

Supplementary Material:

Defining an additivity framework for mixture research in inducible whole-cell biosensors

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Supplementary Material SM1 (Table). Summary of non-linear models and estimated parameters together with relevant statistical information of the model fits for the response of *Synechococcus elongatus* PCC 7942 pBG2120 to 6 heavy metals and their binary mixtures (Zn, Cu, Cd, Ag, Co and Hg)

Metal	Model Function	Parameter estimates				Residual Standard Error	
		Estimate value	Std.Error	t-value	p-		
Zn	lgau2	b	0.351996	0.048207	7.301822	0.0000	0.1698429
		c	1.475965	0.597634	2.469679	0.0199	
		d	80.099960	9.894407	8.095479	0.0000	
		e	2.245102 (2245.102) ^a	0.043678	51.401066	0.0000	
		f	2.662339	0.829132	3.210994	0.0033	
		Cd	lgau2	b	0.562495	0.039451	
c	1.039686	0.314707		3.303666	0.0031		
d	49.728622	3.290085		15.114693	0.0000		
e	5.340496 (5340.496) ^a	0.093375		57.193828	0.0000		
f	2.358463	0.293418		8.037883	0.0000		
Ag	gau2	b		0.1443642	0.0093814	15.3883702	0.0000
c		1.3247561	0.3296468	4.0187134	0.0007		
d		54.6960138	3.3118291	16.5153493	0.0000		
e		0.3292834 (329.2834) ^a	0.0045334	72.6353256	0.0000		
f		3.4229734	0.4677340	7.3182051	0.0000		
Co		lgau2	b	0.532205	0.066033	8.059677	0.0000
c	0.955349		0.336941	2.835362	0.0119		
d	18.297557		1.270958	14.396664	0.0000		
e	2.413876 (2413.876) ^a		0.084272	28.643759	0.0000		
f	2.028618		0.403140	5.032046	0.0001		
Cu	lgau2		b	0.24392	0.0096496	25.277	0.0000
c		0.40810	0.18429	2.2145	0.0354		
d		43.998	1.6215	27.134	0.0000		
e		0.046606 (46.606) ^a	0.00028072	166.02	0.0000		
f		2.1294	0.13881	15.341	0.0000		
Hg		lgau2	b	0.3284459 ^a	0.0724137	4.5356872	0.0002
c	0.9965343 ^a		0.5464225	1.8237431	0.0818		
d	33.5822889 ^a		2.9519420	11.3763375	0.0000		
e	0.0679623 ^a		0.0017048	39.8664205	0.0000		
f	1.0307636 ^a		0.1737224	5.9333959	0.0000		
Cu: Cd	Gau2		b	0.833872	0.087886	9.488139	0.0000
c		1.587702	0.559394	2.838253	0.0098		
d		32.661863	2.571750	12.700250	0.0000		
e		2.526442	0.039160	64.515964	0.0000		
f		2.226572	0.326413	6.821331	0.0000		
Cu: Zn		Lgau2	b	0.210524	0.020723	10.159021	0.0000
c	1.058583		0.215034	4.922875	0.0002		
d	111.998627		5.055904	22.152047	0.0000		
e	1.584642		0.016992	93.255607	0.0000		
f	1.442243		0.112803	12.785522	0.0000		

Zn:Cd	Lgau2	b	0.555188	0.015215	36.489732	0.0000	0.02654068
		c	-0.290451	0.583670	-0.497628	0.626	
		d	42.910857	0.943991	45.456837	0.0000	
		e	2.321820	0.012425	186.867587	0.0000	
		f	2.024344	0.134982	14.997109	0.0000	
		<hr/>					
Cu:Hg	Lgau2	b	0.6340408	0.0362401	17.4955546	0.0000	0.05278326
		c	2.2452456	0.3135964	7.1596667	0.0000	
		d	74.6073845	3.0968760	24.0911760	0.0000	
		e	0.0260586	0.0004689	55.5735249	0.0000	
		f	3.1835757	0.3918444	8.1245914	0.0000	
		<hr/>					
Cu:Co	Gau2	b	0.85374	0.010441	81.771	0.0000	0.03405409
		c	1.3777	0.13300	10.359	0.0000	
		d	21.115	0.52473	40.239	0.0000	
		e	1.4961	0.0070987	210.75	0.0000	
		f	6.0718	0.35879	16.923	0.0000	
		<hr/>					
Co:Cd	Lgau2	b	0.26824	0.0098237	27.305	0.0000	0.05352349
		c	1.8005	0.18445	9.7614	0.0000	
		d	35.467	1.2264	28.920	0.0000	
		e	3.2161	0.013300	241.81	0.0000	
		f	2.8076	0.26146	10.738	0.0000	
		<hr/>					
Ag:Cd	Gau2	b	0.59045	0.017055	34.620	0.0000	0.0487012
		c	1.4009	0.19988	7.0088	0.0000	
		d	77.971	2.1637	36.037	0.0000	
		e	2.7331	0.0078159	349.69	0.0000	
		f	2.1606	0.079377	27.220	0.0000	
		<hr/>					
Cu:Ag	Lgau2	b	0.34083	0.013952	24.429	0.0000	0.05808011
		c	1.8282	0.24210	7.5516	0.0000	
		d	78.149	2.8113	27.798	0.0000	
		e	0.20627	0.0010609	194.43	0.0000	
		f	2.2139	0.12447	17.787	0.0000	
		<hr/>					
Zn:Ag	Gau2	b	0.28513	0.0077488	36.797	0.0000	0.04642924
		c	1.1717	0.18042	6.4942	0.0000	
		d	123.94	3.2011	38.717	0.0000	
		e	1.5822	0.0039700	398.53	0.0000	
		f	2.0776	0.061918	33.553	0.0000	
		<hr/>					
Co:Ag	Gau2	b	0.40242	0.038248	10.521	0.0000	0.04745158
		c	1.7071	0.30221	5.6487	0.0000	
		d	11.328	0.99761	11.356	0.0000	
		e	1.0509	0.0099931	105.16	0.0000	
		f	3.0655	0.74799	4.0984	0.0007	
		<hr/>					
Zn:Co	Gau2	b	0.42157	0.0097373	43.295	0.0000	0.03552789
		c	1.7071	0.30221	5.6487	0.0000	
		d	11.328	0.99761	11.356	0.0000	
		e	2.0648	0.0047810	431.88	0.0000	
		f	2.0479	0.054401	37.644	0.0000	
		<hr/>					
Cu:Hg	Lgau2	b	0.6340408	0.0362401	17.49555	0.0000	0.05278326
		c	2.2452456	0.3135964	7.1596667	0.0000	
		d	74.6073845	3.0968760	24.0911760	0.0000	
		e	0.0260586	0.0004689	55.5735249	0.0000	
		f	3.1835757	0.3918444	8.1245914	0.0000	
		<hr/>					
Cd:Hg	Lgau2	b	0.335736	0.010892	30.824749	0.0000	0.03659033
		c	1.487436	0.158866	9.362838	0.0000	
		d	71.957893	1.550272	46.416307	0.0000	
		e	2.487738	0.017196	144.672177	0.0000	

		f	2.508632	0.142398	17.617043	0.0000	
Zn:Hg	Gau2	b	0.28384	0.015798	17.967	0.0000	0.07234654
		c	1.3458	0.29692	4.5326	0.0001	
		d	154.63	8.0164	1.9290	0.0000	
		e	1.3592	0.0060743	223.76	0.0000	
		f	2.2107	0.13004	16.999	0.0000	
Hg:Co	Lgau2	b	0.464864	0.054759	8.489311	0.0000	0.05336395
		c	2.154873	0.322521	6.681348	0.0000	
		d	65.070756	2.618477	24.850612	0.0000	
		e	0.754579	0.030447	24.783295	0.0000	
		f	2.812375	0.814988	3.450817	0.0000	
Hg:Ag	Gau2	b	0.071195	0.0014252	49.954	0.0000	0.02301
		c	-0.0050033	0.12298	-0.040684	0.968	
		d	34.655	0.58610	59.128	0.0000	
		e	0.18673	0.00079776	234.07	0.0000	
		f	1.9507	0.062492	31.215	0.0000	

^a (nM)

gau and lgau refers to the Normal and log-normal biphasic dose-response models described in the gaussian {drc} functions in *drc* R package ¹. Parameter estimates and estimated residual standard errors are calculated using the function *drm* {drc} which is based on the function *optim* {stats} ² which relies on the minimisation of the minus log likelihood function. For a quantitative response this reduces to least squares estimation, which is carried out by minimising the following sums of squares

$$\sum_{i=1}^N [w_i (y_i - f_i)]^2$$

where y_i , f_i , and w_i correspond to the observed value, expected value, and the weight respectively, for the i th observation (from 1 to N).

Supplementary Material SM2 (Table). *EDp* vectors (-50, 0, +50) for Cu, Cd, Zn, Cu, Hg and Co.

