Supplemental Information for

Machine learning bandgaps of double perovskites

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Figure 1. Parity plot comparing the PBE and GLLB-SC bandgaps with the corresponding experimentally measured bandgaps for selected single metal oxides. The plotted data is from Ref. [1].

Primary features and optimal primary Ω -D descriptors						
Down-selected primary features		Identities of the primary descriptors				
Primary feature	Feature representation	Descriptor dimension	Descriptor representation			
f_1	r_{dA}^+	1-D	$[f_2]$			
f_2	l_A^+	2-D	$[f_2, f_{13}]$			
f_3	h_A^+	3-D	$[f_2, f_9, f_{13}]$			
f_4	χ^A	4-D	$[f_2, f_5, f_9, f_{12}]$			
f_5	χ^+_B	5-D	$[f_2, f_5, f_9, f_{12}, f_{13}]$			
f_6	r_{dA}^-	6-D	$[f_2, f_3, f_5, f_9, f_{12}, f_{13}]$			
f_7	I_B^-	7-D	$[f_2, f_3, f_5, f_7, f_9, f_{12}, f_{13}]$			
f_8	r_{dB}^+	8-D	$[f_2, f_3, f_5, f_7, f_9, f_{12}, f_{13}, f_{15}]$			
f_9	χ^B	9-D	$[f_2, f_3, f_4, f_5, f_7, f_9, f_{12}, f_{13}, f_{15}]$			
f_{10}	r_{dB}^-	10-D	$[f_2, f_3, f_4, f_5, f_7, f_9, f_{12}, f_{13}, f_{15}, f_{16}]$			
f_{11}	I_B^+	11-D	$[f_1, f_2, f_3, f_4, f_5, f_7, f_9, f_{12}, f_{13}, f_{15}, f_{16}]$			
f_{12}	l_A^-	12-D	$[f_1, f_2, f_3, f_4, f_5, f_7, f_9, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
f_{13}	h_B^+	13-D	$[f_1, f_2, f_3, f_4, f_5, f_7, f_9, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
f_{14}	h_A^-	14-D	$[f_1, f_2, f_3, f_4, f_5, f_6, f_7, f_9, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
f_{15}	h_B^-	15-D	$[f_1, f_2, f_3, f_4, f_5, f_6, f_7, f_9, f_{10}, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
f_{16}	r_{sA}^-	16-D	$[f_1, f_2, f_3, f_4, f_5, f_6, f_7, f_8, f_9, f_{10}, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			

Table 1. Identified optimal primary $\Omega\text{-}D$ descriptors.

Compound features and optimal compound Ω -D descriptors						
Down-selected compound features		Identities of the compound descriptors				
Compound feature	Feature representation	Descriptor dimension	Descriptor representation			
f_1	$(r_{sA}^+)^2 \cdot (I_A^+)^3 \cdot \sqrt{(l_A^+)}$	1-D	[<i>f</i> ₁]			
f_2	$(r_{sA}^+)^2 \cdot (I_A^+)^3 \cdot exp(\chi_B^-)$	2-D	$[f_2, f_{15}]$			
f_3	$(h_A^+)^2 \cdot (r_{pB}^+)^3 \cdot exp(l_B^-)$	3-D	$[f_2, f_3, f_{15}]$			
f_4	$(I_A^+)^3 \cdot (l_A^+)^3 \cdot exp(r_{pB}^+)$	4-D	$[f_2, f_3, f_{11}, f_{15}]$			
f_5	$(r_{pB}^+)^3 \cdot \sqrt{(h_A^+) \cdot exp(l_B^-)}$	5-D	$[f_1, f_3, f_9, f_{12}, f_{15}]$			
f_6	$(r_{dA}^+)^3 \cdot exp(r_{pB}^-) \cdot exp(I_A^-)$	6-D	$[f_1, f_3, f_6, f_8, f_{12}, f_{15}]$			
f_7	$(\chi_A^+)^3 \cdot exp(r_{dB}^+) \cdot exp(l_A^-)$	7-D	$[f_1, f_2, f_3, f_6, f_8, f_{12}, f_{15}]$			
f_8	$\left \sqrt{(h_A^-)} \cdot ln(1+\chi_A^-) \cdot ln(1+l_A^-)\right $	8-D	$[f_1, f_2, f_3, f_6, f_8, f_{11}, f_{12}, f_{15}]$			
f_9	$(h_B^+)^2 \cdot (\chi_A^+)^3 \cdot ln(1+l_A^-)$	9-D	$[f_1, f_2, f_3, f_6, f_8, f_{10}, f_{11}, f_{12}, f_{15}]$			
f_{10}	$(l_A^+)^3 \cdot (l_A^+)^3 \cdot ln(1+l_A^-)$	10-D	$[f_1, f_2, f_3, f_6, f_8, f_{11}, f_{12}, f_{13}, f_{15}, f_{16}]$			
f_{11}	$(\chi_A^+)^3 \cdot \sqrt{(l_A^-)} \cdot exp(h_B^-)$	11-D	$[f_1, f_2, f_3, f_6, f_8, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
<i>f</i> ₁₂	$(r_{dB}^+)^3 \cdot (h_B^+)^3 \cdot (l_B^-)^3$	12-D	$[f_1, f_2, f_3, f_6, f_8, f_{10}, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
<i>f</i> ₁₃	$\sqrt{(\pmb{\chi}_A^+)}\cdot \sqrt{(h_B^+)}\cdot \sqrt{(r_{sA}^+)}$	13-D	$[f_1, f_2, f_3, f_6, f_7, f_8, f_{10}, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
f_{14}	$(l_A^+)^2 \cdot (r_{pB}^+)^3 \cdot exp(I_B^-)$	14-D	$[f_1, f_2, f_3, f_6, f_7, f_8, f_9 f_{10}, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
f15	$(\pmb{\chi}_B^+)^2\cdot\sqrt{(\pmb{\chi}_A^+)}\cdot\sqrt{(L_B^+)}$	15-D	$[f_1, f_2, f_3, f_5, f_6, f_7, f_8, f_9 f_{10}, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			
f ₁₆	$(r_{dB}^+)^2 \cdot \sqrt{(I_A^-)} \cdot exp(L_B^-)$	16-D	$[f_1, f_2, f_3, f_4, f_5, f_6, f_7, f_8, f_9, f_{10}, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}]$			

Table 2. Identified optimal compound Ω -D descriptors.

References

 Castelli, I.E., Olsen, T., Datta, S., Landis, D.D., Dahl, S., Thygesen, K.S., Jacobsen, K.W. Energy Environ. Sci. 5, 5814 (2012).