**Pse-in-One:** a web server for generating various modes of pseudo components of DNA, RNA, and protein sequences

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**Home-page**:<http://bioinformatics.hitsz.edu.cn/Pse-in-One/>







# **Content**



# <span id="page-2-0"></span>**1. DNA**

# <span id="page-2-1"></span>**1.1 Deoxyribonucleic acid composition**

## <span id="page-2-2"></span>**1.1.1 Basic kmer (Kmer)**

Basic kmer [\(1\)](#page-27-2) is the simplest approach to represent the DNAs, in which the DNA sequences are represented as the occurrence frequencies of *k* neighboring nucleic acids. This approach has been successfully applied to human gene regulatory sequence prediction [\(2,](#page-27-3)[3\)](#page-27-4), enhancer identification [\(1\)](#page-27-2), etc.

#### <span id="page-2-3"></span>**1.1.2 Reverse complementary kmer (RevKmer)**

The reverse complementary kmer  $(2,3)$  $(2,3)$  is a variant of the basic kmer, in which the kmers are not expected to be strand-specific, so reverse complements are collapsed into a single feature. For example, if *k*=2, there are totally 16 basic kmers ('AA', 'AC', 'AG', 'AT', 'CA', 'CC', 'CG', 'CT', 'GA', 'GC', 'GG', 'GT', 'TA', 'TC', 'TG', 'TT'), but by removing the reverse complementary kmers, there are only 10 distinct kmers in the reverse complementary kmer approach ('AA', 'AC', 'AG', 'AT', 'CA', 'CC', 'CG', 'GA', 'GC', 'TA'). For more information of this approach, please refer to [\(2,](#page-27-3)[3\)](#page-27-4).

## <span id="page-2-4"></span>**1.2 Autocorrelation**

#### <span id="page-2-5"></span>**1.2.1 Dinucleotide-based auto covariance (DAC)**

Suppose a DNA sequence **D** with *L* nucleic acid residues; i.e.

$$
\mathbf{D} = \mathbf{R}_1 \mathbf{R}_2 \mathbf{R}_3 \mathbf{R}_4 \mathbf{R}_5 \mathbf{R}_6 \mathbf{R}_7 \cdots \mathbf{R}_L
$$
 (1)

where  $R_1$  represents the nucleic acid residue at the sequence position 1,  $R_2$  the nucleic acid residue at position 2 and so forth.

The DAC [\(4-6\)](#page-27-5) measures the correlation of the same physicochemical index between two dinucleotides separated by a distance of *lag* along the sequence, which can be calculated as:<br>  $\text{DAC}(u, lag) = \sum_{i=1}^{L-lag-1} (P_u(\text{R}_i\text{R}_{i+1}) - \overline{P}_u)(P_u(\text{R}_{i+lag}\text{R}_{i+lag+1}) - \overline{P}_u)/(L-lag-1)$ calculated as: *L lag* eotides separated by a distance of *lag* along the sequence, which<br>as:<br> $u, lag$  =  $\sum_{i=1}^{L-lag-1} (P_u(R_iR_{i+1}) - \overline{P}_u)(P_u(R_{i+lag}R_{i+lag+1}) - \overline{P}_u)/(L-lag)$ separated by a distance of *lag* along the sequence, which can be<br>=  $\sum_{i=1}^{L-lag-1} (P_u(R_iR_{i+1}) - \overline{P}_u)(P_u(R_{i+lag}R_{i+lag+1}) - \overline{P}_u)/(L-lag-1)$  (2)

ulated as:  
\n
$$
DAC(u, lag) = \sum_{i=1}^{L-lag-1} (P_u(R_iR_{i+1}) - \overline{P}_u)(P_u(R_{i+lag}R_{i+lag+1}) - \overline{P}_u)/(L-lag-1)
$$
\n(2)

where *u* is a physicochemical index, *L* is the length of the DNA sequence,  $P_u(R_iR_{i+1})$ means the numerical value of the physicochemical index *u* for the dinucleotide  $R_iR_{i+1}$ at position  $i$ ,  $P_u$  is the average value for physicochemical index  $u$  along the whole sequence:

$$
\overline{P_u} = \sum_{j=1}^{L-1} P_u(\mathbf{R}_j \mathbf{R}_{j+1}) / (L-1)
$$
\n(3)

In such a way, the length of DAC feature vector is *N*∗LAG, where *N* is the number of physicochemical indices (**Table 1**) extracted from two papers [\(6,](#page-27-6)[7\)](#page-27-7), and LAG is the maximum of  $lag$  ( $lag = 1, 2, \ldots$ , LAG).

#### <span id="page-3-0"></span>**1.2.2 Dinucleotide-based cross covariance (DCC)**

Given a DNA sequence **D** (**Eq. 1**), the DCC [\(4,](#page-27-5)[6\)](#page-27-6) approach measures the correlation of two different physicochemical indices between two dinucleotides separated by *lag* nucleic acids along the sequence, which can be calculated by: que<br><sup>L-lag</sup>

different physicochemical indices between two anticreotides separated by *tag*  
acids along the sequence, which can be calculated by:  

$$
DCC(u_1, u_2, lag) = \sum_{i=1}^{L-lqg-1} (P_{u_1}(R_i R_{i+1}) - \overline{P}_{u_1})(P_{u_2}(R_{i+lqg} R_{i+lqg+1}) - \overline{P}_{u_2})/(L-lqg-1)
$$
 (4)

where  $u_1$ ,  $u_2$  are two different physicochemical indices,  $L$  is the length of the DNA sequence,  $P_{u_1}(\mathbf{R}_i \mathbf{R}_{i+1})$   $(P_{u_2}(\mathbf{R}_i \mathbf{R}_{i+1}))$  is the numerical value of the physicochemical index  $u_1$  (*u*<sub>2</sub>) for the dinucleotide  $R_iR_{i+1}$  at position *i*,  $P_{u_1}$  ( $P_{u_2}$ ) is the average value for physicochemical index value  $u_1(u_2)$  along the whole sequence:

$$
\overline{P_u} = \sum_{j=1}^{L-1} P_u(\mathbf{R}_j \mathbf{R}_{j+1}) / (L-1)
$$
\n(5)

In such a way, the length of the DCC feature vector is  $N^*(N-1)^*LAG$ , where LAG is the maximum of *lag* (*lag*=1, 2, …, LAG); *N* is the number of physicochemical indices (**Table 1**).

#### <span id="page-3-1"></span>**1.2.3 Dinucleotide-based auto-cross covariance (DACC)**

DACC [\(4](#page-27-5)[,6\)](#page-27-6) is a combination of DAC and DCC. Therefore, the length of the DACC feature vector is *N*\**N*\*LAG, where *N* is the number of physicochemical indices (**Table 1**) and LAG is the maximum of *lag* (*lag* = 1, 2, …, LAG).

#### <span id="page-3-2"></span>**1.2.4 Trinucleotide-based auto covariance (TAC)**

Given a DNA sequence **D** (**Eq. 1**), the TAC approach [\(4-6\)](#page-27-5) measures the correlation of the same physicochemical index between two trinucleotides separated by *lag*<br>
nucleic acids along the sequence, which can be calculated as:<br>
TAC(*lag*,*u*) =  $\sum_{i=1}^{L-lag-2} (P_u(R_iR_{i+1}R_{i+2}) - \overline{P}_u)(P_u(R_{i+lag}R_{i+lag+1}R_{i$ /s1c<br>ong<br>L<sup>\_lag</sup> sicochemic<br>ong the seq

nucleic acids along the sequence, which can be calculated as:  
\n
$$
TAC(lag, u) = \sum_{i=1}^{L-lag-2} (P_u(R_iR_{i+1}R_{i+2}) - \overline{P}_u)(P_u(R_{i+lag}R_{i+lag+1}R_{i+lag+2}) - \overline{P}_u)/(L-lag-2)
$$
\n(6)

where *u* is a physicochemical index, *L* is the length of the DNA sequence,

 $P_u(R_iR_{i+1}R_{i+2})$  represents the numerical value of the physicochemical index *u* for the trinucleotide  $R_i R_{i+1} R_{i+2}$  at position *i*,  $P_u$  is the average value for physicochemical index *u* along the whole sequence:

$$
\overline{P_u} = \sum_{j=1}^{L-2} P_u(\mathbf{R}_j \mathbf{R}_{j+1} \mathbf{R}_{j+2}) / (L-2)
$$
\n(7)

In such a way, the length of TAC feature vector is *N*∗LAG, where *N* is the number of physicochemical indices (**Table 2**) extracted from [\(6\)](#page-27-6), and LAG is the maximum of *lag* (lag=1, 2, …, LAG).