Metal	Fractional effect	<i>EDp</i> (μM , BIF)	
		<i>D(p)</i> (μM)	<i>E(p)</i> (BIF)
Zn	<i>ED</i> ₋₅₀	1.508±0.082	40.79±3.33
	<i>ED</i> ₀	2.8±0.11	79.31±8.89
	<i>ED</i> ₊₅₀	3.34±0.18	4.79±7.38
Cd	<i>ED</i> ₋₅₀	2.8±0.11	25.38±1.69
	<i>ED</i> ₀	5.94±0.18	49.24±3.03
	<i>ED</i> ₊₅₀	10.19±0.39	25.38±1.49
Ag	<i>ED</i> ₋₅₀	0.17±0.006	28.01±1.79
	<i>ED</i> ₀	0.37±0.013	54.16±3.12
	<i>ED</i> ₊₅₀	0.49±0.012	28.01±4.39
Co	<i>ED</i> ₋₅₀	1.29±0.07	9.63±15
	<i>ED</i> ₀	2.61±0.1	18.12±1.17
	<i>ED</i> ₊₅₀	4.51±0.24	9.63±0.76
Cu	<i>ED</i> ₋₅₀	0.035±0.0004	22.2±0.97
	<i>ED</i> ₀	0.048±0.0003	43.56±1.53
	<i>ED</i> ₊₅₀	0.062±0.0007	22.2±0.95
Hg ^a	<i>ED</i> ₋₅₀	0.043±0.003	17.29±1.24
	<i>ED</i> ₀	0.068±0.001	33.25±3.04
	<i>ED</i> ₊₅₀	0.11±0.008	17.29±1.08

±: Standard error. Standard error are estimated from the non-linear fitted model. Fitted non-linear models and estimated parameters can be found in Table SM1.

^a (nM).

Supplementary Material SM3 (Tutorial)

Fitting non-monotonic dose-response with differential maximal effects and analysis of departures from additivity based on multivariate Loewe additivity using R.

From: *Defining an additivity framework for mixture research in inducible whole-cell biosensors.*

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A novel additivity framework for mixture-effect research in the framework of whole-cell inducible biosensors has been mathematically developed. The method proposes a multivariate extension of the effective dose (*ED_p*) notation in order to take into account the occurrence of differential maximal effects and inhibition beyond the maximum permissive concentrations (MPCs). This allow a dimensional extension of Loewe additivity which enables its direct application in a biphasic dose-response framework. The utilities that allow to achieve this new approach have been incorporated in the (*drc*) package for R¹.

#Example data:

The dataset “metaldata.csv” and the functional R-script “SM3_Script_R.R” used in the present example are freely available from <http://dx.doi.org/10.6084/m9.figshare.1476176>

In the present tutorial, we will explain how to use the novel method developed in order to model dose-response profiles of an inducible whole cell biosensor to individual *stimuli* and mixtures (in the present case, different heavy metals). We will analyse the “metaldata.csv” dataset. This dataset includes the raw data resulted from the individual exposure of the inducible whole cell biosensor *Synechococcus elongatus* PCC 7942 pBG2120³ to six metals and their 15 possible binary combinations.

The dataset is importable as data.frame in R as follows: (from the root directory:

```
metaldata<-read.csv(file="metaldata.csv")
```

The data frame have 3 variables: “metal” (factor), “conc” (numeric), “IR” (induction factor, the same asBIF in the main text) (numeric). In the tutorial, we will explain the *drc* extension using the data for Zn, Cd and its mixture, ZnCd.

#Make a subset with the Zn data

```
Zn <- metaldata[metaldata$metal=="Zn",]
```

```
Zn
```

	metal	conc	IR
1	Zn	0.0369	0.9142857
2	Zn	0.0369	0.9756098
3	Zn	0.0369	0.8974359
4	Zn	0.0925	0.9523810
5	Zn	0.0925	0.8780488
6	Zn	0.0925	1.1666667
7	Zn	0.1859	0.9523810
8	Zn	0.1859	1.1707317
9	Zn	0.1859	1.2115385
10	Zn	0.5693	1.7523810
11	Zn	0.5693	1.6585366
12	Zn	0.5693	1.7948718
13	Zn	0.9684	5.9809524
14	Zn	0.9684	4.6341463
15	Zn	0.9684	4.8461538
16	Zn	1.3836	14.2857143
17	Zn	1.3836	19.7073171
18	Zn	1.3836	22.7051282
19	Zn	1.4472	43.9500000
20	Zn	1.4472	44.0869565
21	Zn	1.4472	43.2000000
22	Zn	2.0371	67.1238095
23	Zn	2.0371	74.0975610
24	Zn	2.0371	86.0192308
25	Zn	3.2111	31.1619048
26	Zn	3.2111	61.2195122
27	Zn	3.2111	64.6153846
28	Zn	4.4946	3.8857143
29	Zn	4.4946	4.8292683
30	Zn	4.4946	5.3846154
31	Zn	10.7532	0.3428571
32	Zn	10.7532	0.5853659
33	Zn	10.7532	0.6730769

#Fitting biphasic dose-response profiles:

Inducible whole cell biosensors usually present inverted v-shaped biphasic dose-response profiles. This specific type of dose-response pattern may be fitted using nonlinear regression model equations as Gaussian (gau) or LogGaussian (lgau) with or without the use of variance-stabilizing Box-Cox transform-both-sides approach. (For more detail see section 2.1 *Fitting biphasic dose-response profiles* of the manuscript).

#gaussian function:

```
Zn.gau <- drm(IR~conc, data=Zn, fct=gaussian(), na.action=na.omit)
```

```
summary(Zn.gau)
```

Model fitted: Gaussian (5 parms)

Parameter estimates:

	Estimate	Std. Error	t-value	p-value
b:(Intercept)	8.8613e-01	9.3682e-03	9.4589e+01	0.0000
c:(Intercept)	2.1660e+00	1.2821e+00	1.6895e+00	0.1022
d:(Intercept)	7.5746e+01	3.3920e+00	2.2331e+01	0.0000
e:(Intercept)	2.3418e+00	8.6316e-03	2.7131e+02	0.0000

```
f:(Intercept) 1.3880e+01 2.8981e+00 4.7894e+00 0.0000
```

Residual standard error:

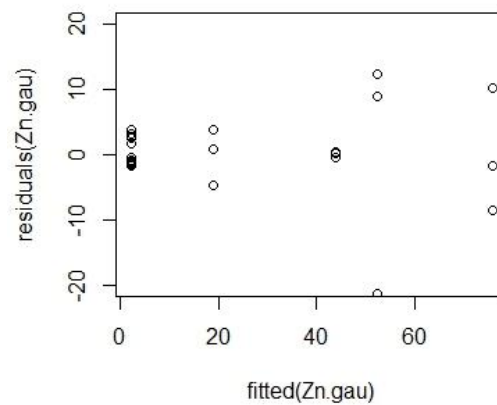
5.87511 (28 degrees of freedom)

For complete information of the `drm {drc}` consult the tutorial of `drc` package <http://cran.r-project.org/web/packages/drc/index.html>

Model checking

Best-fit models can be selected based on the residual standard error that is indicated in the model summary. For visual observation they can be plotted:

```
plot(fitted(Zn.gau), residuals(Zn.gau), ylim = c(-20, 20))
```



Gaussian function with Box-Cox transform

```
Zn.gau2 <- drm(IR~conc, data=Zn, fct=gaussian(), na.action=na.omit, bcVal = 0, bcAdd = 10)
```

```
summary(Zn.gau2)
```

Model fitted: Gaussian (5 parms)

Parameter estimates:

	Estimate	Std. Error	t-value	p-value
b:(Intercept)	0.793259	0.075520	10.503961	0.0000
c:(Intercept)	1.613775	0.500908	3.221697	0.0032
d:(Intercept)	81.080825	10.982114	7.382989	0.0000
e:(Intercept)	2.422227	0.042576	56.892278	0.0000
f:(Intercept)	3.115795	0.624967	4.985533	0.0000

Residual standard error:

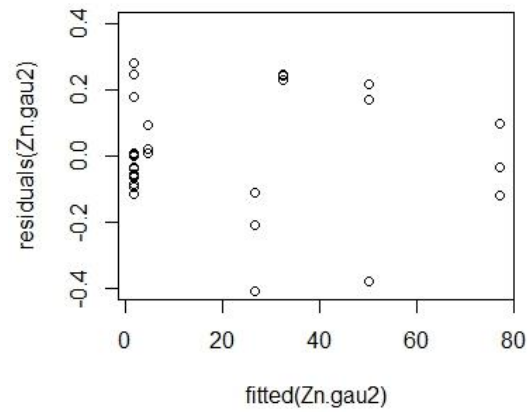
0.17677 (28 degrees of freedom)

Non-normality/heterogeneity adjustment through optimal Box-Cox transformation

Specified lambda: 0

Model checking

```
plot(fitted(Zn.gau2), residuals(Zn.gau2), ylim = c(-0.4, 0.4))
```



