## Supporting Information for

## MEDYAN: Mechanochemical Simulations of Contraction and Polarity Alignment in Actomyosin Networks

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## A comparison of MEDYAN to other agent-based cytoskeletal models.

This table is shown on the next page, with comparison categories as discussed in the Introduction section. Those categories are organized as follows:

- Chemistry The implementation of cytoskeletal chemistries within the model, which could include (but not limited to) filament, cross-linker, and molecular motor chemical dynamics.
- Mechanics The force-field description of semi-flexible filaments in the model, as well as other mechanical elements, including cross-linkers and molecular motors.
- **Diffusion and active transport** The capability of the model to include diffusion and active transport of some or all of its cytoskeletal species.
- Mechanochemical feedback The model's capability to include force-dependent reaction rates for some or all of its cytoskeletal species, which are updated dynamically during runtime.
- Dimensionality, time and length scales The previous time and length scales achieved by the model in its publications.
- Public code availability The access of source code and/or example applications for the model in a public repository.

Model	Chemistry	Mechanics	Diffusion and active transport	Mechanochemical feedback	Dimensionality, time and length scales	Public code availability	Refs
SCPR, Bidone et al. 2014, Tang et al. 2014, Laporte et al. 2012, Wang et al. 2008	Stochastic growth of actin filaments     Binding of cross-linkers and motors from bulk reservoir     No filament branching reported	Langevin dynamics with a coarse-grained point-like representation for filaments     Actin filament bending and stretching, motor and cross-linker interaction potentials     No inter-filament excluded volume effects reported	• Filaments diffuse via Brownian motion	None reported	<ul> <li>2D, 3D</li> <li>1000 s timescales</li> <li>5-15 µm length scales</li> </ul>	None reported	[1-4]
Cytosim, Nédélec and Foethke 2002-2007	<ul> <li>Stochastic growth of filaments</li> <li>Binding of cross-linkers and motors from bulk reservoir</li> <li>Filament branching</li> </ul>	Langevin dynamics with a coarse-grained point-like representation for filaments     Interaction potentials for filaments, cross-linkers, motors, branching molecules, in various verisons.     Repulsion or attraction between filament points for excluded volume effects	• Filaments diffuse via Brownian motion	Mechanochemical models for filaments, cross-linkers, motors	2D, 3D     Time and length scales vary greatly depending on simulated system	Example applications available for download at www.cytosim.org	[5, 6]
Jung et al 2015, Kim et al. 2009-2014	Stochastic growth of actin filaments Binding of cross-linkers from bulk reservoir Stochastic myosin II filament binding and walking	Langevin dynamics with a coarse-grained cylindrical segmentation for actin filaments     Cross-linker interaction potentials and very detailed myosin II potentials     Nearest-distance repulsion for cylinder excluded volume	Filaments diffuse via Brownian motion     Myosin II filaments diffuse via Brownian motion     Actin monomers and cross-linkers do not diffuse	Detailed mechanochemical models for cross-linker unbinding, and myosin II filament walking and unbinding	• 3D • 200 s timescales • 2-5 µm length scales	None reported	[7-9]
Muller et al. 2015, Cyron et al. 2009-2013	<ul> <li>Cross-linker spatially resolved binding onto filaments</li> <li>No growth or nucleation of filaments</li> <li>Does not implement filament branching</li> </ul>	Finite-element Brownian dynamics of semi-flexible filament bending and stretching     Cross-linker interaction potentials     Inter-filament excluded volume not reported in detail	Filaments and cross-linkers diffuse via Brownian motion     Actin monomers do not diffuse	None reported	• 3D • 1000 s timescales • 1-10 $\mu m$ length scales	None reported	[10-13]
Odell et al. 2008	Spatially resolved, stochastic chemical reactions via cytoplasmic domains     Mass-action kinetic equations for chemical reactions within cytoplasmic domains     Stochastic nucleation and growth of microtubules	Coarse-grained microtubules by spring segments, with bending and stretching potentials  No inter-filament excluded volume reported	Continuum diffusive flux between cytoplasmic domains     Convective transport modeled by viscous drag force on cytoplasmic domains	Mechanochemical model for microtubules	• 3D • 500 $s$ timescales • 80 $\mu m$ length scales	Example application available for download at www.celldynamics.org	[14]
Rafelski et al. 2008, Alberts et al. 2004	Spatially resolved, stochastic chemical reactions via partial differential equation reaction-diffusion scheme     Stochastic branching, nucleation and growth of actin filaments     Stochastically varying biochemical states of filament	Brownian dynamics of branched, rigid actin filaments and collision interactions with surfaces     No inter-filament excluded volume reported	Partial differential equation reaction-diffusion scheme for actin monomers and branching molecules	None reported	• 3D   • 100 $s$ timescales   • 10 $\mu m$ length scales	Source code and example application available for download at www.celldynamics.org	[15, 16]
MEDYAN	Stochastic reaction-diffusion master equation     Stochastic, spatially resolved filament nucleation and branching, growth, and state transitions     Cross-linker and motor dynamics	Conjugate gradient energy minimization     Interaction potentials for cross-linkers, motors, branching molecules, and filaments     Novel cylindrical rigid body repulsion	Stochastic, compartment based reaction-diffusion scheme for general transport of any unbound cytosolic species     No Brownian motion of filaments	Detailed mechanochemical models for filaments, cross-linkers, and motors	• 3D • 2000 $s$ timescales • 1-3 $\mu m$ length scales	Source code and example applications available for download at www.medyan.org	-

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