black line represents the
 28 overall regression coefficient obtained from a GLMM on the entire dataset. Each panel represents
 29 thresholds of 20, 40, 60, and 80% of the maximum.

Reference	Expt	System	Trophic Group	Max S	Max F	r
Ball et al. 2009 ³	1	T	Dead organic matter	4	7	0.07
Bardgett & Shine 1999 ⁴	1	T	Dead organic matter	6	4	0.09
BioCON (E140) ⁵	1	T	Primary Producer	16	5	0.02
BioCON (E140) ⁵	2	T	Primary Producer	16	5	0.14
BioCON (E140) ⁵	3	T	Primary Producer	16	5	0.10
BioCON (E140) ⁵	4	T	Primary Producer	16	5	0.01
BIODEPTH (Hector et al. 1999) ⁶	1	T	Primary Producer	16	5	0.06
BIODEPTH (Hector et al. 1999) ⁶	2	T	Primary Producer	18	7	0.14
BIODEPTH (Hector et al. 1999) ⁶	3	T	Primary Producer	8	5	-0.01
BIODEPTH (Hector et al. 1999) ⁶	4	T	Primary Producer	14	6	0.16
BIODEPTH (Hector et al. 1999) ⁶	5	T	Primary Producer	12	4	0.14
BIODEPTH (Hector et al. 1999) ⁶	6	T	Primary Producer	11	7	0.16
BIODEPTH (Hector et al. 1999) ⁶	7	T	Primary Producer	12	6	0.22
BIODEPTH (Hector et al. 1999) ⁶	8	T	Primary Producer	32	7	0.05
Blair et al. 1990 ⁷	1	T	Dead organic matter	3	3	-0.33
Boyer et al. 2009 ⁸	1	A	Primary Producer	6	2	0.39
Boyer et al. 2009 ⁸	2	A	Primary Producer	6	2	0.62
Boyer et al. 2009 ⁸	3	A	Primary Producer	6	2	-0.43
Boyer et al. 2009 ⁸	4	A	Primary Producer	6	2	0.24
Bruno & O'Connor 2005 ⁹	1	A	Carnivore	5	2	-0.15
Caliman et al. 2007 ¹⁰	1	A	Detritivore	3	2	1.00
Caliman et al. 2007 ¹⁰	2	A	Detritivore	3	2	1.00
Caliman et al. 2007 ¹⁰	3	A	Detritivore	3	2	0.90
Cardinale & Palmer 2002 ¹¹	1	A	Detritivore	3	5	-0.06
Cardinale & Palmer 2002 ¹¹	2	A	Detritivore	3	3	0.18
Cedar Creek (E120) ¹	1	T	Primary Producer	17	11	0.19
Dang et al. 2005 ¹²	1	A	Detritivore	8	2	-0.10
Dang et al. 2005 ¹²	2	A	Detritivore	8	2	0.07
Dang et al. 2005 ¹²	3	A	Detritivore	8	2	0.10
De Deyn et al. 2009 ¹³	1	T	Primary Producer	6	2	0.74
De Deyn et al. 2009 ¹³	2	T	Primary Producer	6	2	0.84
Douglass et al. 2008 ¹⁴	1	A	Herbivore	3	2	-0.33
Douglass et al. 2008 ¹⁴	2	A	Herbivore	3	3	0.11
Douglass et al. 2008 ¹⁴	3	A	Herbivore	3	3	0.11
Douglass et al. 2008 ¹⁴	4	A	Herbivore	3	3	0.11
Douglass et al. 2008 ¹⁴	5	A	Carnivore	3	3	0.11
Duarte et al. 2006 ¹⁵	1	A	Detritivore	4	3	0.11
Duffy et al. 2003 ¹⁶	1	A	Herbivore	6	10	0.06
Duffy et al. 2005 ¹⁷	1	A	Herbivore	4	9	0.26
Duffy et al. 2005 ¹⁷	2	A	Herbivore	4	9	0.10
Dzialowski & Smith 2008 ¹⁸	1	A	Herbivore	4	4	0.28
Dzialowski & Smith 2008 ¹⁸	2	A	Herbivore	4	4	0.08
Gamfeldt et al. 2005 ¹⁹	1	A	Herbivore	3	2	1.00

Gamfeldt et al. 2005 ¹⁹	2	A	Primary Producer	3	2	0.67
Godbold et al. 2009 ²⁰	1	A	Herbivore	3	2	-0.67
Hägele & Rowell-Rahier 1999 ²¹	1	T	Primary Producer	6	2	0.59
Hägele & Rowell-Rahier 1999 ²¹	2	T	Primary Producer	6	2	0.14
Hägele & Rowell-Rahier 1999 ²¹	3	T	Primary Producer	6	2	0.52
Hättenschwiler & Bretscher 2001 ²²	1	T	Dead organic matter	3	2	-0.33
Hättenschwiler & Bretscher 2001 ²²	2	T	Dead organic matter	3	2	-0.67
Hillebrand et al. 2009 ²³	1	A	Herbivore	6	2	0.28
Hillebrand et al. 2009 ²³	2	A	Herbivore	4	2	0.22
Jena Experiment ²⁴	1	T	Primary Producer	60	12	0.10
Jiang 2007 ²⁵	1	A	Detritivore	4	2	-0.02
Jiang 2007 ²⁵	2	A	Detritivore	4	3	-0.09
Karanika et al. 2007 ²⁶	1	T	Primary Producer	14	2	0.76
Keith et al. 2008 ²⁷	1	T	Dead organic matter	5	6	0.08
King et al. 2002 ²⁸	1	T	Dead organic matter	4	4	0.07
Laossi et al. 2008 ²⁹	1	T	Primary Producer	4	3	0.47
Madritch & Cardinale 2007 ³⁰	1	T	Dead organic matter	6	3	0.05
Madritch & Cardinale 2007 ³⁰	2	T	Dead organic matter	6	3	-0.11
Madritch & Cardinale 2007 ³⁰	3	T	Dead organic matter	6	3	-0.17
Maestre & Reynolds 2007 ³¹	1	T	Primary Producer	3	2	0.52
Maestre & Reynolds 2007 ³¹	2	T	Primary Producer	3	2	0.59
Maestre & Reynolds 2007 ³¹	3	T	Primary Producer	3	2	0.68
Maestre & Reynolds 2007 ³¹	4	T	Primary Producer	3	2	0.43
McKie et al. 2008 ³²	1	A	Detritivore	3	2	0.33
McKie et al. 2009 ³³	1	A	Detritivore	3	3	0.17
McKie et al. 2009 ³³	2	A	Detritivore	3	3	0.18
McKie et al. 2009 ³³	3	A	Detritivore	3	3	0.12
McKie et al. 2009 ³³	4	A	Detritivore	3	3	0.68
Meier & Bowman 2008 ³⁴	1	T	Dead organic matter	4	3	-0.05
Nilsson et al. 2008 ³⁵	1	A	Carnivore	3	7	0.02
Power & Cardinale 2009 ³⁶	1	A	Primary Producer	5	3	0.33
Redondo-Brenes & Montagini 2006 ³⁷	1	T	Primary Producer	3	2	1.00
Redondo-Brenes & Montagini 2006 ³⁷	2	T	Primary Producer	3	2	1.00
Redondo-Brenes & Montagini 2006 ³⁷	3	T	Primary Producer	3	2	1.00
Ritchie & Tilman 1993 ³⁸	1	T	Herbivore	3	2	-0.43
Ritchie & Tilman 1993 ³⁸	2	T	Herbivore	3	2	-0.33
Rixen & Mulder 2005 ³⁹	1	T	Primary Producer	8	4	0.00
Rixen & Mulder 2005 ³⁹	2	T	Primary Producer	8	4	-0.19
Rixen & Mulder 2005 ³⁹	3	T	Primary Producer	8	4	0.15
Rixen & Mulder 2005 ³⁹	4	T	Primary Producer	8	4	-0.02
Sanpera-Calbet et al. 2009 ⁴⁰	1	A	Dead organic matter	3	4	0.11
Spaekova & Leps 2001 ⁴¹	1	T	Primary Producer	6	2	0.78
Spaekova & Leps 2001 ⁴¹	2	T	Primary Producer	6	2	0.67
Stachowicz et al. 2008 ⁴²	1	A	Primary Producer	4	2	-0.40

Sullivan & Zedler 1999 ⁴³	1	T	Primary Producer	6	5	-0.03
Sullivan & Zedler 1999 ⁴³	2	T	Primary Producer	3	5	-0.07
Sullivan et al. 2007 ⁴⁴	1	T	Primary Producer	6	4	-0.18
Van Peer et al. 2004 ⁴⁵	1	T	Primary Producer	8	2	0.42
von Felten & Schmid 2008 ⁴⁶	1	T	Primary Producer	4	2	0.11
Wardle et al. 2003 ²	1	T	Primary Producer	9	8	-0.01
Wojdak 2005 ⁴⁷	1	A	Herbivore	3	6	0.59

30

31 **Supplementary Table 1: A list of all studies used in the analysis.** *Expt* represents independent
32 experiments conducted within the same study. *System* is either *A* = Aquatic or *T* = Terrestrial. *Max S*
33 represents the maximum species richness manipulated. *Max F* represents the maximum number of
34 functions recorded. The average correlation *r* is the mean of all pairwise rank correlations (Kendall's *r*)
35 among functions in a given experiment.