#### <span id="page-4-0"></span>**1.2.5 Trinucleotide-based cross covariance (TCC)**

Given a DNA sequence **D** (**Eq. 1**), the TCC [\(4](#page-27-5)[,6\)](#page-27-6) approach measures the correlation nucleic acids along the sequence, which can be calculated by:<br> $\frac{L - \log 2}{L} (B \times R - R) \times \overline{B} \times (B \times R - R)$ 

of two different physicochemical indices between two trinucleotides separated by *lag*  
nucleic acids along the sequence, which can be calculated by:  

$$
TCC(u_1, u_2, \text{lag}) = \sum_{i=1}^{L-lag-2} (P_{u_1}(R_i R_{i+1} R_{i+2}) - \overline{P}_{u_1})(P_{u_2}(R_{i+lag} R_{i+lag+1} R_{i+lag+2}) - \overline{P}_{u_2})/(L-lag-2)
$$
(8)

where  $u_1, u_2$  are two physicochemical indices; *L* is the length of the DNA sequence;  $P_{u_1}$ (R<sub>i</sub>R<sub>i+1</sub>R<sub>i+2</sub>) ( $P_{u_2}$ (R<sub>i</sub>R<sub>i+1</sub>R<sub>i+2</sub>)) represents the numerical value of the physicochemical index  $u_1(u_2)$  for the trinucleotide  $R_iR_{i+1}R_{i+2}$  at position *i*;  $P_{u_1}(P_{u_2})$  is the average

value for physicochemical index  $u_1(u_2)$  along the whole sequence:

$$
\overline{P_u} = \sum_{j=1}^{L-2} P_u(\mathbf{R}_j \mathbf{R}_{j+1} \mathbf{R}_{j+2}) / (L-2)
$$
\n(9)

In such a way, the length of TCC feature vector is  $N^*(N-1)^*LAG$ , where *N* is the number of physicochemical index (**Table 2**) extracted from [\(6\)](#page-27-6), and LAG is the maximum of  $lag$  ( $lag = 1, 2, \ldots$ , LAG).

#### <span id="page-4-1"></span>**1.2.6 Trinucleotide-based auto-cross covariance (TACC)**

TACC [\(4,](#page-27-5)[6\)](#page-27-6) is a combination of TAC and TCC. Therefore, the length of the TACC feature vector is  $N^*N^*LAG$ , where *N* is the number of physicochemical indices (**Table 2**) extracted from [\(6\)](#page-27-6), and LAG is the maximum of *lag* (*lag* = 1, 2, …, LAG).

## <span id="page-4-2"></span>**1.3 Pseudo deoxyribonucleic acid composition**

#### <span id="page-4-3"></span>**1.3.1 Pseudo dinucleotide composition (PseDNC)**

PseDNC [\(8\)](#page-27-8) is an approach incorporating the contiguous local sequence-order information and the global sequence-order information into the feature vector of the DNA sequence.

Given a DNA sequence **D** (**Eq. 1**), the PseDNC feature vector of **D** is defined:<br> **D** =  $\begin{bmatrix} d_1 & d_2 & \cdots & d_{16} & d_{16+1} & \cdots & d_{16+\lambda} \end{bmatrix}^T$ 

$$
\mathbf{D} = \begin{bmatrix} d_1 & d_2 & \cdots & d_{16} & d_{16+1} & \cdots & d_{16+\lambda} \end{bmatrix}^{\mathbf{T}}
$$
 (10)

where

$$
d_{k} = \begin{cases} \frac{f_{k}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (1 \leq k \leq 16) \\ \frac{w \theta_{k-16}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (17 \leq k \leq 16 + \lambda) \end{cases}
$$
(11)

where  $f_k$  ( $k=1,2,\dots,16$ ) is the normalized occurrence frequency of dinucleotides in the DNA sequence; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; *w* is the weight factor ranged from 0 to 1;  $\theta_i$  ( $j=1,2,\dots, \lambda$ ) is called the *j*-tier correlation factor that reflects the sequence-order correlation between all the most *j*-tier contiguous dinucleotides along a DNA sequence, which is defined:<br> $\theta_1 = \frac{1}{L_2} \sum_{i=1}^{L-2} \Theta(R_i R_i)$ 

ch is defined:  
\n
$$
\theta_{1} = \frac{1}{L-2} \sum_{i=1}^{L-2} \Theta(R_{i}R_{i+1}, R_{i+1}R_{i+2})
$$
\n
$$
\theta_{2} = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_{i}R_{i+1}, R_{i+2}R_{i+3})
$$
\n
$$
\theta_{3} = \frac{1}{L-4} \sum_{i=1}^{L-4} \Theta(R_{i}R_{i+1}, R_{i+3}R_{i+4}) \qquad (\lambda < L)
$$
\n
$$
\dots
$$
\n
$$
\theta_{\lambda} = \frac{1}{L-1-\lambda} \sum_{i=1}^{L-1-\lambda} \Theta(R_{i}R_{i+1}, R_{i+\lambda}R_{i+\lambda+1})
$$
\n(12)

where the correlation function is given by  
\n
$$
\Theta(R_i R_{i+1}, R_j R_{j+1}) = \frac{1}{\mu} \sum_{u=1}^{\mu} [P_u(R_i R_{i+1}) - P_u(R_j R_{j+1})]^2
$$
\n(13)

where  $\mu$  is the number of physicochemical indices, in this approach, 6 indices reflecting the local DNA structural properties [\(8\)](#page-27-8) (**Table 3**) are employed to generate the PseDNC feature vector;  $P_u(R_iR_{i+1})$   $(P_u(R_jR_{j+1}))$  represents the numerical value of the *u*-th ( $u = 1, 2, \dots, \mu$ ) physicochemical index of the dinucleotide  $R_i R_{i+1}$  ( $R_j R_{j+1}$ ) at position *i* (*j*).

#### <span id="page-5-0"></span>**1.3.2 Pseudo** *k***-tuple nucleotide composition (PseKNC)**

PseKNC [\(9,](#page-27-9)[10\)](#page-27-10) extends the PseDNC approach by incorporating *k*-tuple nucleotide composition.

Given a DNA sequence **D** (**Eq. 1**), the feature vector of **D** is defined:  
\n
$$
\mathbf{D} = \begin{bmatrix} d_1 & d_2 & \cdots & d_{4^k} & d_{4^k+1} & \cdots & d_{4^k+1} \end{bmatrix}^T
$$
\n(14)

where

$$
d_{u} = \begin{cases} \frac{f_{u}}{\sum_{i=1}^{4^{k}} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (1 \le u \le 4^{k}) \\ \frac{w \theta_{u-4^{k}}}{\sum_{i=1}^{4^{k}} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (4^{k} \le u \le 4^{k} + \lambda) \end{cases}
$$
(15)

where  $\lambda$  is the number of the total counted ranks (or tiers) of the correlations along a DNA sequence;  $f_u(u=1,2,\dots,4^k)$  is the frequency of oligonucleotide that is normalized to  $\sum_i^4$  $\int_{-1}^{k} f_i = 1$ 

$$
\sum_{i=1}^{4^{\circ}} f_i = 1; \text{ w is a weight factor; } \theta_j \text{ is given by}
$$
  

$$
\theta_j = \frac{1}{L-j-1} \sum_{i=1}^{L-j-1} \Theta(R_i R_{i+1}, R_{i+j} R_{i+j+1}) \quad (j = 1, 2, \dots, \lambda; \lambda < L)
$$
 (16)

which represents the *j*-tier structural correlation factor between all the *j-*th most

contiguous dinucleotides. The correlation function 
$$
\Theta(\mathbf{R}_i \mathbf{R}_{i+1}, \mathbf{R}_{i+j} \mathbf{R}_{i+j+1})
$$
 is defined by  
\n
$$
\Theta(\mathbf{R}_i \mathbf{R}_{i+1}, \mathbf{R}_{i+j} \mathbf{R}_{i+j+1}) = \frac{1}{\mu} \sum_{\nu=1}^{\mu} [P_{\nu}(\mathbf{R}_i \mathbf{R}_{i+1}) - P_{\nu}(\mathbf{R}_{i+j} \mathbf{R}_{i+j+1})]^2
$$
\n(17)

where  $\mu$  is the number of physicochemical indices, in this study, 6 indices reflecting the local DNA structural properties [\(8\)](#page-27-8) (**Table 3**) are employed to generate the PseKNC feature vector;  $P_v(R_iR_{i+1})$   $(P_v(R_{i+j}R_{i+j+1}))$  represents the numerical value of the *v*-th ( $v = 1, 2, \dots, \mu$ ) physicochemical index for the dinucleotide  $R_i R_{i+1}$  $(R_{i+j}R_{i+j+1})$  at position *i* (*i*+*j*).

