

## **Supplementary Materials**

### **Supplementary Methods**

Here we describe the methods for obtaining the overall sensitivity, specificity, AUC, PVP, and PVN of the two-stage approach. First, we obtain the overall sensitivity and specificity as follows. Denote the cutoffs used at the first and second stages as  $c_1$  and  $c_2$ , and  $P(\text{AnyBRCA})$  at these two stages as  $Pr_1$  and  $Pr_2$ , respectively. Consider a specific first-stage tool and denote its sensitivity and specificity at  $c_1$  as  $Se.1 = P(Pr_1 > c_1 | \text{positive genetic test})$  and  $Sp.1 = P(Pr_1 < c_1 | \text{negative genetic test})$ . Further, denote the sensitivity and specificity of the second stage at  $c_2$  given the results of the first stage as  $Se.2|1$  and  $Sp.2|1$ , respectively. These can be estimated by evaluating the subsample of patients with  $Pr_1 > c_1$  who undergo the second stage. A counselee will be considered at high risk overall, and referred for genetic testing, only if  $Pr_1 > c_1$  and  $Pr_2 > c_2$ . Thus, the sensitivity  $Se.O$  and the specificity  $Sp.O$  of the overall two-stage procedure can be calculated as

$$Se.O = P(Pr_2 > c_2 | Pr_1 > c_1, \text{ positive genetic test}) * P(Pr_1 > c_1 | \text{positive genetic test}) = Se.2|1 * Se.1, \text{ and}$$

$$Sp.O = P(Pr_1 < c_1 | \text{negative genetic test}) + P(Pr_2 < c_2 | Pr_1 > c_1, \text{ negative genetic test}) * P(Pr_1 > c_1 | \text{negative genetic test}) = Sp.1 + Sp.2|1 * (1 - Sp.1).$$

By varying the values of  $c_1$  and  $c_2$ , we can get a range of sensitivities and specificities for the two-stage approach. Next, we plot the  $Se.O$  versus  $1 - Sp.O$  over the range of  $c_1$  and  $c_2$  to obtain an empirical ROC curve, and estimate the AUC using trapezoidal rule. Also, we calculate the overall predictive values,  $PVP.O$  and  $PVN.O$  from  $Se.O$  and  $Sp.O$  values by using the Bayes rule. We obtain 95% CI for overall sensitivity, specificity, and predictive values using the bootstrap method [1]. For AUC, we use an asymptotic CI [2,3].

## **References**

1. Efron B, Tibshirani R: An Introduction to the Bootstrap. Chapman and Hall/CRC 1994.
2. Pepe M: The Statistical Evaluation of Medical Tests for Classification and Prediction. Oxford University Press, 2004
3. Hanley JA, McNeil BJ: The meaning and use of the area under a receiver operating characteristic (ROC) curve. Radiology. 143:29-36, 1982

