

Arbitrary-Region Raster Image Correlation **Spectroscopy**

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ABSTRACT Combining imaging with correlation spectroscopy, as in raster image correlation spectroscopy (RICS), makes it possible to extract molecular translational diffusion constants and absolute concentrations, and determine intermolecular interactions from single-channel or multicolor confocal laser-scanning microscopy (CLSM) images. Region-specific RICS analysis remains very challenging because correlations are always calculated in a square region-of-interest (ROI). In this study, we describe a generalized image correlation spectroscopy algorithm that accepts arbitrarily shaped ROIs. We show that an image series can be cleaned up before arbitrary-region RICS (ARICS) analysis. We demonstrate the power of ARICS by simultaneously measuring molecular mobility in the cell membrane and the cytosol. Mobility near dynamic subcellular structures can be investigated with ARICS by generating a dynamic ROI. Finally, we derive diffusion and concentration pseudo-maps using the ARICS method. ARICS is a powerful expansion of image correlation spectroscopy with the potential of becoming the new standard for extracting biophysical parameters from confocal fluorescence images.

INTRODUCTION

Fluorescence fluctuation spectroscopy (FFS) methods probe molecular parameters of diffusive fluorescent substances, classically by analyzing the temporal correlation function of fluorescence signals $(1-3)$. FFS methods have seen a tremendous increase in popularity since the 1990s with the improvement and commercialization of confocal microscopes, which brought correlation analyses from the physics field to a broad scientific community. Combining FFS methods with fluorescence imaging, as originally done in image correlation spectroscopy (ICS) ([4\)](#page-11-0), allows quantitative molecular properties to be extracted from microscopy images. Many variations on the original ICS method have appeared over the years. For example, two-color image cross-correlation spectroscopy (ICCS) allows quantifying clustering of two types of fluorescently labeled molecules ([5\)](#page-11-0). Temporal ICS (TICS) can be used for measuring the dynamics of slowly diffusing complexes [\(6\)](#page-11-0). Spatiotemporal ICS (STICS) is a method that can be used for quantifying the

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directionality and velocity of flow phenomena ([7\)](#page-11-0). Imaging mean squared displacement (iMSD) can be used to study diffusion mechanisms ([8\)](#page-11-0). The k-space ICS method (kICS) is used to efficiently deal with fluorophores that exhibit a significant blinking ([9](#page-11-0)). Finally, the raster image correlation spectroscopy (RICS) method can be used to study the molecular translational diffusion constant (D) , absolute concentration (c), and intermolecular binding constants of diffusive molecules in single or multicolor confocal laser scanning microscopy (CLSM) images $(10-12)$.

ICS provides a popular powerful quantification and characterization tool for microscopy images. With RICS in particular, molecular parameters can be quantified in a (bio-) chemically interesting and exceptionally large dynamic range $(D \approx 0.1 - 500 \ \mu m^2/s, c \approx 10^{-6} - 10^{-9} \text{ M}$. RICS analyses suffer much less from photobleaching- and blinking-related artifacts than their single-point confocal counterparts, since fluorescence is probed over a large area ([13\)](#page-11-0). This larger probed area also increases experimental robustness against location-specific artifacts. Measurement times reduced to a few or even a single image frame suffice, in turn opening the door toward robust kinetic analysis. Most importantly, RICS can be carried out on almost any CLSM; most manufacturers nowadays offer plug-and-play RICS extensions, and different groups worldwide provide well-documented moreadvanced RICS analysis software [\(10,13,14\)](#page-11-0).

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The RICS method, however, also has limitations that have prevented its widespread usage. For example, the classical algorithm used in RICS analysis only accepts n^2 ROIs, where n is the number of pixels in each direction of the ROI [\(4](#page-11-0)). Placing a squared ROI inside an imaged sample, such as a cell or cell organelle, can be difficult. Decreasing n reduces this problem and even allows mapping of molecular parameters in a complex sample $(15,16)$, but limited statistics prevent an accurate spatial correlation analysis below $n \approx 64$. A static square ROI is also disadvantageous when dealing with organelles such as the endoplasmic reticulum (ER) or mitochondria that have complex shapes and are dynamic in a live-cell imaging experiment.

