## Localised Ag<sup>+</sup> vibrations at the origin of ultralow thermal conductivity in layered thermoelectric AgCrSe<sub>2</sub>

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Supplementary material

Table S1: Rietveld refinement results of high resolution synchrotron X-ray powder diffractogram of AgCrSe<sub>2</sub> at 295 K and 80 K (space group R3m (n°160, H setting) with all atoms on Wyckoff position 3a (0, 0, *z*)).

Temperature	295 K	80 K
Cell parameters (Å)		
а	3.6836(2)	3.6844(2)
С	21.2375(12)	21.11561(10)
Cell volume $V(\text{\AA}^3)$	249.6(2)	248.2(2)
Ag (0, 0, <i>z</i> )	0.1529(3)	0.1513(2)
Cr(0, 0, z)	0	0
$Se_1(0, 0, z)$	0.2713(3)	0.2709(3)
$Se_{2}(0, 0, z)$	0.7337(3)	0.7336(3)
$U_{\text{anisotropic}}$ (Å <sup>2</sup> )		
Ag $U_{11}$	0.081(6)	0.016(7)
Ag <i>U</i> <sub>33</sub>	0.004(2)	0.010(3)
Nb. of reflections	63	63
Nb. of parameters	17	17
Bragg R factor	3.88	4.28
$\chi^2$	2.04	3.18

Temperature	295 K	80 K
Distances (Å)		
Ag-Se <sub>1</sub>	2.5162(1) (x1)	2.5284(1)
Ag-Se <sub>2</sub>	2.8025(4) (x3)	2.7792(4)
Cr-Se <sub>1</sub>	2.4970(5) (x3)	2.5005(3)
Cr-Se <sub>2</sub>	2.5624(5) (x3)	2.5505(5)
Cr-Cr <sub>in</sub>	3.6836(2) (x6)	3.6844(1)
Cr-Cr <sub>out</sub>	7.3918(4) (x6)	7.3530(4)
$Cr-Cr_{in}$ (2 <sup>nd</sup> neighbour)	6.380(1) (x6)	6.381(1)
$CrSe_2$ layer thickness (Å)	2.738(1)	2.721(1)
AgSe <sub>4</sub> height (Å)	4.341(1)	4.317(1)
Angles (°)		
Se-Cr-Se <sub>in</sub>	91.91(3)	92.49(3)
Se-Cr-Se <sub>out</sub>	86.49(3)	86.29(3)
S-Ag-S	130.63(3)	130.06(3)

Table S2: Selected inter-atomic distances and angles in AgCrSe<sub>2</sub> at 295 K and 80 K (from high resolution synchrotron X-ray powder diffractograms).

Figure S1 : (Left) Total (black) and partial (red : Ag, blue : Cr, magenta : Se) simulated structure factors obtained from the ab-initio molecular dynamics calculations at 150 K. (Right) Partial density of state for the Ag atoms, projected along the [110] axis (« in plane » vibrations, in blue), and along the [001] direction (« out of plane » vibrations, in red).



Figure S2 : Temperature evolution of the  $AgCrSe_2$  cell parameter *a* and cell volume *V*. The red line is a Debye fit, and the blue line is a guide to the eye.



Figure S3 : Spin-wave calculation performed modelling the incommensurate magnetic structure of AgCrSe<sub>2</sub> at 2 K, with the following magnetic exchange values:  $J_{ab} \sim 2.1$  meV,  $J_{NN} \sim -0.71$  meV and  $J_C \sim -0.09$  meV (see text for definition of J's).



Figure S4 : Dynamical properties of  $AgCrS_2$ . The red arrow indicates the localised mode attributed to the in-plane vibration of  $Ag^+$ .



AgCrS<sub>2</sub>