#lgaussian function

```
Zn.lgau <- drm(IR~conc, data=Zn, fct=lgaussian(), na.action=na.omit)
summary(Zn.lgau)
```

Model fitted: Log-Gaussian (5 parms)

Parameter estimates:

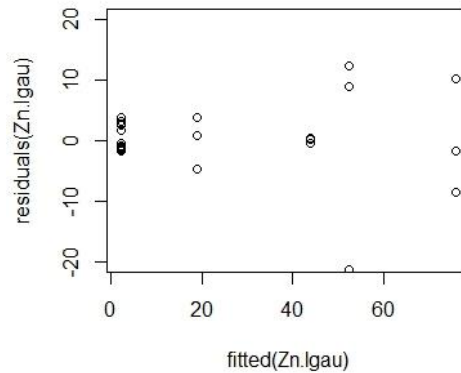
	Estimate	Std. Error	t-value	p-value
b:(Intercept)	4.0134e-01	6.4603e-03	6.2124e+01	0.0000
c:(Intercept)	2.1661e+00	1.2821e+00	1.6895e+00	0.1022
d:(Intercept)	7.5747e+01	3.3920e+00	2.2331e+01	0.0000
e:(Intercept)	2.1746e+00	1.2839e-02	1.6938e+02	0.0000
f:(Intercept)	9.1066e+00	1.8773e+00	4.8510e+00	0.0000

Residual standard error:

5.87511 (28 degrees of freedom)

#Model checking

```
plot(fitted(Zn.lgau), residuals(Zn.lgau), ylim = c(-20, 20))
```



lgaussian function with Box-Cox transform

```
Zn.lgau2 <- drm(IR~conc, data=Zn, fct=lgaussian(), na.action=na.omit, bcVal = 0, bcAdd = 10)
```

```
summary(Zn.lgau2)
```

Model fitted: Log-Gaussian (5 parms)

Parameter estimates:

	Estimate	Std. Error	t-value	p-value
b:(Intercept)	0.351996	0.048207	7.301822	0.0000
c:(Intercept)	1.475965	0.597634	2.469679	0.0199
d:(Intercept)	80.099960	9.894407	8.095479	0.0000
e:(Intercept)	2.245102	0.043678	51.401066	0.0000
f:(Intercept)	2.662339	0.829132	3.210994	0.0033

Residual standard error:

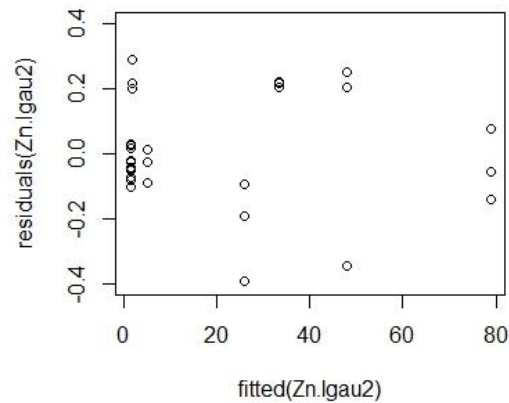
0.1698429 (28 degrees of freedom)

Non-normality/heterogeneity adjustment through optimal Box-Cox transformation

Specified lambda: 0

#Model checking

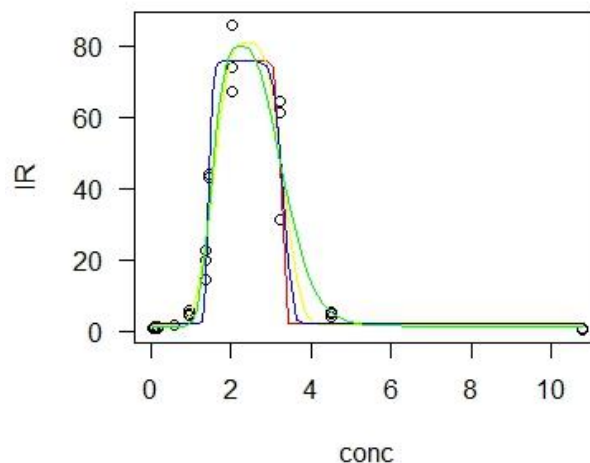
```
plot(fitted(Zn.lgau2), residuals(Zn.lgau2), ylim = c(-0.4, 0.4))
```



#plot:

We can visually observe all the functions used in order to have a visual overview of the models fitted.

```
plot(Zn.gau, type = "obs", col= "black", log = "")
plot(Zn.gau, type = "none", add = TRUE, col = "red")
plot(Zn.gau2, type = "none", add = TRUE, col = "yellow")
plot(Zn.lgau, type = "none", add = TRUE, col = "blue")
plot(Zn.lgau2, type = "none", add = TRUE, col = "green")
```



Based on the residuals standard errors and the visual examination, we can conclude that the LogGaussian with Box-Cox modification (green line) is the model that fit better the experimental data, therefore it will be used for fitting Zn response in the rest of calculations.

#Effective doses (ED_p) calculation:

Using the `ED {drc}` function, we can get the $D(p)$ vectors at any desired fractional effect p . We selected the three representative p levels: -50 (half of the E_{max} , in the induction region), 99.9 (E_{max}) and +50 (half of the E_{max} , in the inhibition region) (*Equivalent to the -50, 0, +50 p levels in the manuscript*). For more details, see section 2.2 *a multivariate extension of the effective dose notation of the manuscript*. Note: to get the $E(p)$ values, for the moment it is required to use the `indicesFct {drc}` function which will be described in next sections.

```
ED(Zn.lgau2, -50, interval = "delta", bound = FALSE)
```

```
Estimate Std. Error Lower Upper
1:-50 1.508038 0.082849 1.338329 1.6777
```

```
ED(Zn.lgau2, 99.9,interval = "delta")
```

```
Estimate Std. Error Lower Upper
1:99.9 2.32300 0.10458 2.10877 2.5372
```

```
ED(Zn.lgau2, 50, interval = "delta")
```

```
Estimate Std. Error Lower Upper
1:50 3.34241 0.18363 2.96627 3.7186
```

#Cd fit:

Now, we are going to fit the second data component, in that case, Cd. For that, we use the same steps as for Zn.

#Make a subset with the Cd data

```
Cd <- metaldata[metaldata$metal=="Cd",]
```

```
Cd
```

#Fitting biphasic dose-response profiles:

#gaussian function

```
Cd.gau <- drm(IR~conc, data=Cd, fct=gaussian(), na.action=na.omit)
```

```
summary(Cd.gau)
```

```
Model fitted: Gaussian (5 parms)
```

```
Parameter estimates:
```

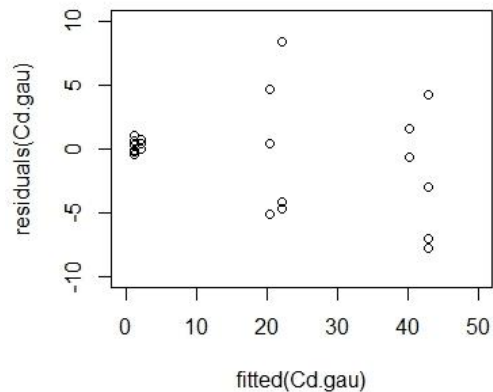
```
Estimate Std. Error t-value p-value
b:(Intercept) 4.079689 0.115139 35.432648 0.0000
c:(Intercept) 1.283627 1.275138 1.006657 0.3246
d:(Intercept) 42.981885 1.907644 22.531393 0.0000
e:(Intercept) 6.850150 0.070015 97.838717 0.0000
f:(Intercept) 7.805005 3.237173 2.411056 0.0243
```

```
Residual standard error:
```

```
4.4849 (23 degrees of freedom)
```

#Model checking

```
plot(fitted(Cd.gau), residuals(Cd.gau), ylim = c(-10, 10))
```



#Gaussian function with Box-Cox transform

```
Cd.gau2 <- drm(IR~conc, data=Cd, fct=gaussian(), na.action=na.omit, bcVal = 0, bcAdd = 10)
```

```
summary(Cd.gau2)
```

Model fitted: Gaussian (5 parms)

Parameter estimates:

	Estimate	Std. Error	t-value	p-value
b:(Intercept)	4.056422	0.090069	45.036766	0.0000
c:(Intercept)	1.202271	0.352358	3.412072	0.0024
d:(Intercept)	42.700145	2.340528	18.243805	0.0000
e:(Intercept)	6.851570	0.053432	128.230478	0.0000
f:(Intercept)	7.234677	1.057973	6.838241	0.0000

Residual standard error:

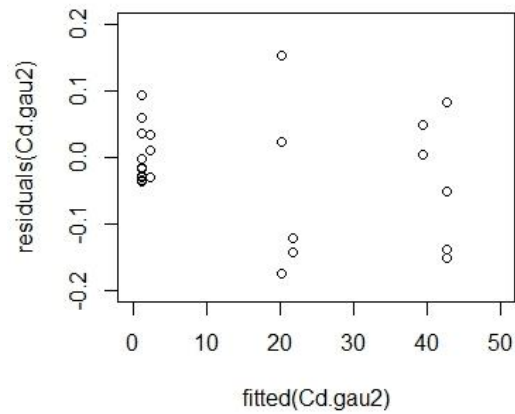
0.1088791 (23 degrees of freedom)

Non-normality/heterogeneity adjustment through optimal Box-Cox transformation

Specified lambda: 0

#Model checking

```
plot(fitted(Cd.gau2), residuals(Cd.gau2), ylim = c(-0.2, 0.2))
```



#lgaussian function

```
Cd.lgau <- drm(IR~conc, data=Cd, fct=lgaussian(), na.action=na.omit)
```

```
summary(Cd.lgau)
```

Model fitted: Log-Gaussian (5 parms)

Parameter estimates:

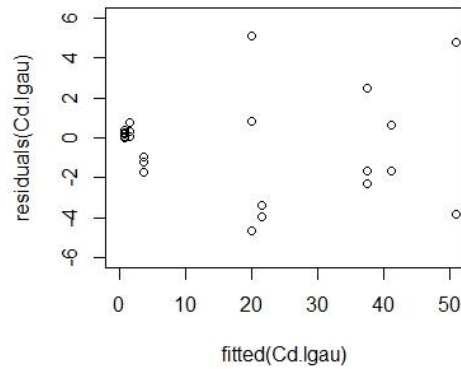
	Estimate	Std. Error	t-value	p-value
b:(Intercept)	0.544683	0.032578	16.719520	0.0000
c:(Intercept)	0.806563	0.920847	0.875893	0.3901
d:(Intercept)	51.009281	2.143174	23.800808	0.0000
e:(Intercept)	5.315768	0.093498	56.854176	0.0000
f:(Intercept)	2.105116	0.261655	8.045382	0.0000

Residual standard error:

3.086809 (23 degrees of freedom)

#Model checking

```
plot(fitted(Cd.lgau), residuals(Cd.lgau), ylim = c(-6, 6), xlim = c(0, 50))
```



#lgaussian function with Box-Cox transform

```
Cd.lgau2 <- drm(IR~conc, data=Cd, fct=lgaussian(), na.action=na.omit, bcVal = 0, bcAdd = 10)
```

```
summary(Cd.lgau2)
```

Model fitted: Log-Gaussian (5 parms)

Parameter estimates:

	Estimate	Std. Error	t-value	p-value
b:(Intercept)	0.562495	0.039451	14.258093	0.0000
c:(Intercept)	1.039686	0.314707	3.303666	0.0031
d:(Intercept)	49.728622	3.290085	15.114693	0.0000
e:(Intercept)	5.340496	0.093375	57.193828	0.0000
f:(Intercept)	2.358463	0.293418	8.037883	0.0000

Residual standard error:

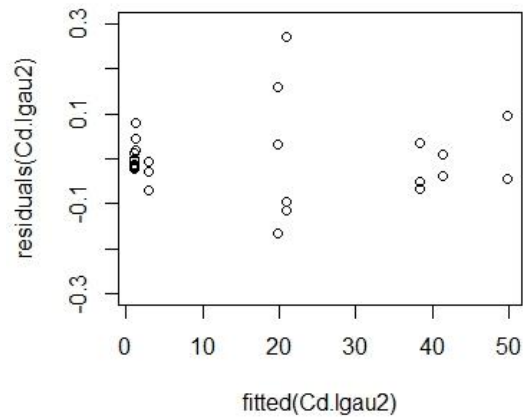
0.09005292 (23 degrees of freedom)

Non-normality/heterogeneity adjustment through optimal Box-Cox transformation

Specified lambda: 0

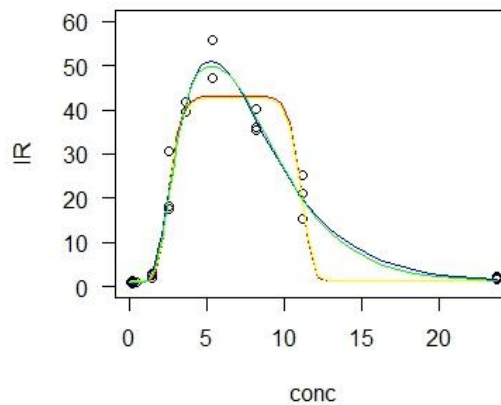
#Model checking

```
plot(fitted(Cd.lgau2), residuals(Cd.lgau2), ylim = c(-0.3, 0.3))
```



#plot:

```
plot(Cd.gau, type = "obs", col= "black", log = "", ylim = c(0, 60))
plot(Cd.gau, type = "none", add = TRUE, col = "red")
plot(Cd.gau2, type = "none", add = TRUE, col = "yellow")
plot(Cd.lgau, type = "none", add = TRUE, col = "blue")
plot(Cd.lgau2, type = "none", add = TRUE, col = "green")
```



Based on the residuals standard errors and the visual examination, we can observed that the LogGaussian with Box-Cox modification (green line) is the model that fits better Cd experimental data, therefore it will be used for fitting Cd response in the rest of calculations.

#Effective doses ($D(p)$) calculation:

```
ED(Cd.lgau2, -50, interval = "delta", bound = FALSE)
```

	Estimate	Std. Error	Lower	Upper
1:-50	2.79902	0.10714	2.57737	3.0207


```
ED(Cd.lgau2, 99.9,interval = "delta")
```

```
Estimate Std. Error Lower Upper  
1:99.9 5.56039 0.11333 5.32594 5.7948
```

```
ED(Cd.lgau2, 50,interval = "delta")
```

```
Estimate Std. Error Lower Upper  
1:50 10.18961 0.39005 9.38273 10.996
```

#Fitting mixture data:

In order to predict the biosensor response to any combination of the individual metals and also, to be able to analyse departures from additivity, it is required to fit the mixture data to a nonlinear regression model equation. Zn and Cd mixture data are used as example.

Make a subset with the ZnCd data

```
ZnCd <- metaldata[metaldata$metal=="ZnCd",]
```

#gaussian function

```
ZnCd.gau <- drm(IR~conc, data=ZnCd, fct=gaussian(), na.action=na.omit)
```

```
summary(ZnCd.gau)
```

```
Model fitted: Gaussian (5 parms)
```

```
Parameter estimates:
```

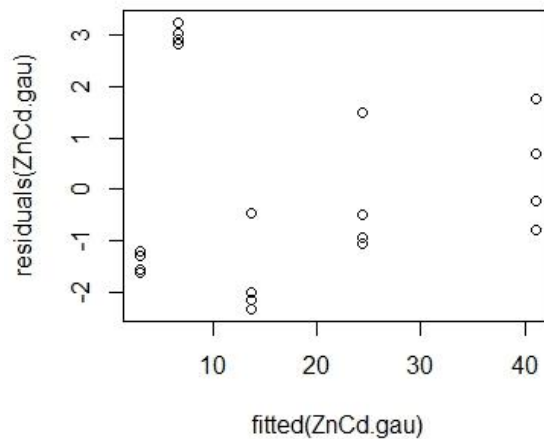
```
Estimate Std. Error t-value p-value  
b:(Intercept) 9.1892e-03 NA NA NA  
c:(Intercept) 2.3311e+00 1.1228e+00 2.0760e+00 0.0555  
d:(Intercept) 1.0401e+03 NA NA NA  
e:(Intercept) 2.8890e+00 2.3606e-02 1.2239e+02 0.0000  
f:(Intercept) 4.1168e-01 1.6657e-02 2.4716e+01 0.0000
```

```
Residual standard error:
```

```
2.123171 (15 degrees of freedom)
```

#Model checking

```
plot(fitted(ZnCd.gau), residuals(ZnCd.gau))
```



#Gaussian function with Box-Cox transform

```
ZnCd.gau2 <- drm(IR~conc, data=ZnCd, fct=gaussian(), na.action=na.omit, bcVal = 0, bcAdd = 10)
```

```
summary(ZnCd.gau2)
```

Model fitted: Gaussian (5 parms)

Parameter estimates:

	Estimate	Std. Error	t-value	p-value
b:(Intercept)	0.040441	0.032399	1.248238	0.2311
c:(Intercept)	0.561210	1.249161	0.449269	0.6597
d:(Intercept)	330.288516	136.118307	2.426481	0.0283
e:(Intercept)	2.899675	0.049022	59.151001	0.0000
f:(Intercept)	0.473996	0.074228	6.385670	0.0000

Residual standard error:

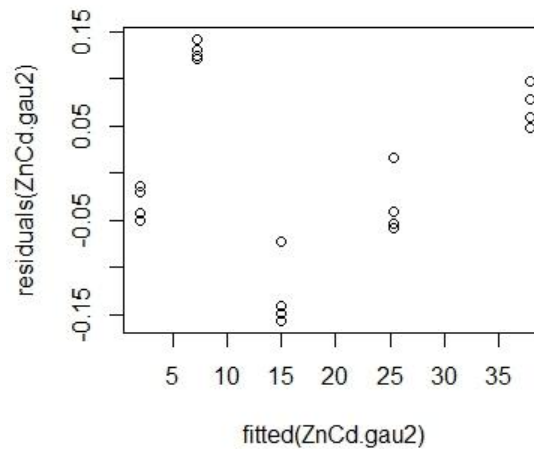
0.1078746 (15 degrees of freedom)

Non-normality/heterogeneity adjustment through optimal Box-Cox transformation

Specified lambda: 0

#Model checking

```
plot(fitted(ZnCd.gau2), residuals(ZnCd.gau2), ylim = c(-0.15, 0.15))
```



#lgaussian function

```
ZnCd.lgau <- drm(IR~conc, data=ZnCd, fct=lgaussian(), na.action=na.omit)
```

```
summary(ZnCd.lgau)
```

Model fitted: Log-Gaussian (5 parms)

Parameter estimates:

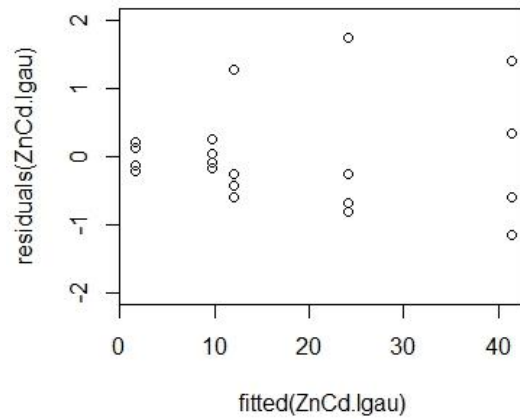
	Estimate	Std. Error	t-value	p-value
b:(Intercept)	0.555663	0.015419	36.038564	0.0000
c:(Intercept)	-0.274800	1.032831	-0.266065	0.7938
d:(Intercept)	42.904780	0.747360	57.408441	0.0000
e:(Intercept)	2.321479	0.018413	126.077969	0.0000
f:(Intercept)	2.028462	0.164444	12.335300	0.0000

Residual standard error:

0.834502 (15 degrees of freedom)

#Model checking

```
plot(fitted(ZnCd.lgau), residuals(ZnCd.lgau), ylim = c(-2, 2))
```



#lgaussian function with Box-Cox transform

```
ZnCd.lgau2 <- drm(IR~conc, data=ZnCd, fct=lgaussian(), na.action=na.omit, bcVal = 0, bcAdd = 10)
```

```
summary(ZnCd.lgau2)
```

Model fitted: Log-Gaussian (5 parms)

Parameter estimates:

	Estimate	Std. Error	t-value	p-value
b:(Intercept)	0.555188	0.015215	36.489732	0.000
c:(Intercept)	-0.290451	0.583670	-0.497628	0.626
d:(Intercept)	42.910857	0.943991	45.456837	0.000
e:(Intercept)	2.321820	0.012425	186.867587	0.000
f:(Intercept)	2.024344	0.134982	14.997109	0.000

Residual standard error:

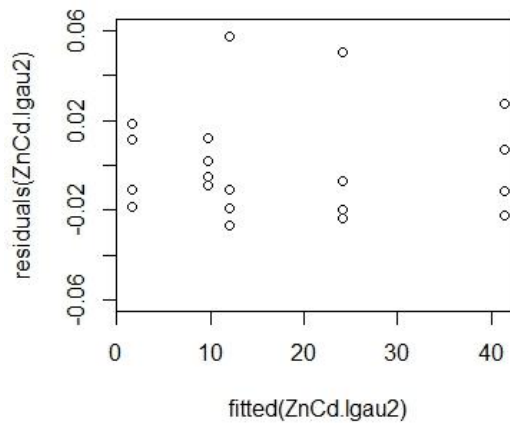
0.02654068 (15 degrees of freedom)

Non-normality/heterogeneity adjustment through optimal Box-Cox transformation

Specified lambda: 0

#Model checking

```
plot(fitted(ZnCd.lgau2), residuals(ZnCd.lgau2), ylim = c(-0.06, 0.06))
```



#Plot:

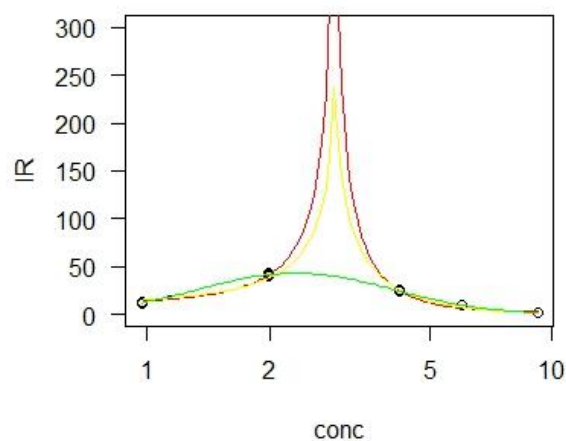
```
plot(ZnCd.gau, type = "obs", col= "black", ylim = c(0, 300))
```

```
plot(ZnCd.gau, type = "none", add = TRUE, col = "red")
```

```
plot(ZnCd.gau2, type = "none", add = TRUE, col = "yellow")
```

```
plot(ZnCd.lgau, type = "none", add = TRUE, col = "blue")
```

```
plot(ZnCd.lgau2, type = "none", add = TRUE, col = "green")
```



Based on the residuals standard errors and visual observation, we can infer that the LogGaussian with Box-Cox modification (green line) is the model that fits better the experimental data, therefore it will be used for fitting ZnCd response in the rest of calculations.

#Effective doses ($D(p)$) calculation:

```
ED(ZnCd.lgau2, -50, interval = "delta", bound = FALSE)
```

	Estimate	Std. Error	Lower	Upper
1:-50	1.209189	0.014632	1.178001	1.2404

```
ED(ZnCd.lgau2, 99.9, interval = "delta")
```

	Estimate	Std. Error	Lower	Upper
1:99.9	2.382456	0.015367	2.349703	2.4152

```
ED(ZnCd.lgau2, 50, interval = "delta")
```

	Estimate	Std. Error	Lower	Upper
1:50	4.458236	0.053948	4.343248	4.5732

#Additivity predictions and departures from additivity:

$E(p)$ calculation

We apply the method to perform additivity predictions and to study the nature of the interaction through the *indicesFct* {drc} command. The first datum that has to be indicated is the ratio in which metals are present in the mixture. After that, we have to introduce the list with the model equations fitted for the mixture and the individual metals, respectively. The ratio only has to be indicated for the individual metal indicated first. (For example, in the case below, the ratio Zn: Cd is 0.355:0.645, therefore, as Zn is the first individual metal introduced, we indicated is 0.355 as ratio data). In c() vector we indicated the fractional effect (p) which we want to be considered.

```
indicesFct(0.355, list(ZnCd.lgau2, Zn.lgau2, Cd.lgau2), c(-0.2, -0.5, -1, -2, -5, -10, -20, -30, -40, -50, -60, -70, -80, -90, -99, 99, 80, 70, 60, 50, 40, 30, 20, 10, 5, 2, 1, 0.5, 0.2))
```

#ECmat: Matrix with the fitted nonlinear regression model equations concentration data for the mixture (ECmix, Zn: Cd), the first individual metal indicated (EC1, Zn) and the second individual metal indicated (EC2, Cd) and the standard error, respectively. These data correspond to the $D(p)$ data for all the fractional effect indicated in indicesFct.