Another limitation of FFS is that fluctuation analyses perform well only on relatively homogenous samples. For example, as little as a single contamination that is significantly brighter than the average fluorescent species is detrimental for the correlation function when not removed a priori from the data. A commonly used trick to deal with this during FCS analysis is to monitor the moving average count rate over time; when it temporarily exceeds a certain relative or absolute threshold, all photons detected during this period are omitted from the correlation analysis. To our knowledge, a similar approach has not yet been incorporated for spatial correlations.

Lastly, because molecular information is averaged over space, the RICS method has not been used for generating pixel-resolution diffusion or concentration maps, unlike imaging-based FFS methods such as scanning FCS (SFCS) $(17,18)$ $(17,18)$ $(17,18)$, TICS (5) (5) , imaging total internal reflection (ITIR)-FCS [\(19](#page-11-0)), and single-plane illumination microscopy (SPIM)-FCS ([20\)](#page-11-0). In these methods, however, diffusion maps are mostly obtained only for relatively slowly diffusing molecules, such as, e.g., membrane proteins. Finally, when imaging using a CLSM for methods based on correlation between consecutive frames, the maximal scanning speed of the laser determines the highest mobility of molecules that can be quantified, which in our experience was around $D = 0.01 \ \mu \text{m}^2/\text{s}$ ([21\)](#page-11-0). In addition to diffusion maps, concentration maps of slowly diffusing molecules can also be generated using imaging-based FFS methods. For fast diffusing molecules, concentration maps can also be generated using the number and brightness method ([22\)](#page-11-0), which derives concentration info from the photon distribution per pixel. However, being an obligate single-pixel analysis method such as TICS, a fair number of images are needed to obtain a map of sufficient quality.

In this work, we describe an adapted version of the original ICS algorithm that now accepts ROIs of any shape. We implemented our algorithm in an all-graphical ICS analysis program that utilizes ROIs that can be generated freehand or automatically. Hence, any arbitrarily shaped region from an image series can be selected before correlation analysis. Using different proof-of-principle experiments, we illustrate some of the possibilities of arbitrary-region RICS (ARICS): removing artifacts from images before a correlation analysis, simultaneous analysis of diffusion and concentration in the membrane and cytosol, quantifying diffusion near complex and dynamic organelles such as the ER, and finally, generating pseudo-maps of diffusion and concentration. Considering all the advantages of ARICS analysis, we expect this approach to be beneficial to a number of spatial correlation methods and to replace the classical RICS algorithm.

THEORY

Classical ICS algorithm

For comparison, we first briefly summarize the classical ICS algorithm [\(4](#page-11-0)), in which correlations are typically calculated using the following fluctuation image $\delta I(x,y)$:

$$
\delta I(x, y) = I(x, y) - \langle I \rangle_{XY}, \tag{1}
$$

where I is the original fluorescence intensity image of size $X \times Y$, $I(x,y)$ is the intensity of pixel (x,y) ([Fig. 1](#page-2-0) A), and $\langle I \rangle_{XY}$ is the mean image intensity. The unnormalized spatial autocorrelation function (SACF) over a selected ROI (Fig. $1 \, B$) is typically defined as follows:

$$
G(\xi, \psi) = \frac{\langle \delta I(x, y) \times \delta I(x + \xi, y + \psi) \rangle_{XY}}{(X - |\xi|)(Y - |\psi|)}, \quad (2)
$$

where $\langle \rangle_{XY}$ denotes two-dimensional (2D) cross-correlation, i.e., $\sum_{y=1}^{Y} \sum_{x=1}^{X} () , (X - | \xi |) (Y - | \psi |)$ is the number of times a particular spatial lag (ξ,ψ) can be sampled, and | | denotes the absolute value. As illustrated in [Fig. 1](#page-2-0) C , the correlation is averaged over fewer elements as the spatial lag increases. Analogously to fluorescence correlation spectroscopy, $G(\xi,\psi)$ is typically normalized by $\langle I \rangle_{XY}^2$ so that the amplitude of the SACF scales inversely with the number concentration N (the reader is referred to Eq. 14 for the fitting model used for the RICS analysis). In ICS, the correlation is calculated for each frame individually and the resulting SACFs are averaged over all frames to increase signal-to-noise.