**Supplement Table 1:** First Stage Results (with CI) for NWH data

|                    | Cutoff | BRCAPRO                        | BRCAPROLYTE                       | BRCAPROLYTE-Plus                 | BRCAPRO-Simple                    |
|--------------------|--------|--------------------------------|-----------------------------------|----------------------------------|-----------------------------------|
| <b>Sensitivity</b> | 0.001  | 0.97 (0.93, 0.99)              | 0.99 (0.97, 1)                    | 0.96 (0.92, 0.99)                | 0.97 (0.93, 0.99)                 |
| <b>Specificity</b> |        | 0.07 (0.05, 0.08)              | 0 (0, 0.01)                       | 0.09 (0.07, 0.1)                 | 0.06 (0.04, 0.07)                 |
| <b>Sensitivity</b> | 0.003  | 0.92 (0.87, 0.96)              | 0.97 (0.93, 0.99)                 | 0.91 (0.86, 0.96)                | 0.93 (0.88, 0.97)                 |
| <b>Specificity</b> |        | 0.17 (0.15, 0.19)              | 0.05 (0.04, 0.07)                 | 0.18 (0.15, 0.2)                 | 0.1 (0.08, 0.12)                  |
| <b>Sensitivity</b> | 0.005  | 0.89 (0.83, 0.94)              | 0.97 (0.93, 0.99)                 | 0.86 (0.79, 0.92)                | 0.9 (0.85, 0.95)                  |
| <b>Specificity</b> |        | 0.22 (0.2, 0.24)               | 0.07 (0.05, 0.08)                 | 0.26 (0.24, 0.28)                | 0.14 (0.13, 0.16)                 |
| <b>Sensitivity</b> | 0.007  | 0.84 (0.77, 0.9)               | 0.96 (0.92, 0.99)                 | 0.8 (0.73, 0.87)                 | 0.89 (0.83, 0.94)                 |
| <b>Specificity</b> |        | 0.27 (0.25, 0.3)               | 0.08 (0.06, 0.09)                 | 0.33 (0.3, 0.36)                 | 0.21 (0.19, 0.23)                 |
| <b>Sensitivity</b> | 0.01   | 0.8 (0.73, 0.87)               | 0.93 (0.88, 0.97)                 | 0.76 (0.68, 0.83)                | 0.83 (0.76, 0.89)                 |
| <b>Specificity</b> |        | 0.33 (0.3, 0.35)               | 0.1 (0.08, 0.12)                  | 0.4 (0.37, 0.42)                 | 0.29 (0.27, 0.32)                 |
| <b>Sensitivity</b> | 0.03   | 0.63 (0.55, 0.71)              | 0.84 (0.77, 0.9)                  | 0.54 (0.46, 0.63)                | 0.6 (0.51, 0.69)                  |
| <b>Specificity</b> |        | 0.54 (0.51, 0.57)              | 0.29 (0.27, 0.32)                 | 0.61 (0.58, 0.64)                | 0.53 (0.5, 0.55)                  |
| <b>Sensitivity</b> | 0.05   | 0.54 (0.45, 0.62)              | 0.7 (0.61, 0.78)                  | 0.49 (0.4, 0.58)                 | 0.54 (0.45, 0.62)                 |
| <b>Specificity</b> |        | 0.64 (0.61, 0.66)              | 0.41 (0.39, 0.44)                 | 0.71 (0.68, 0.73)                | 0.64 (0.61, 0.67)                 |
| <b>Sensitivity</b> | 0.1    | 0.46 (0.37, 0.54)              | 0.57 (0.48, 0.66)                 | 0.39 (0.31, 0.48)                | 0.43 (0.34, 0.52)                 |
| <b>Specificity</b> |        | 0.75 (0.72, 0.77)              | 0.56 (0.53, 0.59)                 | 0.83 (0.81, 0.85)                | 0.79 (0.77, 0.81)                 |
| <b>Sensitivity</b> | 0.2    | 0.39 (0.31, 0.48)              | 0.46 (0.37, 0.54)                 | 0.32 (0.24, 0.4)                 | 0.34 (0.25, 0.42)                 |
| <b>Specificity</b> |        | 0.86 (0.84, 0.88)              | 0.74 (0.72, 0.77)                 | 0.9 (0.88, 0.92)                 | 0.88 (0.86, 0.9)                  |
| <b>PVP</b>         | 0.001  | 0.1 (0.08, 0.11)               | 0.09 (0.08, 0.11)                 | 0.1 (0.08, 0.11)                 | 0.1 (0.08, 0.11)                  |
| <b>PVN</b>         |        | 0.95 (0.9, 0.99)               | 0.83 (0.5, 1)                     | 0.95 (0.91, 0.99)                | 0.95 (0.89, 0.99)                 |
| <b>PVP</b>         | 0.003  | 0.1 (0.08, 0.12)               | 0.09 (0.08, 0.11)                 | 0.1 (0.08, 0.12)                 | 0.1 (0.08, 0.11)                  |
| <b>PVN</b>         |        | 0.95 (0.93, 0.98)              | 0.94 (0.88, 0.99)                 | 0.95 (0.92, 0.98)                | 0.93 (0.88, 0.97)                 |
| <b>PVP</b>         | 0.005  | 0.1 (0.09, 0.12)               | 0.1 (0.08, 0.11)                  | 0.11 (0.09, 0.13)                | 0.1 (0.08, 0.12)                  |
| <b>PVN</b>         |        | 0.95 (0.92, 0.97)              | 0.95 (0.9, 0.99)                  | 0.95 (0.92, 0.97)                | 0.94 (0.9, 0.97)                  |
| <b>PVP</b>         | 0.007  | 0.11 (0.09, 0.13)              | 0.1 (0.08, 0.11)                  | 0.11 (0.09, 0.13)                | 0.1 (0.09, 0.12)                  |
| <b>PVN</b>         |        | 0.94 (0.92, 0.97)              | 0.95 (0.9, 0.99)                  | 0.94 (0.92, 0.96)                | 0.95 (0.92, 0.97)                 |
| <b>PVP</b>         | 0.01   | 0.11 (0.09, 0.13)              | 0.1 (0.08, 0.11)                  | 0.11 (0.09, 0.14)                | 0.11 (0.09, 0.13)                 |
| <b>PVN</b>         |        | 0.94 (0.92, 0.96)              | 0.93 (0.89, 0.97)                 | 0.94 (0.92, 0.96)                | 0.94 (0.92, 0.97)                 |
| <b>PVP</b>         | 0.03   | 0.12 (0.1, 0.15)               | 0.11 (0.09, 0.13)                 | 0.13 (0.1, 0.15)                 | 0.12 (0.09, 0.14)                 |
| <b>PVN</b>         |        | 0.93 (0.92, 0.95)              | 0.95 (0.92, 0.97)                 | 0.93 (0.91, 0.95)                | 0.93 (0.91, 0.95)                 |
| <b>PVP</b>         | 0.05   | 0.13 (0.1, 0.16)               | 0.11 (0.09, 0.13)                 | 0.15 (0.11, 0.18)                | 0.13 (0.1, 0.16)                  |
| <b>PVN</b>         |        | 0.93 (0.91, 0.95)              | 0.93 (0.91, 0.95)                 | 0.93 (0.91, 0.95)                | 0.93 (0.91, 0.95)                 |
| <b>PVP</b>         | 0.1    | 0.16 (0.12, 0.2)               | 0.12 (0.09, 0.14)                 | 0.19 (0.14, 0.24)                | 0.17 (0.13, 0.22)                 |
| <b>PVN</b>         |        | 0.93 (0.91, 0.95)              | 0.93 (0.91, 0.94)                 | 0.93 (0.91, 0.94)                | 0.93 (0.92, 0.95)                 |
| <b>PVP</b>         | 0.2    | 0.22 (0.17, 0.28)              | 0.15 (0.12, 0.19)                 | 0.25 (0.18, 0.32)                | 0.22 (0.16, 0.28)                 |
| <b>PVN</b>         |        | 0.93 (0.92, 0.95)              | 0.93 (0.91, 0.95)                 | 0.93 (0.91, 0.94)                | 0.93 (0.91, 0.94)                 |
| <b>AUC</b>         |        | 0.65 (0.59, 0.70)              | 0.63 (0.57, 0.68)                 | 0.64 (0.59, 0.7)                 | 0.64 (0.58, 0.7)                  |
| <b>O/E</b>         |        | 125/146.45 = 0.85<br>(0.71, 1) | 125/228.94 = 0.55<br>(0.46, 0.64) | 125/113.98 = 1.10<br>(0.91, 1.3) | 125/135.37 = 0.92<br>(0.77, 1.09) |

