

Supplementary material

Title: Stochastic Induction of Long-Term Potentiation and Long-Term Depression

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Supplementary Fig. S1. Ca²⁺ pulses used as input signals

Supplementary Fig. S2. Replots of the curves showed in Fig. 2 with standard error bars

Supplementary Fig. S3. Block diagram of the model with α CaMKII

Supplementary Fig. S4. Activation of the signalling network during MEK-induced LTD and Ca²⁺-induced LTD

Supplementary Fig. S5. Activations of the components of the model during LTP and LTD in single synapses

Supplementary Fig. S6. Curves of synaptic modifications as functions of Ca²⁺ elevations with different durations

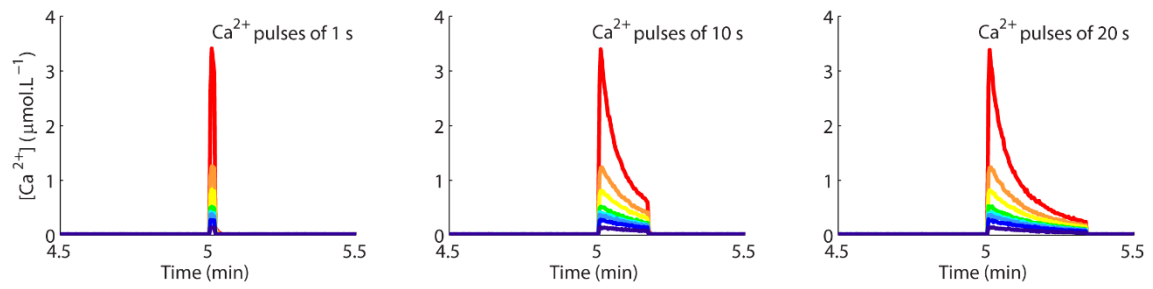
Supplementary Fig. S7. Time courses of synaptic plasticity for altered signalling networks

Supplementary Fig. S8. Dose-response curves

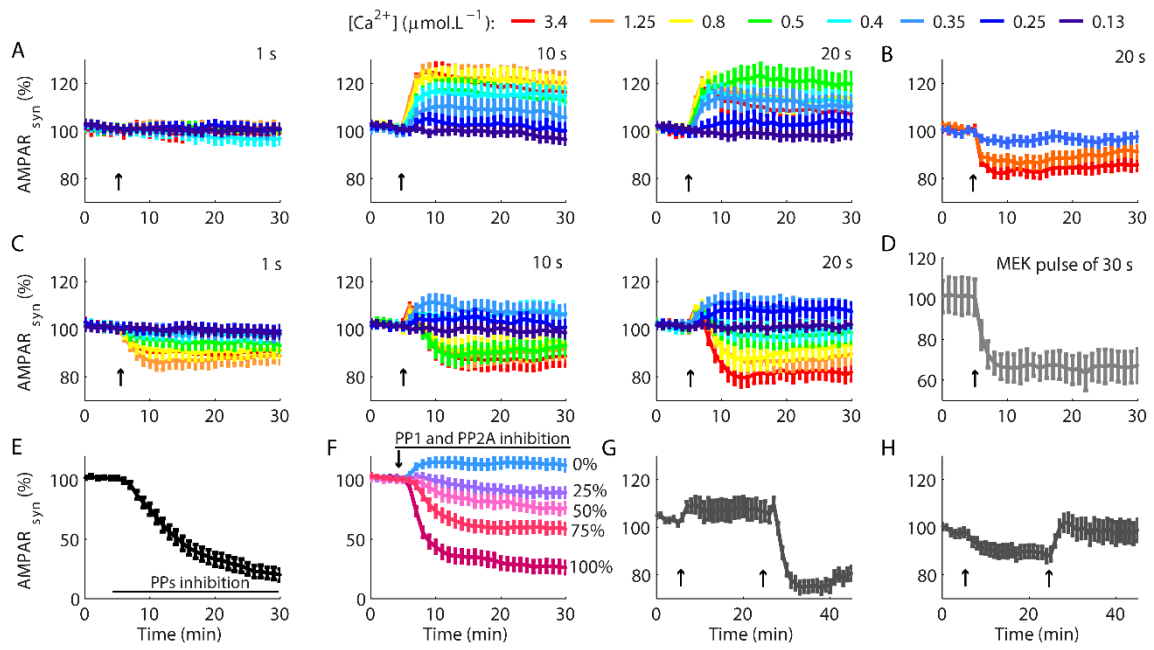
Supplementary Fig. S9. Sensitivity analyses

Supplementary Methods

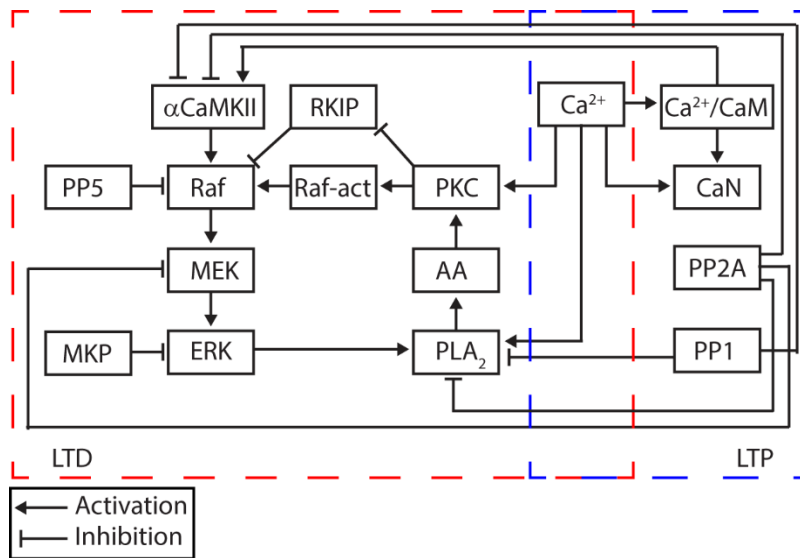
Supplementary Table S1. Parameters of the model



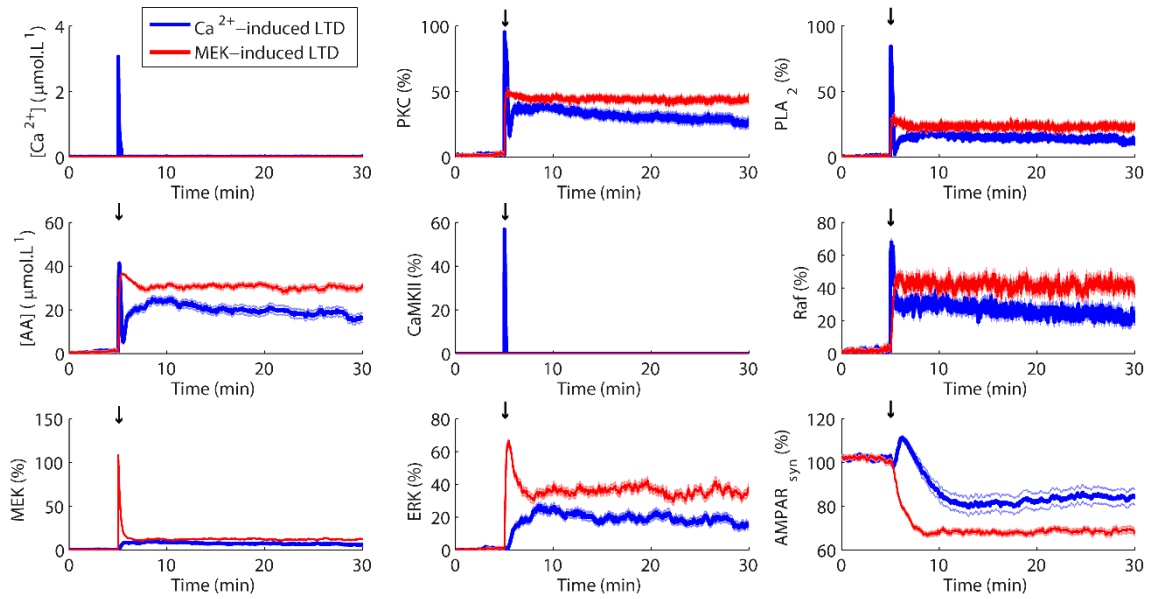
Supplementary Fig. S1. Ca²⁺ pulses used as input signals. These pulses were the input signals for the simulations showed in Fig. 2A. The shape of the pulses resulted from the Ca²⁺ dynamics implemented. Each curve is the average result of 100 single runs of the model.



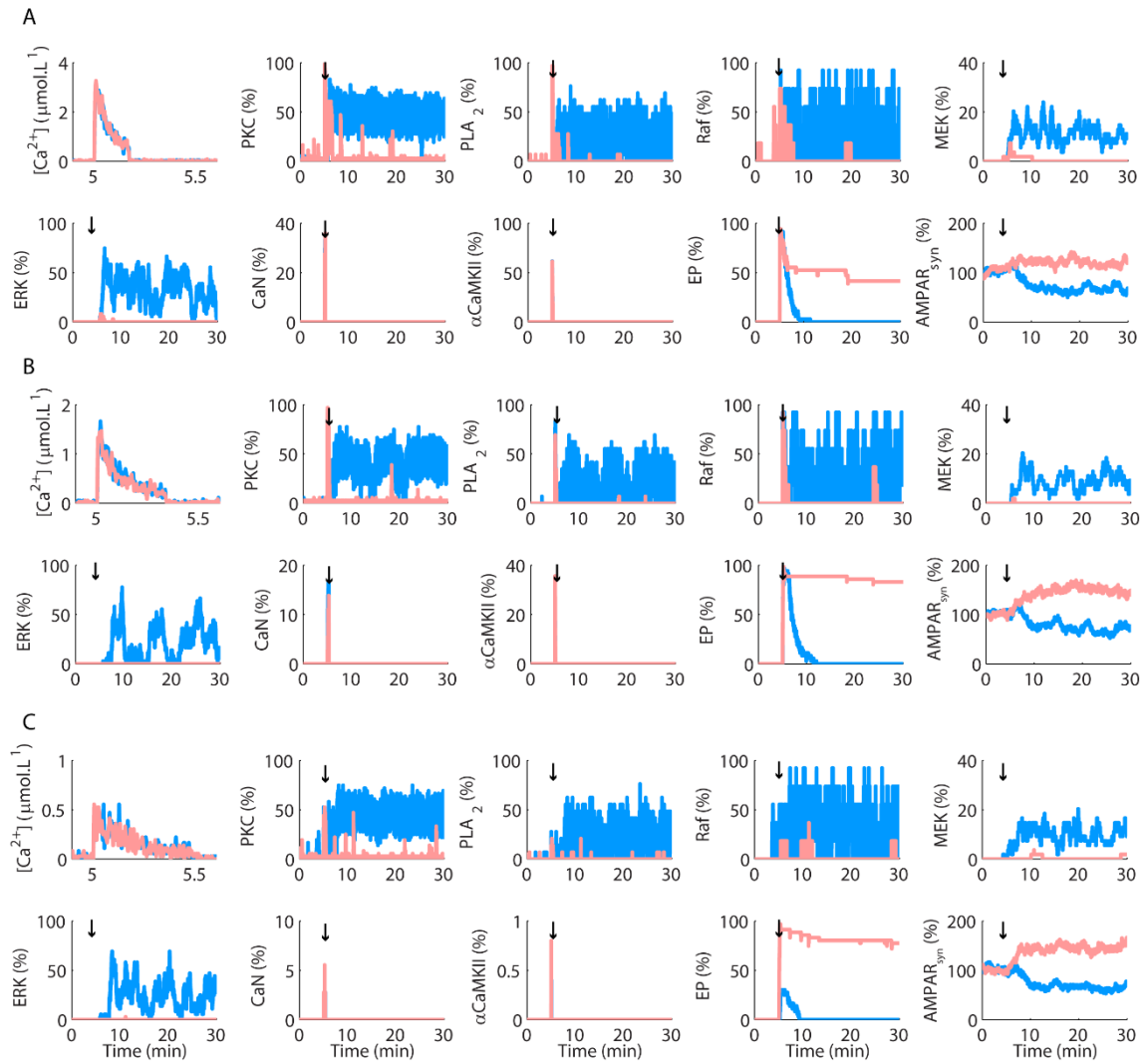
Supplementary Fig. S2. Replots of the curves showed in Fig. 2 with standard error bars. Each curve represents mean \pm standard error of the mean calculated from 100 (A-D) or 50 (E-H) single runs of the model.



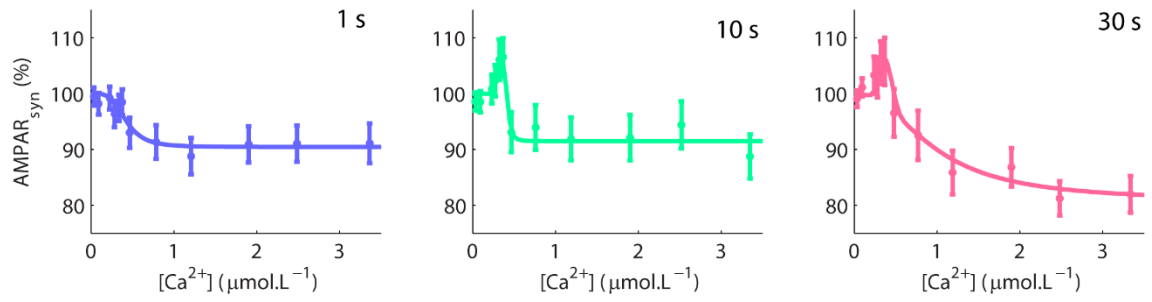
Supplementary Fig. S3. Block diagram of the model with α CaMKII. During LTD, α CaMKII acted as a Raf kinase.



