

1 **Supplemental details: Theory, models and Python code**

2

3 **Appendix 1: Rapid equilibration between air-saturated water surrounding newly**
4 **cavitated vessels**

5

6 **(1) Final equilibrium of gas pressure**

7 Henry's law states that the concentration C_G ($\text{mol}\cdot\text{L}^{-1}$) of a gas species 'G' dissolved in
8 water is in equilibrium with the partial pressure P_G^* of the gas species in air.

$$C_G = K_G P_G^* \quad (\text{A1.1})$$

9 , where K_G ($\text{mol}\cdot\text{L}^{-1}\cdot\text{atm}^{-1}$) is the Henry's law constant.

10 If this is dissolved in a finite volume of solution, $(1-\alpha)V$, then the number of moles
11 of solute n_s in solution is

$$n_s = (1 - \alpha)VC_G = (1 - \alpha)VK_G P_G^* \quad (\text{A1.2})$$

12 The two main gases in Eq. A1.2 are O_2 and N_2 with K_G values of 1.3×10^{-3} and 8.1×10^{-4}
13 respectively and the partial pressure of O_2 and N_2 in air are 0.21 and 0.78 atm. If a
14 fraction, α , of volume V is embolized and no additional air is added to the system then n_s
15 moles of gas will be divided into n_1 moles of gas in the cavitated volume and n_2 moles in
16 the water such that $n_s = n_1 + n_2$.

17 If P_G is the partial pressure of gas in the cavitated volume (αV) then the ideal gas law
18 can be used to yield

$$n_1 = \frac{\alpha V P_G}{RT} \quad (\text{A1.3})$$

19 , where RT = the gas constant times Kelvin temperature, and the number of moles in the
20 liquid will be given by

$$n_2 = (1 - \alpha)VK_G P_G \quad (\text{A1.4})$$

21 Equating Eq. A1.2 to A1.3 + A1.4 and solving for P_G yields Eq. 1 in the introduction.

$$P_G = \frac{(1 - \alpha)K_G P_G^*}{\alpha/RT + (1 - \alpha)K_G} \quad (\text{A1.5})$$

22 The atmosphere consists of about 78% nitrogen and 21% oxygen, hence the final
23 equilibrium bubble pressure should be the sum of the equilibrium pressure of nitrogen,
24 the equilibrium pressure of oxygen and a full vapor pressure, which is a function of

25 temperature (3.2 kPa at 298K).

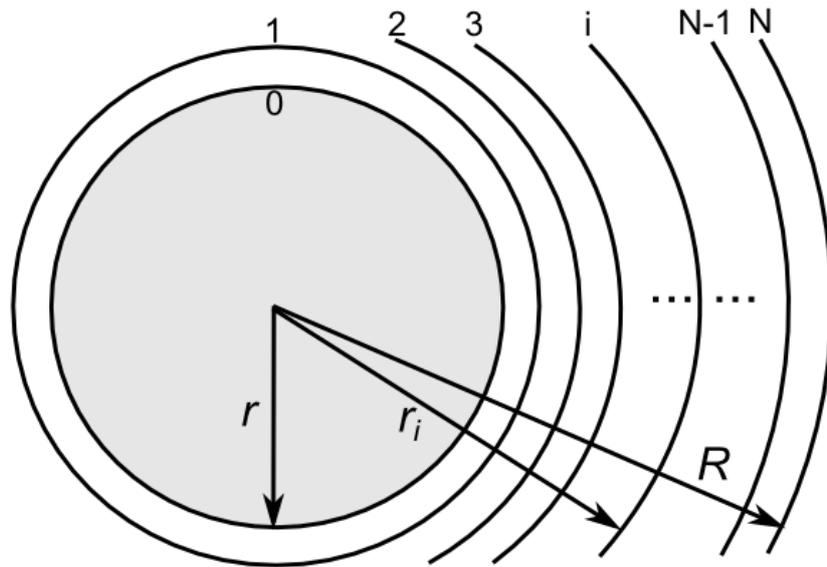
26

27 **(2) Diffusion time (cylindrical diffusion from bulk water)**

28 The tempo of approach to equilibrium Eq. A1.5 can be computed by Fick's Law, which
29 indicates that the radial diffusion rate of the gas species 'G' is proportional to the
30 concentration gradient where diffusion occurs:

$$J_G = 2\pi D_G \cdot \frac{C_2 - C_1}{\ln(b/a)} \quad (\text{A1.6})$$

31 , Eq. A1.6 describes the diffusion in a unit length of cylinder where J_G is the diffusion rate
32 in $\text{mol}\cdot\text{s}^{-1}$ per m of cylinder and D_G is the diffusion coefficient of gas; Eq. A1.6 describes
33 the diffusion in a cylinder, where C_2 and C_1 are the concentration at the cylindrical
34 surfaces with radius b and a , respectively (Crank, 1975).



35

36 **Figure S1.** Model of cylindrical diffusion in stem. R and r are the radius of water ($R =$
37 maximum radius) surrounding the vessel ($r =$ vessel radius) , where r_i is the external
38 radius of the i th layer of the N layers.