ICS algorithm generalized for an arbitrary ROI

To generalize Eq. 2, we first define an arbitrarily shaped binary ROI mask $R(x, y)$ with size equal to the image size, and with intensity one inside and zero outside the included region of interest (Fig. $1 D$):

$$
R(x, y) = 1(\text{inside}) \text{ or } 0(\text{outside}). \tag{3}
$$

The image can then be masked by an elementwise multiplication with R:

$$
I_R(x, y) = R(x, y)I(x, y), \qquad (4)
$$

FIGURE 1 Comparison of the ROI and ICS normalization in normal and generalized ICS. (A) Schematic representation of a 20×20 pixel² image of a cell exhibiting fluorescence in the cytosol and, to a lesser extent, in the nucleus, is shown. (B) Normal ROI, encompassing the whole image including the cell and extracellular space is provided. (C) Graphical representation of the number of times a particular spatial lag is sampled, i.e., $(X-|\xi|)(Y-|\psi|)$ in Eq. 2 or the denominator in Eq. 6. Spatial lags larger than half the ROI size are not used. (D) Arbitrary ROI mask, generated by intensity thresholding, encompassing only the cytosolic interior of the cell is shown. White pixels in the binary mask are unity; dark gray pixels are zero. (E) Spatial autocorrelation of the mask, displaying the number of times a particular spatial lag is sampled. For example, the lag (0,0) is sampled 81 times, which is equal to the number of unity pixels in the arbitrary ROI. To see this figure in color, go online.

and the fluctuation image $\delta I_R(x, y)$ can again be defined as follows:

$$
\delta I_R(x, y) = R(x, y) (I_R(x, y) - \langle I_R \rangle_{XY}), \tag{5}
$$

where $\langle I_R \rangle_{XY}$ is now the mean intensity of all pixels included in the ROI. Then, similar to what has previously been done ([23\)](#page-11-0), we define the unnormalized SACF as follows:

$$
G(\xi, \psi) = \frac{\langle \delta I_R(x, y) \times \delta I_R(x + \xi, y + \psi) \rangle_{XY}}{\langle R(x, y) \times R(x + \xi, y + \psi) \rangle_{XY}}, \quad (6)
$$

where the correlation in the denominator again dictates the number of times a particular spatial lag (ξ,ψ) is sampled (Fig. 1 E). Hence, we average each shift in the correlation function by the number of times this shift is observable in the ROI. Finally, $G(\xi,\psi)$ is normalized by the average intensity of the selected pixels, $\langle I_R \rangle_{XY}^2$, and averaged over all frames. For both numerator and denominator, the same fast Fourier transform algorithm used for classical ICS can be applied to speed up the calculations. An additional change we made to the algorithm is to explicitly zero-pad images to avoid aliasing effects. The associated MATLAB (The MathWorks, Natick, MA) code and analysis software is available on request. Taken together, to generalize the ICS calculation algorithm for any ROI shape, we apply a ROI mask during image correlation, exploiting the fact that pixels with zero intensity cancel from the calculation, and normalizing the correlation at each spatial lag accordingly.

Generating the ROI

A ROI is classically defined in ICS as a square or rectangle positioned somewhere on an image in the image series. Here, we use three alternative ways for generating an ROI: 1) Many programming languages have built-in functions for manually drawing an arbitrarily shaped ROI, which can be useful for masking, e.g., an intracellular region. In MATLAB, we use the imfreehand command for this purpose. 2) Certain pixel characteristics can be used for defining the ROI, e.g., its absolute intensity:

$$
R(x, y) = 0 \text{ if } \langle I \rangle_{a \times b} < \text{or} > I_{threshold}, \tag{7}
$$

where $\langle I \rangle_{a \times b}$ is the average intensity in an $a \times b$ area around pixel (x,y) and $I_{threshold}$ is an absolute intensity threshold above or below which pixel intensities should lie. Empirically, we found that a 5×5 -pixel² area worked well. For methods such as RICS where the correlation function is calculated on each image individually, the threshold selection criteria can be dynamic and the ROI variable for each frame. In this way, corrections can be made in movies where large aggregates or dark vesicles diffusing through the image series. Importantly, since thresholding is done using a spatial averaging filter, the pixels in the arbitrary ROI still constitute a complete intensity distribution histogram. This is important for spatial correlation methods such as RICS, as illustrated experimentally in this work, but also for methods in which the actual distribution is analyzed, e.g., photon counting histogram (24) (24) or number and brightness analysis [\(22](#page-11-0)). Absolute or relative intensity or intensity variance thresholds can also be used, for which the reader is referred to the [Supporting Material](#page-10-0). 3) The ROI can be defined in another imaging channel, where a particular structure is specifically labeled.