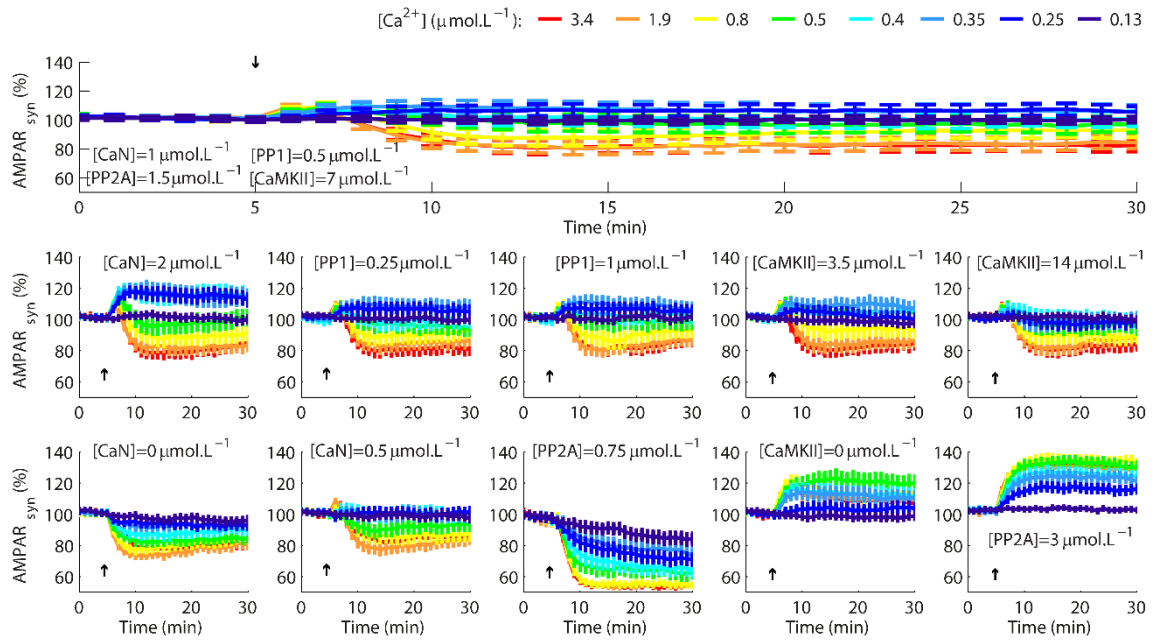
Supplementary Fig. S4. Activation of the signalling network during MEK-induced LTD and Ca^{2+} -induced LTD. A pulse of activated MEK (30 s of duration) induced a strong depression in the model through the activation of the positive feedback loop formed by PKC, PLA₂, and ERK pathway, without the activation of αCaMKII . Each curve represents mean (bold lines) \pm standard error of the mean (light lines) from 50 single runs of the model. The arrows indicate the moment of occurrence of the pulse of stimulation.



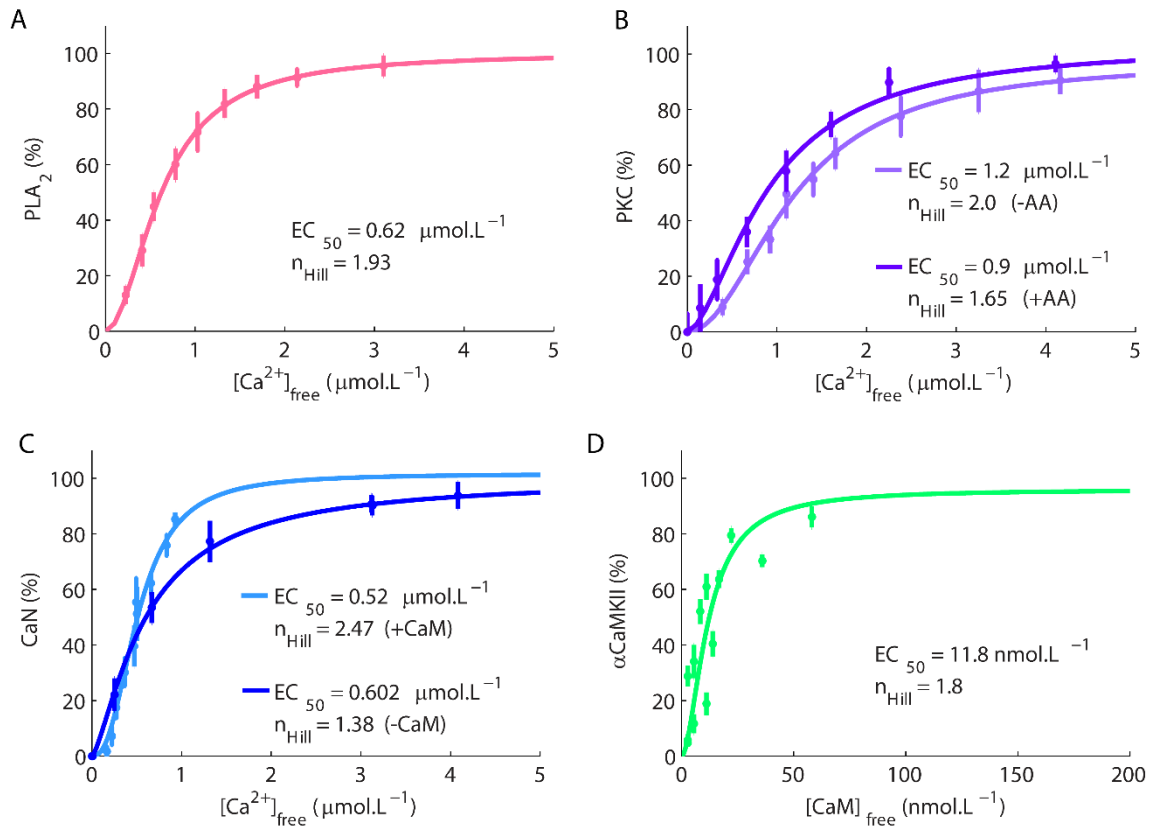
Supplementary Fig. S5. Activations of the components of the model during LTP and LTD in single synapses. (A-C) Time courses of the activities of the components of the model during LTD (light blue lines) and LTP (light pink lines) induced with Ca^{2+} pulses of 10 s (A), 20 s (B), and 30 s (C) of duration. The arrows indicate the instant of the occurrence of the Ca^{2+} pulses.



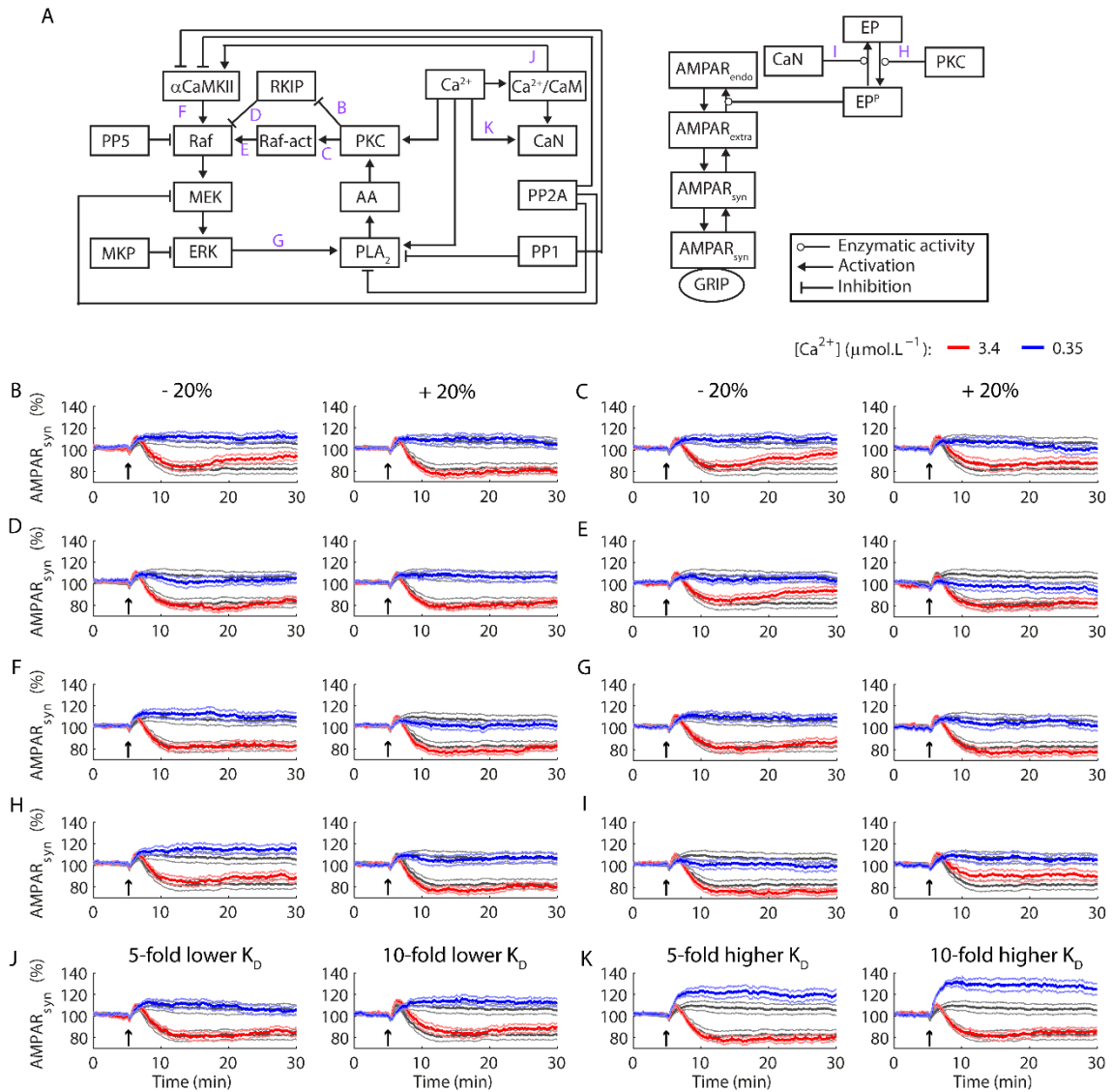
Supplementary Fig. S6. Curves of synaptic modifications as functions of Ca²⁺ elevations with different durations. The durations are indicated in the panels. Each dot is the mean \pm standard error of the mean calculated for 100 runs of the model.



Supplementary Fig. S7. Time courses of synaptic plasticity for altered signalling networks. Time courses of $AMPA_{syn}$ used to obtain the curves showed in Fig. 5. The first panel shows the results of the control model. The arrows indicated the moment of the occurrences of the Ca^{2+} pulses (duration of 20 s, the peak amplitudes are indicated in the legend). Each curve is the mean \pm standard error of the mean calculated from 100 simulations.



Supplementary Fig. S8. Dose-response curves. We used dose-response curves to validate the implementation of isolated Ca^{2+} -dependent components of the model through comparisons with experimental data. **(A)** Dose-response curve of the activation of PLA_2 as a function of $[\text{Ca}^{2+}]$. Experimental estimations reported n_{Hill} of 1.8^1 and EC_{50} of $\sim 0.7 \mu\text{mol.L}^{-1}$. **(B)** Dose-response curves of PKC activation as a function of $[\text{Ca}^{2+}]$ in the absence and in the presence of AA ($10 \mu\text{mol.L}^{-1}$ of AA and $1 \mu\text{mol.L}^{-1}$ of PKC). Experimental studies reported EC_{50} of $\sim 1.3 \mu\text{mol.L}^{-1}$ and n_{Hill} of 2.28 for the interaction of Ca^{2+} with PKC associated with membranes³. **(C)** Dose-response curves of CaN activation as a function of $[\text{Ca}^{2+}]$ in the absence and in presence of CaM ($10 \mu\text{mol.L}^{-1}$). These results are consistent with published experimental observations, which reported EC_{50} of $0.67 \mu\text{mol.L}^{-1}$ and n_{Hill} of 1.2 for the interaction of CaN with Ca^{2+} in absence of CaM, and EC_{50} of approximately $0.5 \mu\text{mol.L}^{-1}$ and n_{Hill} around 2.5 - 3 in the presence of CaM^{4,5}. **(D)** Dose-response curve of the autophosphorylation of αCaMKII as a function of $[\text{CaM}]$ in presence of $[\text{Ca}^{2+}]$ ($50 \mu\text{mol.L}^{-1}$). Experimental data reported n_{Hill} of 1.8 - 1.9 and EC_{50} around 4 - 20nmol.L^{-1} ⁶⁻⁸ in the presence of nucleotides. Each dot is the average result of 10 simulations (mean \pm standard error of the mean). The curves were fitted with 95% of confidence interval.



Supplementary Fig. S9. Sensitivity analyses. (A) Diagram of the model indicating the reactions analysed (purple letters B-I). (B-I) Simulations of the model with slower or faster rate constants (decrease of 20% and increase of 20%, respectively). For the analyses, we performed simulations of the model with a LTP and a LTD protocol and compared the results with the control model (gray lines, previously showed in Fig. 2B and Fig. S7). (J-K) Simulations of the model with changes in the affinities (indicated as dissociation constant, K_D) for the interaction of α CaMKII and Ca²⁺/CaM (J) and Ca²⁺ with the subunit CNB of CaN (K). Each curve is the average result of 50 runs of the model (mean \pm standard error of the mean). Further details are described in the Supplementary Methods.

Supplementary Methods

The computational model presented in this study consists of a well-mixed compartment containing mechanisms of calcium ion (Ca^{2+}) dynamics and the components of the signalling network. The development of the model involved two stages. Initially, we implemented each one of the Ca^{2+} -dependent components (calmodulin (CaM), calcineurin (CaN), protein kinase C (PKC), cytosolic phospholipases A_2 (PLA₂), and Ca^{2+} /Calmodulin protein kinase II α (αCaMKII)) isolated. We built these components based on the reaction mechanisms and parameters involved in their activations described in the literature. CaM and CaN were implemented according to previous descriptions^{9,10}. The other components, including the members of the extracellular signal-regulated protein kinase (ERK) and the species involved with Ca^{2+} -dynamics, were implemented according to a previous model of cerebellar long-term depression (LTD)¹¹. We validated the reactions and parameters used to simulate PKC, PLA₂, CaN, and αCaMKII by comparing their dose-response curves of activation with experimental data. After that, we coupled them with the other components of the model according to the diagrams showed in Fig. 1 and Supplementary Fig. S3.