39

40 The cylinder was divided into N layers, each of which has a thickness of $\Delta x = (R -$
41 $r)/N$. The boundaries of the i th layer of water $[r_{i-1}, r_i]$ are $[r + (i - 1)\Delta x, r + i\Delta x]$; the

42 distance of half volume site of the layer to the center of the vessel, x_i , is $\sqrt{(r_{i-1}^2 + r_i^2)}/2$.

43 At a time interval Δt , the gas diffusion rate in mol s⁻¹ that diffuses out from the i th layer
44 to $i-1$ th layer will be:

$$\Delta n_i = 2\pi D_G \cdot \frac{C_{G,i} - C_{G,i-1}}{\ln(x_i/x_{i-1})} \cdot L \cdot \Delta t \quad (\text{A1.7a})$$

45 , where $C_{G,i}$ is the gas concentration of gas species 'G' in i th layer, which can be
46 computed by Eq. A1.1, and $C_{G,0}$ is the equilibrium gas concentration in the cavitated
47 vessel and L is an arbitrary length of the cylinder were diffusion occurs. Eq. A1.7 is used
48 to compute the stem increase in dissolved gas concentration in the i th cylindrical annulus
49 in Fig. S1. The concentration change at i th layer would be $(\Delta n_{i+1} - \Delta n_i)/V_i$, where $V_i =$
50 $2\pi(r_i^2 - r_{i-1}^2)L$ so when this equation is substituted into A1.7 the value of L cancels out
51 as does the 2π . So the equation for the increase in concentration in time step Δt is:

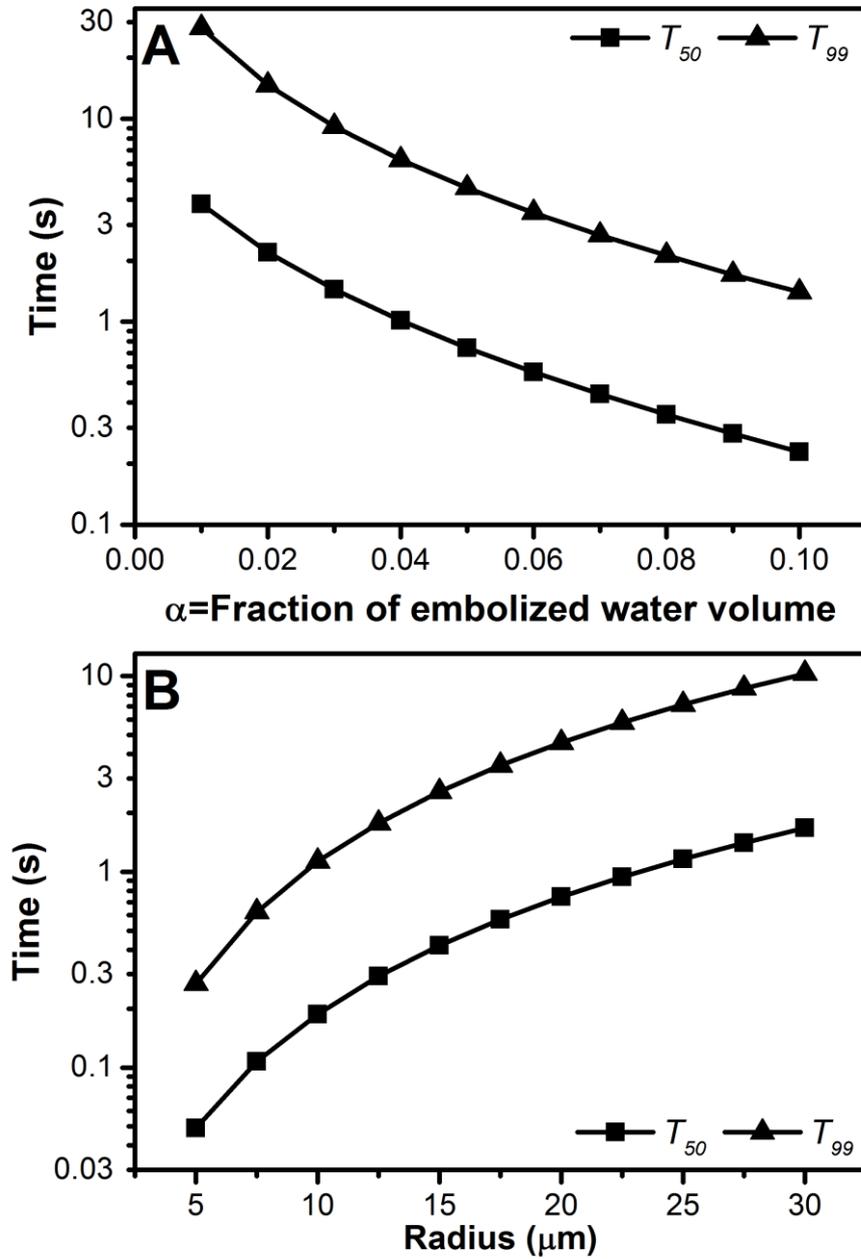
$$\Delta C_{G,i} = \frac{D_G \Delta t}{(r_i^2 - r_{i-1}^2)} \cdot \left[\frac{C_{G,i+1} - C_{G,i}}{\ln(x_{i+1}/x_i)} - \frac{C_{G,i} - C_{G,i-1}}{\ln(x_i/x_{i-1})} \right] \quad (\text{A1.7b})$$

52 For initial condition at time 0 it is assumed that the cavitated vessel is filled with
53 water vapor and the gases that were originally in the cavitated vessel before cavitation
54 event happen (1.2 kPa N₂ and 0.6 kPa O₂). Therefore the gas pressure can be estimated by
55 accumulating gas moles:

$$P_{G,t} = P_{G,t-\Delta t} + \frac{\Delta n_{1,t} RT}{2\pi r L} \quad (\text{A1.8})$$

56 , where P_t and $P_{t-\Delta t}$ represent the gas pressure of gas species 'G' at time t and $t - \Delta t$
57 respectively, $\Delta n_{1,t}$ is the gas moles exchange in a time interval Δt at the time t .

