

SUPPLEMENTARY TABLE

**Emergence of collective changes in travel direction of starling flocks  
from individual birds' fluctuations**

Alessandro Attanasi<sup>1,2</sup>, Andrea Cavagna<sup>1,2,3</sup>, Lorenzo Del Castello<sup>1,2</sup>, Irene Giardina<sup>1,2,3</sup>‡, Asja Jelic<sup>1,2</sup>‡,\*  
Stefania Melillo<sup>1,2</sup>, Leonardo Parisi<sup>1,2,4</sup>, Oliver Pohl<sup>1,2</sup>,† Edward Shen<sup>1,2</sup>, and Massimiliano Viale<sup>1,2</sup>

<sup>1</sup> *Istituto Sistemi Complessi, Consiglio Nazionale delle Ricerche, UOS Sapienza, 00185 Rome, Italy*

<sup>2</sup> *Dipartimento di Fisica, Università Sapienza, 00185 Rome, Italy*

<sup>3</sup> *Initiative for the Theoretical Sciences, The Graduate Center,  
City University of New York, 10016 New York, USA*

<sup>4</sup> *Dipartimento di Informatica, Università Sapienza, 00198 Rome, Italy and*

‡ *e-mail: asja.jelic@gmail.com, irene.giardina@roma1.infn.it*

EVENT	EVENT	$N$	$\Phi$	$\mathbf{I}_1 \cdot \mathbf{G}$	$\mathbf{I}_3 \cdot \mathbf{G}$	$\mathbf{V}_1 \cdot \mathbf{G}$	$\mathbf{I}_3 \cdot \mathbf{V}_1$	$\mathbf{I}_3 \cdot \mathbf{V}_2$	$\mathbf{I}_3 \cdot \frac{\mathbf{d}_0}{\ \mathbf{d}_0\ }$	$\mathbf{V}_1 \cdot \frac{\mathbf{d}_0}{\ \mathbf{d}_0\ }$	$\mathbf{V}_2 \cdot \frac{\mathbf{d}_0}{\ \mathbf{d}_0\ }$
NUMBER	LABEL			at $t_1$	at $t_1$	at $t_1$	at $t_1$	at $t_1$	at $t_1$	at $t_2$	at $t_1$
E1	20110208.ACQ3	176	0.806	0.95	0.15	0.47	0.14	0.93	0.97	0.08	-0.91
E2	20111124.ACQ1	125	0.959	0.97	0.15	0.01	0.65	0.99	0.97	0.81	-0.78
E3	20111125.ACQ1	50	0.866	0.86	0.42	0.26	0.41	0.88	0.91	0.05	-0.82
E4	20111214.ACQ4.F1	154	0.940	0.69	0.72	0.03	0.12	0.63	0.97	0.10	-0.83
E5	20111215.ACQ1	384	0.801	0.97	0.16	0.13	0.24	0.92	0.98	0.05	-0.94
E6	20111125.ACQ2	502	0.841	0.98	0.16	0.35	0.38	0.89	1.00	0.43	0.74
E7	20110217.ACQ2	404	0.854	0.91	0.32	0.39	0.34	0.96	0.78	0.83	-0.89
E8	20111220.ACQ2	197	0.907	0.98	0.03	0.94	0.30	0.90	0.56	0.20	-0.53
E9	20111201.ACQ3.F1	133	0.793	0.76	0.46	0.04	0.21	0.99	0.89	0.21	0.78
E10	20110211.ACQ1	595	0.757	0.94	0.10	0.34	0.03	0.36	0.91	0.37	-0.96
E11	20111214.ACQ4.F2.T1	139	0.890	0.35	0.87	0.67	0.92	0.56	0.84	0.74	0.08
E12	20111214.ACQ4.F2.T2	139	0.808	0.66	0.74	0.11	0.58	0.79	0.89	0.15	0.39

TABLE S1. **Global quantitative properties of the turning events.** We analyzed twelve turning events, of which two (E11 and E12) are performed by the same flock one after the other (therefore marked T1 and T2 in the event label).  $N$  is the number of birds in the flock. The polarization is defined as  $\Phi = \|(1/N) \sum_i \mathbf{v}_i / \|\mathbf{v}_i\|\|$ . In the remaining columns we report absolute values of the scalar products between yaw  $\mathbf{I}_1$  (the axis relative to the shortest dimension of the flock), the longest elongation axis  $\mathbf{I}_3$ , and gravity  $\mathbf{G}$ , with the direction of motion before and after the turn given by velocity vectors  $\mathbf{V}_1$  and  $\mathbf{V}_2$  at times  $t_1$  and  $t_2$ , respectively. The scalar products are calculated using the values of appropriate quantities at times  $t_1$  of the start of the turn, or  $t_2$  at the end of the turn, as indicated. Note that the vectors  $\mathbf{I}_1$ ,  $\mathbf{I}_3$ , and  $\mathbf{G}$  are unitary by definition, while for the direction of motion we used normalized velocity vectors  $\mathbf{n}_1 \equiv \mathbf{n}(t_1) = \mathbf{V}(t_1) / \|\mathbf{V}(t_1)\|$  and  $\mathbf{n}(t_2) = \mathbf{V}(t_2) / \|\mathbf{V}(t_2)\|$ , which are for clarity called  $\mathbf{V}_1$  and  $\mathbf{V}_2$  in the column titles. Finally, in order to quantify the location of the origin of the turn, we use a mean relative position of the 10 top-ranked birds with respect to the barycenter of the flock,  $\mathbf{d}_0$ , as defined in the main text. We calculate absolute scalar products of the normalized vector  $\mathbf{d}_0 / \|\mathbf{d}_0\|$  with the unitary vector  $\mathbf{I}_3$  of the longest elongation axes at  $t_1$ , as well as with the direction of motion at the start of the turn  $\mathbf{n}_1$ . In the last column, we report the scalar product between  $\mathbf{d}_0 / \|\mathbf{d}_0\|$  and the new direction of motion after the turn, given by the unitary velocity vector  $\mathbf{n}(t_2) = \mathbf{V}(t_2) / \|\mathbf{V}(t_2)\|$  (called  $\mathbf{V}_2$  for simplicity). Note that absolute values of all scalar products are reported, except for the last one whose negative values signify that the top-ranked birds initiated the turn in the direction towards the flock's barycenter (towards inside of the flock and not outside).

\* Present address: The Abdus Salam International Centre for Theoretical Physics (ICTP), Strada Costiera 11, 34014 Trieste, Italy.

† Present address: Institut für Theoretische Physik, Technische Universität Berlin, Hardenbergstrasse 36, D-10623 Berlin-Charlottenburg, Germany.