Supplementary Note 1: R Code

```
#####  
#  
#           META-ANALYSIS OF BIODIVERSITY AND ECOSYSTEM MULTIFUNCTIONALITY           #  
#  
#####  
  
#Authors: Jon Lefcheck & Jarrett Byrnes  
  
#Last updated: 2015-01-27  
  
#####  
#                               TABLE OF CONTENTS                               #  
#   Line 23: Required libraries                                               #  
#   Line 32: Importing and formatting the data                               #  
#   Line 74: Data exploration                                                 #  
#   Line 179: Multiple threshold approach                                    #  
#   Line 554: Turnover approach                                              #  
#   Line 1198: Averaging approach                                            #  
#   Line 1247: Multiplicative approach                                       #  
#  
#####  
  
library(ggplot2) #Calls: ggplot  
library(gridExtra) #Calls: grid.arrange  
library(MASS) #Calls: glmmPQL  
library(nlme) #Calls: lmeControl  
library(plotrix) #Calls: std.error  
library(plyr) #Calls: ddply, rbind.fill  
library(reshape2) #Calls: melt  
  
#####  
#                               IMPORTING AND FORMATTING THE DATA                               #  
#####  
  
#Import from file: Monoculture meta-master ALL DATA.xlsx  
multifunc=read.csv("Lefcheck et al Multifunc Meta.csv")  
  
#Remove the rows where Direction!="Positive" or !="Negative"  
multifunc=droplevels(subset(multifunc,multifunc$Direction=="Positive" | multifunc$Direction=="Negative"))  
  
#Convert all response means, sample sizes, and standard deviations to numeric  
#First, extract names of columns for response means, N, and SD  
Y.colnames=colnames(multifunc)[ grep("Y",colnames(multifunc)) [grep("Y",colnames(multifunc))>=27] ]  
N.colnames=colnames(multifunc)[ grep("N",colnames(multifunc)) [grep("N",colnames(multifunc))>=27] ]  
SD.colnames=colnames(multifunc)[ grep("SD",colnames(multifunc)) [grep("SD",colnames(multifunc))>=27] ]  
#Convert response values to numeric  
multifunc[,c(Y.colnames,N.colnames,SD.colnames)]=apply(multifunc[,c(Y.colnames,N.colnames,SD.colnames)],2,func  
tion(x) as.numeric(as.character(x)) )  
  
#Check recorded number of species (Smax) against actual number of species in maximum polyculture treatment  
#First, retrieve the column name of the last column with actual values  
poly.colnames=apply(multifunc[,Y.colnames],1,function(x) { y=rev(x[is.finite(x)])[1]; names(y)[length(y)] })  
#Use regular expressions to grab the number in the column name and convert them to a numeric vector  
Smax.colnames=as.numeric(gsub("X([0-9]+).*", "\\1", poly.colnames))  
cbind(as.character(multifunc$Reference), Smax.colnames, multifunc$Smax, Smax.colnames==multifunc$Smax)  
  
#Check to see if any experiments report only one function  
byexpt=ddply(multifunc,c("Reference", "Study", "Expt"),nrow)  
byexpt[byexpt$V1==1,c("Reference", "Study", "Expt")]  
  
#If Direction=="Negative", then transform based on Byrnes et al. 2014 MEE:  $x = -x + \max(x)$   
multifunc[,Y.colnames]=ddply(multifunc,1,function(x)  
  if(x$Direction=="Negative") -x[Y.colnames]+max(x[Y.colnames],na.rm=T) else x[Y.colnames] )[, -1]  
  
#If any responses are negative, scale so that they are all >0  
multifunc[,Y.colnames]=ddply(multifunc,1,function(x)  
  if(any(x[Y.colnames]<0,na.rm=T)) x[Y.colnames]+max(abs(x[Y.colnames]),na.rm=T) else x[Y.colnames] )[, -1]  
  
#Create a dataset with values scaled by the maximum value (for averaging approach)  
multifunc.scaled=multifunc  
multifunc.scaled[,SD.colnames]=ddply(multifunc,1,function(x) x[SD.colnames]/max(abs(x[Y.colnames]),na.rm=T)  
  )[, -1]  
multifunc.scaled[,Y.colnames]=ddply(multifunc,1,function(x) x[Y.colnames]/max(abs(x[Y.colnames]),na.rm=T) )[, -  
1]  
  
#####  
#                               DATA EXPLORATION                               #  
#####  
  
#Number of studies  
nrow(ddply(multifunc,"Study",nrow))  
#Number of experiments  
nrow(ddply(multifunc,c("Study", "Expt"),nrow))
```

```

#Total number of functions
nrow(multifunc)
#Number of experiments for each function
table(ddply(multifunc,c("Study","Expt"),nrow)$V1)

#Number of habitats
count(ddply(multifunc,c("Study","Expt","Sys1"),nrow),vars="Sys1")
#Number of trophic levels
count(ddply(multifunc,c("Study","Expt","FTG"),nrow),vars="FTG")
#And both
count(ddply(multifunc,c("Study","Expt","Sys1","FTG"),nrow),vars=c("FTG","Sys1"))

#Level of richness within an experiment
hist(multifunc$Smax)
median(multifunc$Smax)
range(multifunc$Smax)
#Level of richness within an experiment by habitat
ddply(multifunc,c("Sys1"),summarize,median=median(Smax))
ddply(multifunc,c("Sys1"),function(x) data.frame(min=range(x$Smax)[1],max=range(x$Smax)[2]))
#Level of richness within an experiment by trophic level
ddply(multifunc,c("FTG"),summarize,median=median(Smax))
ddply(multifunc,c("FTG"),function(x) data.frame(min=range(x$Smax)[1],max=range(x$Smax)[2]))

#Number of functions per experiment
median(ddply(multifunc,c("Study","Expt"),nrow)$V1)
range(ddply(multifunc,c("Study","Expt"),nrow)$V1)
#Number of functions per experiment by habitat
ddply(ddply(multifunc,c("Study","Expt","Sys1"),nrow),"Sys1",function(x) data.frame(median=median(x$V1)))
ddply(ddply(multifunc,c("Study","Expt","Sys1"),nrow),"Sys1",function(x)
data.frame(min=range(x$V1)[1],max=range(x$V1)[2]))
#Number of functions per experiment by trophic level
ddply(ddply(multifunc,c("Study","Expt","FTG"),nrow),"FTG",function(x) data.frame(median=median(x$V1)))
ddply(ddply(multifunc,c("Study","Expt","FTG"),nrow),"FTG",function(x)
data.frame(min=range(x$V1)[1],max=range(x$V1)[2]))

#Look at average pairwise correlation between all functions within a study
pairwisecor.df=ddply(multifunc,c("Reference","Study","Expt","Sys1","FTG"),function(x) {
  Smax=unique(x$Smax)
  x=x[,Y.colnames]
  cormat=cor(t(x),use="complete.obs",method=c("kendall"))
  data.frame(
    Smax=Smax,
    no.fn=nrow(x),
    avg.cor=mean(cormat[lower.tri(cormat)]))
}); pairwisecor.df
#And across all studies
mean(pairwisecor.df$avg.cor); std.error(pairwisecor.df$avg.cor)
#By habitat
ddply(pairwisecor.df,"Sys1",summarize,mean(avg.cor),std.error(avg.cor))
#By trophic level
ddply(pairwisecor.df,"FTG",summarize,mean(avg.cor),std.error(avg.cor))
#Plot as a function of number of functions
ggplot(pairwisecor.df,aes(x=no.fn,y=avg.cor))+
  geom_hline(yintercept=0,lwd=0.8,lty=1,col="grey30")+
  geom_point(size=3)+
  scale_x_continuous(breaks=seq(2,12,2))+
  labs(x="Number of functions",y="Average pairwise correlation")+
  theme_bw(base_size=18)+
  theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank())

#Look at number of positive / negative relationships
#First cast data.frame longways
multifunc.long=melt(cbind(multifunc[,c(2:4,6:7,9,12)],multifunc[,Y.colnames]),id.vars=c(1:7),measure.vars=c(8:
12))
multifunc.long$richness=suppressWarnings(
  ifelse(grepl("mono",multifunc.long$variable),1,as.numeric(gsub("X([0-
9]+).*","\\1",multifunc.long$variable)))
)

#Next calculate correlation between richness and functioning for each function
diversitycor.df=ddply(multifunc.long,c("Reference","Study","Expt","Sys1","FTG","Ydesc"),function(x)
  data.frame(cor=cor(x$richness,x$value,use="complete.obs",method="kendall"),
    p.value=cor.test(x$richness,x$value,na.action=na.omit,method="kendall")$p.value)
)

#Calculate number of positive/negative functions for each study
propcor.df=ddply(diversitycor.df,c("Study","Expt","Reference"),function(x)
  cbind(no.fn=length(unique(x$Ydesc)),
    sig.neg=sum(x[x$p.value<=0.05,"cor"]<0),
    sig.pos=sum(x[x$p.value<=0.05,"cor"]>0),
    neutral=length(x[x$p.value>0.05,"cor"]))
)

propcor.df=melt(propcor.df,id.vars=c(1:4),measure.vars=c(5:7))
propcor.df$variable=factor(propcor.df$variable,levels=c("sig.pos","sig.neg","neutral"))
levels(propcor.df$variable)=c("Positive","Negative","Neutral")
#Set symbols based on references in simulation, below
# propcor.df=adply(propcor.df,1,function(x) {
#   if(x$Reference=="Wardle et al. 2003") "diamond" else
#   if(x$Reference=="Cedar Creek (E120)" "triangle" else "none" })
#

#Plot results

