Hierarchical dynamics of informational patterns and decision making

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Supplementary Material:

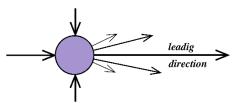


Figure S1. Illustration of a metastable state with several unstable separatrices: the system is moving with highest probability along the leading direction that corresponds to the largest positive eigenvalue λ_j .

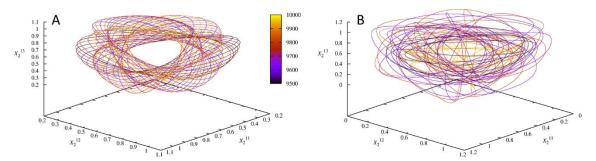


Figure S2: Projection of events X_2^{1m} in three different modalities m=1,2,3 as described by equation (3.1). All parameters are specified below. Time is encoded in the color bar. Panel A: One can see the forbidden region in the center of the figure which is related to the strong ($\xi=0.8$) competition between different modalities. Panel B: For weaker modality coupling values (e.g. $\xi=0.5$), this forbidden region disappears.

Model parameters

Model parameters for equations (2.3)–(2.6), Figs. 2 and 3: $N_{events}^{k} = 3; k = 1,2,3$ $\sigma_{1}^{0} = 7.24, \ \sigma_{2}^{0} = 5.85, \ \sigma_{3}^{0} = 8.30;$ $\sigma_{1}^{1} = 9.93, \ \sigma_{2}^{1} = 6.0, \ \sigma_{3}^{1} = 5.18; \ \sigma_{1}^{2} = 7.21, \ \sigma_{2}^{2} = 5.79, \ \sigma_{3}^{2} = 8.41,; \ \sigma_{1}^{3} = 8.29, \ \sigma_{2}^{3} = 7.86, \ \sigma_{3}^{3} = 9.16$ $\rho_{ii}^{k} = 1; k = 0,1,2,3; \ i = 1,2,3$ $\rho_{12}^{0} = \sigma_{1}^{0} / \sigma_{2}^{0} + 0.51; \ \rho_{21}^{0} = \sigma_{2}^{0} / \sigma_{1}^{0} - 0.5; \ \rho_{23}^{0} = \sigma_{2}^{0} / \sigma_{3}^{0} + 0.51;$ $\rho_{32}^{0} = \sigma_{3}^{0} / \sigma_{2}^{0} - 0.5; \ \rho_{31}^{0} = \sigma_{3}^{0} / \sigma_{1}^{0} + 0.51; \ \rho_{13}^{0} = \sigma_{1}^{0} / \sigma_{3}^{0} - 0.5;$ $\rho_{12}^{1} = \sigma_{1}^{0} / \sigma_{2}^{0} + 0.51; \ \rho_{21}^{1} = \sigma_{2}^{0} / \sigma_{1}^{0} - 0.5; \ \rho_{23}^{1} = \sigma_{2}^{0} / \sigma_{3}^{0} + 0.51;$ $\rho_{32}^{1} = \sigma_{3}^{0} / \sigma_{2}^{0} - 0.5; \ \rho_{31}^{1} = \sigma_{2}^{0} / \sigma_{1}^{0} + 0.51; \ \rho_{13}^{1} = \sigma_{1}^{0} / \sigma_{3}^{0} - 0.5;$ $\rho_{12}^{2} = \sigma_{1}^{0} / \sigma_{2}^{0} + 0.51; \ \rho_{21}^{2} = \sigma_{2}^{0} / \sigma_{1}^{0} - 0.5; \ \rho_{23}^{2} = \sigma_{2}^{0} / \sigma_{3}^{0} + 0.51;$ $\rho_{12}^{2} = \sigma_{1}^{0} / \sigma_{2}^{0} + 0.51; \ \rho_{21}^{2} = \sigma_{2}^{0} / \sigma_{1}^{0} - 0.5; \ \rho_{23}^{2} = \sigma_{2}^{0} / \sigma_{3}^{0} + 0.51;$

$$\begin{split} &\rho_{32}^2 = \sigma_3^0 \, / \, \sigma_2^0 - 0.5; \, \rho_{31}^2 = \sigma_3^0 \, / \, \sigma_1^0 + 0.51; \, \rho_{13}^2 = \sigma_1^0 \, / \, \sigma_3^0 - 0.5; \\ &\rho_{12}^3 = \sigma_1^0 \, / \, \sigma_2^0 + 0.51; \, \rho_{21}^3 = \sigma_2^0 \, / \, \sigma_1^0 - 0.5; \, \rho_{23}^3 = \sigma_2^0 \, / \, \sigma_3^0 + 0.51; \\ &\rho_{32}^3 = \sigma_3^0 \, / \, \sigma_2^0 - 0.5; \, \rho_{31}^3 = \sigma_3^0 \, / \, \sigma_1^0 + 0.51; \, \rho_{13}^3 = \sigma_1^0 \, / \, \sigma_3^0 - 0.5; \\ &\tau_e = 0.899, \, b = 0.01, \, \tau_E = 0.7, \, \theta = 1.1, \, \beta = 1 \\ &\xi^{11} = 1, \, \xi^{12} = 1.4, \, \xi^{13} = 0.5; \, \xi^{21} = 0.5, \, \xi^{22} = 1, \, \xi^{23} = 1.4; \, \xi^{31} = 1.4, \, \xi^{32} = 0.5, \, \xi^{33} = 1 \end{split}$$

Model parameters for equations (3.1)–(3.5):

$$N_{events} = 6; k = 1,2,3; M = 3$$

 $\sigma_1^m = 1.73, \sigma_2^m = 1.123, \sigma_3^m = 1.301, \sigma_4^m = 1.203, \sigma_5^m = 1.458, \sigma_6^m = 1.903; m = 1,..., M$
 $\rho_{ii}^{km} = 1; \forall k, m$

$$\rho_{13}^{km} = \rho_{35}^{km} = \rho_{51}^{km} = 5.0; \quad \rho_{46}^{km} = \rho_{24}^{km} = \rho_{62}^{km} = 2.0; \quad \rho_{16}^{km} = \rho_{21}^{km} = \rho_{32}^{km} = \rho_{43}^{km} = \rho_{54}^{km} = \rho_{65}^{km} = 1.5; \forall k, m$$
Only $\rho_{ii}^{km} \neq 0$ are indicated above.

$$\tau_{X_k} = 1; \tau_Y = 0.1; b' = 0.1; \theta = 0.05; \zeta_k = 0.2$$

Fig. S2A and Fig. 4b:

$$\xi_{11}^{k11} = \xi_{11}^{k12} = \xi_{11}^{k22} = \xi_{11}^{k23} = \xi_{11}^{k31} = \xi_{33}^{k11} = \xi_{33}^{k12} = \xi_{33}^{k23} = \xi_{33}^{k31} = \xi_{55}^{k31} = \xi_{55}^{k12} = \xi_{55}^{k23} = \xi_{55}^{k31} = 0.8; \forall k$$

Only $\xi_{ii}^{kml} \neq 0$ are indicated above.

Fig. S2B:

$$\xi_{11}^{k11} = \xi_{11}^{k12} = \xi_{11}^{k23} = \xi_{11}^{k31} = \xi_{33}^{k31} = \xi_{33}^{k11} = \xi_{33}^{k12} = \xi_{33}^{k23} = \xi_{33}^{k31} = \xi_{55}^{k11} = \xi_{55}^{k12} = \xi_{55}^{k23} = \xi_{55}^{k31} = 0.5; \forall k$$

Only $\xi_{ii}^{kml} \neq 0$ are indicated above.