58 The air pressure in vessels results from the combined diffusion of O₂ and N₂ which
59 have different diffusion coefficients. Using an average vessel radius at 20 μm , the half
60 time (T_{50}) and 99% equilibrium time (T_{99}) can be calculated and is shown in Fig. S2A,
61 hence we can conclude that the initial bubble pressure can be reached in a short period of
62 time.



63

64 **Figure S2.** Relationship between α /radius and the half time and 99% equilibrium time.

65 T_{50} and T_{99} refer to the half time (solid square) and 99% equilibrium time (solid triangle),

66 respectively. Panel A: half time and 99% equilibrium time of the vessel with diameter of

67 20 μm when α range from 0.01 to 0.10. And in panel A α represents the fraction of

68 embolized water volume in the stem. Panel B: half time and 99% equilibrium time of the

69 vessel with diameter range from 5 to 30 μm when α is 0.05.

70

71 **(3) Mass flow from the biggest pit pore**

72 The following calculations demonstrate that mass flow of air through the biggest pit pore
 73 that seeds cavitation is very slow. According to the air-seeding hypothesis (Cochard et al.,
 74 1992; Sperry et al., 1996), an air bubble is pulled through the largest pit membrane pore
 75 connecting an embolized vessel to water-filled vessel. In this calculation let us assume the
 76 pore length, L , is 1 μm and the pore diameter, D , is 14.4 nm. A pore diameter this size
 77 would seed a cavitation at a tension of 2 MPa if the contact angle of the air-water
 78 interface with the pore wall is 0° and at lesser tension if the contact angle is $>0^\circ$. This
 79 calculation assumes the pore remains filled with air and that pneumatic flow of air occurs
 80 indefinitely driven by the pressure difference between one vessel filled with air at
 81 atmospheric pressure to a recently cavitated vessel initially at 0 pressure.

82 Poiseuille's law for pneumatic flow is:

$$F_x = \frac{\pi\rho}{128\eta} \cdot D^4 \cdot \frac{dP_x}{dL} \quad (\text{A1.9})$$

83 , where F_x is the mass flow rate ($\text{Kg}\cdot\text{s}^{-1}$), ρ is the density of air, η is the viscosity of air
 84 (which is nearly constant when $P_x < 500$ kPa). According to Cohen et al. (2003), the air
 85 conductivity can be computed by $C = \frac{QLP}{A\Delta P\bar{P}}$, where Q is the volume flow rate ($\text{m}^3\cdot\text{s}^{-1}$)
 86 1), L is the length of a pipe, A is the cross-section area of the pipe, P is the pressure where
 87 Q is measured, ΔP is the pressure difference across the pipe and \bar{P} is the average pressure
 88 which equals to the mean of pressures at the two ends of the pipe (P_{in} and P_{out} below). So
 89 the atmospheric volume flow rate $F_{V,x}$ will be:

$$F_{V,x} = \frac{\pi D^4}{256\eta P_{baro} L} \cdot (P_{out}^2 - P_{in}^2) \quad (\text{A1.10})$$

90 And the maximum flow rate $F_{V,max}$ will be the flow rate when P_{out} is P_{baro} and P_{in} is 0.
 91 And the volume of the vessel is $V_V = 0.25 \cdot \pi D_v^2 \cdot L_v$, where D_v and L_v are the diameter
 92 and length of the vessel. The average volumes of vessel lumen are $1.54\text{E-}11$ m^3 (*Acer*
 93 *mono*) and $5.94\text{E-}11$ m^3 (*Populus 84K*), and the maximum volume flow rate (at
 94 atmospheric pressure) are $2.89\text{E-}17$ $\text{m}^3\cdot\text{s}^{-1}$ for both species on the assumption of same pit
 95 pore size. So the half time for an vacuum-filled vessel to obtain a bubble pressure about
 96 50 kPa from the biggest pit pore will be $T_{half} = \ln 2 \cdot V_{vessel} / F_{V,max}$. And the T_{half} for an
 97 *Acer mono* vessel is about 3.1 days and T_{half} for a *Populus 84K* vessel is about 11.9 days.

98

99

100 **Appendix 2: The Hydraulic Recovery Model: a model for estimating bubble**
101 **pressure in vessels from measurements of stem k_h versus decreasing T_c in a cavitron.**

102 The case of bubble pressure equilibrium in a vessel without pressure gradient has been
103 discussed in Eq. 2 to 6 in the main paper. Below we discuss how the situation changes
104 when there is a pressure gradient. The primary problem is to arrive at computational code
105 that can transform Fig. 2 (the conductivity of a single vessel without a pressure gradient)
106 to Fig 3 (the conductivity of many vessels in a stem segment in an environment with a
107 quadratic pressure gradients), and also the case of linear positive pressure gradient. Linear
108 pressure gradients arise when a conductivity apparatus is used in conjunction with a
109 Sperry rotor whereas quadratic pressure gradients arise when measuring conductivity in a
110 spinning Cochard rotor.