For more information about this approach, please refer to  $(9,10)$  $(9,10)$ .

## <span id="page-6-0"></span>**1.3.3 General parallel correlation pseudo dinucleotide composition (PC-PseDNC-General)**

In PC-PseDNC-General [\(11\)](#page-27-11) approach, the users cannot only select the 148 built-in physiochemical indices (**Table 1**), but also can upload their own indices to generate the PC-PseDNC-General feature vector.

Given a DNA sequence **D** (**Eq. 1**), the PC-PseDNC-General feature vector of **D** is defined:

$$
\mathbf{D} = \begin{bmatrix} d_1 & d_2 & \cdots & d_{16} & d_{16+1} & \cdots & d_{16+\lambda} \end{bmatrix}^{\mathbf{T}}
$$
 (18)

where

$$
d_{k} = \begin{cases} \frac{f_{k}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (1 \leq k \leq 16) \\ \frac{w\theta_{k-16}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (16+1 \leq k \leq 16+\lambda) \end{cases}
$$
(19)

where  $f_k$  ( $k=1,2,\dots,16$ ) is the normalized occurrence frequency of dinucleotides in the DNA sequence; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; *w* is the weight factor ranging from 0 to 1;  $\theta_j$  (*j*=1, 2, …,  $\lambda$ ) is called the *j*-tier correlation factor that reflects the sequence-order correlation between all the most contiguous dinucleotides along a DNA sequence, which is defined:<br> $\theta_1 = \frac{1}{I-2} \sum_{i=1}^{L-2} \Theta(R_i R_i)$ 

1 is defined:  
\n
$$
\begin{cases}\n\theta_{1} = \frac{1}{L-2} \sum_{i=1}^{L-2} \Theta(R_{i}R_{i+1}, R_{i+1}R_{i+2}) \\
\theta_{2} = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_{i}R_{i+1}, R_{i+2}R_{i+3}) \\
\theta_{3} = \frac{1}{L-4} \sum_{i=1}^{L-4} \Theta(R_{i}R_{i+1}, R_{i+3}R_{i+4}) \\
\cdots \\
\theta_{\lambda} = \frac{1}{L-1-\lambda} \sum_{i=1}^{L-1-\lambda} \Theta(R_{i}R_{i+1}, R_{i+\lambda}R_{i+\lambda+1})\n\end{cases}
$$
\n(20)

where the correlation function is given by  
\n
$$
\Theta(R_i R_{i+1}, R_j R_{j+1}) = \frac{1}{\mu} \sum_{u=1}^{\mu} [P_u(R_i R_{i+1}) - P_u(R_j R_{j+1})]^2
$$
\n(21)

where  $\mu$  is the number of physicochemical indices listed in the **Table 1**;  $P_{\mu}(\mathbf{R}_i \mathbf{R}_{i+1})$  $(P_u(R_j R_{j+1}))$  represents the numerical value of the *u*-th ( $u = 1, 2, \dots, \mu$ ) physicochemical index for the dinucleotide  $R_iR_{i+1}$  ( $R_jR_{j+1}$ ) at position *i* (*j*).

## <span id="page-7-0"></span>**1.3.4 General parallel correlation pseudo trinucleotide composition (PC-PseTNC-General)**

In PC-PseTNC-General [\(11\)](#page-27-11) approach, the users cannot only select the 12 built-in physiochemical indices (**Table 2**), but also can upload their own indices to generate the PC-PseTNC-General feature vector.

Given a DNA sequence **D** (**Eq. 1**), the PC-PseTNC-General feature vector of **D** is defined:

$$
\mathbf{D} = \begin{bmatrix} d_1 & d_2 & \cdots & d_{64} & d_{64+1} & \cdots & d_{64+\lambda} \end{bmatrix}^{\mathrm{T}}
$$
 (22)

where

$$
d_{k} = \begin{cases} \frac{f_{k}}{\sum_{i=1}^{64} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (1 \leq k \leq 64) \\ \frac{w \theta_{k-64}}{\sum_{i=1}^{64} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (64+1 \leq k \leq 64 + \lambda) \end{cases}
$$
(23)

where  $f_k$  ( $k=1,2,\dots,64$ ) is the normalized occurrence frequency of trinucleotide in the DNA sequence; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; *w* is the weight factor ranging from 0 to 1;  $\theta$ <sub>*i*</sub> (*j*=1, 2, …,  $\lambda$ ) is called the *j*-tier correlation factor that reflects the sequence-order correlation between all the most contiguous trinucleotides along a DNA sequence, which is defined:

$$
\begin{cases}\n\theta_{i} = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_{i}R_{i+1}R_{i+2}, R_{i+1}R_{i+2}R_{i+3}) \\
\theta_{2} = \frac{1}{L-4} \sum_{i=1}^{L-4} \Theta(R_{i}R_{i+1}R_{i+2}, R_{i+2}R_{i+3}R_{i+4}) \\
\theta_{3} = \frac{1}{L-5} \sum_{i=1}^{L-5} \Theta(R_{i}R_{i+1}R_{i+2}, R_{i+3}R_{i+4}R_{i+5}) \\
\cdots \\
\theta_{\lambda} = \frac{1}{L-2-\lambda} \sum_{i=1}^{L-2-\lambda} \Theta(R_{i}R_{i+1}R_{i+2}, R_{i+3}R_{i+3}R_{i+3+2})\n\end{cases} (24)
$$

where the correlation function is given by

$$
L^{-2-\lambda} \overline{f}_{i=1}
$$
  
the correlation function is given by  

$$
\Theta(R_i R_{i+1} R_{i+2}, R_j R_{j+1} R_{j+2}) = \frac{1}{\mu} \sum_{u=1}^{\mu} [P_u(R_i R_{i+1} R_{i+2}) - P_u(R_j R_{j+1} R_{j+2})]^2
$$
(25)

where  $\mu$  is the number of physicochemical indices considered that are listed in the **Table 2**;  $P_u(R_iR_{i+1}R_{i+2})$   $(P_u(R_jR_{j+1}R_{j+2}))$  represents the numerical value of the *u*-th  $(u=1,2,\dots,\mu)$  physicochemical index for the tri-nucleotide  $R_iR_{i+1}R_{i+2}$   $(R_jR_{j+1}R_{j+2})$ at position *i* (*j*).

## <span id="page-8-0"></span>**1.3.5 General series correlation pseudo dinucleotide composition (SC-PseDNC-General)**

SC-PseDNC-General [\(11\)](#page-27-11) is a variant of PC-PseDNC-General, which differs in the equations of calculating the correlation factors reflecting the sequence-order correlation between all the most contiguous dinucleotides along a DNA sequence.