#Emat: Matrix with the fitted nonlinear regression model equations effect data for the mixture (ECmix, Zn: Cd), the first individual metal indicated (EC1, Zn) and the second individual metal indicated (EC2, Cd) and the standard error, respectively. These data correspond to the $E(p)$ data for all the fractional effect indicated.

```
#ECmat
```

```
$ECmat
  ECmix  EC1  EC2  SEMix  SE1  SE2
-0.2 0.3377212 0.9063974 1.038593 0.04011755 0.13046075 0.14144360
-0.5 0.3908416 0.9554918 1.155985 0.03941034 0.11453523 0.13457294
-1 0.4403353 0.9982981 1.262736 0.03821894 0.10068741 0.12756483
-2 0.5008234 1.0475599 1.390481 0.03621944 0.08504322 0.11864606
-5 0.6052838 1.1265598 1.605791 0.03175981 0.06167670 0.10360652
-10 0.7130718 1.2020991 1.823015 0.02636580 0.04433297 0.09065132
-20 0.8635123 1.3004321 2.121074 0.01865975 0.03990628 0.08155946
-30 0.9854817 1.3758876 2.360446 0.01376951 0.05191294 0.08431427
```

```

-40 1.0980212 1.4431499 2.580827 0.01236843 0.06724096 0.09380770
-50 1.2091890 1.5080376 2.799017 0.01463218 0.08284889 0.10714382
-60 1.3247947 1.5744593 3.027361 0.01900860 0.09824789 0.12269719
-70 1.4513381 1.6465755 3.280125 0.02418490 0.11340309 0.13948356
-80 1.5994438 1.7311354 3.581510 0.02937550 0.12816148 0.15641649
-90 1.7951676 1.8452853 3.993509 0.03323070 0.14111191 0.17001128
-99 2.1420593 2.0701401 4.797048 0.02491718 0.13005296 0.14361250
99 2.5166671 2.4348518 5.945510 0.02927474 0.15296534 0.17799479
80 3.3704531 2.9116638 7.963371 0.06190199 0.21555976 0.34778696
70 3.7144001 3.0611923 8.695064 0.06189626 0.21083069 0.36974764
60 4.0691968 3.2014066 9.421043 0.05838621 0.19977109 0.38182950
50 4.4582362 3.3424130 10.189613 0.05394832 0.18362621 0.39004910
40 4.9096050 3.4926962 11.051070 0.05530320 0.16273586 0.40168347
30 5.4702694 3.6634419 12.082839 0.07643259 0.13822354 0.43159454
20 6.2429337 3.8760073 13.446443 0.13490439 0.11894280 0.51704222
10 7.5600385 4.1930688 15.644902 0.27953208 0.15463881 0.77795888
5 8.9063184 4.4742271 17.761275 0.46732288 0.24495419 1.14596724
2 10.7639755 4.8116429 20.511540 0.77844851 0.39061976 1.75019587
1 12.2426021 5.0490772 22.586587 1.06259775 0.50924519 2.28175498
0.5 13.7929269 5.2752772 24.672378 1.39080342 0.63234981 2.87221259
0.2 15.9624260 5.5610094 27.461096 1.89615994 0.80041434 3.73986448

```

\$Emat

```

      Emix   E1   E2  SEmix  SE1  SE2
-0.2 -0.2040480 1.633213 1.137063 0.5205959 0.4644456 0.2752171
-0.5 -0.0744441 1.869085 1.283130 0.4604050 0.7311427 0.2751321
-1 0.1415624 2.262205 1.526575 0.3871991 1.2358878 0.3226767
-2 0.5735755 3.048445 2.013464 0.2880300 2.0127812 0.4429080
-5 1.8696147 5.407164 3.474132 0.1717987 3.3361324 0.6960765
-10 4.0296801 9.338364 5.908579 0.2052600 4.1595662 0.8915007
-20 8.3498109 17.200764 10.777473 0.2567516 4.0115727 1.0526113
-30 12.6699416 25.063163 15.646367 0.3034367 3.2581518 1.2316369
-40 16.9900724 32.925563 20.515260 0.4120100 2.9174574 1.4676017
-50 21.3102031 40.787962 25.384154 0.5412729 3.3301463 1.6940712
-60 25.6303338 48.650362 30.253047 0.6439274 4.0714852 1.8533158
-70 29.9504646 56.512761 35.121941 0.6877660 4.7374010 1.9219699
-80 34.2705953 64.375161 39.990835 0.6544011 5.2893357 1.9432093
-90 38.5907261 72.237560 44.859728 0.5856322 6.2821053 2.1387117
-99 42.4788438 79.313720 49.241733 0.8282188 9.1805150 3.0337516
99 42.4788438 79.313720 49.241733 0.8505941 8.8935420 3.0498938
80 34.2705953 64.375161 39.990835 0.5437934 7.9318629 1.6544342
70 29.9504646 56.512761 35.121941 0.5390104 8.5289396 1.5638688
60 25.6303338 48.650362 30.253047 0.4828725 8.3180725 1.5340835
50 21.3102031 40.787962 25.384154 0.3876131 7.3784991 1.4919847
40 16.9900724 32.925563 20.515260 0.2912417 5.9051575 1.4375273
30 12.6699416 25.063163 15.646367 0.2511280 4.2123056 1.3878589
20 8.3498109 17.200764 10.777473 0.2655813 2.9172177 1.3277733
10 4.0296801 9.338364 5.908579 0.2112043 2.6130773 1.1303774
5 1.8696147 5.407164 3.474132 0.1460100 2.2864276 0.8458768
2 0.5735755 3.048445 2.013464 0.2697191 1.4925741 0.5097317
1 0.1415624 2.262205 1.526575 0.3772735 0.9548770 0.3522130
0.5 -0.0744441 1.869085 1.283130 0.4551203 0.6017063 0.2840370
0.2 -0.2040480 1.633213 1.137063 0.5183190 0.4483813 0.2753855

```

#CAx: data frame including a series of relevant parameters from the mixture models:

CAX\$ComInd is the Combination Index calculated for the dose dimension for each p level, CAX\$seCI is the standard errors of the combination index, CAX\$Diff is the difference from 1 of the Combination index, CAX\$CAdiffp: p-value of the two tailed Student T-test of the Null hypothesis $CI=1$. CAX\$PredAdd is the prediction of the dose (D) required to produce each p level under the hypothesis of additivity, and CAX\$sePredAdd is the standard error of the dose (D) required to produce each p level under the hypothesis of additivity.

#CAy: The same that #CAx but for the empirical effect (E) axis.

CAx

	combInd	seCI	CAdiff	ciloCAdiff	cihiCAdiff	CAdiffp	PredAdd	sePredAdd
-0.2	0.3420080	0.05318707	-0.65799204	0.2377613	0.4462546	0.000000e+00	0.987466	0.09911044
-0.5	0.3632882	0.04784768	-0.63671184	0.2695067	0.4570696	0.000000e+00	1.075845	0.09115646
-1	0.3815069	0.04315301	-0.61849311	0.2969270	0.4660868	0.000000e+00	1.154200	0.08371682
-2	0.4020365	0.03779096	-0.59796346	0.3279663	0.4761068	0.000000e+00	1.245716	0.07480133
-5	0.4338613	0.02955270	-0.56613872	0.3759380	0.4917846	0.000000e+00	1.395109	0.06059542
-10	0.4628736	0.02259682	-0.53712644	0.4185838	0.5071633	0.000000e+00	1.540533	0.04910660
-20	0.4983135	0.01643862	-0.50168648	0.4660938	0.5305332	0.000000e+00	1.732870	0.04319287
-30	0.5235555	0.01542966	-0.47644447	0.4933134	0.5537977	0.000000e+00	1.882287	0.04884191
-40	0.5445192	0.01718988	-0.45548075	0.5108271	0.5782114	0.000000e+00	2.016497	0.05946825
-50	0.5632927	0.02011918	-0.43670733	0.5238591	0.6027263	0.000000e+00	2.146644	0.07213750
-60	0.5809637	0.02340490	-0.41903632	0.5350901	0.6268373	0.000000e+00	2.280340	0.08584242
-70	0.5982965	0.02666656	-0.40170354	0.5460300	0.6505629	0.000000e+00	2.425784	0.10027830
-80	0.6160407	0.02959570	-0.38395927	0.5580332	0.6740483	0.000000e+00	2.596328	0.11525769
-90	0.6352995	0.03143490	-0.36470046	0.5736871	0.6969119	0.000000e+00	2.825703	0.12966401
-99	0.6553495	0.02578785	-0.34465050	0.6048053	0.7058937	0.000000e+00	3.268576	0.12286943
99	0.6399498	0.02556564	-0.36005016	0.5898412	0.6900585	0.000000e+00	3.932601	0.15029770
80	0.6839299	0.03500694	-0.31607013	0.6153163	0.7525435	0.000000e+00	4.928068	0.23544563
70	0.7062854	0.03399879	-0.29371461	0.6396478	0.7729230	0.000000e+00	5.259064	0.23750546
60	0.7298207	0.03209315	-0.27017933	0.6669181	0.7927232	0.000000e+00	5.575612	0.23176311
50	0.7557176	0.02961498	-0.24428238	0.6976723	0.8137630	2.220446e-16	5.899341	0.21988492
40	0.7855666	0.02697002	-0.21443342	0.7327053	0.8384278	1.776357e-15	6.249763	0.20268872
30	0.8220989	0.02531321	-0.17790112	0.7724850	0.8717128	2.095213e-12	6.654029	0.18257472
20	0.8712462	0.02819427	-0.12875384	0.8159854	0.9265069	4.955426e-06	7.165522	0.17260888
10	0.9517409	0.04511972	-0.04825907	0.8633063	1.0401756	2.848093e-01	7.943378	0.23568287
5	1.0300894	0.06966783	0.03008942	0.8935405	1.1666384	6.658154e-01	8.646160	0.36895879
2	1.1326403	0.10816823	0.13264027	0.9206305	1.3446500	2.201082e-01	9.503437	0.59274946
1	1.2103851	0.14078794	0.21038505	0.9344407	1.4863294	1.350868e-01	10.114634	0.78322652
0.5	1.2887785	0.17615178	0.28877851	0.9435210	1.6340360	1.011356e-01	10.702325	0.98752619
0.2	1.3939205	0.22701557	0.39392053	0.9489700	1.8388711	8.270296e-02	11.451461	1.27584661