111 Once a computational algorithm is achieved for getting a stem segment conductivity,
112 k_h , at any given initial bubble pressure (P_b^*) assigned at a high T_c values, the next step is
113 use a curve fitting algorithm with root mean square error (E_{rms}) calculations to arrive at
114 the value of P_b^* that best fits (minimizes E_{rms}) experimental data of k_h versus T_c for all the
115 lower values of T_c during an experiment like those shown in Figs. 7 and 8.

116

117 **(1) Pressure equilibrium between water and air in a single vessel with superimposed**
118 **pressure gradient**

119 In a centrifuge, there can be a static pressure gradient without flow of water wherein
120 the most negative pressure occurs at the axis of rotation, and the pressure falls as a
121 quadratic function of distance from the center ($P_w = \frac{x^2 - R^2}{R^2} \cdot T_c + P_{baro}$, where x is the
122 distance to the rotation axis). The centrifugal force will push the air bubble to the rotation
123 axis hence the water will flow into the distal end of the vessel when $P_w + P_c > P_b$. In a
124 conductivity apparatus (gravity flow system or flow meter), the water pressure will
125 decrease linearly with distance in a stem and the bubble will tend to be oriented with the
126 bubble at the low-pressure end of the vessel. However bubbles can 'stick' in small pipes

127 by a process similar to the static coefficient of friction so the bubble could be anywhere in
 128 the vessel although for simplicity it is illustrated at the low pressure end of the vessel.

129 In an embolized vessel that is filled with an air bubble at a pressure of P_b^* under high
 130 tension in centrifuge, the bubble will collapse when the tension is decreased and the
 131 pressure equilibrium is achieved as shown in Fig. S3, where the meaning of R_{dv} and L_w is
 132 defined. At any given pressure gradient, the water and bubble lengths (or volumes) in the
 133 cavitated vessel finally equilibrate. The water pressure can be computed by a quadratic
 134 function in Cavitron system and from a linear function in a conductivity apparatus; the
 135 bubble pressure can be obtained by applying the ideal gas law as in Eq. 2. Eq. A2.2a gives
 136 the linear pressure gradient in a conductivity apparatus, and Eq. A2.2b gives the quadratic
 137 pressure gradient in a cavitron.

$$P_w = P_0 - \lambda L_w \quad (A2.2a)$$

$$P_w = P_{baro} + \left(\frac{(R_{dv} - L_w)^2}{R^2} - 1 \right) \cdot T_C \quad (A2.2b)$$

138 , where λ is the coefficient of the pressure gradient, R is the maximum distance from the
 139 water level to the axis of rotation, P_w is the water pressure at the air/water interface at
 140 final equilibrium. The air bubble in the vessels are compressed hence the bubble pressure
 141 at final equilibrium P_b can be derived by the ideal gas law:

$$P_b = \frac{L_v}{L_v - L_w} \cdot P_b^* \quad (A2.3a)$$

142 . However, we have to take the air re-dissolved into the surrounding water as discussed in
 143 the main body. The equilibrium bubble pressure should be:

$$P_b = \frac{(1 - \alpha) \cdot K_A + \alpha/RT}{(1 - \alpha + \alpha \cdot L_w/L_v) \cdot K_A + \alpha \cdot L_b/L_v/RT} \cdot P_b^* \quad (A2.3b)$$

144 where K_A is the Henry's Law constant for air and RT is the gas constant times Kelvin
 145 temperature. Therefore the final equilibrium in two systems can be given by:

$$P_0 - \lambda L_w + P_C = P_b \quad (A2.4a)$$

$$P_{baro} + \left(\frac{(R_{dv} - L_w)^2}{R^2} - 1 \right) \cdot T_C + P_C = P_b \quad (A2.4b)$$

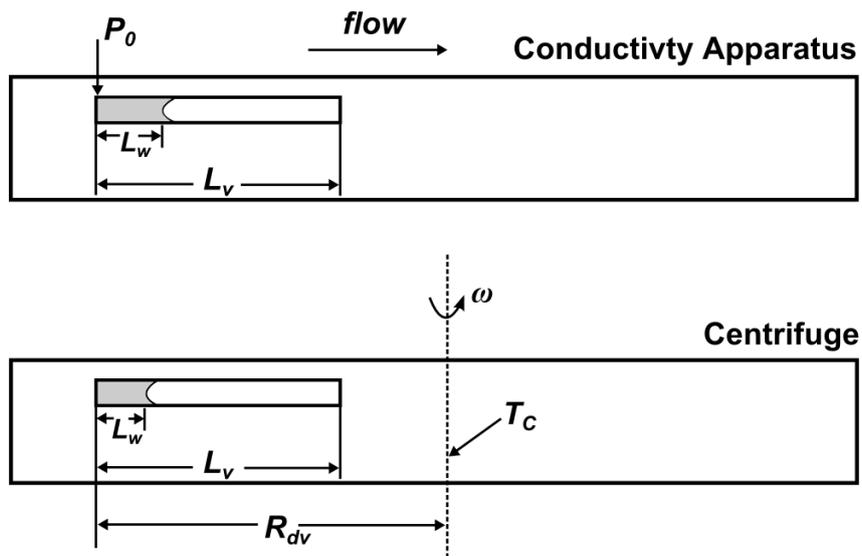
146 , where P_C is the capillary pressure computed by Eq. 3a. Here Eq. A2.4a and A2.4b show
 147 the equilibrium of a vessel in Flow Meter system and Cavitron system, respectively.