```

```

ggplot(propcor.df, aes(x=no.fn, y=value/no.fn, group=variable, col=variable, shape=variable)) + #, shape=V1) +
  geom_point(size=4, alpha=0.5, position="jitter") +
  scale_x_continuous(breaks=c(2, 4, 6, 8, 10, 12)) +
  scale_color_manual(values=c("red", "blue", "grey20"), name="") +
  scale_shape_manual(values=15:17, name="") +
  # scale_shape_manual(values=c(15, 1, 17), guide="none") +
  stat_smooth(method="glm", family=binomial(), aes(lty=variable), lwd=2, se=F) +
  scale_linetype(guide="none") +
  labs(x="Total number of functions", y="Proportion of total functions") +
  theme_bw(base_size=18) +
  theme(panel.grid.major=element_blank(), panel.grid.minor=element_blank(),
        legend.direction="horizontal", legend.position="bottom")

#####
# MULTIPLE THRESHOLD APPROACH
#####

#Create vector of thresholds from 1-99%
thresholds=(1:99)/100

#Loop through thresholds and studies to calculate number of treatments > threshold
thresholds.df=ldply(thresholds, .progress="text", function(thresh) {
  ddply(multifunc, c("Reference", "Study", "Expt"), function(x) {
    #Melt response values and relevant metadata
    responses=melt(cbind(x[,c(2:4, 6:7, 9, 12)], x[,Y.colnames]), id.vars=c(1:7), measure.vars=c(8:112))
    #Remove NA values
    #responses=responses[!is.na(responses$value), ]
    #Create a column for richness
    responses$richness=suppressWarnings(
      ifelse(grepl("mono", responses$variable), 1, as.numeric(gsub("X{[0-9]+}.*", "\\1", responses$variable))) )
    #Determine whether each response for each functions >= some percentage (threshold) of maximum
    responses=ddply(responses, "Ydesc", function(y) cbind(y, greater.than=y$value>=thresh*max(y$value, na.rm=T)) )
    #Summarize for each treatment
    ddply(responses, c("Study", "Expt", "Reference", "Sys1", "FTG", "variable", "richness"), function(z) {
      data.frame(
        threshold=thresh,
        no.fn=length(z$greater.than),
        no.fn.greater=sum(z$greater.than),
        prop.fn.greater=sum(z$greater.than)/length(z$greater.than) ) ) ) ) ) )

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#Use mixed models to look at trends generally across all studies by fitting raw counts to
#quasipoisson distribution for each level of threshold
rawmods.list=ddply(thresholds.df, "threshold", .progress="text", function(i) {
  #Set lmeControl for certain thresholds
  if(i$threshold %in% c(0.02, 0.99)) control=lmeControl(opt="optim", msTol=1e-6) else
    control=lmeControl(opt="optim")
  #Function to run models
  f=function(x) glmmPQL(no.fn.greater~richness*no.fn, random=~richness|Study,
    family=quasipoisson(link="identity"), start=c(0.15, 0.05, 0.1, 0.001),
    control=control,
    verbose=F, data=x)
  #Run model, return NA if model fails
  safef=failwith(NA, f)
  safef(i)
})

#Extract predicted fit for muscle plot
#Modified from: http://glmm.wikidot.com/faq
predictraw.df=ldply(1:99, .progress="text", function(i) {
  ldply(2:12, function(j) {
    #Create dataframe for predicted values only for richness
    newdata=expand.grid(
      threshold=i/100,
      richness=1:max(subset(thresholds.df, no.fn==j) [!is.na(subset(thresholds.df, no.fn==j)$no.fn.greater), "richness"]
    ),
    no.fn=j,
    no.fn.greater=NA)
    if(!"glmmPQL" %in% class(rawmods.list[[i]])) {
      return(newdata)
    } else {
      #Generate predicted values from model
      newdata$no.fn.greater=predict(rawmods.list[[i]], newdata, type="response", level=0)
      #Return newdata
      return(newdata)
    }
  })
})

#Remove predictions that exceed the number of functions measured or drop below zero
predictraw.sub.df=ddply(predictraw.df, "no.fn", function(x) {
  x=subset(x, no.fn.greater<=x$no.fn & no.fn.greater>=0)
  data.frame(
    threshold=x$threshold,
    richness=x$richness,
    no.fn=x$no.fn,
    no.fn.greater=x$no.fn.greater)
})

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predictraw.sub.df=ddply(predictraw.df,"no.fn",function(x) subset(x,no.fn.greater<=no.fn))

#Plot predicted values against richness
ggplot(predictraw.sub.df,aes(x=richness,y=no.fn.greater,color=threshold,group=threshold))+
  geom_line(lwd=1,alpha=0.6)+
  geom_hline(aes(yintercept=no.fn),lwd=1,alpha=0.6,ltty=1)+
  scale_color_gradientn(colours=rev(rainbow(5)),name="Threshold")+
  labs(x="Richness",y="Number of functions > threshold")+
  facet_wrap(~no.fn,scales="free",nrow=4)+
  theme_bw(base_size=18)+
  theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank(),
        legend.position=c(0.8,0.1))

#Break out no.fn=max(no.fn) for Figure 2 panel a
p1=ggplot(subset(predictraw.df,no.fn==12 & no.fn.greater<=12 &
no.fn.greater>=0),aes(x=richness,y=no.fn.greater,color=threshold,group=threshold))+
  #geom_hline(yintercept=1,lwd=0.8,ltty=1,col="grey30")+
  geom_line(lwd=1,alpha=0.6)+
  geom_hline(yintercept=12,lwd=1,alpha=0.6,ltty=1)+
  scale_color_gradientn(colours=rev(rainbow(5)),name="Threshold")+
  labs(x="Richness",y="Number of functions > threshold")+
  scale_x_continuous(breaks=c(1,20,40,60))+
  scale_y_continuous(limits=c(-0.1,14.5),breaks=c(0,4,8,12))+
  annotate("text",x=1,y=Inf,label="a",vjust=1.5,col="black",fontface="bold",size=7)+
  theme_bw(base_size=18)+
  guides(colour=guide_colourbar(title.position="top"))+
  theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank(),legend.background=element_blank(),
        legend.position=c(0.7,0.9),legend.direction="horizontal",legend.box="horizontal"); p1

#Extract coefficients and standard errors
rawcoefs.df=ldply(2:max(thresholds.df$no.fn),.progress="text",function(i) {
  ldply(rawmods.list,function(j) {
    if("glmPQL" %in% class(j)) {
      data.frame(
        no.fn=i,
        Intercept=summary(j)$tTable["(Intercept)","Value"]+i*summary(j)$tTable["no.fn","Value"],
        Intercept.Std.Error=sqrt(
          (summary(j)$tTable["(Intercept)","Std.Error"]^2+summary(j)$tTable["no.fn","Std.Error"]^2+
            2*j$varFix["(Intercept)","no.fn"]) ),
        Estimate=summary(j)$tTable["richness","Value"]+i*summary(j)$tTable["richness:no.fn","Value"],
        #Std.Error=summary(j)$tTable["richness","Std.Error"] )
        Estimate.Std.Error=sqrt(
          (summary(j)$tTable["richness","Std.Error"]^2+summary(j)$tTable["richness:no.fn","Std.Error"]^2+
            2*j$varFix["richness","richness:no.fn"]) ) )
    } else {
      data.frame(no.fn=i,Intercept=NA,Intercept.Std.Error=NA,Estimate=NA,Estimate.Std.Error=NA) }
  } ) } )
#Determine which thresholds are significantly different from zero
rawcoefs.df$sig=ifelse(rawcoefs.df$Estimate>2*rawcoefs.df$Estimate.Std.Error,"sig","not.sig")

#Extract threshold of max diversity effect & max threshold at which diversity has a positive effect
maxeffect.df=ddply(rawcoefs.df,"no.fn",function(x) {
  rbind(
    #Find threshold of maximum diversity effect
    cbind(type="max.div.effect",x[which.max(x$Estimate)],),
    #Find maximum threshold at which diversity has a significant positive effect
    cbind(type="max.threshold",x[rev(which(x$sig=="sig"))][1],) ) )
})

#Rename levels for plotting
#levels(maxeffect.df$type)=c("Threshold of maximum diversity effect","Maximum threshold where diversity effect
> 0")
maxeffect.df$type=factor(maxeffect.df$type,levels=c("max.div.effect","max.threshold"))

#Plot threshold against effect size with 95% confidence intervals
p2=ggplot(rawcoefs.df,aes(x=threshold,y=Estimate,group=no.fn))+
  geom_hline(xintercept=0,lwd=0.8,ltty=1,col="grey70")+
  geom_ribbon(aes(fill=no.fn,ymax=Estimate+2*Estimate.Std.Error,ymin=Estimate-
2*Estimate.Std.Error),alpha=0.05)+
  scale_fill_gradientn(high="red",low="blue",name="Number of \nfunctions")+
  geom_line(size=1,aes(col=no.fn))+
  scale_color_gradientn(high="red",low="blue",name="Number of \nfunctions")+
  labs(x="Threshold",y="Diversity effect (Linear coefficients)")+
  geom_point(data=subset(maxeffect.df,no.fn %in% c(2,12)),
            aes(x=threshold,y=Estimate,shape=as.factor(threshold),fill=no.fn,col="white",size=8,width=2))+
  scale_shape_manual(values=c(21:24),guide=F)+
  annotate("text",x=0.01,y=Inf,label="b",vjust=1.5,col="black",fontface="bold",size=7)+
  theme_bw(base_size=18)+
  #guides(colour=guide_colourbar(title.position="top"))+
  theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank(),
        legend.direction="horizontal",legend.box="horizontal",legend.position=c(0.275,0.1)); p2

#Generate Figure 2
grid.arrange(arrangeGrob(p1,p2,ncol=2,widths=c(1.5,2)))

#Look at how intercept changes as a function of threshold
ggplot(rawcoefs.df,aes(x=threshold,y=Intercept))+
  geom_ribbon(aes(fill=no.fn,ymax=Intercept+2*Intercept.Std.Error,ymin=Intercept-2*Intercept.Std.Error),
            alpha=0.2)+

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scale_fill_gradient(high="red",low="blue",name="Number of\nfunctions")+
geom_line(size=1,aes(col=no.fn))+
scale_color_gradient(high="red",low="blue",name="Number of\nfunctions")+
facet_wrap(~no.fn,scales="free",nrow=2)+
labs(x="\nThreshold",y="Intercept\n")+
theme_bw(base_size=18)+
theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank(),legend.position="none")

#Plot against number of functions
ggplot(maxeffect.df,aes(x=no.fn,y=threshold,group=type,fill=no.fn))+
#Add trend line
geom_line()+
#Scale points by the size of the diversity effect
geom_point(aes(size=Estimate),shape=21)+

#geom_text(data=data.frame(type=c("max.threshold","max.div.effect"),no.fn=c(2.3,2.3),threshold=c(0.935,0.795),
lab=c("d","c")),
# aes(label=lab),size=8,fontface="bold")+
#Break out panels by response
facet_wrap(~type,ncol=1,scales="free_y")+
scale_fill_gradient(high="red",low="blue",name="Number of\nfunctions")+
scale_size(range=c(4,8),name="Effect size")+
labs(x="\nNumber of functions",y="Threshold\n")+
#Specify axis breaks
scale_x_continuous(breaks=c(2,4,6,8,10,12))+
theme_bw(base_size=18)+
theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank(),
strip.background=element_blank(),strip.text=element_blank())

#Break out into separate plots
ggplot(subset(maxeffect.df,type=="max.div.effect"),aes(x=no.fn,y=threshold,fill=no.fn))+
#Add trend line
geom_line()+
#Scale points by the size of the diversity effect
geom_point(aes(size=Estimate),shape=21)+
scale_fill_gradient(high="red",low="blue",name="Number of\nfunctions",guide=F)+
scale_size(range=c(4,8),name="Effect size")+
labs(x="\nNumber of functions",y="Threshold of maximum diversity effect\n")+
#Specify axis breaks
scale_x_continuous(breaks=c(2,4,6,8,10,12))+
theme_bw(base_size=18)+
theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank(),
strip.background=element_blank(),strip.text=element_blank(),
legend.position=c(0.85,0.24))

ggplot(subset(maxeffect.df,type=="max.threshold"),aes(x=no.fn,y=threshold,fill=no.fn))+
#Add trend line
geom_line()+
#Scale points by the size of the diversity effect #Scale points by the size of the diversity effect
geom_point(aes(size=Estimate),shape=21)+
scale_fill_gradient(high="red",low="blue",name="Number of\nfunctions",guide=F)+
scale_size(range=c(4,8),name="Effect size")+
labs(x="\nNumber of functions",y="Threshold at which\ndiversity effect is not significant")+
#Specify axis breaks
scale_x_continuous(breaks=c(2,4,6,8,10,12))+
theme_bw(base_size=18)+
theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank(),
strip.background=element_blank(),strip.text=element_blank(),
legend.position=c(0.85,0.28))

#####

#Extract slopes for each individual experiment from mixed model

#Create dataframe for predicted values for each study
predictindividual.df=ldply(1:99,.progress="text",function(i) {
  ldply(unique(thresholds.df$Study),function(j) {
    #Generate dataframe for predicted values
    newdata=expand.grid(
      Study=j,
      threshold=i/100,
      richness=1:max(subset(thresholds.df,Study==j)[!is.na(subset(thresholds.df,Study==j)$no.fn.greater),"richness"]
    ),
    no.fn=max(subset(thresholds.df,Study==j)$no.fn)
  #Add predicted values with varying slope of richness for each study
  newdata$no.fn.greater=predict(rawmods.list[[i]],newdata,type="response")
  #Return dataframe
  return(newdata)
  } ) } )

#Add column for reference (for panel headers)
predictindividual.df$Reference=multifunc[match(predictindividual.df$Study,multifunc$Study),"Reference"]
#Generate muscle plots
ggplot(predictindividual.df,aes(x=richness,y=no.fn.greater,col=threshold,group=threshold))+
geom_line(lwd=1,alpha=0.6)+
scale_color_gradientn(colours=rev(rainbow(5)),name="Threshold")+
labs(x="\nRichness",y="Number of functions > than threshold\n")+

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facet_wrap(~Reference, scales="free")+
theme_bw(base_size=18)+
theme(panel.grid.major=element_blank(), panel.grid.minor=element_blank(), strip.text.x=element_text(size=12),
       legend.position="right" )

#Extract coefficients for muscle plots
individualcoefs.df=ldply(1:99, .progress="text", function(i) {
  ldply(unique(thresholds.df$Study), function(j) {
    ldply(unique(thresholds.df[thresholds.df$Study==j, "no.fn"]), function(k) {
      data.frame(
        Study=rownames(coef(rawmods.list[[i]])) [j],
        no.fn=k,
        threshold=i/100,
        Intercept=coef(rawmods.list[[i]]) [j,1]+k*coef(rawmods.list[[i]]) [j,3],
        Estimate=coef(rawmods.list[[i]]) [j,2]+k*coef(rawmods.list[[i]]) [j,4] )
    } ) ) } )

#Add column for reference (for panel headers)
individualcoefs.df$Reference=multifunc[match(individualcoefs.df$Study, multifunc$Study), "Reference"]
#Plot coefs against threshold
ggplot(individualcoefs.df, aes(x=threshold, y=Estimate, group=no.fn, col=no.fn)) +
  geom_hline(xintercept=0, lwd=0.8, lty=1, col="grey70") +
  geom_line(lwd=1.2) +
  facet_wrap(~Reference, scales="free", ncol=5) +
  scale_color_gradient(high="red", low="blue", name="Number of\nfunctions") +
  scale_x_continuous(breaks=c(0, 0.5, 1), labels=c("0", "0.5", "1")) +
  labs(x="Threshold", y="Diversity Effect") +
  theme_bw(base_size=18) +
  theme(panel.grid.major=element_blank(), panel.grid.minor=element_blank(),
        strip.text.x=element_text(size=12), strip.background=element_blank(),
        legend.direction="horizontal", legend.position=c(0.55, 0.025))
#Plot intercept against threshold
ggplot(individualcoefs.df, aes(x=threshold, y=Intercept, group=no.fn, col=no.fn)) +
  geom_hline(xintercept=0, lwd=0.8, lty=1, col="grey70") +
  geom_line(lwd=1.2) +
  facet_wrap(~Reference, scales="free") +
  scale_color_gradient(high="red", low="blue", name="Number of\nfunctions") +
  labs(x="\nThreshold", y="Intercept\n") +
  theme_bw(base_size=18) +
  theme(panel.grid.major=element_blank(), panel.grid.minor=element_blank(), strip.text.x=element_text(size=12))

#####

#Explore whether this relationship changes as a function of system or trophic level
thresholds.df$FTG=relevel(thresholds.df$FTG, "Primary Producer")
globalmods.list=dlply(thresholds.df, "threshold", .progress="text", function(i) {
  #Set lmeControl for certain thresholds
  if(i$threshold %in% c(0.46)) control=lmeControl() else
    control=lmeControl(opt="optim", msTol=1e-6)
  #Function to run models
  f=function(x) glmmPQL(no.fn.greater~richness*no.fn+richness*Sys1+richness*FTG, random=~richness|Study,
                       family=quasipoisson(link="identity"),
                       start=c(1, 0.1, 0.5, rep(0, 11)),
                       control=control,
                       verbose=F, data=x)

  safef=failwith(NA, f)
  safef(i)
} )

#Create dataframe for predicted values for each system
predictglobal.df=ldply(1:99, .progress="text", function(i) {
  ldply(unique(thresholds.df$Sys1), function(j) {
    ldply(unique(thresholds.df$FTG), function(k) {
      #Subset dataframe
      data=subset(thresholds.df, Sys1==j & FTG==k)
      data=data[!is.na(data$no.fn.greater), ]
      if("glmmPQL" %in% class(globalmods.list[[i]])) {
        if(nrow(data)==0) {
          data.frame()
        } else {
          #Create new dataframe to store predictions
          newdata=expand.grid(
            Sys1=j,
            FTG=k,
            threshold=i/100,
            richness=1:max(data$richness),
            no.fn=max(data$no.fn)
          )
          #Generate predicted values
          newdata$no.fn.greater=predict(globalmods.list[[i]], newdata, type="response", level=0)
          return(newdata)
        }
      } else {
        data.frame()
      }
    } ) ) } )
} ) ) )

#Plot predicted results by trophic group and system
ggplot(predictglobal.df, aes(x=richness, y=no.fn.greater, col=threshold, group=threshold)) +
  geom_line(lwd=1, alpha=0.6) +
  scale_color_gradientn(colours=rev(rainbow(5)), name="Threshold") +

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theme(panel.grid.major=element_blank(), panel.grid.minor=element_blank(),
      strip.text.x=element_blank(), strip.background=element_blank(),
      legend.background=element_blank(), legend.key=element_blank(),
      legend.direction="horizontal", legend.box="horizontal", legend.position=c(0.2, 0.77))

#Plot intercepts against threshold
ggplot(globalcoefs.df, aes(x=threshold, y=Intercept, col=no.fn, group=no.fn)) +
  geom_hline(xintercept=0, lwd=0.8, lty=1, col="grey70") +
  geom_line(lwd=1.2) +
  scale_color_gradient(high="red", low="blue", name="Number of\nfunctions") +
  facet_grid(Sys1~FTG, scales="free") +
  scale_x_continuous(breaks=c(0, 0.25, 0.5, 0.75, 1)) +
  labs(x="\nThreshold", y="Intercept\n") +
  theme_bw(base_size=18) +
  theme(panel.grid.major=element_blank(), panel.grid.minor=element_blank(),
        strip.text.x=element_text(size=12), legend.position=c(0.075, 0.25) )

#####

#Look at sensitivity of trophic levels results to Smax
#Identify studies with Smax > 6
ref.remove=unique(
  c(as.character(multifunc[multifunc$Smax > 6, "Reference"]),
    as.character(multifunc[!multifunc$FTG %in% c("Primary Producer", "Herbivore"), "Reference"])) )
#Subset thresholds.sub.df to remove all experiments that manipulated Smax > 6
thresholds.sub.df=subset(thresholds.df, !Reference %in% ref.remove)
thresholds.sub.df$FTG=relevel(thresholds.sub.df$FTG, "Primary Producer")
#Re-run GLMMs
globalmods.sub.list=dply(thresholds.sub.df, "threshold", .progress="text", function(i) {
  #Function to run models
  f=function(x) glmmPQL(no.fn.greater~richness*no.fn+richness*Sys1+richness*FTG, random=~richness|Study,
    family=quasipoisson(link="identity"),
    start=c(1, 0.1, 0.5, rep(0, 5)),
    control=lmeControl(opt="optim", msTol=1e-4),
    verbose=F, data=x)

  safef=failwith(NA, f)
  safef(i)
})

#Extract coefficients for muscle plots
globalcoefs.sub.df=ldply(1:99, .progress="text", function(i) {
  ldply(unique(thresholds.sub.df$Sys1), function(k) {
    ldply(unique(thresholds.sub.df$FTG), function(l) {
      data=subset(thresholds.sub.df, Sys1==k & FTG==l)
      if(nrow(data)==0) data.frame() else {
        ldply(2:max(data$no.fn), function(j) {
          if("glmmPQL" %in% class(globalmods.sub.list[[i]])) {
            mod=globalmods.sub.list[[i]]
            data.frame(
              threshold=i/100,
              Sys1=k,
              FTG=l,
              no.fn=j,
              Intercept=
                summary(mod)$tTable["Intercept", "Value"] +
                ifelse(k=="Aquatic", 0, summary(mod)$tTable[paste("Sys1", k, sep=""), "Value"]) +
                ifelse(l=="Primary Producer", 0, summary(mod)$tTable[paste("FTG", l, sep=""), "Value"]) +
                j*summary(mod)$tTable["no.fn", "Value"],
              Estimate=
                summary(mod)$tTable["richness", "Value"] +
                ifelse(k=="Aquatic", 0, summary(mod)$tTable[paste("richness:Sys1", k, sep=""), "Value"]) +
                ifelse(l=="Primary Producer", 0, summary(mod)$tTable[paste("richness:FTG", l, sep=""), "Value"]) +
                j*summary(mod)$tTable["richness:no.fn", "Value"] )
          } else {
            data.frame() } }
        } ) } } ) } )

#Plot coefs against threshold (subset out max number of functions): 9" x 5"
ggplot(
  data=ddply(subset(globalcoefs.sub.df, FTG %in% c("Primary Producer", "Herbivore")), c("Sys1", "FTG"), function(x)
  subset(x, no.fn==max(no.fn))),
  aes(x=threshold, y=Estimate, col=Sys1, group=Sys1)) +
  geom_rect(data=data.frame(
    FTG=levels(globalcoefs.sub.df$FTG)[c(1, 5)],
    Sys1=rep(levels(globalcoefs.sub.df$Sys1), each=4),
    threshold=0, Estimate=0),
    aes(fill=FTG, xmin=-Inf, xmax=Inf, ymin=-Inf, ymax=Inf, alpha=0.15, show_guide=F) +
  scale_fill_manual(values=c("deepskyblue3", "forestgreen"), guide="none") +
  geom_hline(xintercept=0, lwd=0.8, lty=1, col="grey30") +
  geom_line(lwd=1) + #aes(lty=Sys1, lwd=1) +
  #scale_linetype_manual(values=c(1, 6)) +
  scale_color_manual(values=c("blue2", "darkgreen"), guide=guide_legend(ncol=1), name="") +
  facet_grid(~FTG, scales="free", space="free") +
  scale_x_continuous(breaks=c(0, 0.5, 1), labels=c("0", "0.5", "1")) +
  geom_text(data=data.frame(
    FTG=levels(globalcoefs.sub.df$FTG)[c(1, 5)],
    Sys1=rep(levels(globalcoefs.sub.df$Sys1), each=4),

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labels=letters[1:2]),
aes(x=0.1,y=Inf,label=labels),vjust=1.5,col="black",fontface="bold",size=6)+
geom_text(data=data.frame(
  FTG=levels(globalcoefs.sub.df$FTG)[c(1,5)],
  Sys1=rep(levels(globalcoefs.sub.df$Sys1),each=4)),
aes(x=0.15,y=-0.2,label=FTG),vjust=0,hjust=0,col="black",size=5)+
labs(x="Threshold",y="Diversity Effect")+
theme_bw(base_size=18)+
theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank(),
strip.text.x=element_blank(),strip.background=element_blank(),
legend.background=element_blank(),legend.key=element_blank(),
legend.direction="horizontal",legend.box="horizontal",legend.position=c(0.12,0.77))

#####

#Simulations to explore the dip in diversity effect around 50% threshold for high numbers of functions
#Extract data for studies that exhibit the dip for further simulations
cedarcreek.df=subset(multifunc.long,Reference=="Cedar Creek (E120)" & value!="NA")
wardle.df=subset(multifunc.long,Reference=="Wardle et al. 2003" & value!="NA")

sim.df=ldply(1:100,.progress="text",function(rep) {
  ldply(seq(0,1,0.1),function(i) { #Percent of negative functions
    ldply(list(cedarcreek.df,wardle.df),function(j) {
      #Specify number of functions
      no.fn=length(unique(j$Ydesc))
      #Specify diversity levels
      divlevels=j[j$Ydesc %in% unique(j$Ydesc)[1],"richness"]
      #Construct data.frame with appropriate dims
      newdf=cbind(
        data.frame(diversity=divlevels),
        matrix(rep(NA,length(divlevels)*no.fn),nrow=length(divlevels)) )
      #Populate with values
      newdf[,2:ncol(newdf)]=colwise(function(x) rnorm(nrow(newdf),newdf$diversity,1))(newdf[,2:ncol(newdf)])
      #Define % of functions that have a negative relationship with diversity
      negcol=round(no.fn*i)
      #Convert that number in newdf to negative
      if(negcol>0) newdf[,2:(negcol+1)]=-newdf[,2:(negcol+1)]+max(newdf[,2:(negcol+1)]) else newdf=newdf
      #Scale response
      #newdf[,2:ncol(newdf)]=colwise(function(x) x/max(x))(newdf[,2:ncol(newdf)])
      #Generate threshold data
      thresh.df=ldply(1:99/100,function(k)
        cbind(
          diversity=newdf[,1],
          thresh=k,
          no.fn.greater=rowSums(colwise(function(x) x>=max(x)*k)(newdf[,2:ncol(newdf)])) ) )
      #Get linear slopes
      ddply(thresh.df,"thresh",function(x) {
        mod=try(glm(no.fn.greater~diversity,data=x,family=quasipoisson(link="identity"),start=c(0,0.1)))
        if(class(mod) == "try-error")
          cbind(
            rep=rep,
            Reference=as.character(unique(j$Reference)),
            pneg=i,
            no.fn=no.fn,
            thresh=unique(x$thresh),
            Estimate=NA,
            Std.Error=NA,
            N=NA) else
            cbind(
              rep=rep,
              Reference=as.character(unique(j$Reference)),
              pneg=i,
              no.fn=no.fn,
              thresh=unique(x$thresh),
              Estimate=summary(mod)$coefficients["diversity",1],
              Std.Error=summary(mod)$coefficients["diversity",2],
              n=mod$df.residuals) ) )
      } )
    } )
  } )
) )

sim.df[,3:7]=apply(sim.df[,3:7],2,function(x) as.numeric(x))

#Summarize for plotting
sim.df.summary=ddply(sim.df,c("Reference","pneg","no.fn","thresh"),function(x)
  data.frame(
    Reference=unique(x$Reference),
    pneg=unique(x$pneg),
    no.fn=unique(x$no.fn),
    thresh=unique(x$thresh),
    Estimate=mean(x$Estimate),
    Std.Error=std.error(x$Estimate)) )
# Std.Error=sqrt(sum(x$Std.Error/x$n)) ) )

#Graph results
ggplot(sim.df,aes(x=thresh,y=Estimate,group=rep))+
  geom_hline(yintercept=0,col="grey50",lwd=0.5)+
  # geom_ribbon(aes(ymin=Estimate-Std.Error,ymax=Estimate+Std.Error),col="blue")+