The signalling network used to describe LTD and long-term potentiation (LTP) in the synapses between granule cells and Purkinje neurons consisted of a positive feedback loop formed by PKC-PLA₂-ERK pathway, which is implicated with LTD, and several protein phosphatases involved with LTP. The model of the positive feedback loop PKC-PLA₂-ERK pathway was based on a previous stochastic model¹¹ that we altered extensively to incorporate more recent experimental data. We included new components as part of the signalling machinery that simulates LTD (Raf kinase inhibitor protein (RKIP)¹², CaM, and αCaMKII ¹³) and also made extensive changes in the reactions and parameters used to simulate PKC and PLA₂ based on experimental data. Therefore, the only components of the model that were simulated entirely using the same reactions and parameters implemented previously¹¹ were some members of ERK pathway, and the species (pumps and exchanger) involved with Ca^{2+} -dynamics as listed in Supplementary Table S1. Also, we changed the software used to build the model¹¹. We implemented the model described in this work using BioNetGen¹⁴, a rule-based software for modelling biochemical networks.

The signalling molecules implicated with LTP consisted of several phosphatases that were included in the previous model of LTD to counteract the activation of the components of the feedback loop. In addition to these phosphatases, we implemented

CaN, which is involved exclusively with LTP in Purkinje cells¹⁵. Moreover, we implemented an extensive mechanism of AMPA receptors (AMPA) trafficking to simulate the expression of both LTP and LTD. The previous model of LTD simulated the trafficking of AMPARs and the persistent reduction in the population of synaptic AMPARs (AMPA_{syn}) as the mechanism of LTD expression¹¹ based on several experimental evidences¹⁶⁻²¹. However, to simulate LTP, which is expressed as an increase in the population of AMPAR_{syn}²², we expanded the mechanisms of AMPARs trafficking extensively to incorporate activity-driven mechanisms of exocytosis and reparametrized the reactions involved with endocytosis to balance the occurrence of both processes at rest and keep a stable basal population of AMPAR_{syn}. Most parameters of the model were obtained from the experimental literature. The other parameters were tuned manually to reproduce LTP and LTD in single synapses with magnitudes and time courses consistent with experimental data. All the other results presented in the work were emergent properties of the simulated system.

The details about the construction of the different components of the model are described in the following sections.

Ca²⁺ Dynamics

The Ca²⁺ dynamics of the model consisted of mechanisms responsible for the regulation of the intracellular Ca²⁺ concentration ([Ca²⁺]), and comprised the Ca²⁺ influx and extrusion from the cytosol. The Ca²⁺ influx, used to elevate the levels of [Ca²⁺] and promote plasticity, consisted of a first-order reaction that simulated pulses with specific durations and magnitudes. We also implemented a zero-order reaction that simulated a constant leak of Ca²⁺ to the cytosol to counteract the mechanisms of Ca²⁺ extrusion and sustain a basal [Ca²⁺] of approximately 50 nmol.L⁻¹¹¹. We simulated the mechanisms of Ca²⁺ extrusion as described previously¹¹. The extrusion was carried out by three species: the plasma membrane Ca²⁺-ATPase (PMCA), the sarco/endoplasmic reticulum Ca²⁺-ATPase (SERCA), and the sodium/Ca²⁺ exchanger (NCX). The description of the reactions and parameters of the Ca²⁺ dynamics are listed in Supplementary Table S1 (ID 1-4).

PLA₂

PLA₂ is a esterase composed by an α/β hydrolase domain and a C2 Ca²⁺-binding domain that binds two Ca²⁺ with positive cooperativity^{23,24}. The binding of Ca²⁺ to PLA₂

promotes its translocation to cellular membranes where its interfacial activation takes place and its substrates are located^{23,24}. We simulated the association of two Ca^{2+} to PLA_2 in two successive and reversible steps. Each step consisted of a reaction of Ca^{2+} association and a reaction of Ca^{2+} dissociation ($\text{Ca}^{2+} + \text{PLA}_2 \xrightleftharpoons[k_b]{k_f} (\text{Ca}^{2+})\text{PLA}_2$, forward rate constant (k_f) = $1.83 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ and backward rate constant (k_b) = 110 s^{-1} ; for the second ion: $\text{Ca}^{2+} + (\text{Ca}^{2+})\text{PLA}_2 \xrightleftharpoons[k_b]{k_f} (\text{Ca}^{2+})_2\text{PLA}_2$ $k_f = 11 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$, $k_b = 110 \text{ s}^{-1}$)^{1,23}. The binding of Ca^{2+} promoted the reversible translocation of PLA_2 to the membrane. We implemented the interaction of PLA_2 with the membrane as a pseudo-first order reaction ($k_f = 26 \text{ s}^{-1}$)²⁴. Experimental estimations of the k_b for the dissociation reaction vary from 14 s^{-1} to 0.002 s^{-1} ^{24,25}. We set k_b as 0.05 s^{-1} . In the model, PLA_2 also interacted with the membrane in absence of Ca^{2+} or in presence of a single Ca^{2+} associated to its structure. For all these interactions, we kept k_f unchanged (26 s^{-1}). PLA_2 bound to a single Ca^{2+} dissociated from the membrane with $k_b = 2.5 \text{ s}^{-1}$. In the absence of Ca^{2+} , we assumed a very weak affinity for the interaction of the membrane with PLA_2 and set $k_b = 260 \text{ s}^{-1}$.

In the presence of the membrane, PLA_2 exhibits higher affinities for Ca^{2+} ²³. To simulate this process, we kept the k_f used for the interactions of PLA_2 with Ca^{2+} in absence of membrane unchanged, and recalculated the dissociation rate constants ($k_b = 2.5 \text{ s}^{-1}$ and 0.41 s^{-1} for the first and second ion, respectively)¹.

In the membrane, PLA_2 catalyses the release of arachidonic acid (AA). We implemented this catalysis according to a previous description¹¹. The catalytic activity of PLA_2 is regulated by its phosphorylation catalyzed by ERK²⁵. In the model, the phosphorylated PLA_2 catalyzed the released of AA with a higher catalytic rate (k_{cat})². Additionally, the phosphorylation of PLA_2 increased its affinity for the membrane²⁵. PLA_2 was dephosphorylated by protein phosphatase 2A (PP2A) and 1 (PP1)¹¹. The reactions and parameters used to simulate PLA_2 are listed in Supplementary Table S1 (ID 5-22).

PKC

Several co-factors regulate PKC activity in a highly synergistic manner³. In the model, PKC interacted with Ca^{2+} , AA, and the cellular membrane with a random order. Typically, the association of PKC with Ca^{2+} and/or AA promotes its translocation to the cellular membrane, where its interfacial activation occurs^{3,26}. In absence of Ca^{2+} and AA,

PKC interacts with the membrane with a weak affinity ($K_D \sim 50 \mu\text{mol.L}^{-1}$)²⁷. The association between PKC and the membrane, in the absence or presence of co-factors, was simulated as a pseudo-first order reaction, and the dissociation as a first-order reaction ($PKC \xrightleftharpoons[k_b]{k_f} PKC_{memb}$, where PKC_{memb} states for PKC associated to the membrane). The k_f was set as 420 s^{-1} ²⁸. In the absence of Ca^{2+} and AA, we defined $k_b = 8400 \text{ s}^{-1}$ based on the weak affinity of this interaction²⁷. In the presence of Ca^{2+} and AA, PKC has a stronger apparent affinity for the membrane²⁷, which we modelled through changes in the k_b for the dissociation reactions.

PKC interacts with three Ca^{2+} ²⁹. We simulated the binding/unbinding of the three ions as sequential and reversible reactions. One of the Ca^{2+} -binding site of PKC binds Ca^{2+} with higher affinity ($K_D \sim 0.9 \mu\text{mol.L}^{-1}$) than the other two Ca^{2+} -binding sites ($K_D \sim 22.2 \mu\text{mol.L}^{-1}$)²⁹. The values of k_f for the interaction of PKC with the first, second and third ion were $1111 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$, $45.45 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$, and $45.45 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$, respectively. The values of k_b for the dissociation of PKC from the first, second and third ion was: 1000 s^{-1} ^{11,29}. PKC bound to the membrane has stronger affinities for Ca^{2+} . To simulate this property, we kept the rate constants of the binding of Ca^{2+} to PKC unchanged, and altered the rates of Ca^{2+} unbinding^{11,28,29}.

In the presence of Ca^{2+} , PKC has a stronger affinity for the membrane²⁷. We simulated this property by changing the rate for PKC dissociation (k_b) from the membrane gradually according to the number of ions bound to the enzyme^{11,24}. We kept k_f unchanged (420 s^{-1})²⁸.

PKC interacted with AA in the model with a stoichiometry of 1:1. The k_f for this interaction was $1 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$, and k_b was 10 s^{-1} ¹¹. Typically, the activation of PKC by AA occurs in the presence of Ca^{2+} ²⁶. However, experimental evidences indicated that high concentrations of AA activates PKC in absence of Ca^{2+} ²⁶. We implemented the activation of PKC by AA assuming that it mediated its interaction with the membrane with a weak affinity, simulated with a k_b of 420 s^{-1} . The k_f for this interaction remained unchanged. The presence of AA in combination with a single Ca^{2+} associated to PKC promoted a reduction of the k_b for the dissociation of the enzyme from the membrane (k_b of 42 s^{-1}), without affecting the affinity of the enzyme for Ca^{2+} directly³⁰. PKC bound to AA and two Ca^{2+} dissociated from the membrane with a k_b of 0.00017 s^{-1} . The complex PKC associated to AA and three Ca^{2+} had a k_b of 0.000017 s^{-1} , which implied that the dissociation of Ca^{2+} or AA preceded the unbinding of PKC from the membrane²⁴. In the

model, PKC were catalytically active when it was associated to the membrane and three Ca^{2+} , to the membrane and AA, or to the membrane, AA and Ca^{2+} . The complete description of reactions and parameters used to simulate PKC are listed in Supplementary Table S1 (ID 23-37).

ERK pathway

ERK pathway consists of three protein kinases organized in a hierarchical sequence: Rapidly accelerated fibrosarcoma (Raf), mitogen-activated ERK kinase (MEK), and ERK. The activation of MEK and ERK require dual phosphorylations, which we simulated as distributive events¹¹. However, based on recent experimental data, we implemented new mechanisms for the regulation of Raf.

We implemented Raf activation involving a single phosphorylation step¹¹. In the feedback loop PKC-PLA₂-ERK, PKC participates in the activation of Raf, but indirectly¹¹. Previously, the simulation of this process involved a Raf activator (Raf-act), a hypothetical kinase activated by PKC, that phosphorylated Raf in the model¹¹. However, recent data revealed that PKC regulates Raf activation by phosphorylating RKIP¹², a Raf inhibitor. We then implemented the inhibition of Raf through its interaction with RKIP in the model, which prevents MEK activation. RKIP binds to Raf both in its phosphorylated and non-phosphorylated states³¹. Depending of the residues phosphorylated, the K_D for the interaction between Raf and RKIP vary from 0.1 to approximately $100 \mu\text{mol.L}^{-1}$ ³¹. Nevertheless, as Raf has several putative phosphorylation residues³¹, and many of them appear to regulate its affinity for RKIP³¹, we opted to simulate the interaction between RKIP and Raf, phosphorylated and dephosphorylated, with the same affinity. The K_D for this interaction was $1 \mu\text{mol.L}^{-1}$ ($k_f = 1 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$, $k_b = 1 \text{ s}^{-1}$). Thus, at rest, Raf was inhibited by RKIP in the model. The activation of PKC promoted the phosphorylation of RKIP³² which resulted in a 100-fold reduction in its affinity for Raf in the model. The phosphorylation of RKIP by PKC was simulated with a K_M of $57 \mu\text{mol.L}^{-1}$ ³² that we converted in the velocity rate constants for the catalysis. We implemented RKIP dephosphorylation as a first-order process with a rate of 30 s^{-1} ³³.

Though the disinhibition of Raf by PKC is involved in ERK regulation¹², this process alone was not enough to activate ERK pathway in the model because it did not cause Raf activation. As PKC, PLA₂, and ERK pathway integrate a positive feedback loop during LTD³⁴, they must present mechanisms that ensure the consecutive activation of all its components. Consequently, we decided to maintain the activation of Raf through

Raf-act implemented previously¹¹. Therefore, PKC regulated Raf in the model through the inhibition of RKIP and the activation of Raf-act. Protein Phosphatase 5 (PP5) dephosphorylated Raf³⁵.

The activation of Raf promoted the activation of MEK and ERK, which we simulated as described previously¹¹. ERK phosphorylates PLA₂ and contributes to sustain its activity in absence of Ca²⁺²⁵. This process was implemented as described previously¹¹, but we updated the rate constants used in the simulations³⁶. The full description of the reactions and rate constants used to simulate ERK pathway is listed in Supplementary Table S1 (reactions 38-64).

CaM

To expand the LTD model to simulate LTP, we implemented CaM, a small Ca²⁺-binding protein that acts both as a Ca²⁺ buffer and as a Ca²⁺ mediator in the activation of several proteins³⁷. CaM is the only Ca²⁺ buffer implemented in the model. Purkinje cells contain high concentrations of several Ca²⁺ buffers that are important to shape the Ca²⁺ signals. However, we used Ca²⁺ pulses with controlled duration and amplitude in our model. Nevertheless, we implemented CaM to act as a Ca²⁺ mediator in the activation of CaN and α CaMKII. The model of the interaction of Ca²⁺ to CaM was implemented as described previously⁹.