148 Both the water pressure and bubble pressure are functions of L_w , hence we can solve

149 the functions to get the exact value of L_w . Newton iteration (details can be found on
 150 Wikipedia) is used to solve Eq. A2.4a and A2.4b to get the L_w in any given vessel location
 151 in a conductivity apparatus or centrifuge by assuming initial water length $L_{w,0} = 0$ and a
 152 function of $f(L_w) = P_w - P_b$ at the beginning and then:

$$L_{w,i} = L_{w,i-1} + f(L_{w,i-1})/f'(L_{w,i-1}) \quad (\text{A2.5})$$

153 , where $L_{w,i}$ and $L_{w,i-1}$ are the length of water at i th iteration, and L_w can be gained when
 154 $L_{w,i} = L_{w,i-1}$. When pressure gradient $\lambda = 0$ and $P_0 = P_{baro}$ in a conductivity apparatus, L_w
 155 can be calculated by Eq. A2.4b with the value of $T_C = 0$, and this is how the Sperry PLC
 156 is simulated in Table I in the main body. Therefore, with Eq. A2.4 we are able to compute
 157 any pressure equilibrium of a vessel at any vessel that begin at a known slice that is R_{dv}
 158 far from the rotation axis, and hence to calculate the resistance of a cavitated vessel by
 159 Eq. 5.



160
 161 **Figure S3.** Model of water/air interface equilibrium in a single vessel. The upper panel
 162 shows equilibrium of a vessel in a stem connected to a conductivity apparatus while the
 163 lower panel shows equilibrium of vessel in a stem spun in a centrifuge. L_w and L_v
 164 represent the length of water and vessel, respectively. In the upper panel, P_0 is the water
 165 pressure at the upstream end of the vessel, and the pressure difference gradient is λ in
 166 $kPa \cdot m^{-1}$; and the water finally equilibrates with bubble as in Eq. A2.4a. In the lower panel,
 167 the central tension of the stem is T_C from angular speed ω , and the distance between the
 168 distal end of the vessel and the axis of rotation is R_{dv} ; and water equilibrates with bubble

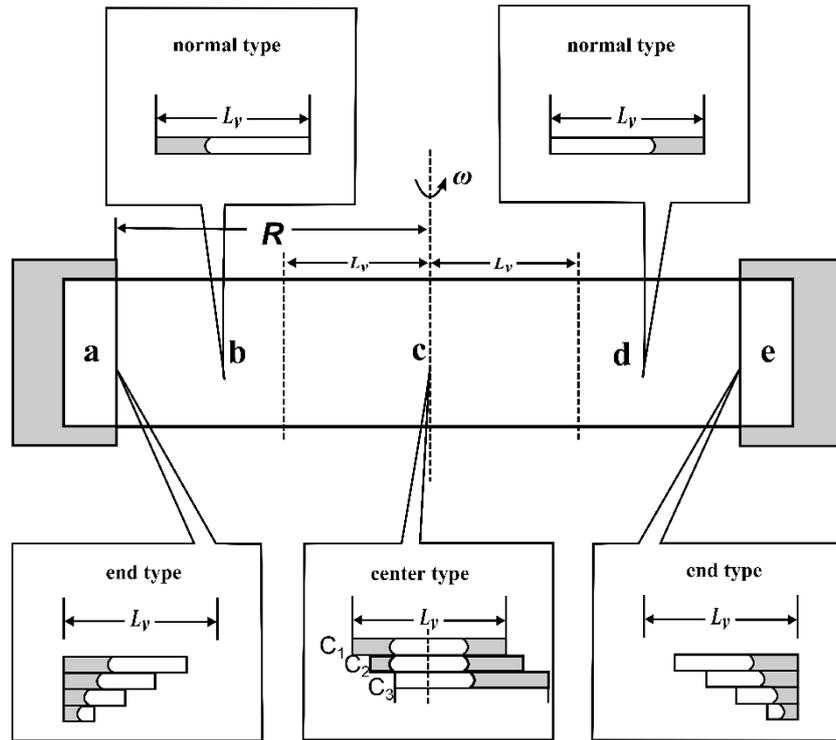
169 as in Eq. A2.4b.

170 **(2) Random vessel distribution and different equilibrium types**

171 Vessels that are located in different places have different water pressure at the air/water
172 interface and different bubble-length, so they have different final pressure equilibriums.
173 Vessels are randomly distributed in stem such that any cross-section has the same
174 possibility of vessel ends, vessel length distribution and vessel diameter. To make it
175 simple, average vessel length and average vessel diameter were used to build the model
176 instead of vessel-length distributions and vessel-diameter distributions.