```

```

geom_line(lwd=0.3,alpha=0.7)+
scale_x_continuous(breaks=c(0,0.5,1),labels=c("0","0.5","1"))+
#scale_color_gradient(high="green",low="firebrick1",name="Number of\nfunctions")+
facet_grid(Reference~pneg,scales="free")+
labs(x="Threshold",y="Diversity effect")+
theme_bw(base_size=18)+
theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank())

#####

#Conduct sensitivity analysis by removing each study individually, and re-generating coef plot
rawmods.sensitivity.df=ldply(c("0.2","0.4","0.6","0.8"),function(i) {
  ldply(unique(thresholds.df$Study),.progress="text",function(j) {
    #Subset data
    data=subset(thresholds.df,Study!=j & threshold==i)
    #Function to run models
    f=function(x) glmmPQL(no.fn.greater~richness*no.fn.random=~richness|Study,
                        family=quasipoisson(link="identity"),start=c(0.15,0.05,0.1,0.001),
                        control=lmeControl(opt="optim",msTol=1e-4),
                        verbose=F,data=x)
    #Run model, return NA if model fails
    safef=failwith(NA,f)
    mod=safef(data)
    #Extract coefficient and standard error and return in data.frame
    if(is.na(mod)) data.frame(Study.removed=j,threshold=i,coef=NA,coef.se=NA) else
      data.frame(
        Study.removed=j,
        threshold=i,
        coef=summary(mod)$tTable[2,1],
        coef.se=summary(mod)$tTable[2,2] )
  } )
})

rawmods.sensitivity.df$Ref.removed=thresholds.df[match(rawmods.sensitivity.df$Study,thresholds.df$Study),"Reference"]
rawmods.sensitivity.df$threshold=factor(rawmods.sensitivity.df$threshold)
levels(rawmods.sensitivity.df$threshold)=c("20%","40%","60%","80%")

#Plot results: 12" x 8"
ggplot(rawmods.sensitivity.df,aes(y=coef,x=Ref.removed,col=Ref.removed))+
  geom_hline(data=data.frame(
    threshold=c("20%","40%","60%","80%"),
    coef=c(summary(rawmods.list[[20]])$tTable[2,1],
           summary(rawmods.list[[40]])$tTable[2,1],
           summary(rawmods.list[[60]])$tTable[2,1],
           summary(rawmods.list[[80]])$tTable[2,1] ) ,
    aes(yintercept=coef),lwd=1,alpha=0.6,ltty=1)+
  geom_point(size=3)+
  geom_errorbar(aes(ymax=coef+2*coef.se,ymin=coef-2*coef.se))+
  coord_flip()+
  facet_wrap(~threshold,nrow=1)+
  labs(y="Regression coefficient",x="Study removed")+
  theme_bw(base_size=12)+
  theme(legend.position="none",panel.grid.major=element_blank(),panel.grid.minor=element_blank())

#####
#
# TURNOVER APPROACH
#
#####

#First, extract only mono data for each experiment and store in a list
mono.list=ldply(multifunc,c("Reference","Study","Expt","Smax","Sys1","FTG"),function(i) {
  #Get monocultures and metadata
  monos=i[,c(2:4,9,grep("mono",colnames(i)))]
  #Melt monos dataframe
  monos.melt=melt(monos,id.vars=c(1:4),measures.vars=c(5:ncol(monos)))
  #Split columns based on response (Y, N, SD, or ID)
  monos.melt=cbind(monos.melt[1:4],
                  t(matrix(unlist(strsplit(gsub("[0-9]+","\\1-",monos.melt$variable),"~"),nrow=2)),
                    value=monos.melt[, "value"]))
  names(monos.melt)[5:6]=c("treatment","variable")
  #Cast variables
  monos.cast=dcast(monos.melt,Study+Expt+Reference+Ydesc+treatment~variable,value.var="value")
  #Remove rows where Y=NA
  monos.cast=monos.cast[!is.na(monos.cast$Y),]
  #Convert responses to numeric
  monos.cast[,c("Y","SD","N")]=apply(monos.cast[,c("Y","SD","N")],2,as.numeric)
  #Return dataframe
  return(monos.cast)
})

#Determine the most extreme species for each function, then sum the number of unique most extreme species
#across all functions within an experiment
extremesp.df=ldply(mono.list,function(i) {
  data.frame(no.sp=length(unique(i$treatment)),no.fn=length(unique(i$Ydesc)),
             no.max.sp=length(unique(ddply(i,"Ydesc",function(x) x[which.max(x$Y),"ID"])$V1)),
             no.min.sp=length(unique(ddply(i,"Ydesc",function(x) x[which.min(x$Y),"ID"])$V1)) ) )
})

#Mean turnover in extreme species across all functions measured within an experiment