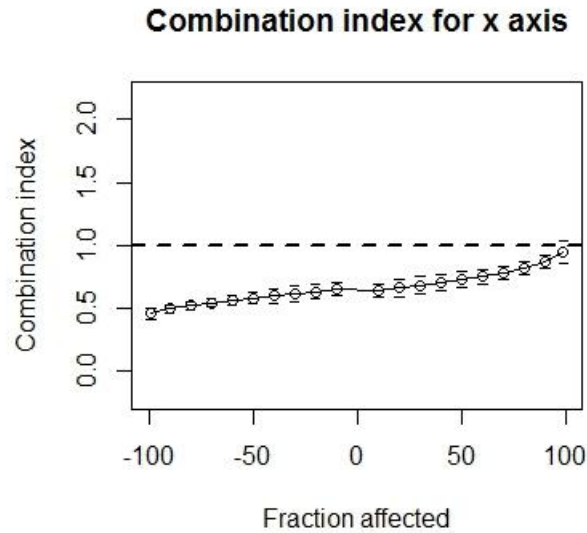
\$CAy

	combInd	seCI	CAdiff	ciloCAdiff	cihiCAdiff	CAdiffp	PredAdd	sePredAdd	
-0.2	-6.246141	15.98104655	-7.2461407	-37.56899190	25.076711	6.502457e-01	1.274513	0.2445852	
-0.5	-19.394622	120.00348198	-20.3946216	-254.60144624	215.812203	8.650493e-01	1.443815	0.2728977	
-1	12.191095	33.44643940	11.1910951	-53.36392614	77.746116	7.379287e-01	1.725801	0.3687187	
-2	3.991448	2.21941650	2.9914484	-0.35860794	8.341505	1.777055e-01	2.289397	0.5466498	
-5	2.128313	0.50514537	1.1283131	1.13822818	3.118398	2.550674e-02	3.979126	0.8707750	
-10	1.686106	0.28392387	0.6861065	1.12961568	2.242597	1.566985e-02	6.794470	1.0905217	
-20	1.488006	0.14727617	0.4880064	1.19934505	1.776668	9.212100e-04	12.424572	1.1688759	
-30	1.424987	0.10187579	0.4249871	1.22531058	1.624664	3.024410e-05	18.054504	1.2161818	
-40	1.394013	0.08747537	0.3940133	1.22256162	1.565465	6.659910e-06	23.684387	1.3707492	
-50	1.375597	0.08196254	0.3755970	1.21495038	1.536244	4.593528e-06	29.314251	1.5799862	
-60	1.363389	0.07675733	0.3633885	1.21294418	1.513833	2.198644e-06	34.944103	1.7605632	
-70	1.354702	0.06969076	0.3547019	1.21810797	1.491296	3.587174e-07	40.573950	1.8677796	
-80	1.348205	0.06198961	0.3482051	1.22670549	1.469705	1.941297e-08	46.203793	1.9325552	
-90	1.343163	0.05981961	0.3431629	1.22591650	1.460409	9.657907e-09	51.833633	2.1703342	
-99	1.339502	0.07761812	0.3395018	1.18737028	1.491633	1.219894e-05	56.900487	3.1048805	
99	1.339502	0.07750054	0.3395018	1.18760072	1.491403	1.183326e-05	56.900487	3.0886847	
80	1.348205	0.06306100	0.3482051	1.22460557	1.471805	3.356992e-08	46.203793	2.0329821	
70	1.354702	0.07300699	0.3547019	1.21160816	1.497796	1.182997e-06	40.573950	2.0610678	
60	1.363389	0.08273892	0.3633885	1.20122026	1.525557	1.123176e-05	34.944103	2.0158471	
50	1.375597	0.09101584	0.3755970	1.19720591	1.553988	3.679729e-05	29.314251	1.8648365	
40	1.394013	0.09968792	0.3940133	1.19862501	1.589402	7.734919e-05	23.684387	1.6443250	
30	1.424987	0.11575340	0.4249871	1.19811046	1.651864	2.411433e-04	18.054504	1.4222600	
20	1.488006	0.15814184	0.4880064	1.17804835	1.797964	2.029524e-03	12.424572	1.2599316	
10	1.686106	0.28267095	0.6861065	1.13207141	2.240142	1.521475e-02	6.794470	1.0819760	
5	2.128313	0.47901587	1.1283131	1.18944201	3.067184	1.849871e-02	3.979126	0.8399322	
2	3.991448	2.08412857	2.9914484	-0.09344358	8.076340	1.511881e-01	2.289397	0.5196061	
1	12.191095	32.58457772	11.1910951	-51.67467725	76.056867	7.312618e-01	1.725801	0.3510270	
0.5	-19.394622	118.62396439	-20.3946216	-251.89759175	213.108349	8.634952e-01	1.443815	0.2646745	
0.2	-6.246141	15.91107245	-7.2461407	-37.43184268	24.939561	6.488107e-01	1.274513	0.2433053	

#Plot the CI for the x axis:

```
plotFACI(0.355,list(ZnCd.lgau2, Zn.lgau2, Cd.lgau2), "x", ylim = c(-0.2, 2.2), faValues = c(-10, -20, -30, -40, -50, -60, -70, -80, -90, -99, 99, 90, 80, 70, 60, 50, 40, 30, 20, 10), showPoints = TRUE)
```

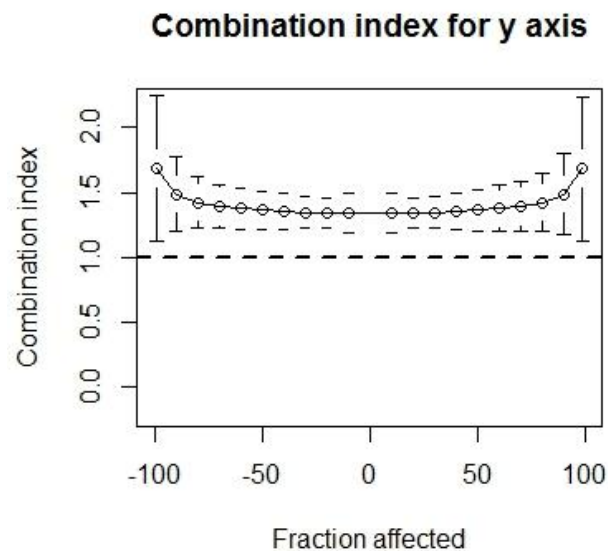
```
title("Combination index for x axis")
```



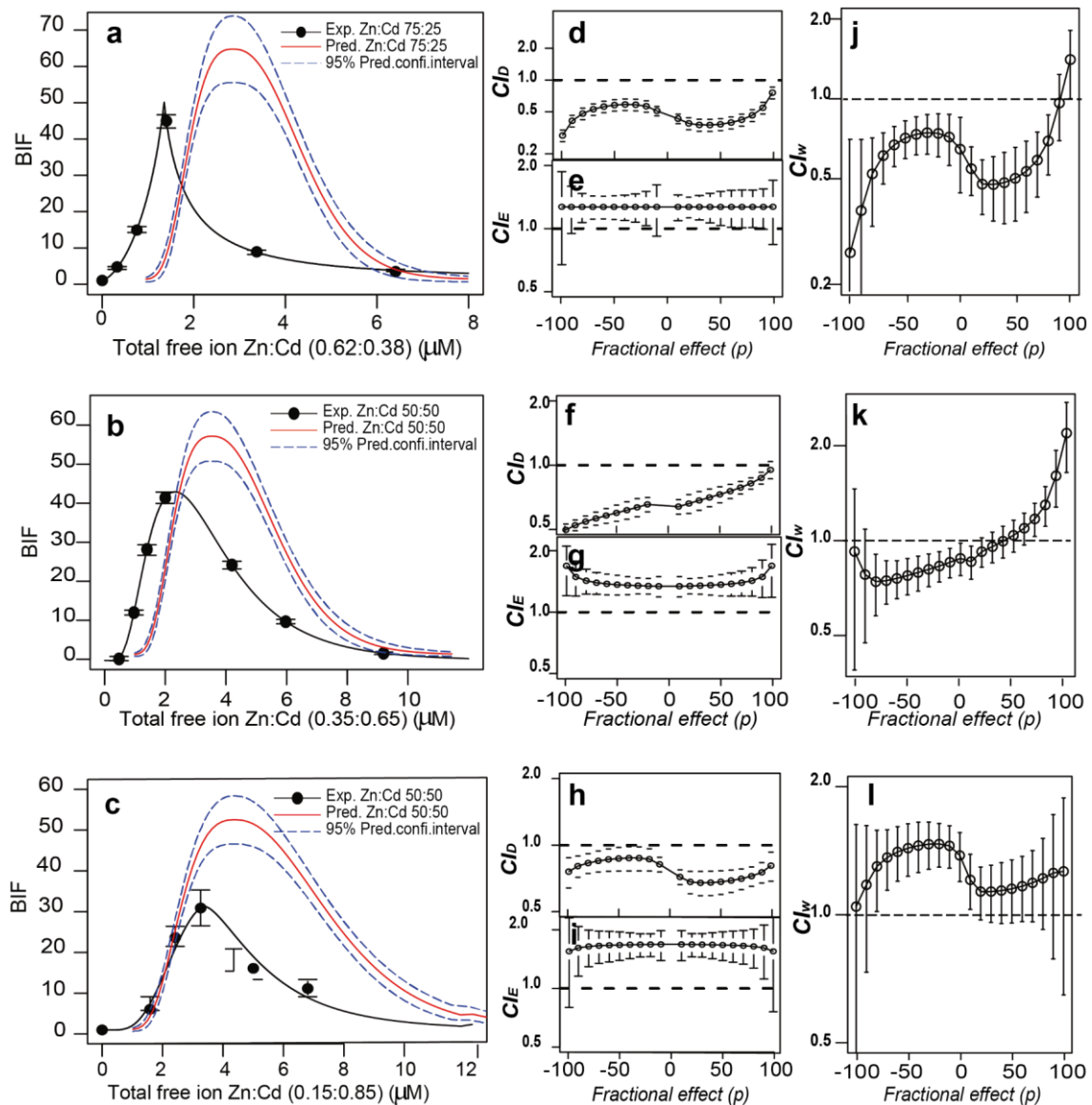
#Plot CI for the y axis

```
plotFACI(0.355,list(ZnCd.lgau2, Zn.lgau2, Cd.lgau2), "y", ylim = c(-0.2, 2.2), faValues = c(-10, -20, -30, -40, -50, -60, -70, -80, -90, -99, 99, 90, 80, 70, 60, 50, 40, 30, 20, 10), showPoints = TRUE)
```

```
title("Combination index for y axis")
```



