

Figure S6: **Strategies on the lattice.** The current player, C, has to choose the direction of the next player, N, according to the direction of the previous player, P. If player C is frozen, this player can only choose the strategy corresponding to the black line; if not frozen, this player can choose to follow any of the blue lines.