177 As discussed above, in those vessels off the axis, bubbles are pushed towards the
178 center because of the centrifugal force; but in those vessels that extend across the axis,
179 water may enter from both ends and force bubble aggregate in the center as shown in Fig.
180 S4. Air bubbles cannot exist in the sections of the stem immersed in water filled cuvettes
181 (region a and e in Fig. S4). In our model the stem is divided into 5 parts: a, b, c, d and e as
182 shown in Fig. S4; where a & e are immersed in water, c is the central region with length
183 $2L_v$, and b & d are the remaining parts. When equilibriums are obtained in a Cavitron
184 system, different computational algorithms apply based on different regions because of
185 the vessel distribution. However, situation is simpler when segments are measured in a
186 conductivity apparatus since bubbles tend to be pushed to the low-pressure ends, and
187 hence Eq. A2.4a applies to the whole embolized segment.

188 In the Cavitron system, (1) in regions a and e, no air-seeding embolism can develop;
189 (2) in regions b and d, equilibrium in normal type vessel can be given by Eq. A2.4b while
190 end type vessel can be assumed as a normal type vessel with a shorter vessel length; (3) in
191 region c, vessels can obtain equilibrium from one end just like the vessels in regions b/d,
192 like vessel C_3 in Fig. S4; and can obtain equilibriums from both ends like vessels C_1 and
193 C_2 in Fig. S4, and in this case the bubble length in these vessels is same as vessels that are
194 symmetrically bisected by the rotation axis as vessel C_1 in Fig. S4. And the vessels like C_1
195 can be treated as two normal type vessels with length of $L_v/2$.



196

197 **Figure S4** Model of stem divided into 5 regions and three types of cross-section. Five
 198 regions (a, b, c, d and e) are divided by the location and stature of vessels as described in
 199 Appendix 2.2. Three types of vessels (end, normal and center type) are defined based on
 200 the vessel location in any given slice. End type vessels are those that are open to the a/e
 201 boundaries, normal type vessels are those that locate between a/e boundaries and rotation
 202 axis, and center type vessels are those that cross the center.

203

204 (3) Stem model: adding up the resistances

205 Resistance of stem could be computed as $R_S = \sum R_{dx} dx$, where R_{dx} is the resistance of a dx -
 206 thick cross-section from the stem. To make it easy to understand, we use the average
 207 hydraulic recovery ratio of all the embolized vessels that pass through the slice to
 208 represent the hydraulic recovery ratio in the slice: $k = \sum k_i / N$, where k_i is the hydraulic
 209 recovery ratio of the i th vessel and N is the total number of vessels. So vessels are divided
 210 into three different type: end, normal and center types as described in Fig. S4.

211 Therefore, when equilibrium is obtained in end type vessels, the embolized vessel
 212 will recover its conductance by a ratio of $k = \frac{2l_w l_v}{l_w^2 + l_v^2}$ (which follows from Eq. 5 in the main
 213 body), and here $l_v < L_v$ and l_w can be computed by Eq. A2.5. When equilibrium is obtained

214 in normal type vessel, embolized vessel recover its conductance by a ratio of $k = \frac{2l_w l_v}{l_w^2 + l_v^2}$,
 215 and here l_v is the average vessel length L_v and l_w is computed by Eq. A2.5. In those center
 216 type vessels where equilibrium can only occur from one end, embolized vessels recover
 217 conductance by the ratio of $k = \frac{2l_w l_v}{l_w^2 + l_v^2}$, here l_v is the average vessel length L_v and l_w is
 218 computed by Eq. A2.5. And in these center type vessels where equilibrium can occur
 219 from both ends, embolized vessels recover conductance by a ratio of $k = \frac{2l_w l_v}{l_w^2 + l_v^2}$, and here
 220 l_v should be $L_v/2$ and l_w should be computed by using $L_v/2$ as vessel length as described
 221 above. When equilibrium occurs from both ends in the vessels that are a little off the axis
 222 like vessel C₂, we can find that the length of bubble should be the same hence the
 223 resistance of the vessel should be the same with that of C₁, where the whole-length
 224 vessels behave like two vessels with length of $L_v/2$ that behave like normal type vessels
 225 that locate in b/d region, therefore the pressure equilibrium of a half-length vessel was
 226 used to represent the final equilibrium in center type vessels where equilibrium
 227 establishes from both ends.

228 In the slices in b/d, some of the vessels are open to the boundaries of a/e hence
 229 partial length vessels are used to compute hydraulic recovery ratio, together with the full
 230 length vessels to compute the average k . In the slices in c, some of the vessels are open to
 231 the center, hence equilibrium is able to form in two ends in which case can be treated as
 232 vessel C₁ in Fig. S4; and those vessels that are off the center and those that cross the
 233 center but with equilibrium only at one end can be treated as normal type vessels and
 234 share the same equation to compute k . And in this way, every embolized vessel that cross
 235 a given slice can be computed and then average k can be derived.

