

Parameter	Value	Units	Description
$\alpha$	5.6e5	$\mu\text{L}$	Conversion factor from Blood to Ln (max. blood volume)
host_Ln	50	count	Number of lymph nodes in the host
$\lambda$	[1e-5, 1e-3]	""	Mtb-specific frequency
Sn4*	$N_{Ln,4} \times (\alpha / \text{host\_Ln})$	Cell/ $\mu\text{L}$ *day	Thymic output of naive CD4 cells
Sn8*	$N_{Ln,8} \times (\alpha / \text{host\_Ln})$	Cell/ $\mu\text{L}$ *day	Thymic output of naive CD8 cells
hs <sub>1</sub>	25	Cell count	Naive CD4 recruitment half saturation
hs <sub>4</sub>	10	Cell count	Precursor CD4 proliferation half saturation
hs <sub>5</sub>	10	Cell count	Precursor CD4 differentiation half saturation
hs <sub>8</sub>	40	Cell count	Central Memory CD4 recruitment half saturation
hs <sub>10</sub>	357.7	Cell count	Naive CD8 recruitment half saturation
hs <sub>11</sub>	10	Cell count	Naive CD8 priming half saturation
hs <sub>13</sub>	10	Cell count	Precursor CD8 proliferation half saturation
hs <sub>14</sub>	10	Cell count	Precursor CD8 differentiation half saturation
hs <sub>17</sub>	157	Cell count	Central Memory CD8 recruitment half saturation
k <sub>1</sub>	[5e-1,1]	day <sup>-1</sup>	Naive CD4 recruitment rate
k <sub>2</sub>	[1e-3,1e-1]	day <sup>-1</sup>	Naive CD4 Priming rate
k <sub>3</sub>	[1e-7,1e-4]	day <sup>-1</sup>	Central Memory CD4 reactivation rate
k <sub>4</sub>	[.5,1.5]	day <sup>-1</sup>	Precursor CD4 proliferation rate
k <sub>5</sub>	[0.01,0.5]	day <sup>-1</sup>	Precursor CD4 differentiation to Effector rate
k <sub>6</sub>	0.004	day <sup>-1</sup>	Precursor CD4 differentiation to Central Memory
k <sub>7</sub>	[0.005,0.1]	day <sup>-1</sup>	Effector CD4 differentiation to Effector Memory
k <sub>8</sub>	[0.1,0.31]	day <sup>-1</sup>	Central Memory CD4 recruitment rate
k <sub>10</sub>	[5e-1,1]	day <sup>-1</sup>	Naive CD8 recruitment rate
k <sub>11</sub>	[1e-3,1e-1]	day <sup>-1</sup>	Naive CD8 priming rate
k <sub>12</sub>	[1e-7,1e-4]	day <sup>-1</sup>	Central Memory CD8 reactivation rate
k <sub>13</sub>	[.5,1.5]	day <sup>-1</sup>	Precursor CD8 proliferation rate
k <sub>14</sub>	[0.01,0.5]	day <sup>-1</sup>	Precursor CD8 differentiation to Effector rate
k <sub>15</sub>	0.004	day <sup>-1</sup>	Precursor CD8 differentiation to Central Memory
k <sub>16</sub>	[0.005,0.1]	day <sup>-1</sup>	Effector CD8 differentiation to Effector Memory
k <sub>17</sub>	0.5	day <sup>-1</sup>	Central Memory CD8 recruitment rate
$\mu_1$	0.2	day <sup>-1</sup>	Effector CD4 death rate
$\mu_2$	0.04	day <sup>-1</sup>	Effector Memory CD4 death rate
$\mu_3$	0.2	day <sup>-1</sup>	Effector CD8 death rate
$\mu_4$	0.04	day <sup>-1</sup>	Effector Memory CD8 death rate
$\mu_5$	[0.1,1]	day <sup>-1</sup>	APC death rate
$\mu_6$	0.1	day <sup>-1</sup>	Precursor CD4 death rate
$\mu_7$	0.1	day <sup>-1</sup>	Precursor CD8 death rate
$\mu_8$	6e-4	day <sup>-1</sup>	Naive CD4 death rate
$\mu_9$	4e-4	day <sup>-1</sup>	Naive CD8 death rate
$\rho_1$	3e8	Cell count	Precursor carrying capacity
Wp <sub>4</sub>	0.735	""	Weight factor for Precursor CD4 in CD8 priming
$\xi_1^*$	$\xi_2 \times (N_{Ln,nc4} / N_{B,nc4}) / \alpha$	day <sup>-1</sup>	Naive CD4 Lymph Influx
$\xi_2$	[0.637,1]	day <sup>-1</sup>	Naive CD4 Lymph Efflux
$\xi_3$	[2,5]	day <sup>-1</sup>	Effector CD4 Lymph Efflux
$\xi_4^*$	$\xi_5 \times (CM_{Ln,nc4} / CM_{B,nc4}) / \alpha$	day <sup>-1</sup>	Central Memory CD4 Lymph Influx
$\xi_5$	0.489	day <sup>-1</sup>	Central Memory CD4 Lymph Efflux
$\xi_6$	[2,5]	day <sup>-1</sup>	Effector Memory CD4 Lymph Efflux
$\xi_7^*$	$\xi_8 \times (N_{Ln,nc8} / N_{B,nc8}) / \alpha$	day <sup>-1</sup>	Naive CD8 Lymph Influx
$\xi_8$	[0.643,1]	day <sup>-1</sup>	Naive CD8 Lymph Efflux
$\xi_9$	[2,5]	day <sup>-1</sup>	Effector CD8 Lymph Efflux
$\xi_{10}^*$	$\xi_{11} \times (CM_{Ln,nc8} / CM_{B,nc8}) / \alpha$	day <sup>-1</sup>	Effector CD8 Lymph Influx
$\xi_{11}$	[2,5]	day <sup>-1</sup>	Central Memory CD8 Lymph Efflux
$\xi_{12}$	[2,5]	day <sup>-1</sup>	Effector Memory CD8 Lymph Efflux
proliferationTime	8	hrs	Doubling time for cognate T cells in the lung
maxDivisions	4	--	Max number of divisions for T cells in the lung

**Supplementary Table 9.** The baseline parameters used in the blood, lymph node ODE compartments. \*Parameters calculated based upon the initial conditions of the system and the corresponding lymph efflux term. These parameters were not varied during LHS experiments as they were constrained by a corresponding lymph efflux parameter and the assumption that our initial conditions meet homeostasis.