

## Supporting Information

### S3 Table

Empirical Type 1 Error of MQLS-LIN, MQLS-LOG, CERAMIC and GEMMA, with Partially Missing Data.

Setting of ( $\pi_a, \pi_c$ )	MQLS-LIN	MQLS-LOG	CERAMIC	GEMMA with genotype imputation	GEMMA without genotype imputation
(0, .8)	.048	.049	.049	<b>.059</b>	<b>.032</b>
(.2, .6)	.050	.050	.050	<b>.062</b>	<b>.035</b>
(.4, .4)	.051	.051	.050	<b>.063</b>	<b>.032</b>
(.6, .2)	.050	.050	.051	<b>.063</b>	<b>.030</b>
(.8, 0)	.049	.049	.050	<b>.055</b>	<b>.032</b>

All tests adjust for covariates. Traits are generated by the liability threshold model, where  $\pi_a$  is the proportion of total liability variance that is due to polygenic effects and  $\pi_c$  is the proportion due to covariate effects. Ascertainment setting A is used. The number of individuals sampled in each simulation replicate is 1200. Association is tested at a non-causal SNP, which has MAF .2, and type 1 error is assessed empirically at significance level .05. Empirical type 1 error is based on 25,000 replicates. The radius of the 95% confidence interval is .0027. Bold indicates a type 1 error rate that is outside the 95% confidence interval.