**Supplement Table 2:** Numbers of referrals made at each stage using a two-stage approach, as compared to using BRCAPRO only on all probands for CGN+MDA data. For each combination of  $c_1$  and  $c_2$ , three numbers are provided – number of probands with first stage probability exceeding  $c_1$  ( $n_1$ ), out of  $n_1$ , the number of probands with second stage probability exceeding  $c_2$  ( $n_2$ ), and out of  $n_2$ , the number of probands tested positive for BRCA mutation.

|                   |    | BRCAPOLYTE |      |      |      | BRCAPOLYTE-Plus |      |      |      |      |
|-------------------|----|------------|------|------|------|-----------------|------|------|------|------|
|                   |    | $c_2$ (%)  |      |      |      | $c_2$ (%)       |      |      |      |      |
|                   |    | 1          | 3    | 5    | 10   | 1               | 3    | 5    | 10   |      |
| $c_1$ (%)         | 1  | 2584       | 2584 | 2584 | 2584 | 1               | 2003 | 2003 | 2003 |      |
|                   | 3  | 2070       | 1624 | 1361 | 1036 | 3               | 1909 | 1582 | 1340 | 1029 |
|                   | 5  | 548        | 498  | 458  | 414  | 5               | 532  | 494  | 456  | 413  |
|                   | 10 | 2255       | 2255 | 2255 | 2255 | 10              | 1477 | 1477 | 1477 | 1477 |
|                   | 3  | 2012       | 1620 | 1359 | 1035 | 3               | 1470 | 1429 | 1280 | 1006 |
|                   | 5  | 541        | 496  | 456  | 413  | 5               | 471  | 468  | 444  | 409  |
|                   | 10 | 2028       | 2028 | 2028 | 2028 | 10              | 1244 | 1244 | 1244 | 1244 |
|                   | 3  | 1881       | 1576 | 1350 | 1031 | 3               | 1240 | 1231 | 1191 | 980  |
|                   | 5  | 526        | 494  | 456  | 413  | 5               | 438  | 438  | 429  | 401  |
| $c_1$ (%)         | 10 | 1632       | 1632 | 1632 | 1632 | 10              | 903  | 903  | 903  | 903  |
|                   | 3  | 1559       | 1410 | 1276 | 1023 | 3               | 902  | 902  | 898  | 867  |
|                   | 5  | 490        | 472  | 447  | 412  | 5               | 379  | 379  | 378  | 372  |
| BRCAPOLYTE-Simple |    |            |      |      |      |                 |      |      |      |      |
|                   |    | $c_2$ (%)  |      |      |      | BRCAPRO         |      |      |      |      |
|                   |    | 1          | 3    | 5    | 10   | 1               | 3    | 5    | 10   |      |
| $c_1$ (%)         | 1  | 2300       | 2300 | 2300 | 2300 | 1               | 2070 | 1624 | 1361 | 1036 |
|                   | 3  | 2044       | 1619 | 1359 | 1036 | 3               | 548  | 498  | 458  | 414  |
|                   | 5  | 546        | 497  | 457  | 414  | 5               |      |      |      |      |
|                   | 10 | 1789       | 1789 | 1789 | 1789 | 10              |      |      |      |      |
|                   | 3  | 1725       | 1536 | 1330 | 1024 | 3               |      |      |      |      |
|                   | 5  | 509        | 483  | 454  | 412  | 5               |      |      |      |      |
|                   | 10 | 1522       | 1522 | 1522 | 1522 | 10              |      |      |      |      |
|                   | 3  | 1494       | 1415 | 1299 | 1018 | 3               |      |      |      |      |
|                   | 5  | 484        | 472  | 450  | 412  | 5               |      |      |      |      |
| $c_1$ (%)         | 10 | 1167       | 1167 | 1167 | 1167 | 10              |      |      |      |      |
|                   | 3  | 1160       | 1141 | 1100 | 978  | 3               |      |      |      |      |
|                   | 5  | 426        | 423  | 415  | 399  | 5               |      |      |      |      |