Given a DNA sequence **D** (**Eq. 1**), the SC-PseDNC-General feature vector of **D** is defined:<br> **D** =  $\begin{bmatrix} d_1 & d_2 & \cdots & d_{16} & d_{16+1} & \cdots & d_{16+\lambda} & d_{16+\lambda+1} & \cdots & d_{16+\lambda}\end{bmatrix}^T$ defined:

$$
\mathbf{D} = \begin{bmatrix} d_1 & d_2 & \cdots & d_{16} & d_{16+1} & \cdots & d_{16+\lambda} & d_{16+\lambda+1} & \cdots & d_{16+\lambda}\end{bmatrix}^{\mathrm{T}} \tag{26}
$$

where

$$
d_{k} = \begin{cases} \frac{f_{k}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{\lambda \Lambda} \theta_{j}} & (1 \leq k \leq 16) \\ \frac{w \theta_{k-16}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{\lambda \Lambda} \theta_{j}} & (17 \leq k \leq 16 + \lambda \Lambda) \end{cases}
$$
(27)

where  $f_k$  ( $k=1, 2, \dots, 16$ ) is the normalized occurrence frequency of dinucleotide in the DNA sequence; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; *w* is the weight factor ranging from 0 to 1; Λ is the number of physicochemical indices (**Table 1**);  $θ_j$  ( $j = 1, 2, \dots, \lambda$ ) is called the *j*-tier correlation factor that reflects the sequence-order correlation between all the most contiguous dinucleotides along a DNA sequence, which is defined:

$$
\begin{cases}\n\theta_{1} = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^{1} \\
\theta_{2} = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^{2} \\
\vdots \\
\theta_{\Lambda} = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^{\Lambda} \\
\vdots \\
\theta_{\Lambda-1} = \frac{1}{L-\lambda-2} \sum_{i=1}^{L-\lambda-2} J_{i,i+\lambda}^{\Lambda-1} \\
\theta_{\lambda\Lambda-1} = \frac{1}{L-\lambda-2} \sum_{i=1}^{L-\lambda-2} J_{i,i+\lambda}^{\Lambda}\n\end{cases} \tag{28}
$$

The correlation function is given by

 $\theta_{\lambda A} = \frac{1}{L - \lambda - 2} \sum_{i=1}^{\infty} J_{i, i + \lambda}^{\Lambda}$ <br>
ae correlation function is given by<br>  $J_{i, i+m}^{u} = P_{u}(\mathbf{R}_{i} \mathbf{R}_{i+1}) \cdot P_{u}(\mathbf{R}_{i+m} \mathbf{R}_{i+m+1}) \quad (u = 1, 2, \cdots, \Lambda; m = 1, 2, \cdots, \lambda; i = 1, 2, \cdots, L-m-1)$ (29) where  $P_{u}(\mathbf{R}_{i} \mathbf{R}_{i+1})$  ( $P_{u}(\mathbf{R}_{i+m} \mathbf{R}_{i+m+1})$ ) represents the numerical value of the *u*-th  $(u = 1, 2, \dots, \mu)$  physiochemical index for the dinucleotide  $R_i R_{i+1} (R_{i+m} R_{i+m+1})$  at position *i* (*i+m*).

## <span id="page-9-0"></span>**1.3.6 General series correlation pseudo trinucleotide composition (SC-PseTNC-General)**

SC-PseTNC-General [\(11\)](#page-27-11) is a variant of PC-PseTNC-General, which differs in the equations of calculating the correlation factors reflecting the sequence-order correlation between all the most contiguous dinucleotides along a DNA sequence.

Given a DNA sequence **D** (**Eq. 1**), the SC-PseTNC-General feature vector of **D** is defined:<br> **D** =  $\begin{bmatrix} d_1 & d_2 & \cdots & d_{64} & d_{64+1} & \cdots & d_{64+2} & d_{64+3+1} & \cdots & d_{64+4} \end{bmatrix}^T$ defined:

$$
\mathbf{D} = \begin{bmatrix} d_1 & d_2 & \cdots & d_{64} & d_{64+1} & \cdots & d_{64+2} & d_{64+2+1} & \cdots & d_{64+2} \end{bmatrix}^{\mathrm{T}} \tag{30}
$$

where

$$
d_k = \begin{cases} \frac{f_k}{\sum_{i=1}^{64} f_i + w \sum_{j=1}^{3\lambda} \theta_j} & (1 \le k \le 64) \\ \frac{w\theta_{k-64}}{\sum_{i=1}^{64} f_i + w \sum_{j=1}^{3\lambda} \theta_j} & (64+1 \le k \le 64 + \lambda \Lambda) \end{cases}
$$
(31)

where  $f_k$  ( $k=1, 2, \dots, 64$ ) is the normalized occurrence frequency of trinucleotide in the DNA sequence; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a DNA sequence; *w* is the weight factor ranging from 0 to 1; Λ is the number of physicochemical indices (**Table 2**);  $\theta_j$  ( $j = 1, 2, \dots, \lambda$ ) is called the *j*-tier correlation factor reflecting the sequence-order correlation between all the most contiguous trinucleotides along a DNA sequence, which is defined:

$$
\begin{cases}\n\theta_{1} = \frac{1}{L-4} \sum_{i=1}^{L-4} J_{i,i+1}^{1} \\
\theta_{2} = \frac{1}{L-4} \sum_{i=1}^{L-4} J_{i,i+1}^{2} \\
& \dots \\
\theta_{\Lambda} = \frac{1}{L-4} \sum_{i=1}^{L-4} J_{i,i+1}^{\Lambda} \\
& \lambda < (L-3) \\
& \dots \\
\theta_{\lambda \Lambda - 1} = \frac{1}{L-\lambda - 3} \sum_{i=1}^{L-\lambda - 3} J_{i,i+\lambda}^{\Lambda - 1} \\
\theta_{\lambda \Lambda} = \frac{1}{L-\lambda - 3} \sum_{i=1}^{L-\lambda - 3} J_{i,i+\lambda}^{\Lambda}\n\end{cases} \tag{32}
$$

The correlation function is given by

(33)  
\n
$$
\begin{cases}\nJ_{i,i+m}^{u} = P_{u}(R_{i}R_{i+1}R_{i+2}) \cdot P_{u}(R_{i+m}R_{i+m+1}R_{i+m+2}) \\
u = 1, 2, \cdots, \Lambda; m = 1, 2, \cdots, \lambda; i = 1, 2, \cdots, L-m-2\n\end{cases}
$$

where  $P_u(\mathbf{R}_i \mathbf{R}_{i+1} \mathbf{R}_{i+2})$  ( $P_u(\mathbf{R}_{i+m} \mathbf{R}_{i+m+1} \mathbf{R}_{i+m+2})$ ) represents the numerical value of the *u*-th  $(u = 1, 2, \dots, \mu)$  physiochemical index for the tri-nucleotide  $R_i R_{i+1} R_{i+2}$  $(R_{i+m}R_{i+m+1}R_{i+m+2})$  at position *i* (*i*+*m*).

# <span id="page-10-0"></span>**2. RNA**

## <span id="page-10-1"></span>**2.1 Ribonucleic acid composition**

## <span id="page-10-2"></span>**2.1.1 Basic kmer (Kmer)**

Basic kmer [\(12\)](#page-27-12) is the simplest approach to represent the RNAs, in which the RNA sequences are represented as the occurrence frequencies of *k* neighboring nucleic acids.

## <span id="page-10-3"></span>**2.2 Autocorrelation**

#### <span id="page-10-4"></span>**2.2.1 Dinucleotide-based auto covariance (DAC)**

Suppose an RNA sequence **R** with *L* nucleic acid residues; i.e.

$$
\mathbf{R} = \mathbf{R}_1 \mathbf{R}_2 \mathbf{R}_3 \mathbf{R}_4 \mathbf{R}_5 \mathbf{R}_6 \mathbf{R}_7 \cdots \mathbf{R}_L
$$
 (34)

where  $R_1$  represents the nucleic acid residue at the sequence position 1,  $R_2$  the nucleic acid residue at position 2, and so forth.

The DAC [\(4-6\)](#page-27-5) measures the correlation of the same physicochemical index between two dinucleotides separated by a distance of *lag* along the sequence, which can be calculated as:

$$
DAC(u, lag) = \sum_{i=1}^{L-lag-1} (P_u(R_iR_{i+1}) - \overline{P}_u)(P_u(R_{i+lag}R_{i+lag+1}) - \overline{P}_u)/(L-lag-1)
$$
 (35)

where *u* is a physicochemical index; *L* is the length of the RNA sequence,  $P_u(R_iR_{i+1})$  $(P_u(R_{i+log}R_{i+log+1}))$  means the numerical value of the physicochemical index *u* for the dinucleotide  $R_iR_{i+1}$  ( $R_{i+lag}R_{i+lag+1}$ ) at position *i* (*i*+*lag*),  $P_u$  is the average value for physicochemical index *u* along the whole sequence:

$$
\overline{P_u} = \sum_{j=1}^{L-1} P_u(\mathbf{R}_j \mathbf{R}_{j+1}) / (L-1)
$$
\n(36)

In such a way, the length of DAC feature vector is *N*∗LAG, where *N* is the number of physicochemical indices (**Table 4**), which are extracted from [\(6](#page-27-6)[,7\)](#page-27-7), and LAG is the maximum of  $lag$  ( $lag = 1, 2, \ldots$ , LAG).

