

**S2 Text. Titration experiments.** Association constant  $K_a$  was calculated by solving the protein fraction saturation by a quadratic equation as following:

$$K_a = \frac{[PX]}{[P][X]} \quad \text{eqn S2-1}$$

Where  $[PX]$  is the complex with labeled ligand,  $[P]$  and  $[X]$  are the free protein and free ligand. Therefore, the total protein  $[P_T]$  and total Ligand  $[X_T]$  are defined as:

$$P_T = P + PX \quad \text{eqn S2-2}$$

$$X_T = X + PX \quad \text{eqn S2-3}$$

The fraction protein bound is:

$$Y = \frac{[PX]}{[P_T]} = \frac{[PX]}{[P]+[PX]} \quad \text{eqn S2-4}$$

Likewise in terms of labeled ligand saturation is

$$Y = \frac{[PX]}{[X_T]} = \frac{[PX]}{[X]+[PX]} \quad \text{eqn S2-5}$$

Substituting  $PX$  from eqn S2-1 into eqn S2-5

$$Y = \frac{K_a[P][X]}{[X]+K_a[P][X]} = \frac{K_a[P]}{1+K_a[P]} \quad \text{eqn S2-6}$$

We substitute  $P$  from eqn S2-2 into eqn S2-6

$$Y = \frac{K_a[P_T-PX]}{1+K_a[P_T-PX]} \quad \text{eqn S2-7}$$

From eqn S2-5 we get  $[PX] = Y[X_T]$

$$Y = \frac{K_a\{[P_T]-Y[X_T]\}}{1+K_a\{[P_T]-Y[X_T]\}} \quad \text{eqn S2-8}$$

Eqn S2-8 is a quadratic equation, defined as following:

$$ax^2 + bx + c = 0 \quad \text{eqn S2-9}$$

Rearranging eqn S2-8:

$$Y + K_a P_T Y - Y^2 X_T K_a = K_a P_T - K_a X_T Y \quad \text{eqn S2-10}$$

$$0 = X_T K_a Y^2 - (1 + K_a P_T + K_a X_T) Y + K_a P_T \quad \text{eqn S2-11}$$

Solving the quadratic equation:

$$\mathbf{Y} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

eqn S2-12

Where

$$a = X_T K_a, b = -(1 + K_a P_T + K_a X_T), c = P_T K_a$$