

**Table S2.** Fitted parameters of the mathematical model.

Category	Parameter	Units	Initial value	Biological interval	Fitted Value	Source
<i>Growth</i>	$g_{max}^{sh}$	$\text{cm}^3 \text{h}^{-1}$	0.203	(0.183, 0.223)	0.199	This study
	$g_{max}^r$	$\text{cm}^3 \text{h}^{-1}$	0.084	(0.076, 0.092)	0.088	This study
	$m_{g,sh}$	$\text{cm}^3$	19.349	(17.414, 21.284)	21.053	This study
	$m_{g,r}$	$\text{cm}^3$	7.983	(7.185, 8.782)	7.817	This study
	$a_{g,sh,su} = a_{g,r,su}$	$(\mu\text{g cm}^{-3})^2$	1.372	(1.234, 1.509)	1.366	This study
	$a_{g,sh,ph} = a_{g,r,ph}$	$(\mu\text{g cm}^{-3})^2$	$6.304 \cdot 10^4$	$(5.674 \cdot 10^4, 6.935 \cdot 10^4)$	$6.845 \cdot 10^4$	This study
	$C_{su,gr}^{sh} = C_{su,gr}^r$	$\mu\text{g cm}^{-3}$	360.415	(324.373, 396.456)	324.389	This study
$C_{ph,gr}^{sh} = C_{su,gr}^r$	$\mu\text{g cm}^{-3}$	69.693	(62.724, 76.663)	76.038	This study	
<i>Photosynthesis</i>	$P_{max}$	$\text{mol CO}_2$ $\text{m}^{-2} \text{s}^{-1}$	22.700	(20.000, 55.000)	52.230	Steven Adams (personal com.)

Category	Parameter	Units	Initial value	Biological interval	Fitted Value	Source
	$\alpha$	$\mu \text{ mol CO}_2 \text{ (J PAR)}^{-1}$	0.055	(0.044, 0.065)	0.049	Steven Adams (personal com.)
	$m_{F,ph}$	$\mu \text{ g cm}^{-3}$	100.000	(30.000, 350.000)	47.806	This study
	$s_{F,st}$	$(\mu \text{ g cm}^{-3})^2$	$2.250 \cdot 10^8$	$(2.250 \cdot 10^6, 2.250 \cdot 10^{10})$	$2.250 \cdot 10^8$	This study
	$sd_{F,st}$	dimensionless	0.010	(0.001, 0.200)	0.182	This study
	$s_{F,su}$	$(\mu \text{ g cm}^{-3})^2$	$4.225 \cdot 10^7$	$(4.225 \cdot 10^5, 4.225 \cdot 10^9)$	$4.227 \cdot 10^7$	This study
	$sd_{F,su}$	dimensionless	0.010	(0.0001, 1.000)	0.161	This study
Respiration	$m_{R,1}^{sh} = m_{R,1}^r$	$\mu \text{ g cm}^{-3} \text{ h}^{-1}$	33.333	(10.000, 66.667)	48.273	Rasse & Tocquin (2006)
	$m_{R,2}^{sh} = m_{R,2}^r$	$\mu \text{ g cm}^{-3} \text{ h}^{-1} (\mu \text{ g cm}^{-3})^{-1}$	0.085	(0.026, 0.255)	0.254	Rasse & Tocquin (2006)
	$g_R^{sh} = g_R^r =: g_R$	$\mu \text{ g cm}^{-3}$	$8.070 \cdot 10^3$	$(7.263 \cdot 10^3, 8.877 \cdot 10^3)$	$8.548 \cdot 10^3$	Amthor (2000)

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<i>Phloem</i>	$r$	cm	$5.0 \cdot 10^{-3}$	$(5.000 \cdot 10^{-4}, 5.000 \cdot 10^{-2})$	$5.536 \cdot 10^{-3}$	Sheehy <i>et al.</i> , 1995
<i>Sugar anabolism</i>	$\theta_{su}^{sh}$	$\mu\text{g cm}^{-3}$	$7.740 \cdot 10^4$	$(6.966 \cdot 10^4, 8.514 \cdot 10^4)$	$7.047 \cdot 10^4$	Rains, 1976
	$\theta_{su}^r$	$\mu\text{g cm}^{-3}$	$7.954 \cdot 10^4$	$(7.158 \cdot 10^4, 8.749 \cdot 10^4)$	$7.165 \cdot 10^4$	Rains, 1976
<i>Transpiration</i>	$E_d$	$\text{mol H}_2\text{O cm}^{-2}$ $\text{h}^{-1}$	$1.440 \cdot 10^{-4}$	$(1.296 \cdot 10^{-4}, 1.584 \cdot 10^{-4})$	$1.323 \cdot 10^{-4}$	Lambers <i>et al.</i> , 1998
	$E_n$	$\text{mol H}_2\text{O cm}^{-2}$ $\text{h}^{-1}$	$1.152 \cdot 10^{-4}$	$(1.037 \cdot 10^{-4}, 1.267 \cdot 10^{-4})$	$1.038 \cdot 10^{-4}$	Zeeman (personal com.): $0.8 \cdot E_d$
<i>Phosphate transport</i>	$p_{max}^r$	dimensionless	0.05	(0.010, 1.000)	0.061	This study
	$p_{max}^{sh}$	dimensionless	0.070	(0.010, 1.000)	0.052	This study
<i>Target sugar concentration</i>	$C_{su,t}^{sh}$	$\mu\text{g cm}^{-3}$	$1.0 \cdot 10^3$	$(5.000 \cdot 10^2, 2.500 \cdot 10^3)$	$8.693 \cdot 10^2$	This study

Category	Parameter	Units	Initial value	Biological interval	Fitted Value	Source
<i>Starch</i>	$s_{st}$	$(\mu\text{g cm}^{-3})^2$	$6.400 \cdot 10^{11}$	$(6.400 \cdot 10^9, 6.400 \cdot 10^{13})$	$6.400 \cdot 10^{11}$	This study
	$sd_{st}$	dimensionless	0.010	(0.001, 0.200)	0.142	This study
	$a_{\rho,1}$	$(\mu\text{g cm}^{-3})^2$	$2.250 \cdot 10^6$	$(2.250 \cdot 10^4, 2.250 \cdot 10^8)$	$2.276 \cdot 10^6$	This study
	$s_{\rho,2}$	$(\mu\text{g cm}^{-3})^2$	250.0	(2.500, 25000.000)	105.566	This study
	$s_{\rho,3}$	$(\mu\text{g cm}^{-3})^2$	350.0	$(3.500, 3.500 \cdot 10^4)$	$2.257 \cdot 10^4$	This study
	$k_1$	$h^{-1}$	0.005	(0.001, 0.015)	0.011	This study
	$k_2$	$h^{-1}$	0.010	(0.001, 0.030)	0.020	This study
	$k_3$	$h^{-1}$	0.020	(0.002, 0.060)	0.014	This study