236 In a partly embolized stem, only $\varepsilon = n/N$ of the vessels out of a cross-section are
 237 cavitated or embolized (n is the number of cavitated/embolized vessels and N is the total
 238 number of all the vessels), and it was assumed that all vessels are of the same diameter
 239 and length. When water/air interfaces equilibrate with bubbles, the fraction of non-
 240 embolized vessels $(1-\varepsilon)$ are fully conductive while the fraction of embolized vessels (ε)
 241 recover their conductivity by a ratio of k , and hence the conductivity of the slice is
 242 $[(1 - \varepsilon) + k\varepsilon] \cdot k_{h,0}$, where $k_{h,0}$ is the conductivity of the slice with no embolism; and the

243 resistance of the cavitated vessels will drop as calculated from Eq. 5 and the resistance of
244 the slice will be computed by:

$$R_{dx} = \frac{1}{(1 - \varepsilon) + k\varepsilon} \cdot R_0 \quad (\text{A2.6})$$

245 , where R_0 is the resistance of the dx -thick slice when stem is fully conductive. Here
246 resistance rather than conductance is used because resistance can be added up directly in a
247 series of slices.

248 With the description above, the resistance of every dx -thick could be computed to
249 add up to the overall resistance of the stem by Eq. A2.6. We sacrifice some of the
250 accuracy of the model output in order to simplify some of the calculations and save
251 computational time which is currently about 20 minute per curve fitting. Future models
252 are worth developing with fewer sacrifices.

253 After all the resistances of dx -thick slices are calculated and added up at a given
254 tension, the total resistance of the stem is used to obtain the k_h of the whole stem under
255 different tensions by:

$$R_S = \sum R_{dx} \quad (\text{A2.7a})$$

$$k_h = \frac{R_{S,0}}{R_S} k_{max} \quad (\text{A2.7b})$$

256 , where $R_{S,0}$ is the resistance of the fully conductive stem, and k_{max} is the maximum
257 hydraulic conductivity of the stem.

258 *PLC* distribution in stems from centrifuges has been studied at slightly above
259 atmospheric pressure (Cai et al., 2010), but how *PLC* is distributed in segments spinning
260 in a rotor remains unknown because the bubble pressure of air in vessels in the
261 experimental conditions of Cai et al. (2010) is unknown. In this paper the fraction of
262 embolized vessels (ε) is assumed to be evenly distributed in stem between two reservoirs,
263 hence we assigned the same ε values in sections b, c and d under high tension while a and
264 e sections remain non-embolized ($\varepsilon=0$). In the second paper of this series other
265 distributions are considered and used to check how much the hydraulic recovery curve
266 could be influenced by different distributions of ε in stems spun in centrifuges.

267 In summary, the model assumes that (1) vessel length and vessel diameter were the

268 same in every vessel in the stem, (2) bubble pressure was the same in every cavitating
269 vessel under high tension, (3) embolized vessel fraction ($\varepsilon = n/N$) was evenly distributed
270 in b, c and d parts, and (4) contact angle in vessels was assigned to 45° ($\pi/4$), which
271 ranges from 42° to 55° (Zwieniecki and Holbrook, 2000). Based on these assumptions,
272 the hydraulic recovery model is accomplished by: (1) calculated the resistance of a dx -
273 thick slice, (2) added up the resistances of the stem, (3) computed hydraulic conductivity
274 from resistances, and (4) calculate how hydraulic conductivity changes with decreasing
275 tension.

276 The model was coded and run in Python(x,y) 2.7.5, the code can be found in the
277 supplemental python script in Appendix 3.

278

279 **Appendix 3: Python code of the Model**

280 Note: The sentences after '#' are code descriptions, which will not run in python compiler. And to make it easy to read, we use a monospace font
281 "Consolas" and landscape layout.

282

```
283 # range of central tension from 0.0 to 5.0 MPa
```

```
284 center_tension = []
```

```
285 tmpension = 0.0
```

```
286 while(tmpension <= 5.0):
```

```
287     center_tension.append(tmpension)
```

```
288     tmpension += 0.01
```

289

```
290 KCP_0 = 1.30E-3 #mol.L-3.atm-1
```

```
291 KCP_N = 6.10E-4
```

```
292 KCP_A = 0.80*KCP_N + 0.2*KCP_0
```

```
293 RT = 298.0 * 0.0821 # atm.L.mol-1
```

294

```
295 def find_x(l,ct,bs):
```

```
296     x = 0
```

```
297     count = 0
```

```
298     if (bs ** 2 / 0.127 ** 2 -1) * 1000 * ct + 100 + cp > BP:
```

```
299         while 1:
```

```
300             count = count + 1
```

```
301             if(count >=20):
```

```
302                 x = 1
```

```
303                 break
```

```
304             fr = x / l
```

```

305     fwt = 1.0 - center_PLC/100.0/10.0
306     fbt = center_PLC/100.0/10.0
307     fwe = fr*fbt + fwt
308     fbe = fbt*(1.0-fr)
309     funcKt = KCP_A*fwt + fbt/RT
310     funcKe = KCP_A*fwe + fbe/RT
311     EquilP = BP * funcKt/funcKe
312     # judge here is Pw+Pc-Pb
313     judge = ((abs(bs) - x) ** 2 / 0.127 ** 2 -1) * ct * 1000.0 + 100.0 + cp - EquilP
314     # slope here is the slope of "judge" at x
315     slope = - ct * 1000.0 / 0.127 ** 2 * 2.0 * (abs(bs) -x) + BP*funcKt/(funcKe**2) * (fbt/l*KCP_A -
316 fbt/RT/l)
317     # Newton Iteration
318     x = x - judge / slope
319     #print judge,slope,x
320     if (abs(judge) < 0.0001):
321         # To judge when to stop
322         break
323     # A Statement to avoid overflow
324     if x >= 1 or x < 0:
325         x = 1/1.2
326     return x
327 # A function to compute the resistance of the embolized vessels at any given slice
328 def drawf_PLC(ct,vl):
329     # Begin the slice array from the distal end of region a by the thickness of 0.001 m
330     site = -0.137

