## **Supplementary Information**

## An improved approach for measuring immersion freezing in large droplets over a wide temperature range

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Supplementary Figure S1. Fraction of droplets frozen as a function of temperature for pure water droplets of different volumes. These values are obtained using a classical nucleation theory-based parameterization for homogeneous freezing with a cooling rate of 1°C/min (ref. 32).



Supplementary Figure S2. Size dependence of the settling distances of Snomax or illite NX particles in water at temperatures of 0°C and -34°C. The settling distances after 1, 30 and 60 minutes are estimated based on the terminal setting velocities of the particles (see Supplementary Methods).

## **Supplementary Methods**

According to Stokes' law, the terminal settling velocity (v) of small spherical particles in water is expressed as:

$$v = \frac{(\rho_{\rm p} - \rho_{\rm w}) \cdot g}{18\eta_{\rm w}} \cdot D_{\rm p}^{2}$$
(S1)

where  $\eta_w$  is the viscosity of water,  $\rho_w$  is the density of water,  $\rho_p$  is the density of particles,  $D_p$  is the particle diameter, and g is the gravitational acceleration (= 9.80665 m/s<sup>2</sup>). In the calculations, it is assumed that the  $\eta_w$  and  $\rho_w$  values are temperature dependent parameters in the temperature range between -34°C and 0°C (refs 37 and 38) and that the  $\rho_p$  values of Snomax and illite NX particles are ~1.35 g/cm<sup>3</sup> and ~2.65 g/cm<sup>3</sup>, respectively<sup>29,30</sup>. The settling distances of Snomax and illite NX particles in water at 0°C and -34°C are then estimated using the v values. Supplementary Figure S2 illustrates the settling distances after t minutes (t = 1, 30 and 60). Given that the diameters of Snomax and illite NX particles used here are mainly distributed between about 0.1 and 1  $\mu$ m (refs 29 and 30), it is expected that the majority of them are suspended in 5  $\mu$ L water droplets (a few micrometers in diameter) even at the end of each freezing experiment (i.e., the settling distances of the particles are shorter than the diameter of the droplets).

## References

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