#### <span id="page-11-0"></span>**2.2.2 Dinucleotide-based cross covariance (DCC)**

Given an RNA sequence **R** (**Eq. 34**), the DCC [\(4](#page-27-5)[,6\)](#page-27-6) approach measures the correlation of two different physicochemical indices between two dinucleotides

corelation of two different physicochelential indices between two unincreotides separated by *lag* nucleic acids along the sequence, which can be calculated by:  

$$
DCC(u_1, u_2, lag) = \sum_{i=1}^{L-lag-1} (P_{u_1}(R_i R_{i+1}) - \overline{P}_{u_1})(P_{u_2}(R_{i+lag} R_{i+lag+1}) - \overline{P}_{u_2})/(L-lag-1)
$$
(37)

where  $u_1, u_2$  are two different physicochemical indices,  $L$  is the length of the RNA sequence,  $P_{u_1}(\mathbf{R}_i \mathbf{R}_{i+1})$   $(P_{u_2}(\mathbf{R}_i \mathbf{R}_{i+1}))$  is the numerical value of the physicochemical index  $u_1(u_2)$  for the dinucleotide  $R_iR_{i+1}$  at position *i*,  $P_{u_1}(P_{u_2})$  is the average value for physicochemical index value  $u_1(u_2)$  along the whole sequence:

$$
\overline{P_u} = \sum_{j=1}^{L-1} P_u(\mathbf{R}_j \mathbf{R}_{j+1}) / (L-1)
$$
\n(38)

In such a way, the length of the DCC feature vector is  $N^*(N-1)^*LAG$ , where *N* is the number of physicochemical indices (**Table 4**) and LAG is the maximum of *lag* (*lag*=1, 2, …, LAG).

#### <span id="page-11-1"></span>**2.2.3 Dinucleotide-based auto-cross covariance (DACC)**

DACC [\(4](#page-27-5)[,6\)](#page-27-6) is a combination of DAC and DCC. Therefore, the length of the DACC feature vector is  $N^*N^*LAG$ , where *N* is the number of physicochemical indices (**Table 4**) and LAG is the maximum of *lag* (*lag* = 1, 2, …, LAG).

## <span id="page-11-2"></span>**2.3 Pseudo ribonucleic acid composition**

## <span id="page-12-0"></span>**2.3.1 General parallel correlation pseudo dinucleotide composition (PC-PseDNC-General)**

In PC-PseDNC-General [\(6\)](#page-27-6) approach, the users cannot only select the 22 built-in physiochemical indices (**Table 4**), but also can upload their own indices to generate the PC-PseDNC-General feature vector.

Given an RNA sequence **R** (**Eq. 34**), the PC-PseDNC-General feature vector of **R** is defined:

$$
\mathbf{R} = \begin{bmatrix} d_1 & d_2 & \cdots & d_{16} & d_{16+1} & \cdots & d_{16+\lambda} \end{bmatrix}^{\mathbf{T}}
$$
 (39)

where

$$
d_{k} = \begin{cases} \frac{f_{k}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (1 \leq k \leq 16) \\ \frac{w \theta_{k-16}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{k} \theta_{j}} & (16+1 \leq k \leq 16+\lambda) \end{cases}
$$
(40)

where  $f_k$  ( $k=1,2,\dots,16$ ) is the normalized occurrence frequency of dinucleotide in the RNA sequence; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a RNA sequence; *w* is the weight factor ranging from 0 to 1;  $\theta$ <sub>*j*</sub> (*j*=1, 2, …,  $\lambda$ ) is called the *j*-tier correlation factor reflecting the sequence-order correlation between all the *i*-th most contiguous dinucleotides along an RNA sequence, which is defined:<br> $\theta_1 = \frac{1}{L^2} \sum_{i=1}^{L-2} \Theta(R_i R_i)$ 

$$
\begin{cases}\n\theta_{1} = \frac{1}{L-2} \sum_{i=1}^{L-2} \Theta(R_{i}R_{i+1}, R_{i+1}R_{i+2}) \\
\theta_{2} = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_{i}R_{i+1}, R_{i+2}R_{i+3}) \\
\theta_{3} = \frac{1}{L-4} \sum_{i=1}^{L-4} \Theta(R_{i}R_{i+1}, R_{i+3}R_{i+4}) \\
\cdots \\
\theta_{\lambda} = \frac{1}{L-1-\lambda} \sum_{i=1}^{L-1-\lambda} \Theta(R_{i}R_{i+1}, R_{i+3}R_{i+3+1})\n\end{cases} (A < L)
$$
\n(41)

where the correlation function is given by  
\n
$$
\Theta(R_i R_{i+1}, R_j R_{j+1}) = \frac{1}{\mu} \sum_{u=1}^{\mu} [P_u(R_i R_{i+1}) - P_u(R_j R_{j+1})]^2
$$
\n(42)

where  $\mu$  is the number of physicochemical indices considered that are listed in the **Table 4**;  $P_{u}$ ( $R_{i}$  $R_{i+1}$ )  $(P_{u}$ ( $R_{j}$  $R_{j+1}$ ) represents the numerical value of the *u*-th  $(u = 1, 2, \dots, \mu)$  physicochemical index for the dinucleotide  $R_i R_{i+1} (R_j R_{j+1})$  at position *i* (*j*).

## <span id="page-12-1"></span>**2.3.2 General series correlation pseudo dinucleotide composition (SC-PseDNC-General)**

SC-PseDNC-General [\(6\)](#page-27-6) is a variant of PC-PseDNC-General, which differs in the equations of calculating the correlation factors reflecting the sequence-order correlation between all the most contiguous dinucleotides along an RNA sequence.

Given an RNA sequence **R** (**Eq. 34**), the SC-PseDNC-General feature vector of **R** is defined:<br> **R** =  $\begin{bmatrix} d_1 & d_2 & \cdots & d_{16} & d_{16+1} & \cdots & d_{16+\lambda} & d_{16+\lambda+1} & \cdots & d_{16+\lambda\lambda} \end{bmatrix}^T$  (43 defined:

$$
\mathbf{R} = \begin{bmatrix} d_1 & d_2 & \cdots & d_{16} & d_{16+1} & \cdots & d_{16+\lambda} & d_{16+\lambda+1} & \cdots & d_{16+\lambda}\end{bmatrix}^{\mathrm{T}} \tag{43}
$$

where

$$
d_{k} = \begin{cases} \frac{f_{k}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{\lambda \Lambda} \theta_{j}} & (1 \leq k \leq 16) \\ \frac{w \theta_{k-16}}{\sum_{i=1}^{16} f_{i} + w \sum_{j=1}^{\lambda \Lambda} \theta_{j}} & (16+1 \leq k \leq 16 + \lambda \Lambda) \end{cases}
$$
(44)

where  $f_k$  ( $k=1, 2, \dots, 16$ ) is the normalized occurrence frequency of dinucleotides in the RNA sequence; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along an RNA sequence; *w* is the weight factor ranging from 0 to 1;  $\Lambda$  is the number of physicochemical indices (**Table 4**);  $\theta_j$  ( $j = 1, 2, \dots, \lambda$ ) is called the *j*-tier correlation factor reflecting the sequence-order correlation between all the *j*-th most contiguous dinucleotides along an RNA sequence, which is defined:

$$
\begin{cases}\n\theta_{1} = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^{1} \\
\theta_{2} = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^{2} \\
& \dots \\
\theta_{\Lambda} = \frac{1}{L-3} \sum_{i=1}^{L-3} J_{i,i+1}^{\Lambda} \\
& \lambda < (L-2) \\
& \dots \\
\theta_{\lambda \Lambda - 1} = \frac{1}{L - \lambda - 2} \sum_{i=1}^{L - \lambda - 2} J_{i,i+1}^{\Lambda - 1} \\
\theta_{\lambda \Lambda} = \frac{1}{L - \lambda - 2} \sum_{i=1}^{L - \lambda - 2} J_{i,i+1}^{\Lambda}\n\end{cases} \tag{45}
$$