```

```

331     dsite = 0.001
332     # Stop after the last slice at 0.137 m
333     while(site < 0.138):
334         # The resistance of slices in a/e is constant R0, we use R0=1.0
335         if(abs(site) > 0.127):
336             NEWR.append(1.0)
337             OLDR.append(1.0)
338         # The resistance of slices of end and normal type
339         elif(abs(site) >= v1):
340             klist = []
341             ith = 1
342             while(ith <= 100):
343                 tmpml = ith*0.01*v1 + 0.127-abs(site)
344                 if(tmpml > v1):
345                     tmpml = v1
346                     tmpbs = abs(site) - (v1 - ith*0.01*v1)
347                     tmpwl = find_x(tmpml,ct,tmpbs)
348                     tmpki = 2.0*tmpml*tmpwl / (tmpml**2 + tmpwl**2)
349                     klist.append(tmpki)
350                 else:
351                     tmpwl = find_x(tmpml,ct,0.127)
352                     tmpki = 2.0*tmpml*tmpwl / (tmpml**2 + tmpwl**2)
353                     klist.append(tmpki)
354                 ith += 1
355             kr = numpy.mean(klist)
356             NRdx = 100.0 / ((100.0-center_PLC) + kr*center_PLC)

```

```

357         ORdx = 100.0 / (100.0-center_PLC)
358         NEWR.append(NRdx)
359         OLDR.append(ORdx)
360     # The resistance of slices in region c
361     else:
362         klist = []
363         ith = 1
364         while(ith <= 100):
365             tmpml = vl
366             tmpbs = max(abs(site)+vl-ith*0.01*vl,abs(abs(site)-ith*0.01*vl))
367             tmpes = min(abs(site)+vl-ith*0.01*vl,abs(abs(site)-ith*0.01*vl))
368             if(abs(tmpbs) < vl):
369                 # A judgement use to judge whether the equilibrium establish from both ends
370                 ljjudge = vl / (2*tmpes) * BP
371                 # Patm = 100.0, Tension in MPa
372                 rjudge = cp + ((tmpes/0.127)**2 - 1.0)*ct*1000.0 + 100.0
373                 if(ljjudge >= rjudge):
374                     # When the slice is normal type slice
375                     tmpwl = find_x(vl,ct,tmpbs)
376                     tmpki = 2.0*tmpml*tmpwl / (tmpml**2 + tmpwl**2)
377                     klist.append(tmpki)
378                 else:
379                     # When the slice is center type slice
380                     tmpwl = 2.0 * find_x(vl/2.0,ct,vl/2.0)
381                     tmpki = 2.0*tmpml*tmpwl / (tmpml**2 + tmpwl**2)
382                     klist.append(tmpki)

```

```

383         else:
384             tmpwl = find_x(vl,ct,tmpbs)
385             tmpki = 2.0*tmpml*tmpwl / (tmpml**2 + tmpwl**2)
386             klist.append(tmpki)
387             ith += 1
388             kr = numpy.mean(klist)
389             NRdx = 100.0 / ((100.0-center_PLC) + kr*center_PLC)
390             ORdx = 100.0 / (100.0-center_PLC)
391             NEWR.append(NRdx)
392             OLDR.append(ORdx)
393             site += dsite
394
395 # Main Body of the Code
396 # cp here is actually capillary pressure
397 # Here we use lists to store the values of each parameter
398 cps = [7.0,]
399 vessel_lengths = [0.04,]
400 filenames = ["/Test.txt",]
401 Kmaxs = [1.0E-4,]
402 cPLCs = [50.0,]
403 BPs = [50.0,]
404 # main part
405 for i in range(len(filenames)):
406     # Assign the parameters!
407     OLDR = []
408     NEWR = []

```

```
409     savefilename = filenames[i]
410     kmax = Kmaxs[i]
411     center_PLC = cPLCs[i]
412     BP = BPs[i]
413     cp = cps[i]
414     vessel_length = vessel_lengths[i]
415     savefile = open(savefilename,"w+")
416     savefile.write("Tension\tKh\tPLC\n")
417     # Here we give a limit to vessel length to avoid overflow
418     if vessel_length < 0.127:
419         #cycle through center tensions
420         for tension in center_tension:
421             # Clear OLDR,NEWL in each cycle
422             OLDR = []
423             NEWL = []
424             # Compute the resistance in 275 slices
425             drawf_PLC(tension,vessel_length)
426             tmpkh = kmax * (274.0 / sum(NEWL))
427             tmpplc = 100.0 - 100.0*(274 / sum(NEWL))
428             tmpstr = str(tension) + "\t" + str(tmpkh) + "\t" + str(tmpplc)
429             print tmpstr
430             savefile.write(tmpstr + "\n")
431 # Save the output results and close the file
432 savefile.close()
```

433 **LITERATURE CITED**

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