Supplementary Material SM4 (Figure).



Effect of mixture ratio for the Zn:Cd binary mixture. Experimental vs predicted (under additivity) dose-response patterns for the mixture Zn:Cd at 75:25 (a), 50:50 (b) and 25:75 (c) mixture ratios based on the D_0 concentration of the metals. Extended p -CI plots presenting departures from additivity (as CI values) as a function of the effect level (p) for the D dimension (d, f, h), and the E dimension (e, g, i). Extended p - CI_w plots presenting weighted departures from additivity (as CI_w values) as a function of the effect level (p) for the binary mixture Zn:Cd at 75:25 (j), 50:50 (k), 25:75 (l) mixture ratios. Error bars are standard errors ($n = 3-4$). Total free ion concentrations presented in the Figures are those presented as ED_0 in Supplementary Material SM2 corrected by MINTEQ calculations due to the presence of the two metals used in each mixture.

Supplementary Material SM5 (Table). Combination index (CI) values for the dose (*D*) and empirical effect (*E*) dimensions together with relevant statistical information for 3 selected fractional effect levels (*p*) of the 15 binary metal mixtures of Cu, Cd, Zn, Cu, Hg and Co.

Metal mixture	Fractional affect (<i>p</i>)	CI _D	<i>p</i> -values	CI _E	<i>p</i> -values	CI _w
Cu:Cd	-50	0.89± 0.05	0.03	1.48± 0.15	< 0.01	1.32± 0.2
	0	0.86± 0.03	< 0.01	1.52± 0.14	< 0.01	1.31±0.17
	50	0.77± 0.03	< 0.01	1.48± 0.18	< 0.01	1.14±0.21
Cu:Zn	-50	1.28± 0.05	< 0.01	0.71± 0.08	< 0.01	0.91±0.13
	0	1.11± 0.04	< 0.01	0.7± 0.08	< 0.01	0.77± 0.12
	50	1.07± 0.04	0.04	0.71±0.13	0.02	0.76±0.17
Zn:Cd	-50	0.56± 0.02	< 0.01	1.37± 0.08	< 0.01	0.77±0.1
	0	0.64± 0.02	< 0.01	1.34± 0.08	< 0.01	0.86±0.1
	50	0.75± 0.03	< 0.01	1.37± 0.09	< 0.01	1.03±0.12
Cu:Hg	-50	1.18±0.07	< 0.01	0.58±0.06	< 0.01	0.68±0.13
	0	1.89±0.07	< 0.01	0.59±0.03	< 0.01	1.11±0.10
	50	2.19±0.13	< 0.01	0.58±0.05	< 0.01	1.27±0.18
Co:Cd	-50	1.05 ± 0.03	0.01	1.03±0.09	0.76	1.08±0.12
	0	0.73± 0.02	< 0.01	1.04±0.06	0.45	0.76±0.08
	50	0.53± 0.02	< 0.01	1.03±0.06	0.68	0.54±0.08
Hg:Cd	-50	1.39±0.06	< 0.01	0.69±0.06	< 0.01	0.95±0.12
	0	1.22±0.02	< 0.01	0.69±0.04	< 0.01	0.84±0.06
	50	1.04±0.05	< 0.01	0.69±0.05	< 0.01	0.72±0.10
Ag:Cd	-50	1.41±0.04	< 0.01	0.64±0.04	< 0.01	0.9±0.08
	0	1.07±0.02	< 0.01	0.64±0.04	< 0.01	0.68±0.06
	50	0.73±0.02	< 0.01	0.64±0.04	< 0.01	0.47±0.06 [§]
Zn:Hg	-50	3.61±0.23	< 0.01	0.52±0.05	< 0.01	1.87±0.28
	0	3.10±0.07	< 0.01	0.52±0.06	< 0.01	1.61±0.13
	50	2.45±0.16	< 0.01	0.52±0.09	< 0.01	1.27±0.25
Hg:Co	-50	1.11±0.06	< 0.01	0.29±0.09	< 0.01	0.32±0.15 [§]
	0	1.24±0.04	< 0.01	0.28±0.02	< 0.01	0.35±0.06 [§]
	50	1.17±0.07	< 0.01	0.29±0.02	< 0.01	0.34±0.09 [§]
Cu:Ag	-50	1.13±0.03	< 0.01	0.68±0.04	< 0.01	0.77±0.07
	0	0.97±0.02	0.02	0.68±0.04	< 0.01	0.66±0.06
	50	1.06±0.02	< 0.01	0.68±0.09	< 0.01	0.72±0.11
Zn:Ag	-50	1.54±0.05	< 0.01	0.62±0.05	< 0.01	0.95±0.1
	0	1.07±0.04	< 0.01	0.61±0.06	< 0.01	0.65±0.1
	50	0.94±0.03	0.05	0.62±0.09	< 0.01	0.57±0.12
Hg:Ag	-50	1.26±0.06	< 0.01	1.62±0.10	< 0.01	2.04±0.16 [§]
	0	1.32±0.03	< 0.01	1.58±0.09	< 0.01	2.08±0.12 [§]
	50	1.26±0.05	< 0.01	1.62±0.25	0.01	2.04±0.3 [§]
Co:Ag	-50	1.11±0.07	0.01	1.71±0.27	< 0.01	1.9±0.34
	0	1±0.05	0.94	1.87±0.18	< 0.01	1.87±0.23
	50	0.91±0.03	< 0.01	1.71±0.16	< 0.01	1.56±0.19
Zn:Co	-50	1.1±0.04	0.02	0.50±0.05	< 0.01	0.55±0.09
	0	0.85±0.04	< 0.01	0.49±0.03	< 0.01	0.42±0.07 [§]
	50	0.7±0.03	< 0.01	0.5±0.04	< 0.01	0.35±0.07 [§]
Cu:Co	-50	0.92±0.03	< 0.01	0.87±0.14	0.33	0.8±0.17
	0	1.85±0.04	< 0.01	0.88±0.06	0.04	1.63±0.1
	50	1.60±0.03	< 0.01	0.87±0.08	0.10	1.39±0.11

±: standard errors. For CI_D and CI_E, *P*-values were obtained using the function *Indices.fct* {drc}¹ which essentially performs a two-tailed Student's t-Test against the null hypothesis Ho: CI = 1. Statistical

significance is assumed to exist for p -values lesser than 0.05. For CI_w , it is not possible to directly perform a Student's t -Test since they are not directly computed with a dedicated *drc* function. In this case, statistical significance can be inferred from the absence of overlapping with 1 of the 95% confidence interval ($IC_{95\%} = 1.95 \cdot \text{Estandard deviation}$) for each CI_w value. However, in the paper and in the present Table, the criteria for the analysis of departures from additivity for CI_w is based on the pragmatic thresholds: $Exp < 0.5 \cdot CA$ (synergism) and $Exp > 2 \cdot CA$ (antagonism)^{4,5}, and it is marked by an [§].

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