In brief, CaM is a globular protein containing two pairs of Ca²⁺ binding sites, one located on its N-terminal domain (sites I and II), and the other on its C-terminal domain (sites III and VI). Ca²⁺ binds to the pair of Ca²⁺-binding sites of each CaM domain sequentially and with positive cooperativity⁹. There is no interdomain cooperativity⁹. We assumed that each CaM domain has two macroscopic association constants, K_I and K_{II}. K_I was defined as the sum of the microscopic equilibrium constants. Thus, for each pair of Ca²⁺-binding sites of CaM, K_I is given as follows:

$$K_{N1} = k_I + k_{II}, \text{ for the N-terminal domain} \quad (1)$$

$$K_{C1} = k_{III} + k_{IV}, \text{ for the C-terminal domain} \quad (2)$$

where k_I , k_{II} , k_{III} , and k_{IV} , correspond to the microscopic equilibrium constants of the Ca^{2+} -binding sites I, II, III, and IV, respectively. K_2 is given by the cooperativity for the binding of a second Ca^{2+} to either CaM globular domain as follows:

$$K_{N2} = k_n k_I k_{II}, \text{ for the N-terminal domain} \quad (3)$$

$$K_{C2} = k_c k_{III} k_{IV}, \text{ for the C-terminal domain} \quad (4)$$

k_n and k_c are the intradomain cooperative constants for the binding of the second Ca^{2+} to the N- and C-terminal domains. A full description of the reactions and references used in the model of CaM was published previously⁹. The parameters and reactions implemented to simulate the interaction between Ca^{2+} and CaM are listed in Supplementary Table S1 (ID 65-72).

CaN

CaN is a heterodimer formed by a catalytic subunit (CNA), which contains a Ca^{2+} /CaM-binding site, and a regulatory subunit (CNB) with four Ca^{2+} -binding sites^{4,38}. The interaction of Ca^{2+} with CNB is necessary for binding of Ca^{2+} /CaM to CNA^{4,39}.

CNB contains two globular domains, each one with a pair of Ca^{2+} -binding sites. CNB is structurally similar to CaM and troponin C, in consequence, we simulated the binding/unbinding of Ca^{2+} to the four Ca^{2+} -binding sites of CNB as having intradomain cooperativity, but without interdomain cooperativity. To estimate the microscopic parameters for the interaction of Ca^{2+} to CNB, we used the same approach applied to CaM (equations 1-4). The macroscopic binding constants for Ca^{2+} -binding sites of CNB are $0.094 \mu\text{mol.L}^{-1}$ (K_{C1}), $0.036 \mu\text{mol.L}^{-1}$ (K_{C2}), $1.1 \mu\text{mol.L}^{-1}$ (K_{N1}), and $0.6 \mu\text{mol.L}^{-1}$ (K_{N2})⁴⁰. We assumed that the microscopic affinity for both sites of a given CaN domain are equivalent, and calculated the values of k_{III} and k_{IV} ($0.047 \mu\text{mol.L}^{-1}$), k_I and k_{II} ($0.55 \mu\text{mol.L}^{-1}$), and the values of the cooperative constant for the C-terminal ($k_c = 16.29 \mu\text{mol}^{-1} \cdot \text{L}$), and N-terminal ($k_n = 2 \mu\text{mol}^{-1} \cdot \text{L}$). The k_b for the dissociation of the first Ca^{2+} from the C-terminal was defined as 0.03 s^{-1} ³⁸, which resulted in a k_f of $0.64 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$. We used equal values of k_f for the binding of Ca^{2+} to both sites on the same terminal domain. We calculated the k_b for the dissociation of Ca^{2+} from the second site occupied in the C-terminal as 0.0018 s^{-1} . For the sites of the N-terminal, we used a k_b of 0.05 s^{-1} ³⁸ for the

first Ca^{2+} , and calculated the k_f ($0.09 \mu\text{mol}^{-1}\text{L}\cdot\text{s}^{-1}$). We used the same k_f for the binding of the second ion. The k_b for the unbinding of the second Ca^{2+} was 0.025 s^{-1} .

CaN interacted with $\text{Ca}^{2+}/\text{CaM}$ after the binding of Ca^{2+} to CNB. CaN binds to $\text{Ca}^{2+}/\text{CaM}$ fully or partially loaded with Ca^{2+} ⁴¹. We simulated the interaction of CaN with fully loaded $\text{Ca}^{2+}/\text{CaM}$ using a k_f of $46 \mu\text{mol}^{-1}\text{L}\cdot\text{s}^{-1}$ and a k_b of 0.0012 s^{-1} ⁴². The interaction between CaM and its targets occurs through hydrophobic residues exposed after its binding to Ca^{2+} . The association of a single Ca^{2+} can shift CaM conformation from closed to open and exposes residues for target interaction⁴³, though the binding of a pair of ions is important for stabilizing the open conformation of each domain⁴³. Because the binding of a single ion can change CaM conformation, we assumed that CaN interact with CaM bound to three or two Ca^{2+} with the same affinity reported for the interaction with CaM fully saturated. However, at least one Ca^{2+} -binding site of each CaM domain had to be filled. For interactions of CaN with CaM with Ca^{2+} in only one of its domains, we kept the k_f ($46 \mu\text{mol}^{-1}\text{L}\cdot\text{s}^{-1}$) unchanged. Then, we recalculated the k_b using affinities for the association of CaN with isolated CaM domains ($K_D = 1$ for the C-terminal ($k_b = 46 \text{ s}^{-1}$), and $K_D = 7 \mu\text{mol}\cdot\text{L}^{-1}$ for the N-terminal ($k_b = 322 \text{ s}^{-1}$))⁴¹.

Similarly to other CaM targets³⁷, CaN increases the affinity of Ca^{2+} for CaM^{4,41}. This process was implemented using equations (1)-(4). The presence of CaM targets usually alters the rate constants of Ca^{2+} dissociation from CaM structure⁴⁴. Based on this fact, the k_b s for the dissociation of the first and second ion to each CaM domain associated to CaN were calculated considering the microscopic binding for the sites k_{I} and k_{II} ($0.8 \mu\text{mol}^{-1}\text{L}$) and k_{III} and k_{IV} ($5 \mu\text{mol}^{-1}\text{L}$). We kept the cooperative constants k_n ($80 \mu\text{mol}^{-1}\text{L}$), and k_c ($200 \mu\text{mol}^{-1}\text{L}$) unchanged by the presence of CaN⁹. The complete description of the reactions and parameters used to simulate CaN was published previously¹⁰ and is listed in Supplementary Table S1 (reactions 73-87).

αCaMKII

αCaMKII is a multimeric holoenzyme composed of 12-14 subunits, organized as an assembly of ‘vertical dimers’⁴⁵. Each subunit consists of an N-terminal kinase domain, a regulatory domain, a linker, and a C-terminal association domain⁴⁵. The regulatory domain docks to the substrate-recognition site of the kinase domain and retains the subunit in an inactive state⁴⁵. The binding of $\text{Ca}^{2+}/\text{CaM}$ to the regulatory domain activates αCaMKII kinase activity. Each αCaMKII subunit binds to one $\text{Ca}^{2+}/\text{CaM}$ (23)⁴⁵. αCaMKII interacts with CaM fully or partially saturated with Ca^{2+} ^{46,47}. The association

of $\text{Ca}^{2+}/\text{CaM}$ promotes the trans-autophosphorylation of the residue Thr²⁸⁶, which requires the kinase domain of one subunit to phosphorylate the kinase domain of another subunit within the same holoenzyme⁴⁵. The autophosphorylation of αCaMKII maintains it in a partial Ca^{2+} -independent activated state, which is further stimulated by $\text{Ca}^{2+}/\text{CaM}$ ⁴⁸.

The multimeric structure of αCaMKII with multiple different states makes it a difficult enzyme to model. In consequence, the majority of the available models of αCaMKII adopted strategies of simplification, which typically consist of reducing the states considered for each subunit and reducing the size of the holoenzyme^{49,50}. In our model, we reduced the size of the holoenzyme to two subunits implemented with a detailed mechanism of interaction with $\text{Ca}^{2+}/\text{CaM}$. We simulated two subunits instead of one because αCaMKII binds $\text{Ca}^{2+}/\text{CaM}$ with positive cooperativity^{6,45}.

The interaction of the first subunit with $\text{Ca}^{2+}/\text{CaM}$ was simulated with a k_f of $20 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ ^{7,8} and k_b of 20 s^{-1} . For the binding of the second $\text{Ca}^{2+}/\text{CaM}$, we implemented a reduction in the k_b (18 s^{-1}) to simulate the cooperativity for its interaction with αCaMKII . We manually tuned this value to fit the hill coefficient (n_{hill}) reported for αCaMKII interaction with $\text{Ca}^{2+}/\text{CaM}$ (~ 1.9)⁶.

Experimental findings reported that αCaMKII interacts with CaM partially loaded with Ca^{2+} ^{46,47}. We assumed that αCaMKII interacts with CaM with at least one Ca^{2+} bound to each one of its globular domains with the same rate constants used for the interaction of αCaMKII with CaM fully saturated with Ca^{2+} . The association of αCaMKII with CaM with Ca^{2+} bound only to its N-terminal domain occurs with a very weak affinity^{46,47}. Consequently, we omitted this interaction in the model for simplicity. The interaction between αCaMKII and CaM with Ca^{2+} bound only to the Ca^{2+} -binding sites of the C-terminal domain was implemented considering an affinity 250-fold lower than the affinity used for the interaction between αCaMKII and CaM fully loaded with Ca^{2+} . Experimental reports indicated changes in this affinity ranging from ~ 100 - 500 -fold^{46,47}. We simulated this reduction in the affinity by changing the k_b for the dissociation of CaM from αCaMKII ($k_b = 5000 \text{ s}^{-1}$ and 4500 s^{-1} for the first and second $\text{Ca}^{2+}/\text{CaM}$ molecule, respectively).

The presence of αCaMKII increases the affinity between CaM and Ca^{2+} . However, αCaMKII changes the affinity of the Ca^{2+} -binding sites of CaM for Ca^{2+} asymmetrically^{44,47}. We simulated this process using a reduction of the k_b s for the dissociation of Ca^{2+} from CaM bound to αCaMKII of 100-fold and 20-fold for the Ca^{2+} -binding sites of the N and C-terminal domains, respectively^{44,47}. The autophosphorylation

of α CaMKII did not promote a further enhancement in the affinity between CaM and Ca^{2+} in the model.

Although α CaMKII can interact with CaM partially saturated with Ca^{2+} , the filling of the Ca^{2+} bindings sites I, III and IV of CaM are necessary for α CaMKII activation⁵¹. For simplicity, we assumed that only α CaMKII associated to two molecules of CaM fully saturated with Ca^{2+} could undergo its trans-autophosphorylation. Two molecules of CaM were necessary because α CaMKII autophosphorylation is an inter-subunit process⁴⁵. We implemented the autophosphorylation of α CaMKII as a first-order reaction with a rate constant of 5 s^{-1} ⁵¹. After its autophosphorylation, α CaMKII has a significant increase in its affinity for CaM⁵². We used a 1000-fold reduction in the k_{bS} for the dissociation of CaM from α CaMKII to implement this change in affinity⁵².

We estimated the number of copies of our dimeric α CaMKII in 250^{53} , which corresponds to 500 subunits.

Classically, it was assumed that the autonomy of α CaMKII persisted for hours to sustain long-term forms of synaptic plasticity, especially hippocampal LTP. However, recent experimental findings reported that, in dendritic spines, during hippocampal LTP, the activation of α CaMKII persists only for seconds⁵⁴. Based on these findings, in our model, autonomous α CaMKII was rapidly inactivated by dephosphorylation after its activation caused by a brief Ca^{2+} pulse. Two enzymes, PP1 and PP2A, dephosphorylate α CaMKII⁵⁵. In hippocampal dendritic spines, evidences indicated that PP1 is likely to play a major role in α CaMKII dephosphorylation than PP2A in the postsynaptic density (PSD)⁵⁵. Outside the PSD, PP2A is the main responsible for α CaMKII dephosphorylation⁵⁵. Nevertheless, in Purkinje cells, these differences between PP1 and PP2A activity on α CaMKII have not been investigated. Thus, in the model, both PP1 and PP2A dephosphorylated α CaMKII with equivalent rate constants estimated from experimental reports^{55,56}.

In the model, α CaMKII acted as a Raf kinase^{57,58}. Most models of CaMKII assumed that its autonomous activity is equal to its activity in the presence of Ca^{2+} /CaM. However, the catalytic activity of autonomous α CaMKII toward its substrates is lower (15-25 %) ⁴⁸. To simulate the phosphorylation of Raf by α CaMKII, we assumed that only α CaMKII associated to two molecules of fully saturated Ca^{2+} /CaM had maximum catalytic activity. Autonomous α CaMKII or α CaMKII bound to all the other states of Ca^{2+} /CaM where simulated having a catalytic rate constant (k_{cat}) that corresponded to

20% of its maximum activity. The description of the reactions and parameters used to simulate α CaMKII is listed in Supplementary Table S1 (reactions 88-108).

AMPA trafficking

We simulated AMPARs trafficking using first-order reactions for the reversible lateral diffusion of the synaptic receptors (AMPA_{syn}) to extra-synaptic regions ($\text{AMPA}_{\text{extra}}$)¹¹. We estimated the rate constants for these reactions using the diffusion coefficients of AMPARs and the length of the synaptic and extra-synaptic areas^{11,59,60}. The endocytosis of AMPARs occurred from extra synaptic sites and required the catalytic activity of a phosphorylated endocytic protein (EP). The activation of PKC during LTD caused the synaptic depression through the phosphorylation of AMPA_{syn} ¹¹. PP2A counteracted PKC activity¹¹. The phosphorylation of AMPARs by PKC did not alter their lateral diffusion, but increased their endocytosis rate. We implemented the exocytosis of internalized AMPARs ($\text{AMPA}_{\text{endo}}$) as a first-order reaction that inserted the receptors in the extra-synaptic regions with an exocytosis rate (0.006 s^{-1}) tuned to obtain time courses of LTP observed in Purkinje neurons. The exocytosis of AMPAR required their dephosphorylation in the model.