```

```

mean(extremesp.df$no.max.sp/extremesp.df$no.fn); std.error(extremesp.df$no.max.sp/extremesp.df$no.fn);
range(extremesp.df$no.max.sp/extremesp.df$no.fn)
mean(extremesp.df$no.min.sp/extremesp.df$no.fn); std.error(extremesp.df$no.min.sp/extremesp.df$no.fn);
range(extremesp.df$no.min.sp/extremesp.df$no.fn)

#Parse by system and trophic level
ddply(extremesp.df,"Sys1",function(x) data.frame(
  max.effect.size=mean(x$no.max.sp/x$no.fn),
  max.std.error=std.error(x$no.max.sp/x$no.fn),
  min.effect.size=mean(x$no.min.sp/x$no.fn),
  min.std.error=std.error(x$no.min.sp/x$no.fn) ) )

ddply(extremesp.df,"FTG",function(x) data.frame(
  max.effect.size=mean(x$no.max.sp/x$no.fn),
  max.std.error=std.error(x$no.max.sp/x$no.fn),
  min.effect.size=mean(x$no.min.sp/x$no.fn),
  min.std.error=std.error(x$no.min.sp/x$no.fn) ) )

#####
# AVERAGING APPROACH
#####

#Calculate average level of functioning across all functions for each treatment, for each experiment
multifunc.avg=ddply(multifunc.scaled,c("Reference","Study","Expt","FTG","Sys1","Sys2"),function(x) {
  z=data.frame(
    richness=colnames(x[,Y.colnames]),
    no.fn=length(unique(x$Ydesc)),
    avg.fn=colMeans(x[,Y.colnames]),
    avg.fn.SD=sqrt(
      colSums((x[,N.colnames]-1)*(x[,SD.colnames]^2),na.rm=T)/
      (colSums(x[,N.colnames],na.rm=T)-nrow(x[,N.colnames])) ),
    avg.fn.N=colSums(x[,N.colnames]) )
  #Remove rows where there is no response (i.e., avg.fn==NA)
  z=z[!is.na(z$avg.fn),]
  #Set richness by splitting column names
  z$richness=suppressWarnings(ifelse(grepl("mono",z$richness),1,as.numeric(gsub("X{[0-9]+}.*","\\1",z$richness))))
  return(z) } )

#Investigate proper functional form to use
#Group data for random effects
multifunc.avg.grouped=groupedData(avg.fn~richness|Study,data=multifunc.avg)
#Fit different functional forms using non-linear mixed models
Null=nlme(avg.fn~a,fixed=a~1,random=~a~1,start=c(a=0.2),data=multifunc.avg.grouped)
Linear=nlme(avg.fn~a+b*richness,fixed=a+b~1,random=~a+b~1,start=c(a=1.5,b=1),data=multifunc.avg.grouped)
Logarithmic=nlme(avg.fn~a+b*log(richness),fixed=a+b~1,random=~a+b~1,start=c(a=1,b=1),data=multifunc.avg.grouped)
Power=nlme(avg.fn~a*richness^b,fixed=a+b~1,random=~a+b~1,start=c(a=0.2,b=2),data=multifunc.avg.grouped)
Saturating=nlme(avg.fn~richness/(k+richness),fixed=k~1,random=k~1,start=c(k=1),data=multifunc.avg.grouped)
#Compare models using AIC
AIC(Null,Linear,Logarithmic,Power,Saturating)

#Fit log relationship using linear mixed effects model, allowing slopes and intercepts to vary by Study
avgmods.list=lapply(c("unweighted","variance","sample.size"),function(i) {
  #Subset dataset to include only non-NA data points for each type of analysis
  if(i=="variance") { multifunc.avg=multifunc.avg[!is.na(multifunc.avg$avg.fn.SD),]
  } else if(i=="sample.size") { multifunc.avg=multifunc.avg[!is.na(multifunc.avg$avg.fn.N),]
  } else { multifunc.avg }
  #Fit linear mixed effects model for each weighting scheme
  if(i=="unweighted") {
    mod=glmmPQL(avg.fn~log(richness),random=~richness|Study,family=quasibinomial(link="identity"),
      start=c(0.5,0),data=multifunc.avg,verbose=F)
  } else if(i=="variance") {
    mod=glmmPQL(avg.fn~log(richness),random=~richness|Study,weights=1/((multifunc.avg$avg.fn.SD^2)+0.01),
      family=quasibinomial(link="identity"),start=c(0.5,0),data=multifunc.avg,verbose=F)
  } else {
    mod=glmmPQL(avg.fn~log(richness),random=~richness|Study,weights=sqrt(multifunc.avg$avg.fn.N),
      family=quasibinomial(link="identity"),start=c(0.5,0),data=multifunc.avg,verbose=F) }
  #Return model
  return(mod)
} )
#Append reduced model (S <= 16)
avgmods.list=append(avgmods.list,list(update(avgmods.list[[1]],data=subset(multifunc.avg,richness<=16))) )
#Look at output and diagnostic plots
lapply(avgmods.list,summary); lapply(avgmods.list,plot)

#Extract predicted fits for plot
pred.df.list=lapply(seq_along(avgmods.list),function(i) {
  if(i<4) multifunc.avg=multifunc.avg else multifunc.avg=subset(multifunc.avg,!paste(Study,Expt) %in%
unique(paste(subset(multifunc.avg,richness>16)$Study,subset(multifunc.avg,richness>16)$Expt)))
#Modified from: http://glmm.wikidot.com/faq
#Create dataframe for predicted values for overall fit
newdata=expand.grid(richness=1:max(multifunc.avg$richness),no.fn=2:max(multifunc.avg$no.fn),avg.fn=0)
#Generate predicted values for overall trend
newdata$avg.fn=predict(avgmods.list[[i]],newdata,type="response",level=0)
#Obtain model matrix
mm=model.matrix(terms(avgmods.list[[i]]),newdata)