**Supplement Table 3:** Numbers of referrals made at each stage using a two-stage approach, as compared to using BRCAPRO only on all probands for NWH data. For each combination of  $c_1$  and  $c_2$ , three numbers are provided – number of probands with first stage probability exceeding  $c_1$  ( $n_1$ ), out of  $n_1$ , the number of probands with second stage probability exceeding  $c_2$  ( $n_2$ ), and out of  $n_2$ , the number of probands tested positive for BRCA mutation.

| BRCPOLY            |                    |      |      |      | BRCPOLY-Plus       |     |     |     |                    |
|--------------------|--------------------|------|------|------|--------------------|-----|-----|-----|--------------------|
| c <sub>1</sub> (%) | c <sub>2</sub> (%) |      |      |      | c <sub>2</sub> (%) |     |     |     | c <sub>1</sub> (%) |
|                    | 1                  | 3    | 5    | 10   | 1                  | 3   | 5   | 10  |                    |
| 1                  | 1212               | 1212 | 1212 | 1212 | 1                  | 831 | 831 | 831 | 831                |
|                    | 921                | 641  | 509  | 363  |                    | 795 | 623 | 500 | 356                |
|                    | 100                | 79   | 67   | 57   |                    | 91  | 77  | 66  | 56                 |
|                    | 3                  | 969  | 969  | 969  | 3                  | 540 | 540 | 540 | 540                |
|                    | 836                | 636  | 504  | 360  |                    | 540 | 510 | 450 | 339                |
|                    | 98                 | 79   | 67   | 57   |                    | 68  | 67  | 61  | 53                 |
|                    | 5                  | 803  | 803  | 803  | 5                  | 416 | 416 | 416 | 416                |
|                    | 729                | 592  | 500  | 357  |                    | 416 | 414 | 389 | 312                |
|                    | 83                 | 76   | 67   | 57   |                    | 61  | 61  | 58  | 51                 |
|                    | 10                 | 608  | 608  | 608  | 10                 | 256 | 256 | 256 | 256                |
| 3                  | 585                | 513  | 448  | 347  |                    | 256 | 256 | 252 | 239                |
|                    | 71                 | 68   | 61   | 54   |                    | 49  | 49  | 48  | 47                 |
| BRCPOLY-Simple     |                    |      |      |      | BRCPOLY            |     |     |     |                    |
| c <sub>1</sub> (%) | c <sub>2</sub> (%) |      |      |      | c <sub>2</sub> (%) |     |     |     | c <sub>1</sub> (%) |
|                    | 1                  | 3    | 5    | 10   | 1                  | 3   | 5   | 10  |                    |
|                    | 1                  | 964  | 964  | 964  | 964                | 922 | 642 | 510 | 363                |
|                    | 849                | 635  | 506  | 362  |                    | 100 | 79  | 67  | 57                 |
|                    | 99                 | 78   | 67   | 57   |                    |     |     |     |                    |
|                    | 3                  | 651  | 651  | 651  | 651                |     |     |     |                    |
|                    | 634                | 542  | 470  | 349  |                    |     |     |     |                    |
|                    | 74                 | 72   | 64   | 55   |                    |     |     |     |                    |
|                    | 5                  | 506  | 506  | 506  | 506                |     |     |     |                    |
|                    | 502                | 468  | 417  | 326  |                    |     |     |     |                    |
| 10                 | 67                 | 67   | 60   | 53   |                    |     |     |     |                    |
|                    | 309                | 309  | 309  | 309  |                    |     |     |     |                    |
|                    | 307                | 303  | 290  | 253  |                    |     |     |     |                    |
|                    | 54                 | 54   | 52   | 48   |                    |     |     |     |                    |