Part of the AMPA_{syn} interacted with the glutamate-receptor interacting protein (GRIP) and were simulated as immobile^{16,60}. The phosphorylation of AMPA_{syn} promoted a decrease in their affinity for GRIP and reduced the amount of receptors that interacted with it¹⁶. We used a K_D of $1 \mu\text{mol.L}^{-1}$ for the binding/unbinding of GRIP and AMPA_{syn} . These rates were based on experimental and theoretical data⁶⁰. For the interaction of the phosphorylated AMPA_{syn} with GRIP, we kept k_f unchanged and increased k_b by seven-fold^{16,60}. As a result of this change of k_b , a larger pool of AMPA_{syn} could undergo lateral diffusion and endocytosis, which promoted LTD in the model.

To simulate LTP, we assumed that the internalization of AMPARs required the catalytic activity of phosphorylated EP. This assumption was based on recent data that demonstrated that phosphorylated syndapin participates in the endocytosis of AMPARs through associations with protein interacting with C-kinase 1 (PICK1), and, possibly, dynamin¹⁹. Several proteins involved with vesicle endocytosis are phosphorylated by PKC and dephosphorylated by CaN^{61,62}. Moreover, both PKC and CaN are directly involved with AMPARs trafficking^{16-19,63}. Thus, in our model, CaN counteracted the action of PKC on EP. The dephosphorylation of EP blocked the internalization of AMPARs without affecting their constitutive exocytosis. To define the rate constants for

these reactions, we used a higher K_m for PKC ($5 \mu\text{mol.L}^{-1}$ for PKC and $11 \mu\text{mol.L}^{-1}$ for CaN), but higher rate constants for CaN. This assumption was important to favour the fast action of CaN on EP because CaN has no sustained activity in our model. We implemented PKC action with a higher K_m than CaN to guarantee the phosphorylation of EP under basal conditions to sustain the constitutive AMPARs trafficking. The full description of the reactions and parameters used to simulate AMPARs trafficking is listed in Supplementary Table S1 (reactions 109-129).

Additional methods

For the molecules directly activated by Ca^{2+} , we fitted dose-response curves of activation and compared them with published experimental data for validation. Each molecule was analysed isolated from the other components of the model. We performed these analyses for PLA_2 , PKC, CaN and αCaMKII . We validated CaM previously⁹. The other components were validated as part of the LTD model published before¹¹.

For each dose-response curve, we varied systematically the initial $[\text{Ca}^{2+}]$ and, after the system has reached steady-state, we verified the remaining free $[\text{Ca}^{2+}]$ ($[\text{Ca}^{2+}]_{\text{free}}$) and the concentration of the active enzyme under analysis. Then, we fitted the dose-response curves with the equation:

$$[P] = [P_{\text{max}}] \frac{[\text{Ca}^{2+}]^{n_{\text{Hill}}}}{EC_{50}^{n_{\text{Hill}}} + [\text{Ca}^{2+}]^{n_{\text{Hill}}}} \quad (5)$$

where $[P]$ is the percentage of the activate enzyme, $[P]_{\text{max}}$ is its percentage of maximum activation, n_{Hill} is the Hill coefficient, and EC_{50} is the $[\text{Ca}^{2+}]$ required to activate the half maximum amount of $[P]$. The parameters of the dose-response curves, n_{Hill} and EC_{50} , were compared with experimental data.

The parameters obtained for the dose-response curve of the activation of PLA_2 as a function of $[\text{Ca}^{2+}]$ (Supplementary Fig. S8A) are in accordance with experimental data, which reported an apparent K_{Ca} (EC_{50}) of $\sim 0.7 \mu\text{mol.L}^{-1}$ ². The n_{Hill} for the interaction of Ca^{2+} with PLA_2 associated with membranes was estimated in 1.8^1 . We also obtained parameters for the activation of PKC consistent with experimental findings, which reported EC_{50} of $\sim 1.3 \mu\text{mol.L}^{-1}$ and n_{Hill} of 2.28 for the interaction of Ca^{2+} with PKC associated with membranes³ (Supplementary Fig. S8B). PKC is known to be activated by combinations of its co-factors in a synergistic manner³. Thus, in the presence of a constant

concentration of AA ($10 \mu\text{mol.L}^{-1}$), we verified a decrease in the EC_{50} for the activation of PKC by Ca^{2+} and a slight reduction in its n_{Hill} (Supplementary Fig. S8B). We validated the reactions and parameters used to simulate CaN by verifying its Ca^{2+} requirement in the absence and in the presence of saturating CaM ($1 \mu\text{mol.L}^{-1}$ of CaN and $10 \mu\text{mol.L}^{-1}$ of CaM, respectively). The parameters of the dose-response curves (Supplementary Fig. S8C) obtained by fitting equation (5) are consistent with published experimental observations, which reported EC_{50} of $0.67 \mu\text{mol.L}^{-1}$ and n_{Hill} of 1.2 for the interaction of CaN to Ca^{2+} in absence of saturating CaM, and EC_{50} of approximately $0.5 \mu\text{mol.L}^{-1}$ and n_{Hill} around 2.5-3 in the presence of saturating CaM^{4,5}. Note that the model of CaN used in this work was published previously¹⁰. To validate the model of αCaMKII activation, we verified its autophosphorylation as a function of CaM concentration (in equation (5), we replaced $[\text{Ca}^{2+}]$ with $[\text{CaM}]$) in the presence of Ca^{2+} ($1 \mu\text{mol.L}^{-1}$ of αCaMKII , $50 \mu\text{mol.L}^{-1}$ of Ca^{2+}) (Supplementary Fig. S8D). Experimental data reported n_{Hill} of 1.8-1.9 and K_D around $5\text{-}20 \text{ nmol.L}^{-1}$ ⁶⁻⁸ in the presence of nucleotides (ATP and ADP), which we used for comparison with EC_{50} . Note that, in the absence of nucleotides, αCaMKII interacts with CaM with a 10-fold weaker affinity⁶⁻⁸. However, ATP and ADP, which are co-substrate and co-product of αCaMKII , respectively, are present in concentrations well beyond the levels required to saturate αCaMKII in the cells.

Sensitivity Analyses

Most parameters used in the model were determined experimentally. However, some parameters have not been determined experimentally and were tuned to reproduce the curves of synaptic plasticity. We performed sensitivity analyses to verify which one of these parameters produce the most variation in the time courses of opposite forms of synaptic plasticity. However, we restricted the sensitivity analyses to some reactions of the model because many of its components were analysed previously¹¹. The analyses focused on the rate constants used for the reactions involved in the connections between PKC and ERK pathway through the activation of Raf, an important bottleneck for the activation of the positive feedback loop involved with LTD. We also analysed the rate constants used for the phosphorylation of PLA_2 by ERK and for the phosphorylation/dephosphorylation of EP by PKC and CaN. Supplementary Fig. S9A indicated all the reactions analysed. The analyses consisted in systematic changes in the rate constants (increase of 20% or decrease of 20%) used in the connections between the selected components. All the reactions involved in each connection point analysed were

altered simultaneously and by the same factor. So, for instance, for a catalytic reaction involving an enzyme E, a substrate S and the formation of a product P ($E + S \xrightleftharpoons[k_b]{k_f} ES \xrightarrow{k_{cat}} E + P$), we altered k_f , k_b , and k_{cat} simultaneously (increase of 20% or decrease of 20%) for the analysis. Then, we performed simulations and compared the results with the control model (Supplementary Fig. S9B-I, gray lines) during the occurrence of LTP and LTD in a population of synapses. The results obtained confirmed that the mechanisms involved in the activation of Raf are important bottlenecks of the model of LTD (Supplementary Fig. S9B-F). As a result, reductions in the rate constants for the phosphorylation of RKIP and Raf-act by PKC affected the stability of LTD, but did not alter LTP (Supplementary Fig. S9B-C). Changes in the rate constants for the inhibition of Raf by RKIP promoted no significant modifications in the results of the model (Supplementary Fig. S9D). The occurrence of both LTP and LTD were sensitive to changes in the rate constants for the activation of Raf by Raf-act (Supplementary Fig. S9E), but only slightly affected by alterations in the activation of Raf by α CaMKII (Supplementary Fig. S9F). Changes in the parameters for the phosphorylation of PLA₂ by ERK promoted no modifications of LTP and LTD (Supplementary Fig. S9G). The reduction of the rate constants for the phosphorylation of EP by PKC increased the magnitude of LTP without affecting LTD. However, the increase of the same rate constants had no effects in the model (Supplementary Fig. S9H). In contrast, the decrease of the rate constants of EP dephosphorylation catalyzed by CaN altered the magnitudes of LTP and LTD, but the increase of the same rate constants affected only LTD (Supplementary Fig. S9I). In addition to this analysis, we verified the impacts of the affinity for the interaction between Ca²⁺/CaM and α CaMKII and the affinities of CaN for binding to Ca²⁺ in the results obtained. As mentioned previously, in presence of nucleotides, α CaMKII has an affinity for Ca²⁺/CaM that is approximately 10-fold higher than the affinity measured in absence of nucleotides⁶⁻⁸. In the cells, nucleotides are present in concentrations high above what is required to saturate α CaMKII. However, as many works estimated the affinity for the interaction of Ca²⁺/CaM and α CaMKII in absence of nucleotides, we decreased the affinity for the binding of Ca²⁺/CaM to α CaMKII by 5- and 10-fold to verify its impact on the model (Supplementary Fig. S9J). None of these changes resulted in a significant change in the results of the model (Supplementary Fig. S9J), which indicated that the affinity for the interaction of Ca²⁺/CaM and α CaMKII used in the model was not crucial for the results observed. Next,

we accessed the effects of the affinities for the interactions of Ca^{2+} with the Ca^{2+} -binding sites of the subunit CNB of CaN on the model. As described previously, the binding of Ca^{2+} to the Ca^{2+} -bindings sites of CNB is a precondition for the high affinity⁴² interaction of Ca^{2+} /CaM with CNA^{4,38,39}. Moreover, though CNA interacts with Ca^{2+} /CaM with a very high affinity, the overall Ca^{2+} requirement of CaN to become activated is in the range of 0.5-0.7 $\mu\text{mol.L}^{-1}$ in the model, which is fully consistent with the experimental literature^{4,5,38}. However, to verify whether the Ca^{2+} requirement of CaN could act as a bottleneck to the results observed in this work, we enhanced the affinities for the bindings of Ca^{2+} to the Ca^{2+} -bindings sites of CNB by 5-fold and 10-fold (Supplementary Fig. S9K). The results of this manipulation demonstrated that the increase in the affinity of Ca^{2+} for CNB increased the magnitude of LTP occurrences without affecting LTD (Supplementary Fig. S9K). In the model, CaN is involved only with LTP, which is consistent with previous studies^{15,64}. LTD requires the activation of a positive feedback loop, which presents a robust and sustained activity that occludes the activation of CaN and the expression of LTP. As CaN does not influence the activation of the feedback loop, increasing its activation by changing its affinity for Ca^{2+} does not alter the occurrence of LTD. Therefore, favouring the activation of CaN by increasing its affinity for Ca^{2+} promoted only an enhancement in the magnitude of LTP. Thus, the data presented in our work are not based on the affinity of Ca^{2+} /CaM for αCaMKII or on the affinity of Ca^{2+} for CaN, but resulted from the whole system simulated.

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Supplementary Table S1: Parameters of the model

ID	Species/Reactions	Parameters	Notes	Ref.
	Volume of the compartment	0.06e-15 L	We subtracted the volume of the endoplasmic reticulum to calculate the volume of the compartment simulated	⁵⁹
	Ca ²⁺	~ 50 nmol.L ⁻¹	Basal concentration	¹¹
	SERCA	60 molecules		¹¹
	PMCA	10 molecules		¹¹
	NCX	4 molecules		¹¹
	PLA ₂	0.4 μmol.L ⁻¹		¹¹
	PKC	1 μmol.L ⁻¹		¹¹

	PP2A	$1.5 \mu\text{mol.L}^{-1}$		11
	Raf	$0.15 \mu\text{mol.L}^{-1}$		65
	RKIP	$1.5 \mu\text{mol.L}^{-1}$		This paper
	Raf-act	$0.5 \mu\text{mol.L}^{-1}$		11
	MEK	$1.5 \mu\text{mol.L}^{-1}$		11
	ERK	$1 \mu\text{mol.L}^{-1}$		11
	PP5	$1 \mu\text{mol.L}^{-1}$		11
	MKP	$0.26 \mu\text{mol.L}^{-1}$		11
	CaM	$19 \mu\text{mol.L}^{-1}$		66
	CaN	$1 \mu\text{mol.L}^{-1}$		This paper
	αCaMKII	250 molecules		Estimated from 53

	EP	$1 \mu\text{mol.L}^{-1}$		This paper
	Synaptic AMPAR	~97 molecules		
	Extra-synaptic AMPAR	30 molecules		This paper
	Cytosolic AMPAR	73 molecules		This paper
	GRIP	200 molecules	Number of molecules estimated to sustain the population of AMPAR _{syn} around 100 receptors	This paper
1	$Ca^{2+} + PMCA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PMCA$ $(Ca^{2+})PMCA \xrightarrow{k_{cat}} PMCA$	$k_f = 2500 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 2000 \text{ s}^{-1}$ $k_{cat} = 125 \text{ s}^{-1}$		11