The correlation function is given by

$$
\begin{cases}\n\mathbf{J}_{i,i+m}^{u} = P_{u}(\mathbf{R}_{i}, \mathbf{R}_{i+1}) \cdot P_{u}(\mathbf{R}_{i+m}, \mathbf{R}_{i+m+1}) \\
u = 1, 2, \cdots, \Lambda; \ m = 1, 2, \cdots, \lambda; \ i = 1, 2, \cdots, L-\lambda-2\n\end{cases} (46)
$$

 $P_u(R_iR_{i+1})$  ( $P_u(R_{i+m}R_{i+m+1})$ ) represents the numerical value of the *u*-th ( $u=1, 2, \dots, \mu$ ) physiochemical index for the dinucleotide  $R_iR_{i+1}(R_{i+m}R_{i+m+1})$  at position *i* (*i+m*).

# <span id="page-13-0"></span>**3. Protein**

## <span id="page-13-1"></span>**3.1 Amino acid composition**

## <span id="page-14-0"></span>**3.1.1 Basic kmer (Kmer)**

Basic kmer [\(13\)](#page-27-13) is the simplest approach to represent the proteins, in which the protein sequences are represented as the occurrence frequencies of *k* neighboring amino acids.

## <span id="page-14-1"></span>**3.2 Autocorrelation**

#### <span id="page-14-2"></span>**3.2.1 Auto covariance (AC)**

Suppose a protein sequence **P** with *L* amino acid residues; i.e.

$$
P = R_1 R_2 R_3 R_4 R_5 R_6 R_7 \cdots R_L
$$
\n(47)

where  $R_1$  represents the amino acid residue at the sequence position 1,  $R_2$  the amino acid residue at position 2 and so forth.

The AC [\(4](#page-27-5)[,5](#page-27-14)[,14\)](#page-27-15) approach measures the correlation of the same property between two residues separated by a distance of *lag* along the sequence, which can be calculated as: *L lag*

$$
AC(i, lag) = \sum_{i=1}^{L-lag} (P_u(R_i) - \overline{P}_u)(P_u(R_{i+lag}) - \overline{P}_u)/(L-lag)
$$
(48)

where *u* is a physicochemical index, *L* is the length of the protein sequence,  $P_u(R_i)$ means the numerical value of the physicochemical index *u* for the amino acid R*<sup>i</sup>* at position  $i$ ,  $P_u$  is the average value for physicochemical index  $u$  along the whole sequence:

$$
\overline{P_u} = \sum_{j=1}^{L} P_u(\mathbf{R}_j) / L \tag{49}
$$

In such a way, the length of AC feature vector is *N*∗LAG, where *N* is the number of physicochemical indices (**Table 5**) extracted from AAindex [\(15\)](#page-27-16); LG is the maximum of *lag* (*lag*=1*,*2*,...,*LG).

For more information of this approach, please refer to  $(4,5)$  $(4,5)$ .

#### <span id="page-14-3"></span>**3.2.2 Cross covariance (CC)**

Given a protein sequence **P** (**Eq.47**), the CC [\(4](#page-27-5)[,5](#page-27-14)[,14\)](#page-27-15) approach measures the correlation of two different properties between two residues separated by a distance of *lag* along the sequence, which can be calculated by:

sequence, which can be calculated by:  
\n
$$
CC(u_1, u_2, lag) = \sum_{i=1}^{L-lag} (P_{u_1}(R_i) - \overline{P}_{u_1})(P_{u_2}(R_{i+lag}) - \overline{P}_{u_2})/(L-lag)
$$
\n(50)

where  $u_1, u_2$  are two different physicochemical indices,  $L$  is the length of the protein sequence,  $P_{u_1}(\mathbf{R}_i)$   $(P_{u_2}(\mathbf{R}_{i+log}))$  is the numerical value of the physicochemical index  $u_1$ (*u*<sub>2</sub>) for the amino acid R<sub>*i*</sub> (R<sub>*i+lag*) at position *i* (*i*+*lag*),  $P_{u_1}$  ( $P_{u_2}$ ) is the average value</sub> for physicochemical index value  $u_1(u_2)$  along the whole sequence:

$$
\overline{P_u} = \sum_{j=1}^{L} P_u(\mathbf{R}_j) / L \tag{51}
$$

In such a way, the length of the CC feature vector is  $N^*(N-1)^*LAG$ , where *N* is the number of physicochemical indices (**Table 5**) and LAG is the maximum of *lag* (*lag*=1, 2, …, LAG).

For more information of this approach, please refer to [\(4](#page-27-5)[,5\)](#page-27-14).

#### <span id="page-15-0"></span>**3.2.3 Auto-cross covariance (ACC)**

ACC [\(4](#page-27-5)[,5](#page-27-14)[,14\)](#page-27-15) is a combination of AC and CC. Therefore, the length of the ACC feature vector is *N*\**N*\*LAG, where *N* is the number of physicochemical indices (**Table 5**) and LAG is the maximum of *lag* (*lag* = 1, 2, …, LAG).

## <span id="page-15-1"></span>**3.3 Pseudo amino acid composition**

#### <span id="page-15-2"></span>**3.3.1 Parallel correlation pseudo amino acid composition (PC-PseAAC)**

PC-PseAAC [\(16\)](#page-27-17) is an approach incorporating the contiguous local sequence-order information and the global sequence-order information into the feature vector of the protein sequence.

Given a Protein sequence **P** (**Eq.47**), the PC-PseAAC feature vector of **P** is defined:  
\n
$$
\mathbf{P} = \begin{bmatrix} x_1 & x_2 & \cdots & x_{20} & x_{20+1} & \cdots & x_{20+\lambda} \end{bmatrix}^T
$$
\n(52)

where

$$
x_{u} = \begin{cases} \frac{f_{u}}{\sum_{i=1}^{20} f_{i} + w \sum_{j=1}^{\lambda} \theta_{j}} & (1 \le u \le 20) \\ \frac{w \theta_{u-20}}{\sum_{i=1}^{20} f_{i} + w \sum_{j=1}^{\lambda} \theta_{j}} & (20 + 1 \le u \le 20 + \lambda) \end{cases}
$$
(53)

where  $f_i$  ( $i=1,2,\dots,20$ ) is the normalized occurrence frequency of the 20 amino acids in the protein **P**; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a protein sequence; *w* is the weight factor ranging from 0 to 1;  $\theta_i$  ( $j=1,2,\dots, \lambda$ ) is called the *j*-tier correlation factor reflecting the sequence-order correlation between all the *j*-th most contiguous residues along a protein chain, which is defined:

$$
\begin{cases}\n\theta_{1} = \frac{1}{L-1} \sum_{i=1}^{L-1} \Theta(R_{i}, R_{i+1}) \\
\theta_{2} = \frac{1}{L-2} \sum_{i=1}^{L-2} \Theta(R_{i}, R_{i+2}) \\
\theta_{3} = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_{i}, R_{i+3}) \\
\cdots \\
\theta_{\lambda} = \frac{1}{L-\lambda} \sum_{i=1}^{L-\lambda} \Theta(R_{i}, R_{i+\lambda})\n\end{cases} (54)
$$

where the correlation function is given by  
\n
$$
\Theta(\mathbf{R}_i, \mathbf{R}_j) = \frac{1}{3} \Biggl\{ \Bigl[ H_1(\mathbf{R}_j) - H_1(\mathbf{R}_i) \Bigr]^2 + \Bigl[ H_2(\mathbf{R}_j) - H_2(\mathbf{R}_i) \Bigr]^2 + \Bigl[ M(\mathbf{R}_j) - M(\mathbf{R}_i) \Bigr]^2 \Biggr\} \qquad (55)
$$

where  $H_1(R_i)$ ,  $H_2(R_i)$ , and  $M(R_i)$  are, respectively, the hydrophobicity value, hydrophilicity value, and side-chain mass (**Table 6**) of the amino acid R*i*; Note that before substituting the values of hydrophobicity, hydrophilicity, and side-chain mass into **Eq. 55**, they are all subjected to a standard conversion as described by the following equation:

 $\sqrt{ }$ 

$$
H_{1}(i) = \frac{H_{1}^{0}(i) - \sum_{i=1}^{20} \frac{H_{1}^{0}(i)}{20}}{\sqrt{\sum_{i=1}^{20} \left[H_{1}^{0}(i) - \sum_{i=1}^{20} \frac{H_{1}^{0}(i)}{20}\right]^{2}}}
$$
\n
$$
H_{2}(i) = \frac{H_{2}^{0}(i) - \sum_{i=1}^{20} \frac{H_{2}^{0}(i)}{20}}{\sqrt{\sum_{i=1}^{20} \left[H_{2}^{0}(i) - \sum_{i=1}^{20} \frac{H_{2}^{0}(i)}{20}\right]^{2}}}
$$
\n
$$
M(i) = \frac{M^{0}(i) - \sum_{i=1}^{20} \frac{M^{0}(i)}{20}}{\sqrt{\sum_{i=1}^{20} \left[M^{0}(i) - \sum_{i=1}^{20} \frac{M^{0}(i)}{20}\right]^{2}}}
$$
\n(56)

where  $H_1^0(i)$  is the original hydrophobicity value of the *i*-th amino acid;  $H_2^0(i)$  the corresponding original hydrophilicity value;  $M^0(i)$  the mass of the *i*-th amino acid side chain.

#### <span id="page-16-0"></span>**3.3.2 Series correlation pseudo amino acid composition (SC-PseAAC)**

SC-PseAAC [\(17\)](#page-27-18) is a variant of PC-PseAAC. Given a protein sequence **P** (**Eq.47**), the SC-PseAAC feature vector of **P** is defined:<br>  $P = [p_1 \quad p_2 \quad \cdots \quad p_{20} \quad p_{20+1} \quad \cdots \quad p_{20+\lambda} \quad p_{20+\lambda+1} \quad \cdots \quad p_{20+2\lambda}]^T$ 

$$
\mathbf{P} = \begin{bmatrix} p_1 & p_2 & \cdots & p_{20} & p_{20+1} & \cdots & p_{20+\lambda} & p_{20+\lambda+1} & \cdots & p_{20+2\lambda} \end{bmatrix}^{\mathrm{T}} \tag{57}
$$

where

$$
p_{u} = \begin{cases} \frac{f_{u}}{\sum_{i=1}^{20} f_{i} + w \sum_{j=1}^{2\lambda} \tau_{j}} & (1 \le u \le 20) \\ \frac{w\tau_{u-20}}{\sum_{i=1}^{20} f_{i} + w \sum_{j=1}^{2\lambda} \tau_{j}} & (20 + 1 \le u \le 20 + 2\lambda) \end{cases}
$$
(58)

where  $f_i$  ( $i = 1, 2,..., 20$ ) is the normalized occurrence frequency of the 20 native amino acids in the protein **P**; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a protein sequence; *w* is the weight factor ranging from 0 to 1;  $\tau_j$  the *j*-tier sequence-correlation factor that reflects the sequence-order correlation between all the most contiguous residues along a protein sequence, which is defined:

$$
\begin{cases}\n\tau_{1} = \frac{1}{L-1} \sum_{i=1}^{L-1} H_{i,i+1}^{1} \\
\tau_{2} = \frac{1}{L-1} \sum_{i=1}^{L-1} H_{i,i+1}^{2} \\
\tau_{3} = \frac{1}{L-2} \sum_{i=1}^{L-2} H_{i,i+2}^{1} \\
\tau_{4} = \frac{1}{L-2} \sum_{i=1}^{L-2} H_{i,i+2}^{2} \\
\cdots \\
\tau_{2\lambda-1} = \frac{1}{L-\lambda} \sum_{i=1}^{L-\lambda} H_{i,i+\lambda}^{1} \\
\tau_{2\lambda} = \frac{1}{L-\lambda} \sum_{i=1}^{L-\lambda} H_{i,i+\lambda}^{2}\n\end{cases}
$$
\n(59)

where  $H_{i,j}^1$  and  $H_{i,j}^2$  are the hydrophobicity and hydrophilicity correlation functions given by

$$
\begin{cases}\nH_{i,j}^1 = h^1(\mathbf{R}_i) \cdot h^1(\mathbf{R}_j) \\
H_{i,j}^2 = h^2(\mathbf{R}_i) \cdot h^2(\mathbf{R}_j)\n\end{cases}
$$
\n(60)

where  $h^1(\mathbf{R}_i)$  and  $h^2(\mathbf{R}_i)$  are, respectively, the hydrophobicity and hydrophilicity values(**Table 7**) for the *i*-th ( $i = 1, 2, \ldots, L$ ) amino acid in **Eq.47**, and the dot (•) means the multiplication sign.

Note that before substituting the values of hydrophobicity and hydrophilicity into **Eq.60**, they are all subjected to a standard conversion as described by the following equation:

$$
h^{1}(\mathbf{R}_{i}) = \frac{h_{0}^{1}(\mathbf{R}_{i}) - \sum_{k=1}^{20} \frac{h_{0}^{1}(\mathbb{R}_{k})}{20}}{\sqrt{\sum_{u=1}^{20} \left[ h_{0}^{1}(\mathbb{R}_{u}) - \sum_{k=1}^{20} \frac{h_{0}^{1}(\mathbb{R}_{k})}{20} \right]^{2}}}
$$
\n
$$
h^{2}(\mathbf{R}_{i}) = \frac{h_{0}^{2}(\mathbf{R}_{i}) - \sum_{k=1}^{20} \frac{h_{0}^{2}(\mathbb{R}_{k})}{20}}{20}
$$
\n
$$
h^{2}(\mathbf{R}_{i}) = \frac{\sum_{u=1}^{20} \left[ h_{0}^{2}(\mathbb{R}_{u}) - \sum_{k=1}^{20} \frac{h_{0}^{2}(\mathbb{R}_{k})}{20} \right]^{2}}{20}
$$
\n(61)

where we use the  $\mathbb{R}_i$  (*i* = 1, 2, . . . , 20) to represent the 20 native amino acids. The symbols  $h_0^1$  and  $h_0^2$  represent the original hydrophobicity and hydrophilicity values of the amino acid in the brackets right after the symbols.

For more information of the SC-PseAAC, please refer to [\(17\)](#page-27-18).

## <span id="page-18-0"></span>**3.3.3 General parallel correlation pseudo amino acid composition (PC-PseAAC-General)**

The PC-PseAAC-General approach [\(14\)](#page-27-15) cannot only incorporate comprehensive built-in indices (**Table 5**) extracted from AAindex [\(15\)](#page-27-16), but also allow the users to upload their own indices to generate the PC-PseAAC-General feature vector.