```

```

#Obtain estimate of SE based on fixed effects only
newdata$fixedSE=sqrt(diag(mm %*% tcrossprod(vcov(avgmods.list[[i]]),mm)))

#Create dataframe for predicted values for each study
newdata2=ldply(unique(multifunc.avg$Study),function(j)
  data.frame(Study=j,
    richness=1:max(subset(multifunc.avg,Study==j)$richness),
    no.fn=max(subset(multifunc.avg,Study==j)$no.fn) ) )
#Generate predicted values for each study
newdata2$avg.fn=predict(avgmods.list[[i]],newdata2,type="response",level=1)

#Return dataframes in a list
list(newdata,newdata2)
) )

#Plot predicted values and confidence bands across all studies on top of fitted values for each individual
study
avgplots.list=lapply(1:3,function(i) {
  ggplot()+
    #Plot raw points
    geom_point(data=multifunc.avg,aes(x=richness,y=avg.fn),size=2,col="grey60",alpha=0.5)+
    #Plot curves for each study
    geom_line(data=pred.df.list[[i]][[2]],aes(x=richness,y=avg.fn,group=Study),col="black",lwd=0.8,alpha=0.7)+
    #Add confidence band for mixed model predictions based on fixed effects only
    geom_ribbon(data=pred.df.list[[i]][[1]],
      aes(x=richness,y=avg.fn,ymax=avg.fn+2*fixedSE,ymin=avg.fn-2*fixedSE),
      fill="red",alpha=0.4)+
    #Add line for mixed model predictions
    geom_line(data=pred.df.list[[i]][[1]],aes(x=richness,y=avg.fn),col="red",lwd=1.5,alpha=0.9)+
    scale_x_continuous(breaks=c(1,20,40,60))+
    scale_y_continuous(limits=c(0,1.1),breaks=c(0,0.5,1))+
    labs(x="Richness",y="Average multifunctionality")+
    theme_bw(base_size=18)+
    theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank())
} )#; avgplots.list

#Plot figure 1 with inset from list above (5 x 4.5")
p1=ggplot(data=subset(multifunc.avg,!paste(Study,Expt) %in%
unique(paste(subset(multifunc.avg,richness>16)$Study,subset(multifunc.avg,richness>16)$Expt))),
  aes(x=richness,y=avg.fn))+
  #Plot raw points
  geom_point(size=2.5,col="grey60",alpha=0.3)+
  #Plot curves for each study
  geom_line(data=pred.df.list[[4]][[2]],aes(x=richness,y=avg.fn,group=Study),col="grey20",lwd=0.75,alpha=0.8)+
  #Add confidence band for mixed model predictions based on fixed effects only
  geom_ribbon(data=pred.df.list[[4]][[1]],
    aes(x=richness,y=avg.fn,ymax=avg.fn+2*fixedSE,ymin=avg.fn-2*fixedSE),
    fill="red",alpha=0.4)+
  #Add line for mixed model predictions
  geom_line(data=pred.df.list[[4]][[1]],aes(x=richness,y=avg.fn),col="red",lwd=2.5)+
  coord_cartesian(ylim=c(-0.05,1.1))+
  scale_x_continuous(breaks=c(1,4,8,12,16),labels=c("1","4","8","12","16"))+
  scale_y_continuous(breaks=seq(0,1,0.2))+
  labs(x="Richness",y="Average multifunctionality")+
  geom_text(data=data.frame(
    labels=letters[1]),
    aes(x=-Inf,y=Inf,label=labels),vjust=1.5,hjust=-1.5,col="black",fontface="bold",size=9)+
  theme_bw(base_size=18)+
  theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank())+
annotation_custom(grob=ggplotGrob(avgplots.list[[1]]+labs(x="",y="")+theme(plot.margin=unit(c(0,0,0,0),"cm"))),
  xmin=7,xmax=16,ymin=-0.075,ymax=0.385)

#####

#Look at diversity effects on single functions
#Rearrange scaled responses so they are in the same format as the averaged dataset
multifunc.single=data.frame(
  melt(multifunc.scaled,
    id.vars=c("Reference","Study","Expt","FTG","Sys1","Sys2","Ydesc"),
    measure.vars=c(Y.colnames)),
  fn.N=melt(multifunc.scaled,
    id.vars=c("Reference","Study","Expt","FTG","Sys1","Sys2","Ydesc"),
    measure.vars=c(N.colnames))[9],
  fn.SD=melt(multifunc.scaled,
    id.vars=c("Reference","Study","Expt","FTG","Sys1","Sys2","Ydesc"),
    measure.vars=c(SD.colnames))[9] )
names(multifunc.single)[9:11]=c("fn.mean","fn.N","fn.SD")
multifunc.single=multifunc.single[!is.na(multifunc.single$fn.mean),]
multifunc.single$richness=
  suppressWarnings(ifelse(grepl("mono",multifunc.single$variable),1,as.numeric(gsub("X([0-
9]+).*","\\1",multifunc.single$variable))))

#Fit linear mixed effects model allowing slopes and intercepts to vary by Study
singlemods.list=lapply(c("unweighted","variance"),function(i) { #,"sample.size"),function(i) {
  #Subset dataset to include only non-NA data points for each type of analysis