2	$Ca^{2+} + NCX \xrightleftharpoons[k_b]{k_f} (Ca^{2+})NCX$ $(Ca^{2+})NCX \xrightarrow{k_{cat}} NCX$	$k_f = 800 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 100 \text{ s}^{-1}$ $k_{cat} = 2300 \text{ s}^{-1}$		11
3	$Ca^{2+} + SERCA \xrightleftharpoons[k_{b1}]{k_{f1}} (Ca^{2+})SERCA$ $Ca^{2+} + (Ca^{2+})SERCA \xrightleftharpoons[k_{b2}]{k_{f2}} (Ca^{2+})_2SERCA$ $(Ca^{2+})_2SERCA \xrightarrow{k_{cat}} SERCA$	$k_{f1} = k_{f2} =$ $17147 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_{b1} = k_{b2} = 8426.3 \text{ s}^{-1}$ $k_{cat} = 250 \text{ s}^{-1}$		11
4	$\xrightarrow{k_{leak}} Ca^{2+}$	$k_{leak} = 100 \mu\text{mol} \cdot \text{L}^{-1} \cdot \text{s}^{-1}$	Constant zero-order reaction of Ca^{2+} leak to the cytosol to sustain the basal $[Ca^{2+}]$	This paper
5	$Ca^{2+} + PLA_2 \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PLA_2$	$k_f = 11 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 110 \text{ s}^{-1}$	The phosphorylation of PLA_2 did not alter its rate constants for interactions with Ca^{2+}	1,23

6	$Ca^{2+} + (Ca^{2+})PLA_2 \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PLA_2$	$k_f = 1.83 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 110 \text{ s}^{-1}$		1,23
7	$Ca^{2+} + PLA_{2\text{ memb}} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PLA_{2\text{ memb}}$	$k_f = 11 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 2.5 \text{ s}^{-1}$		1,23
8	$Ca^{2+} + (Ca^{2+})PLA_{2\text{ memb}} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PLA_{2\text{ memb}}$	$k_f = 1.83 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.41 \text{ s}^{-1}$		1,23
9	$(Ca^{2+})_2 PLA_2 \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PLA_{2\text{ memb}}$	$k_f = 26 \text{ s}^{-1}$ $k_b = 0.05 \text{ s}^{-1}$		24,25
	$(Ca^{2+})PLA_2 \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PLA_{2\text{ memb}}$	$k_f = 26 \text{ s}^{-1}$ $k_b = 2.5 \text{ s}^{-1}$		This paper
10	$PLA_2 \xrightleftharpoons[k_b]{k_f} PLA_{2\text{ memb}}$	$k_f = 26 \text{ s}^{-1}$ $k_b = 260 \text{ s}^{-1}$		This paper
11	$(Ca^{2+})_2 PLA_{2\text{ memb}} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PLA_{2\text{ memb}}^* \xrightarrow{k_{cat}} (Ca^{2+})_2 PLA_{2\text{ memb}} + AA$	$k_f = 150 \text{ s}^{-1}$ $k_b = 600 \text{ s}^{-1}$ $k_{cat} = 450 \text{ s}^{-1}$	The term * indicates the complex enzyme substrate	11
12	$PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} PLA_{2\text{ memb}}^{P*} \xrightarrow{k_{cat}} PLA_{2\text{ memb}}^P + AA$	$k_f = 150 \text{ s}^{-1}$ $k_b = 600 \text{ s}^{-1}$ $k_{cat} = 900 \text{ s}^{-1}$	The term ^P indicates PLA ₂ in its	2,11,25

			phosphorylated state	
13	$(Ca^{2+})PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PLA_{2\text{ memb}}^{P*} \xrightarrow{k_{cat}} (Ca^{2+})PLA_{2\text{ memb}}^P + AA$	$k_f = 150\text{ s}^{-1}$ $k_b = 600\text{ s}^{-1}$ $k_{cat} = 900\text{ s}^{-1}$		2,11,25
14	$(Ca^{2+})_2 PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PLA_{2\text{ memb}}^{P*} \xrightarrow{k_{cat}} (Ca^{2+})_2 PLA_{2\text{ memb}}^P + AA$	$k_f = 150\text{ s}^{-1}$ $k_b = 600\text{ s}^{-1}$ $k_{cat} = 900\text{ s}^{-1}$		2,11,25
15	$AA \xrightarrow{k_{deg}}$	$k_{deg} = 0.4\text{ s}^{-1}$	Degradation of AA	¹¹
16	$(Ca^{2+})_2 PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PLA_{2\text{ memb}}^P$	$k_f = 260\text{ s}^{-1}$ $k_b = 0.05\text{ s}^{-1}$		24,25
	$PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} PLA_{2\text{ memb}}^P$	$k_f = 260\text{ s}^{-1}$ $k_b = 260\text{ s}^{-1}$		This paper
17	$(Ca^{2+})PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PLA_{2\text{ memb}}^P$	$k_f = 260\text{ s}^{-1}$ $k_b = 2.5\text{ s}^{-1}$		This paper
18	$PP + PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} PP.PLA_{2\text{ memb}}^P \xrightarrow{k_{cat}} PP + PLA_2$	$k_f = 1.4\text{ }\mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 1.5\text{ s}^{-1}$ $k_{cat} = 2.5\text{ s}^{-1}$	PP states for PP2A or PP1	¹¹

19	$PP + (Ca^{2+})_2 PLA_2^P \xrightleftharpoons[k_b]{k_f} PP.(Ca^{2+})_2 PLA_2^P \xrightarrow{k_{cat}} PP + (Ca^{2+})_2 PLA_2$	$k_f = 1.4 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1.5 \text{ s}^{-1}$ $k_{cat} = 2.5 \text{ s}^{-1}$		11
20	$PP + (Ca^{2+})_2 PLA_2^P \xrightleftharpoons[k_b]{k_f} PP.(Ca^{2+})_2 PLA_2^P \xrightarrow{k_{cat}} PP + (Ca^{2+})_2 PLA_2$	$k_f = 1.4 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1.5 \text{ s}^{-1}$ $k_{cat} = 2.5 \text{ s}^{-1}$		11
21	$PP + (Ca^{2+})_2 PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} PP.(Ca^{2+})_2 PLA_{2\text{ memb}}^P \xrightarrow{k_{cat}} PP + (Ca^{2+})_2 PLA_{2\text{ memb}}$	$k_f = 1.4 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1.5 \text{ s}^{-1}$ $k_{cat} = 2.5 \text{ s}^{-1}$		11
22	$PP + (Ca^{2+})_2 PLA_{2\text{ memb}}^P \xrightleftharpoons[k_b]{k_f} PP.(Ca^{2+})_2 PLA_{2\text{ memb}}^P \xrightarrow{k_{cat}} PP + (Ca^{2+})_2 PLA_{2\text{ memb}}$	$k_f = 1.4 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1.5 \text{ s}^{-1}$ $k_{cat} = 2.5 \text{ s}^{-1}$		11
23	$PKC \xrightleftharpoons[k_b]{k_f} PKC_{\text{memb}}$	$k_f = 420 \text{ s}^{-1}$ $k_b = 8400 \text{ s}^{-1}$		28
24	$Ca^{2+} + PKC \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PKC$	$k_f = 1111 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1000 \text{ s}^{-1}$	The same rate constants were used to simulate the interaction between Ca^{2+}	11,29

			and PKC bound to AA	
25	$Ca^{2+} + (Ca^{2+})PKC \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PKC$	$k_f = 45.45 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1000 \text{ s}^{-1}$		11,29
26	$Ca^{2+} + (Ca^{2+})_2 PKC \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_3 PKC$	$k_f = 45.45 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1000 \text{ s}^{-1}$		11,29
27	$Ca^{2+} + PKC_{memb} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PKC_{memb}$	$k_f = 1111 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 12 \text{ s}^{-1}$		11,28,29
28	$Ca^{2+} + (Ca^{2+})PKC_{memb} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PKC_{memb}$	$k_f = 45.45 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 40 \text{ s}^{-1}$		11,28,29
29	$Ca^{2+} + (Ca^{2+})_2 PKC_{memb} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_3 PKC_{memb}$	$k_f = 45.45 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 40 \text{ s}^{-1}$		11,28,29
30	$(Ca^{2+})PKC \xrightleftharpoons[k_b]{k_f} (Ca^{2+})PKC_{memb}$	$k_f = 420 \text{ s}^{-1}$ $k_b = 4200 \text{ s}^{-1}$		11,24
31	$(Ca^{2+})_2 PKC \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_2 PKC_{memb}$	$k_f = 420 \text{ s}^{-1}$ $k_b = 0.017 \text{ s}^{-1}$		11,24
32	$(Ca^{2+})_3 PKC \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_3 PKC_{memb}$	$k_f = 420 \text{ s}^{-1}$ $k_b = 0.0017 \text{ s}^{-1}$		11,24
33	$AA + PKC \xrightleftharpoons[k_b]{k_f} AA.PKC$	$k_f = 1 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 10 \text{ s}^{-1}$	These rates were kept unchanged	11

			for the interactions between AA and PKC bound to Ca ²⁺ and/or membrane	
34	$AA.PKC \xrightleftharpoons[k_b]{k_f} AA.PKC_{memb}$	$k_f = 420 \text{ s}^{-1}$ $k_b = 420 \text{ s}^{-1}$		This paper
35	$AA.(Ca^{2+})PKC \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})PKC_{memb}$	$k_f = 420 \text{ s}^{-1}$ $k_b = 42 \text{ s}^{-1}$		This paper
36	$AA.(Ca^{2+})_2 PKC \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_2 PKC_{memb}$	$k_f = 420 \text{ s}^{-1}$ $k_b = 0.00017 \text{ s}^{-1}$		This paper
37	$AA.(Ca^{2+})_3 PKC \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_3 PKC_{memb}$	$k_f = 420 \text{ s}^{-1}$ $k_b = 0.000017 \text{ s}^{-1}$		This paper
38	$RKIP + Raf \xrightleftharpoons[k_b]{k_f} RKIP.Raf$ $RKIP + Raf^P \xrightleftharpoons[k_b]{k_f} RKIP.Raf^P$	$k_f = 1 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1 \text{ s}^{-1}$		31
39	$AA.(Ca^{2+})_3 PKC_{memb} + RKIP \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_3 PKC_{memb} \cdot RKIP$ $AA.(Ca^{2+})_3 PKC_{memb} \cdot RKIP \xrightarrow{k_{cat}} AA.(Ca^{2+})_3 PKC_{memb} + RKIP^P$	$k_f = 2.632 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 30 \text{ s}^{-1}$ $k_{cat} = 120 \text{ s}^{-1}$		Estimated

				from 32
40	$AA.(Ca^{2+})_2 PKC_{memb} + RKIP \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_2 PKC_{memb} \cdot RKIP$ $AA.(Ca^{2+})_2 PKC_{memb} \cdot RKIP \xrightarrow{k_{cat}} AA.(Ca^{2+})_2 PKC_{memb} + RKIP^P$	$k_f = 2.632 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 30 \text{ s}^{-1}$ $k_{cat} = 120 \text{ s}^{-1}$		Estim ated from 32
41	$AA.(Ca^{2+}) PKC_{memb} + RKIP \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+}) PKC_{memb} \cdot RKIP$ $AA.(Ca^{2+}) PKC_{memb} \cdot RKIP \xrightarrow{k_{cat}} AA.(Ca^{2+}) PKC_{memb} + RKIP^P$	$k_f = 2.632 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 30 \text{ s}^{-1}$ $k_{cat} = 120 \text{ s}^{-1}$		Estim ated from 32
42	$AA.PKC_{memb} + RKIP \xrightleftharpoons[k_b]{k_f} AA.PKC_{memb} \cdot RKIP$ $AA.PKC_{memb} \cdot RKIP \xrightarrow{k_{cat}} AA.PKC_{memb} + RKIP^P$	$k_f = 2.632 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 30 \text{ s}^{-1}$ $k_{cat} = 120 \text{ s}^{-1}$		Estim ated from 32
43	$(Ca^{2+})_3 PKC_{memb} + RKIP \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_3 PKC_{memb} \cdot RKIP$ $(Ca^{2+})_3 PKC_{memb} \cdot RKIP \xrightarrow{k_{cat}} (Ca^{2+})_3 PKC_{memb} + RKIP^P$	$k_f = 2.632 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ 1 $k_b = 30 \text{ s}^{-1}$ $k_{cat} = 120 \text{ s}^{-1}$		Estim ated from 32
44	$RKIP^P \xrightarrow{k_{dephos}} RKIP$	$k_{dephos} = 30 \text{ s}^{-1}$		33

45	$RKIP^P + Raf \xrightleftharpoons[k_b]{k_f} RKIP^P.Raf$ $RKIP^P + Raf^P \xrightleftharpoons[k_b]{k_f} RKIP^P.Raf^P$	$k_f = 1 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 100 \text{ s}^{-1}$		This paper, estimated from 31
46	$AA.(Ca^{2+})_3 PKC_{memb} + Raf - act \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_3 PKC_{memb}.Raf - act$ $AA.(Ca^{2+})_3 PKC_{memb}.Raf - act \xrightarrow{k_{cat}} AA.(Ca^{2+})_3 PKC_{memb} + Raf - act^P$	$k_f = 5.8 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.56 \text{ s}^{-1}$ $k_{cat} = 0.14 \text{ s}^{-1}$		11
47	$AA.(Ca^{2+})_2 PKC_{memb} + Raf - act \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_2 PKC_{memb}.Raf - act$ $AA.(Ca^{2+})_2 PKC_{memb}.Raf - act \xrightarrow{k_{cat}} AA.(Ca^{2+})_2 PKC_{memb} + Raf - act^P$	$k_f = 5.8 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 3.608 \text{ s}^{-1}$ $k_{cat} = 4.7 \text{ s}^{-1}$		11
48	$AA.(Ca^{2+}) PKC_{memb} + Raf - act \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+}) PKC_{memb}.Raf - act$ $AA.(Ca^{2+}) PKC_{memb}.Raf - act \xrightarrow{k_{cat}} AA.(Ca^{2+}) PKC_{memb} + Raf - act^P$	$k_f = 5.8 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 3.608 \text{ s}^{-1}$ $k_{cat} = 4.7 \text{ s}^{-1}$		11
49	$AA.PKC_{memb} + Raf - act \xrightleftharpoons[k_b]{k_f} AA.PKC_{memb}.Raf - act$ $AA.PKC_{memb}.Raf - act \xrightarrow{k_{cat}} AA.PKC_{memb} + Raf - act^P$	$k_f = 5.8 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 3.608 \text{ s}^{-1}$ $k_{cat} = 4.7 \text{ s}^{-1}$		11