Given a protein sequence **P** (**Eq.47**), the PC-PseAAC-General feature vector of **P** is defined:

$$
\mathbf{P} = \begin{bmatrix} x_1 & x_2 & \cdots & x_{20} & x_{20+1} & \cdots & x_{20+\lambda} \end{bmatrix}^{\mathrm{T}}
$$
 (62)

where

$$
x_{u} = \begin{cases} \frac{f_{u}}{\sum_{i=1}^{20} f_{i} + w \sum_{j=1}^{\lambda} \theta_{j}} & (1 \le u \le 20) \\ \frac{w \theta_{u-20}}{\sum_{i=1}^{20} f_{i} + w \sum_{j=1}^{\lambda} \theta_{j}} & (20 + 1 \le u \le 20 + \lambda) \end{cases}
$$
(63)

where  $f_i$  ( $i=1,2,\dots,20$ ) is the normalized occurrence frequency of the 20 amino acids in the protein **P**; the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a protein sequence; *w* is the weight factor ranging from 0 to 1;  $\theta_i$  ( $j=1,2,\dots, \lambda$ ) is called the *j*-tier correlation factor reflecting the sequence-order correlation between all the *j*-th most contiguous residues along a protein chain, which is defined:

$$
\begin{cases}\n\theta_{1} = \frac{1}{L-1} \sum_{i=1}^{L-1} \Theta(R_{i}, R_{i+1}) \\
\theta_{2} = \frac{1}{L-2} \sum_{i=1}^{L-2} \Theta(R_{i}, R_{i+2}) \\
\theta_{3} = \frac{1}{L-3} \sum_{i=1}^{L-3} \Theta(R_{i}, R_{i+3}) \quad (\lambda < L) \\
\cdots \\
\theta_{\lambda} = \frac{1}{L-\lambda} \sum_{i=1}^{L-\lambda} \Theta(R_{i}, R_{i+\lambda})\n\end{cases} (64)
$$

where the correlation function is given by

$$
\Theta(\mathbf{R}_i, \mathbf{R}_j) = \frac{1}{\mu} \sum_{u=1}^{\mu} [H_u(\mathbf{R}_i) - H_u(\mathbf{R}_j)]^2
$$
(65)

where  $\mu$  is the number of physicochemical indices considered that listed in the **Table 5**;  $H_u(R_i)$  is the *u*-th physicochemical index value of the amino acid  $R_i$ ;  $H_u(R_i)$ , the  $u$ -th physicochemical index value for the amino acid  $R_j$ . Note that before substituting the physicochemical indices values into **Eq.65**, they are all subjected to a standard conversion as described by the following equation:<br> $H_u^0(i) - \sum_{n=0}^{20} \frac{H_u^0(i)}{20}$ 

$$
H_u(i) = \frac{H_u^0(i) - \sum_{i=1}^{20} \frac{H_u^0(i)}{20}}{\sqrt{\sum_{i=1}^{20} \left[H_u^0(i) - \sum_{i=1}^{20} \frac{H_u^0(i)}{20}\right]^2}}
$$
(66)

where  $H_u^0(i)$  is the *u*-th original physicochemical value of the *i*-th amino acid.

#### <span id="page-19-0"></span>**3.3.4 General series correlation pseudo amino acid composition (SC-PseAAC-General)**

The SC-PseAAC-General approach [\(14\)](#page-27-15) cannot only incorporate comprehensive built-in indices (**Table 5**) extracted from AAindex [\(15\)](#page-27-16), but also allow the users to upload their own indices to generate the SC-PseAAC-General feature vector.

Given a protein sequence **P** (**Eq.47**), the SC-PseAAC-General feature vector of **P** is defined:<br>  $P = \begin{bmatrix} p_1 & p_2 & \cdots & p_{20} & p_{20+1} & \cdots & p_{20+\lambda} & p_{20+\lambda+1} & \cdots & p_{20+\lambda\lambda} \end{bmatrix}^T$  (6 defined:

$$
\mathbf{P} = \begin{bmatrix} p_1 & p_2 & \cdots & p_{20} & p_{20+1} & \cdots & p_{20+\lambda} & p_{20+\lambda+1} & \cdots & p_{20+\lambda\lambda} \end{bmatrix}^{\mathrm{T}} \tag{67}
$$

where

$$
p_{u} = \begin{cases} \frac{f_{u}}{\sum_{i=1}^{20} f_{i} + w \sum_{j=1}^{\lambda} \tau_{j}} & (1 \le u \le 20) \\ \frac{w\tau_{u-20}}{\sum_{i=1}^{20} f_{i} + w \sum_{j=1}^{\lambda} \tau_{j}} & (20 + 1 \le u \le 20 + \lambda \Lambda) \end{cases}
$$
(68)

where  $f_i$  ( $i = 1, 2,..., 20$ ) is the normalized occurrence frequency of the 20 native amino acids in the protein **P**, the parameter  $\lambda$  is an integer, representing the highest counted rank (or tier) of the correlation along a protein sequence; *w* is the weight factor ranging from 0 to 1;  $\Lambda$  is the number of physicochemical indices (**Table 5**);  $\tau$ <sub>*j*</sub> the *j* -tier sequence-correlation factor reflecting the sequence-order correlation between all the most contiguous residues along a protein sequence, which is defined:

$$
\begin{cases}\n\tau_{1} = \frac{1}{L-1} \sum_{i=1}^{L-1} H_{i,i+1}^{1} \\
\tau_{2} = \frac{1}{L-1} \sum_{i=1}^{L-1} H_{i,i+1}^{2} \\
& \dots \\
\tau_{\Lambda} = \frac{1}{L-1} \sum_{i=1}^{L-1} H_{i,i+1}^{\Lambda} \qquad \lambda < (L-1) \\
& \dots \\
\tau_{\lambda \Lambda - 1} = \frac{1}{L \lambda} \sum_{i=1}^{L-\lambda} H_{i,i+\lambda}^{\Lambda - 1} \\
\tau_{\lambda \Lambda} = \frac{1}{L \lambda} \sum_{i=1}^{L-\lambda} H_{i,i+\lambda}^{\Lambda}\n\end{cases}
$$
\n(69)

where  $H_{i,i+m}^{\xi}$  is the correlation function given by

$$
\begin{cases}\nH_{i,i+m}^{\zeta} = h^{\zeta}(\mathbf{R}_{i}) \cdot h^{\zeta}(\mathbf{R}_{i+m}) \\
\zeta = 1, 2, \cdots, \Lambda; \ m = 1, 2, \cdots, \lambda; \ i = 1, 2, \cdots, L \cdot m\n\end{cases} (70)
$$

where  $h^{\zeta}(\mathbf{R}_i)$  is the  $\zeta$ -th physicochemical value for the *i*-th (*i* = 1, 2, . . . , *L*) amino acid in **Eq.47**, and the dot  $(\cdot)$  means the multiplication sign.

Note that before substituting the physicochemical values into **Eq.70**, they are all subjected to a standard conversion as described by the following equation:

$$
h^{\zeta}(\mathbf{R}_{i}) = \frac{h_{0}^{\zeta}(\mathbf{R}_{i}) - \sum_{k=1}^{20} \frac{h_{0}^{\zeta}(\mathbb{R}_{k})}{20}}{\sqrt{\sum_{u=1}^{20} \left[h_{0}^{\zeta}(\mathbb{R}_{u}) - \sum_{k=1}^{20} \frac{h_{0}^{\zeta}(\mathbb{R}_{k})}{20}\right]^{2}}}
$$
(71)

where we use the  $\mathbb{R}_i$  (*i* = 1, 2, . . . , 20) to represent the 20 native amino acids. The symbols  $h_0^{\zeta}$  represent the  $\zeta$ -th original physicochemical value of the amino acid in the brackets right after the symbols.

<span id="page-21-0"></span>**Table 1.** The names of the 148 physicochemical indices for dinucleotides (DNA).



The values of 148 physicochemical indices can be found [here](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S1-148.txt).



<span id="page-22-0"></span>**Table 2.** The names of the 12 physicochemical indices for trinucleotides (DNA).

For more information of the indices listed in this table, please click [here,](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S2.pdf) their values can be found [here.](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S2-12.xls)



<span id="page-22-1"></span>**Table 3.** The names of the 6 physicochemical indices for dinucleotides (DNA).

For more information of the indices listed in this table, please click [here,](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S3.pdf) their values can be found [here.](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S3-DNA-6.xlsx)



<span id="page-22-2"></span>**Table 4.** The names of the 22 physicochemical indices for dinucleotides (RNA).

For more information of the indices listed in this table, please click [here,](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S4.pdf) their values can be found [here.](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S4-22%28RNA%29.xlsx)



<span id="page-23-0"></span>**Table 5.** The names of the 547 physicochemical indices for amino acids.



The meanings of the physicochemical indices can be found [here,](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/list_of_indices.txt) and their values can be found **here**.







<span id="page-26-0"></span>**Table 6.** The names of the 3 physicochemical indices for amino acids.

The values of 3 physicochemical indices can be found [here.](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S6-amino%20acid-3.xlsx)



<span id="page-27-0"></span>**Table 7.** The names of the 2 physicochemical indices for amino acids.

The values of 2 physicochemical indices can be found [here.](http://bioinformatics.hitsz.edu.cn/Pse-in-One/static/download/Supporting%20Information%20S7-amino%20acid-2.xlsx)



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