```

```

if(i=="variance") { multifunc.single=multifunc.single[!is.na(multifunc.single$fn.SD),]
} else if(i=="sample.size") { multifunc.single=multifunc.single[!is.na(multifunc.single$fn.N),]
} else { multifunc.single }
#Fit linear mixed effects model for each weighting scheme
if(i=="unweighted") {
  mod=glmmPQL(fn.mean~log(richness), random=~richness|Study/Ydesc, family=quasibinomial(link="identity"),
  start=c(0.5,0), control=lmeControl(msTol=1e-5, opt="optim"), data=multifunc.single, verbose=F)
} else if(i=="variance") {

mod=glmmPQL(fn.mean~log(richness), random=~richness|Study/Ydesc, weights=1/(multifunc.single$fn.SD^2)+0.01),
  family=quasibinomial(link="identity"), start=c(0.5,0), control=lmeControl(msTol=1e-
5, opt="optim"), data=multifunc.single, verbose=F)
} else {
  mod=glmmPQL(fn.mean~log(richness), random=~richness|Study/Ydesc, weights=sqrt(multifunc.single$fn.N),
  family=quasibinomial(link="identity"), start=c(0.2,0), control=lmeControl(msTol=1e-
5, opt="optim"), data=multifunc.single, verbose=F)
}
#Return model
return(mod)
} )
#Look at output and diagnostic plots
lapply(singlemods.list, summary); lapply(singlemods.list, plot)

#Extract predicted fits for plot
singlepred.df.list=lapply(seq_along(singlemods.list), function(i) {
#Modified from: http://glmm.wikidot.com/faq
#Create dataframe for predicted values for overall fit
newdata=expand.grid(richness=1:max(multifunc.single$richness),
  fn.mean=0)
#Generate predicted values for overall trend
newdata$fn.mean=predict(singlemods.list[[i]], newdata, type="response", level=0)
#Obtain model matrix
mm=model.matrix(terms(singlemods.list[[i]]), newdata)
#Obtain estimate of SE based on fixed effects only
newdata$fixedSE=sqrt(diag(mm %*% tcrossprod(vcov(singlemods.list[[i]]), mm)))

#Create dataframe for predicted values for each study
newdata2=ldply(unique(multifunc.single$Study), function(j) {
  ldply(unique(subset(multifunc.single, Study==j)$Expt), function(k) {
    expand.grid(Study=j, Expt=k,
      Ydesc=unique(subset(multifunc.single, Study==j)$Ydesc),
      richness=1:max(subset(multifunc.single, Study==j)$richness)) } ) } )
#Generate predicted values for each study
newdata2$fn.mean=predict(singlemods.list[[i]], newdata2, type="response", level=2)
newdata2$Ydesc=paste(newdata2$Ydesc, newdata2$Study, newdata2$Expt, sep=".")

#Return dataframes in a list
list(newdata, newdata2)
} )

#Plot predicted values and confidence bands across all studies on top of fitted values for each individual
study
singleplots.list=lapply(1:2, function(i) {
  ggplot()+
  #Plot raw points
  #geom_point(data=multifunc.single, aes(x=richness, y=fn.mean), size=2, col="grey60", alpha=0.5)+
  #Plot curves for each function
  # geom_line(data=singlepred.df.list[[i]][[2]], aes(x=richness, y=fn.mean, group=Ydesc),
  # alpha=0.3, lwd=0.8)+
  #Add confidence band for mixed model predictions based on fixed effects only
  geom_ribbon(data=singlepred.df.list[[i]][[1]],
    aes(x=richness, y=fn.mean, ymax=fn.mean+2*fixedSE, ymin=fn.mean-2*fixedSE),
    fill="red", alpha=0.3)+
  #Add line for mixed model predictions
  geom_line(data=singlepred.df.list[[i]][[1]], aes(x=richness, y=fn.mean), col="red", lwd=1.5, alpha=0.9)+
  scale_y_continuous(limits=c(0, 1.1), breaks=seq(0, 1, 0.2))+
  labs(x="Richness", y="Functioning (single functions pooled)")+
  theme_bw(base_size=18)+
  theme(panel.grid.major=element_blank(), panel.grid.minor=element_blank())
} )

#Plot with average multifunctionality
p2=ggplot()+
  geom_point(data=multifunc.single, aes(x=richness, y=fn.mean), size=2, col="grey60", alpha=0.5)+
  # geom_ribbon(data=pred.df.list[[1]][[1]],
  # aes(x=richness, y=avg.fn, ymax=avg.fn+2*fixedSE, ymin=avg.fn-2*fixedSE),
  # fill="red", alpha=0.4)+
  geom_ribbon(data=singlepred.df.list[[1]][[1]],
    aes(x=richness, y=fn.mean, ymax=fn.mean+2*fixedSE, ymin=fn.mean-2*fixedSE),
    fill="blue", alpha=0.3)+
  #Add line for mixed model predictions
  # geom_line(data=pred.df.list[[1]][[1]], aes(x=richness, y=avg.fn), col="red", lwd=1.5, alpha=0.9)+
  geom_line(data=singlepred.df.list[[1]][[1]], aes(x=richness, y=fn.mean), col="blue", lwd=1.5, alpha=0.9)+
  # scale_fill_manual(values=c("red", "blue"), name="")+
  coord_cartesian(ylim=c(-0.05, 1.1), xlim=c(-2, 62))+
  scale_x_continuous(breaks=c(1, 20, 40, 60))+
  scale_y_continuous(breaks=seq(0, 1, 0.2))+
  geom_text(data=data.frame(