50	$\begin{aligned} (Ca^{2+})_3 PKC_{memb} + Raf - act &\xrightleftharpoons[k_b]{k_f} (Ca^{2+})_3 PKC_{memb}.Raf - act \\ (Ca^{2+})_3 PKC_{memb}.Raf - act &\xrightarrow{k_{cat}} (Ca^{2+})_3 PKC_{memb} + Raf - act^P \end{aligned}$	$k_f = 5.8 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 3.608 \text{ s}^{-1}$ $k_{cat} = 4.7 \text{ s}^{-1}$		11
51	$Raf - act^P \xrightarrow{k_{dephos}} Raf - act$	$k_{dephos} = 1 \text{ s}^{-1}$		11
52	$\begin{aligned} Raf - act + Raf &\xrightleftharpoons[k_b]{k_f} Raf - act.Raf \\ Raf - act.Raf &\xrightarrow{k_{cat}} Raf - act + Raf^P \end{aligned}$	$k_f = 1 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 2 \text{ s}^{-1}$ $k_{cat} = 1.5 \text{ s}^{-1}$		11
53	$\begin{aligned} PP5 + Raf^P &\xrightleftharpoons[k_b]{k_f} PP5.Raf^P \\ PP5.Raf^P &\xrightarrow{k_{cat}} PP5 + Raf \end{aligned}$	$k_f = 0.55 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 2 \text{ s}^{-1}$ $k_{cat} = 0.5 \text{ s}^{-1}$		11
54	$\begin{aligned} Raf^P + MEK &\xrightleftharpoons[k_b]{k_f} Raf^P.MEK \\ Raf^P.MEK &\xrightarrow{k_{cat}} Raf^P + MEK^P \\ Raf^P + MEK^P &\xrightleftharpoons[k_b]{k_f} Raf^P.MEK^P \\ Raf^P.MEK^P &\xrightarrow{k_{cat}} Raf^P + MEK^{PP} \end{aligned}$	$k_f = 0.65 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.065 \text{ s}^{-1}$ $k_{cat} = 1 \text{ s}^{-1}$	The term ^P and ^{PP} indicate phosphorylated and double phosphorylated state, respectively	11

55	$PP2A + MEK^{PP} \xrightleftharpoons[k_b]{k_f} PP2A.MEK^{PP}$ $PP2A.MEK^{PP} \xrightarrow{k_{cat}} PP2A + MEK^P$ $PP2A + MEK^P \xrightleftharpoons[k_b]{k_f} PP2A.MEK^P$ $PP2A.MEK^P \xrightarrow{k_{cat}} PP2A + MEK$	$k_f = 0.75 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 2 \text{ s}^{-1}$ $k_{cat} = 0.5 \text{ s}^{-1}$		11
56	$MEK^{PP} + ERK \xrightleftharpoons[k_b]{k_f} MEK^{PP}.ERK$ $MEK^{PP}.ERK \xrightarrow{k_{cat}} MEK^{PP} + ERK^P$	$k_f = 16.2 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.6 \text{ s}^{-1}$ $k_{cat} = 0.15 \text{ s}^{-1}$		11
57	$MEK^{PP} + ERK^P \xrightleftharpoons[k_b]{k_f} MEK^{PP}.ERK^P$ $MEK^{PP}.ERK^P \xrightarrow{k_{cat}} MEK^{PP} + ERK^{PP}$	$k_f = 16.2 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.6 \text{ s}^{-1}$ $k_{cat} = 0.3 \text{ s}^{-1}$		11
58	$MKP + ERK^{PP} \xrightleftharpoons[k_b]{k_f} MKP.ERK^{PP}$ $MKP.ERK^{PP} \xrightarrow{k_{cat}} MKP + ERK^P$	$k_f = 13 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.396 \text{ s}^{-1}$ $k_{cat} = 0.099 \text{ s}^{-1}$		11
59	$MKP + ERK^P \xrightleftharpoons[k_b]{k_f} MKP.ERK^P$ $MKP.ERK^P \xrightarrow{k_{cat}} MKP + ERK$	$k_f = 28 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.56 \text{ s}^{-1}$ $k_{cat} = 0.14 \text{ s}^{-1}$		11
60	$ERK^{PP} + PLA_2 \xrightleftharpoons[k_b]{k_f} ERK^{PP}.PLA_2$ $ERK^{PP}.PLA_2 \xrightarrow{k_{cat}} ERK^{PP} + PLA_2^P$	$k_f = 15.6 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 56 \text{ s}^{-1}$ $k_{cat} = 100 \text{ s}^{-1}$		Estimated

				from 36
61	$ERK^{PP} + (Ca^{2+})PLA_2 \xrightleftharpoons[k_b]{k_f} ERK^{PP} \cdot (Ca^{2+})PLA_2$ $ERK^{PP} \cdot (Ca^{2+})PLA_2 \xrightarrow{k_{cat}} ERK^{PP} + (Ca^{2+})PLA_2^P$	$k_f = 15.6 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 56 \text{ s}^{-1}$ $k_{cat} = 100 \text{ s}^{-1}$		Estim ated from 36
62	$ERK^{PP} + (Ca^{2+})_2 PLA_2 \xrightleftharpoons[k_b]{k_f} ERK^{PP} \cdot (Ca^{2+})_2 PLA_2$ $ERK^{PP} \cdot (Ca^{2+})_2 PLA_2 \xrightarrow{k_{cat}} ERK^{PP} + (Ca^{2+})_2 PLA_2^P$	$k_f = 15.6 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 56 \text{ s}^{-1}$ $k_{cat} = 100 \text{ s}^{-1}$		Estim ated from 36
63	$ERK^{PP} + (Ca^{2+})PLA_{2\text{ memb}} \xrightleftharpoons[k_b]{k_f} ERK^{PP} \cdot (Ca^{2+})PLA_{2\text{ memb}}$ $ERK^{PP} \cdot (Ca^{2+})PLA_{2\text{ memb}} \xrightarrow{k_{cat}} ERK^{PP} + (Ca^{2+})PLA_{2\text{ memb}}^P$	$k_f = 15.6 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 56 \text{ s}^{-1}$ $k_{cat} = 100 \text{ s}^{-1}$		Estim ated from 36
64	$ERK^{PP} + (Ca^{2+})_2 PLA_{2\text{ memb}} \xrightleftharpoons[k_b]{k_f} ERK^{PP} \cdot (Ca^{2+})_2 PLA_{2\text{ memb}}$ $ERK^{PP} \cdot (Ca^{2+})_2 PLA_{2\text{ memb}} \xrightarrow{k_{cat}} ERK^{PP} + (Ca^{2+})_2 PLA_{2\text{ memb}}^P$	$k_f = 15.6 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 56 \text{ s}^{-1}$ $k_{cat} = 100 \text{ s}^{-1}$		Estim ated from 36
65	$Ca^{2+} + CaM_{I,II} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_I \cdot CaM_{II}$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 50000 \text{ s}^{-1}$	In the notation	9

			<p>$(Ca^{2+})_x CaM_y$, the terms x and y indicate the Ca^{2+}-binding sites filled with Ca^{2+} and empty, respectively. Sites that were not declared explicitly did not interfere with the reactions described.</p>	
66	$Ca^{2+} + CaM_{I,II} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{II} \cdot CaM_I$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 50000 \text{ s}^{-1}$		9
67	$Ca^{2+} + (Ca^{2+})_I \cdot CaM_{II} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{I,II} \cdot CaM$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 625 \text{ s}^{-1}$		9
68	$Ca^{2+} + (Ca^{2+})_{II} \cdot CaM_I \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{I,II} \cdot CaM$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 625 \text{ s}^{-1}$		9

69	$Ca^{2+} + CaM_{III,IV} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III}.CaM_{IV}$	$k_f = 800 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 20000 \text{ s}^{-1}$		9
70	$Ca^{2+} + CaM_{III,IV} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{IV}.CaM_{III}$	$k_f = 204 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 5115 \text{ s}^{-1}$		9
71	$Ca^{2+} + (Ca^{2+})_{III}.CaM_{IV} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III,IV}.CaM$	$k_f = 204 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 25.575 \text{ s}^{-1}$		9
72	$Ca^{2+} + (Ca^{2+})_{IV}.CaM_{III} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III,IV}.CaM$	$k_f = 800 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 100 \text{ s}^{-1}$		9
73	$Ca^{2+} + CNB_{I,II} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_I.CNB_{II}$	$k_f = 6.4 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.03 \text{ s}^{-1}$	The terms I, II, III and IV denote the Ca^{2+} -binding sites of CNB. In the notation $(Ca^{2+})_x CNB_y$, the terms x and y indicate the Ca^{2+} -binding sites filled with Ca^{2+} and empty, respectively.	38,40

			Sites that are not declared explicitly did not interfere with the reactions described.	
74	$Ca^{2+} + (Ca^{2+})_I.CNB_{II} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{I,II}.CNB$	$k_f = 6.4 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.0018 \text{ s}^{-1}$		38,40
75	$Ca^{2+} + CNB_{III,IV} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III}.CNB_{IV}$	$k_f = 0.09 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.05 \text{ s}^{-1}$		38,40
76	$Ca^{2+} + (Ca^{2+})_{III}.CNB_{IV} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III,IV}.CNB$	$k_f = 0.09 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.025 \text{ s}^{-1}$		38,40
77	$CNA + (Ca^{2+})_{N,C}.CaM \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{N,C}.CaM.CNA$	$k_f = 46 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.0012 \text{ s}^{-1}$	The term $(Ca^{2+})_{N,C}.CaM$ indicates that both the C and the N-terminal domains of CaM are associated with Ca^{2+} .	42

78	$CNA + (Ca^{2+})_C \cdot CaM \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_C \cdot CaM \cdot CNA$	$k_f = 46 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 46 \text{ s}^{-1}$	The term $(Ca^{2+})_C \cdot CaM$ indicates that only the C-terminal domain of CaM is associated with Ca^{2+} .	41,42
79	$CNA + (Ca^{2+})_N \cdot CaM \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_N \cdot CaM \cdot CNA$	$k_f = 46 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 322 \text{ s}^{-1}$	The term $(Ca^{2+})_N \cdot CaM$ indicates that only the N-terminal domain of CaM is associated with Ca^{2+} .	41,42
80	$Ca^{2+} + CaM_{I,II} \cdot CNA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_I \cdot CaM_{II} \cdot CNA$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 950 \text{ s}^{-1}$		9,41
81	$Ca^{2+} + CaM_{I,II} \cdot CNA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{II} \cdot CaM_I \cdot CNA$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 950 \text{ s}^{-1}$		9,41

82	$Ca^{2+} + (Ca^{2+})_I \cdot CaM_{II} \cdot CNA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{I,II} \cdot CaM \cdot CNA$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 11.9 \text{ s}^{-1}$		9,41
83	$Ca^{2+} + (Ca^{2+})_{II} \cdot CaM_I \cdot CNA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{I,II} \cdot CaM \cdot CNA$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 11.9 \text{ s}^{-1}$		9,41
84	$Ca^{2+} + CaM_{III,IV} \cdot CNA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III} \cdot CaM_{IV} \cdot CNA$	$k_f = 800 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 160 \text{ s}^{-1}$		9,41
85	$Ca^{2+} + CaM_{III,IV} \cdot CNA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{IV} \cdot CaM_{III} \cdot CNA$	$k_f = 204 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 48 \text{ s}^{-1}$		9,41
86	$Ca^{2+} + (Ca^{2+})_{III} \cdot CaM_{IV} \cdot CNA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III,IV} \cdot CaM \cdot CNA$	$k_f = 204 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.24 \text{ s}^{-1}$		9,41
87	$Ca^{2+} + (Ca^{2+})_{IV} \cdot CaM_{III} \cdot CNA \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III,IV} \cdot CaM \cdot CNA$	$k_f = 800 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$		9,41
88	$\alpha\text{CaMKII} + (Ca^{2+})_{N,C} \cdot CaM \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{N,C} \cdot CaM \cdot \alpha\text{CaMKII}$	$k_f = 20 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 20 \text{ s}^{-1}$	The k_b was estimated in this paper. The term $(Ca^{2+})_{N,C} \cdot CaM$ indicates that both the C and the N-terminal domains of CaM	7,8

			are bound to Ca^{2+} .	
89	$(\text{Ca}^{2+})_x \cdot \text{CaM} \cdot \alpha\text{CaMKII} + (\text{Ca}^{2+})_{N,C} \cdot \text{CaM} \xrightleftharpoons[k_b]{k_f} (\text{Ca}^{2+})_{N,C} \cdot \text{CaM} \cdot (\text{Ca}^{2+})_x \cdot \text{CaM} \cdot \alpha\text{CaMKII}$	$k_f = 20 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 18 \text{ s}^{-1}$	The k_b was estimated in this paper.	7,8
90	$\alpha\text{CaMKII} + (\text{Ca}^{2+})_C \cdot \text{CaM} \xrightleftharpoons[k_b]{k_f} (\text{Ca}^{2+})_C \cdot \text{CaM} \cdot \alpha\text{CaMKII}$	$k_f = 20 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 5000 \text{ s}^{-1}$	The term $\text{Ca}^{2+})_C \cdot \text{CaM}$ indicates that only the C-terminal domain of CaM is associated to Ca^{2+} .	7,8,46,47
91	$(\text{Ca}^{2+})_x \cdot \text{CaM} \cdot \alpha\text{CaMKII} + (\text{Ca}^{2+})_C \cdot \text{CaM} \xrightleftharpoons[k_b]{k_f} (\text{Ca}^{2+})_C \cdot \text{CaM} \cdot (\text{Ca}^{2+})_x \cdot \text{CaM} \cdot \alpha\text{CaMKII}$	$k_f = 20 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 4500 \text{ s}^{-1}$	The k_b was estimated in this paper.	7,8,46,47
92	$\text{Ca}^{2+} + \text{CaM}_{I,II} \cdot \alpha\text{CaMKII} \xrightleftharpoons[k_b]{k_f} (\text{Ca}^{2+})_I \cdot \text{CaM}_{II} \cdot \alpha\text{CaMKII}$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 500 \text{ s}^{-1}$		9,44,47
93	$\text{Ca}^{2+} + \text{CaM}_{I,II} \cdot \alpha\text{CaMKII} \xrightleftharpoons[k_b]{k_f} (\text{Ca}^{2+})_{II} \cdot \text{CaM}_I \cdot \alpha\text{CaMKII}$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 500 \text{ s}^{-1}$		9,44,47

94	$Ca^{2+} + (Ca^{2+})_I \cdot CaM_{II} \cdot \alpha CaMKII \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{I,II} \cdot CaM \cdot \alpha CaMKII$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 6.25 \text{ s}^{-1}$		9,44,47
95	$Ca^{2+} + (Ca^{2+})_{II} \cdot CaM_I \cdot \alpha CaMKII \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{I,II} \cdot CaM \cdot \alpha CaMKII$	$k_f = 750 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 6.25 \text{ s}^{-1}$		9,44,47
96	$Ca^{2+} + CaM_{III,IV} \cdot \alpha CaMKII \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III} \cdot CaM_{IV} \cdot \alpha CaMKII$	$k_f = 800 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1000 \text{ s}^{-1}$		9,44,47
97	$Ca^{2+} + CaM_{III,IV} \cdot \alpha CaMKII \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{IV} \cdot CaM_{III} \cdot \alpha CaMKII$	$k_f = 204 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 255.75 \text{ s}^{-1}$		9,44,47
98	$Ca^{2+} + (Ca^{2+})_{III} \cdot CaM_{IV} \cdot \alpha CaMKII \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III,IV} \cdot CaM \cdot \alpha CaMKII$	$k_f = 204 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 1.2788 \text{ s}^{-1}$		9,44,47
99	$Ca^{2+} + (Ca^{2+})_{IV} \cdot CaM_{III} \cdot \alpha CaMKII \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{III,IV} \cdot CaM \cdot \alpha CaMKII$	$k_f = 800 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 5 \text{ s}^{-1}$		9,44,47
100	$\left[(Ca^{2+})_{I,II,III,IV} \cdot CaM \right]_2 \cdot \alpha CaMKII \xrightarrow{k_{cat}} \left[(Ca^{2+})_{I,II,III,IV} \cdot CaM \right]_2 \cdot \alpha CaMKII^P$	$k_{cat} = 5 \text{ s}^{-1}$	Autophosphorylation of CaMKII. ^P indicates phosphorylated state.	51
101	$\alpha CaMKII^P + (Ca^{2+})_{N,C} \cdot CaM \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{N,C} \cdot CaM \cdot \alpha CaMKII^P$	$k_f = 20 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.02 \text{ s}^{-1}$		7,8,52

102	$(Ca^{2+})_x \cdot CaM \cdot \alpha CaMKII^P + (Ca^{2+})_{N,C} \cdot CaM \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{N,C} \cdot CaM \cdot (Ca^{2+})_x \cdot CaM \cdot \alpha CaMKII^P$	$k_f = 20 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.018 \text{ s}^{-1}$		7,8,52
103	$\alpha CaMKII^P + (Ca^{2+})_C \cdot CaM \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_C \cdot CaM \cdot \alpha CaMKII^P$	$k_f = 20 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 5 \text{ s}^{-1}$		7,8,46,47 ,52
104	$(Ca^{2+})_x \cdot CaM \cdot \alpha CaMKII^P + (Ca^{2+})_C \cdot CaM \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_C \cdot CaM \cdot (Ca^{2+})_x \cdot CaM \cdot \alpha CaMKII^P$	$k_f = 20 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 4.5 \text{ s}^{-1}$		7,8,46,47 ,52
105	$PP + \alpha CaMKII^P \xrightleftharpoons[k_b]{k_f} PP \cdot \alpha CaMKII^P \xrightarrow{k_{cat}} PP + \alpha CaMKII$	$k_f = 6.4 \text{ s}^{-1}$ $k_b = 56 \text{ s}^{-1}$ $k_{cat} = 14 \text{ s}^{-1}$	PP states for PP1 or PP2A	55,56
106	$\left[(Ca^{2+})_{I,II,III,IV} \cdot CaM \right]_2 \cdot \alpha CaMKII^P + Raf \xrightleftharpoons[k_b]{k_f} \left[(Ca^{2+})_{I,II,III,IV} \cdot CaM \right]_2 \cdot \alpha CaMKII^P \cdot Raf \xrightarrow{k_{cat}} \left[(Ca^{2+})_{I,II,III,IV} \cdot CaM \right]_2 \cdot \alpha CaMKII^P + Raf^P$	$k_f = 20 \text{ s}^{-1}$ $k_b = 50 \text{ s}^{-1}$ $k_{cat} = 150 \text{ s}^{-1}$		This paper
107	$\left[(Ca^{2+})_x \cdot CaM \right]_y \cdot \alpha CaMKII^P + Raf \xrightleftharpoons[k_b]{k_f} \left[(Ca^{2+})_x \cdot CaM \right]_y \cdot \alpha CaMKII^P \cdot Raf \xrightarrow{k_{cat}} \left[(Ca^{2+})_x \cdot CaM \right]_y \cdot \alpha CaMKII^P + Raf^P$	$k_f = 20 \text{ s}^{-1}$ $k_b = 50 \text{ s}^{-1}$ $k_{cat} = 30 \text{ s}^{-1}$		This paper
108	$\alpha CaMKII^P + Raf \xrightleftharpoons[k_b]{k_f} \alpha CaMKII^P \cdot Raf \xrightarrow{k_{cat}} \alpha CaMKII^P + Raf^P$	$k_f = 20 \text{ s}^{-1}$ $k_b = 50 \text{ s}^{-1}$		This paper

		$k_{cat} = 30 \text{ s}^{-1}$		
109	$AMPAR_{syn} \xrightleftharpoons[k_b]{k_f} AMPAR_{extra}$	$k_f = 0.05 \text{ s}^{-1}$ $k_b = 0.065 \text{ s}^{-1}$		11,59,60
110	$AMPAR_{syn}^P \xrightleftharpoons[k_b]{k_f} AMPAR_{extra}^P$	$k_f = 0.05 \text{ s}^{-1}$ $k_b = 0.065 \text{ s}^{-1}$		11,59,60
111	$EP^P + AMPAR_{extra} \xrightleftharpoons[k_b]{k_f} EP^P \cdot AMPAR_{extra} \xrightarrow{k_{cat}} EP^P + AMPAR_{endo}$	$k_f = 0.03 \text{ s}^{-1}$ $k_b = 0.02 \text{ s}^{-1}$ $k_{cat} = 1 \text{ s}^{-1}$		This paper
112	$EP^P + AMPAR_{extra}^P \xrightleftharpoons[k_b]{k_f} EP^P \cdot AMPAR_{extra}^P \xrightarrow{k_{cat}} EP^P + AMPAR_{endo}^P$	$k_f = 0.12 \text{ s}^{-1}$ $k_b = 0.02 \text{ s}^{-1}$ $k_{cat} = 1 \text{ s}^{-1}$		This paper
113	$AMPAR_{endo} \xrightarrow{k_{exo}} AMPAR_{extra}$	$k_{exo} = 0.005 \text{ s}^{-1}$		This paper
114	$GRIP + AMPAR_{syn} \xrightleftharpoons[k_b]{k_f} GRIP \cdot AMPAR_{syn}$	$k_f = 0.5 \text{ s}^{-1}$ $k_b = 0.5 \text{ s}^{-1}$		11,60
115	$GRIP + AMPAR_{syn}^P \xrightleftharpoons[k_b]{k_f} GRIP \cdot AMPAR_{syn}^P$	$k_f = 0.5 \text{ s}^{-1}$ $k_b = 3.5 \text{ s}^{-1}$		11,60
116	$AA.(Ca^{2+})_3 PKC_{memb} + AMPAR_{syn} \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_3 PKC_{memb} \cdot AMPAR_{syn}$ $AA.(Ca^{2+})_3 PKC_{memb} \cdot AMPAR_{syn} \xrightarrow{k_{cat}} AA.(Ca^{2+})_3 PKC_{memb} + AMPAR_{syn}^P$	$k_f = 0.8 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 5 \text{ s}^{-1}$		This paper

117	$AA.(Ca^{2+})_2 PKC_{memb} + AMPAR_{syn} \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_2 PKC_{memb} \cdot AMPAR_{syn}$ $AA.(Ca^{2+})_2 PKC_{memb} \cdot AMPAR_{syn} \xrightarrow{k_{cat}} AA.(Ca^{2+})_2 PKC_{memb} + AMPAR_{syn}^P$	$k_f = 0.8 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 5 \text{ s}^{-1}$		This paper
118	$AA.(Ca^{2+}) PKC_{memb} + AMPAR_{syn} \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+}) PKC_{memb} \cdot AMPAR_{syn}$ $AA.(Ca^{2+}) PKC_{memb} \cdot AMPAR_{syn} \xrightarrow{k_{cat}} AA.(Ca^{2+}) PKC_{memb} + AMPAR_{syn}^P$	$k_f = 0.8 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 5 \text{ s}^{-1}$		This paper
119	$AA.PKC_{memb} + AMPAR_{syn} \xrightleftharpoons[k_b]{k_f} AA.PKC_{memb} \cdot AMPAR_{syn}$ $AA.PKC_{memb} \cdot AMPAR_{syn} \xrightarrow{k_{cat}} AA.PKC_{memb} + AMPAR_{syn}^P$	$k_f = 0.8 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 5 \text{ s}^{-1}$		This paper
120	$(Ca^{2+})_3 PKC_{memb} + AMPAR_{syn} \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_3 PKC_{memb} \cdot AMPAR_{syn}$ $(Ca^{2+})_3 PKC_{memb} \cdot AMPAR_{syn} \xrightarrow{k_{cat}} (Ca^{2+})_3 PKC_{memb} + AMPAR_{syn}^P$	$k_f = 0.8 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 5 \text{ s}^{-1}$		This paper
121	$PP2A + AMPAR_{syn}^P \xrightleftharpoons[k_b]{k_f} PP2A \cdot AMPAR_{syn}^P \xrightarrow{k_{cat}} PP2A + AMPAR_{syn}$	$k_f = 0.08 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 2 \text{ s}^{-1}$		This paper
122	$PP2A + AMPAR_{extra}^P \xrightleftharpoons[k_b]{k_f} PP2A \cdot AMPAR_{extra}^P \xrightarrow{k_{cat}} PP2A + AMPAR_{extra}$	$k_f = 0.08 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 2 \text{ s}^{-1}$		This paper
123	$PP2A + AMPAR_{endo}^P \xrightleftharpoons[k_b]{k_f} PP2A \cdot AMPAR_{endo}^P \xrightarrow{k_{cat}} PP2A + AMPAR_{endo}$	$k_f = 0.08 \mu\text{mol}^{-1} \cdot \text{L} \cdot \text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$		This paper

		$k_{cat} = 2 \text{ s}^{-1}$		
124	$AA.(Ca^{2+})_3 PKC_{memb} + EP \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_3 PKC_{memb}.EP$ $AA.(Ca^{2+})_3 PKC_{memb}.EP \xrightarrow{k_{cat}} AA.(Ca^{2+})_3 PKC_{memb} + EP^P$	$k_f = 0.2 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 0.2 \text{ s}^{-1}$	The term ^P indicates phosphorylated state.	This paper
125	$AA.(Ca^{2+})_2 PKC_{memb} + EP \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+})_2 PKC_{memb}.EP$ $AA.(Ca^{2+})_2 PKC_{memb}.EP \xrightarrow{k_{cat}} AA.(Ca^{2+})_2 PKC_{memb} + EP^P$	$k_f = 0.2 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 0.2 \text{ s}^{-1}$		This paper
126	$AA.(Ca^{2+}) PKC_{memb} + EP \xrightleftharpoons[k_b]{k_f} AA.(Ca^{2+}) PKC_{memb}.EP$ $AA.(Ca^{2+}) PKC_{memb}.EP \xrightarrow{k_{cat}} AA.(Ca^{2+}) PKC_{memb} + EP^P$	$k_f = 0.2 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 0.2 \text{ s}^{-1}$		This paper
127	$AA.PKC_{memb} + EP \xrightleftharpoons[k_b]{k_f} AA.PKC_{memb}.EP$ $AA.PKC_{memb}.EP \xrightarrow{k_{cat}} AA.PKC_{memb} + EP^P$	$k_f = 0.2 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 0.2 \text{ s}^{-1}$		This paper
128	$(Ca^{2+})_3 PKC_{memb} + EP \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_3 PKC_{memb}.EP$ $(Ca^{2+})_3 PKC_{memb}.EP \xrightarrow{k_{cat}} (Ca^{2+})_3 PKC_{memb} + EP^P$	$k_f = 0.2 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 0.8 \text{ s}^{-1}$ $k_{cat} = 0.2 \text{ s}^{-1}$		This paper
129	$(Ca^{2+})_{N,C}.CaM.CNA + EP^P \xrightleftharpoons[k_b]{k_f} (Ca^{2+})_{N,C}.CaM.CNA.EP^P$ $(Ca^{2+})_{N,C}.CaM.CNA.EP^P \xrightarrow{k_{cat}} (Ca^{2+})_{N,C}.CaM.CNA + EP$	$k_f = 20 \mu\text{mol}^{-1}.\text{L}.\text{s}^{-1}$ $k_b = 50 \text{ s}^{-1}$ $k_{cat} = 170 \text{ s}^{-1}$	Dephosphorylation of EP catalyzed by	This paper

			CaN bound to four Ca ²⁺ and CaM fully saturated	
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