```



```

      avg.fn=0)
#Generate predicted values for overall trend
newdata$avg.fn=predict(avgintmods.list[[i]],newdata,type="response",level=0)
#Obtain model matrix
mm=model.matrix(terms(avgintmods.list[[i]]),newdata)
#Obtain estimate of SE based on fixed effects only
newdata$fixedSE=sqrt(diag(mm %*% tcrossprod(vcov(avgintmods.list[[i]]),mm))
#Return dataframe
return(newdata)
} )

#Plot predicted values and confidence bands across all studies on top of fitted values for each individual
study
lapply(1:3,function(i) {
  ggplot()+
  #Plot raw points
  geom_point(data=multifunc.avg,aes(x=richness,y=avg.fn),size=2,col="grey60",alpha=0.5)+
  #Plot curves for each study
  #geom_line(data=pred.df.list[[i]][[2]],aes(x=richness,y=avg.fn,group=Study),alpha=0.75,lwd=1,alpha=0.75)+
  #Add confidence band for mixed model predictions based on fixed effects only
  geom_ribbon(data=predint.df.list[[i]],
    aes(x=richness,y=avg.fn,ymax=avg.fn+2*fixedSE,ymin=avg.fn-2*fixedSE,group=no.fn,fill=no.fn),
    alpha=0.15)+
  #Add line for mixed model predictions
  geom_line(data=predint.df.list[[i]],aes(x=richness,y=avg.fn,group=no.fn,col=no.fn),lwd=1.5,alpha=0.9)+
  scale_color_gradient(high="red",low="blue",name="Number of\nfunctions")+
  scale_fill_gradient(high="red",low="blue",name="Number of\nfunctions")+
  scale_y_continuous(breaks=seq(0,1,0.2))+
  labs(x="\nRichness",y="Average multifunctionality\n")+
  theme_bw(base_size=18)+
  theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank())
} )

#Extract effect sizes and their standard errors for each level of number of functions
avginteffect.df.list=lapply(avgintmods.list,function(i) {
  ldply(2:max(multifunc.avg$no.fn),function(j)
    data.frame(
      no.fn=j,
      Estimate=summary(i)$tTable["log(richness)","Value"]+j*summary(i)$tTable["log(richness):no.fn","Value"],
      Std.Error=sqrt(
        (summary(i)$tTable["log(richness)","Std.Error"]^2+summary(i)$tTable["log(richness):no.fn","Std.Error"]^2+
          2*i$varFix["log(richness)","log(richness):no.fn"]) ) )
  ) } )

#Plot number of functions against effect size
lapply(avginteffect.df.list,function(i) {
  ggplot(i,aes(x=no.fn,y=Estimate))+
  #Add points for effect sizes
  geom_point(size=4)+
  #And error bars for the standard errors
  geom_errorbar(aes(ymax=Estimate+2*Std.Error,ymin=Estimate-2*Std.Error),width=0)+
  #Specify axis breaks
  scale_x_continuous(breaks=c(2,4,6,8,10,12))+
  labs(x="\nNumber of functions",y="Diversity effect (+/- 95% CI)\n")+
  theme_bw(base_size=18)+
  theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank())
} )

#####
# MULTIPLICATIVE APPROACH
#####

#Calculate multiplicative level of functioning across all functions for each treatment, for each experiment
multifunc.mult=ddply(multifunc.scaled,c("Reference","Study","Expt","FTG","Sys1","Sys2"),function(x) {
  z=data.frame(
    richness=colnames(x[,Y.colnames]),
    no.fn=length(unique(x$Ydesc)),
    mult.fn=apply(x[,Y.colnames],2,prod),
    mult.fn.N=colSums(x[,N.colnames]) )
  #Remove rows where there is no response (i.e., mult.fn.scaled==NA)
  z=z[!is.na(z$mult.fn),]
  #Scale by nth root
  z$mult.fn.scaled=z$mult.fn^(1/nrow(x))
  #Set richness by splitting column names
  z$richness=suppressWarnings(ifelse(grepl("mono",z$richness),1,as.numeric(gsub("X{[0-9]+}.*","\\1",z$richness))))
  return(z) } )

#Investigate proper functional form to use
#Group data for random effects
multifunc.mult.grouped=groupedData(mult.fn.scaled~richness|Study,data=multifunc.mult)
#Fit different functional forms using non-linear mixed models
Null=nlme(mult.fn.scaled~a,fixed=a~1,random=~a~1,start=c(a=0.2),data=multifunc.mult.grouped)
Linear=nlme(mult.fn.scaled~a+b*richness,fixed=a+b~1,random=~a+b~1,start=c(a=1.5,b=1),data=multifunc.mult.grouped)
Logarithmic=nlme(mult.fn.scaled~a+b*log(richness),fixed=a+b~1,random=~a+b~1,start=c(a=1.5,b=1),data=multifunc.mult.grouped)

```

```

Power=nlme(mult.fn.scaled~a*richness^b,fixed=a+b~1,random=~a+b~1,start=c(a=0.2,b=2),data=multifunc.mult.groupe
d)
Saturating=nlme(mult.fn.scaled~richness/(k+richness),fixed=k~1,random=k~1,start=c(k=1),data=multifunc.mult.gro
uped)
#Compare models using AIC
AIC(Null,Linear,Logarithmic,Power,Saturating)

#Fit log relationship using linear mixed effects model, allowing slopes and intercepts to vary by Study
multmods.list=lapply(c("unweighted"),function(i) {
  #Subset dataset to include only non-NA data points for each type of analysis
  if(i=="variance") { multifunc.mult=multifunc.mult[!is.na(multifunc.mult$mult.fn.scaled.SD),]
  } else if(i=="sample.size") { multifunc.mult=multifunc.mult[!is.na(multifunc.mult$mult.fn.scaled.N),]
  } else { multifunc.mult }
  #Fit linear mixed effects model for each weighting scheme
  if(i=="unweighted") {
    mod=glmmPQL(mult.fn.scaled~log(richness),random=~richness|Study,family=quasibinomial(link="identity"),
               start=c(0.5,0),data=multifunc.mult,verbose=F)
  } else if(i=="variance") {

mod=glmmPQL(mult.fn.scaled~log(richness),random=~richness|Study,weights=1/((multifunc.mult$mult.fn.scaled.SD^2
)+0.01),
            family=quasibinomial(link="identity"),start=c(0.5,0),data=multifunc.mult,verbose=F)

  } else {

mod=glmmPQL(mult.fn.scaled~log(richness),random=~richness|Study,weights=sqrt(multifunc.mult$mult.fn.scaled.N),
            family=quasibinomial(link="identity"),start=c(0.5,0),data=multifunc.mult,verbose=F) }
  #Return model
  return(mod)
})
#Append reduced model (S <= 16)
multmods.list=append(multmods.list,list(update(multmods.list[[1]],data=subset(multifunc.mult,richness<=16))))
#Look at output and diagnostic plots
lapply(multmods.list,summary); lapply(multmods.list,plot)

#Extract predicted fits for plot
pred.df.list=lapply(seq_along(multmods.list),function(i) {
  if(i==1) multifunc.mult=multifunc.mult else multifunc.mult=subset(multifunc.mult,!paste(Study,Expt) %in%
unique(paste(subset(multifunc.mult,richness>16)$Study,subset(multifunc.mult,richness>16)$Expt)))
  #Modified from: http://glmm.wikidot.com/faq
  #Create dataframe for predicted values for overall fit

newdata=expand.grid(richness=1:max(multifunc.mult$richness),no.fn=2:max(multifunc.mult$no.fn),mult.fn.scaled=0
)
  #Generate predicted values for overall trend
  newdata$mult.fn.scaled=predict(multmods.list[[i]],newdata,type="response",level=0)
  #Obtain model matrix
  mm=model.matrix(terms(multmods.list[[i]]),newdata)
  #Obtain estimate of SE based on fixed effects only
  newdata$fixedSE=sqrt(diag(mm %*% tcrossprod(vcov(multmods.list[[i]]),mm))

  #Create dataframe for predicted values for each study
  newdata2=ldply(unique(multifunc.mult$Study),function(j)
    data.frame(Study=j,
               richness=1:max(subset(multifunc.mult,Study==j)$richness),
               no.fn=max(subset(multifunc.mult,Study==j)$no.fn) )
  #Generate predicted values for each study
  newdata2$mult.fn.scaled=predict(multmods.list[[i]],newdata2,type="response",level=1)

  #Return dataframes in a list
  list(newdata,newdata2)
})

#Plot predicted values and confidence bands across all studies on top of fitted values for each individual
study
avgplots.list=lapply(1,function(i) {
  ggplot()+
  #Plot raw points
  geom_point(data=multifunc.mult,aes(x=richness,y=mult.fn.scaled),size=2,col="grey60",alpha=0.5)+
  #Plot curves for each study

geom_line(data=pred.df.list[[i]][[2]],aes(x=richness,y=mult.fn.scaled,group=Study),col="black",lwd=0.8,alpha=0
.7)+
  #Add confidence band for mixed model predictions based on fixed effects only
  geom_ribbon(data=pred.df.list[[i]][[1]],
            aes(x=richness,y=mult.fn.scaled,ymax=mult.fn.scaled+2*fixedSE,ymin=mult.fn.scaled-2*fixedSE),
            fill="red",alpha=0.4)+
  #Add line for mixed model predictions
  geom_line(data=pred.df.list[[i]][[1]],aes(x=richness,y=mult.fn.scaled),col="red",lwd=1.5,alpha=0.9)+
  scale_x_continuous(breaks=c(1,20,40,60))+
  scale_y_continuous(limits=c(0,1.1),breaks=c(0,0.5,1))+
  labs(x="Richness",y="Average multifunctionality")+
  theme_bw(base_size=18)+
  theme(panel.grid.major=element_blank(),panel.grid.minor=element_blank())
})#; avgplots.list

#Plot figure 1 with inset from list above (5 x 4.5")
ggplot(data=subset(multifunc.mult,!paste(Study,Expt) %in%

```



```

unique(paste(subset(multifunc.mult, richness>16)$Study, subset(multifunc.mult, richness>16)$Expt)),
  aes(x=richness, y=mult.fn.scaled))+
#Plot raw points
geom_point(size=2.5, col="grey60", alpha=0.3)+
#Plot curves for each study

geom_line(data=pred.df.list[[2]][[2]], aes(x=richness, y=mult.fn.scaled, group=Study), col="grey20", lwd=0.75, alpha
=0.8)+
#Add confidence band for mixed model predictions based on fixed effects only
geom_ribbon(data=pred.df.list[[2]][[1]],
  aes(x=richness, y=mult.fn.scaled, ymax=mult.fn.scaled+2*fixedSE, ymin=mult.fn.scaled-2*fixedSE),
  fill="red", alpha=0.4)+
#Add line for mixed model predictions
geom_line(data=pred.df.list[[2]][[1]], aes(x=richness, y=mult.fn.scaled), col="red", lwd=2.5)+
coord_cartesian(ylim=c(-0.05, 1.1))+
scale_x_continuous(breaks=c(1, 4, 8, 12, 16), labels=c("1", "4", "8", "12", "16"))+
scale_y_continuous(breaks=seq(0, 1, 0.2))+
labs(x="Richness", y="Multiplicative multifunctionality")+
# geom_text(data=data.frame(
#   labels=letters[1]),
#   aes(x=-Inf, y=Inf, label=labels), vjust=1.5, hjust=-1.5, col="black", fontface="bold", size=9)+
theme_bw(base_size=18)+
theme(panel.grid.major=element_blank(), panel.grid.minor=element_blank()+

annotation_custom(grob=ggplotGrob(avgplots.list[[1]]+labs(x="", y="))+theme(plot.margin=unit(c(0, 0, 0, 0), "cm")))
,
  xmin=7, xmax=16, ymin=-0.075, ymax=0.385)

```

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