Multiple ROIs can also be combined in various ways to obtain the final ROI. For example, if a freehand ROI (R_1) is drawn on an image of a cell to roughly select the nuclear region, and an intensity thresholding is additionally carried out to select densely staining regions (R_2) , the final ROI R, used during correlation analysis, is obtained by an elementwise multiplication of the two ROIs, or in general for n ROIs as follows:

$$
R(x, y) = \prod_{i=1}^{n} R_i(x, y),
$$
 (8)

where n is the total number of ROIs.

Image preprocessing

For RICS analyses in live cells, slow fluctuations and spatial inhomogeneities are removed when necessary from the raw image data with a high-pass filter as follows:

$$
I_{RICS}(x, y, f) = I(x, y, f) - \langle I(x, y, f) \rangle_{\Delta F} + \langle I \rangle_{XYF}, \qquad (9)
$$

where $I(x,y,f)$ is the photon count of pixel (x,y) in frame f, $\langle I(x, y, f) \rangle_{\Delta F} = (2\Delta F + 1)^{-1} \sum_{f=-\Delta F}^{\Delta F} I(x, y, f)$ is the moving average series from frames ($f \Delta F$) to frame ($f + \Delta F$), and $\langle I \rangle_{XYF}$ is the mean intensity over all frames F with size $X \times Y$. For live-cell experiments, a moving average of $\Delta F = 1$ was used. Importantly, when performing temporal averages, pixels that were excluded from the ROI anywhere in the time window $f \pm \Delta F$ also need to be excluded from the arbitrary ROI of frame f as follows:

$$
R_{RICS}(x, y, f) = \prod_{i=f-\Delta F}^{f+\Delta F} R(x, y, i).
$$
 (10)

 I_{RICS} and R_{RICS} are subsequently used for correlation with Eq. 6. When performing a moving average, the image with the fluctuation of interest is included in the average and subtracted from the image. Hence, the amplitude of the fluctuation is decreased and the amplitude of the SACF in Eqs. 2 and 6 is also decreased. We correct for this artifact by rescaling the ACF:

$$
G_{corr}(\xi, \psi) = \frac{2\Delta F + 1}{2\Delta F} G(\xi, \psi).
$$
 (11)

Diffusion and concentration pseudo-maps

Since RICS is normally performed in large square image regions (typically $> 64^2$ pixel²) (Eq. 2), the spatial resolution is considerably lowered when molecular parameters (diffusion, concentration, brightness, stoichiometry, and interactions) are mapped. Although ARICS allows analysis in ROIs that do not need to be square (Eq. 6), enough pixels still need to be sampled to create a single correlation function. This leads to a similar resolution limit when mapping with ARICS. By exploiting particular image features, the ARICS method can also be used for creating pseudo higher-resolution maps of molecular parameters.

An example of such a feature is the average pixel intensity: most features that affect the local concentration of a molecule (interactions, exclusion zones, compartmentalization, etc.) also affect its apparent diffusion coefficient. Whereas mere changes in the mobility (e.g., because of different viscosities) create an inverse concentration and consequently intensity gradient in the sample (Fig. S4), interactions with cellular structures are much more complex and do not necessarily follow this relationship. Therefore, the different signal intensities in an image indicate local variations, and dividing an image into different ROIs depending on local intensity might reveal hidden interactions with or exclusions from the local environment.

Additionally, the ROIs do not necessarily have to be generated from the channel that is used for the actual correlation. By labeling an interaction partner or antagonist with a second color, or by imaging certain cellular markers (e.g., chromatin or organelles), the signal intensity in the second channel can then be used to create ROIs.

Practically, when the intensity of the images in a movie is broadly distributed, each image frame can easily be divided into *m* arbitrary ROIs R_m (e.g., $m = 5$), each encompassing pixels in a particular range of intensities (e.g., 0–200, 200–400, ... kHz). For every frame in the series, m SACFs are calculated (Eq. 6) and each SACF is averaged over all frames. The m SACFs are then fitted using Eq. 14 to extract D and N parameters for each of the m ROIs, termed D_i and N_i , respectively. These parameters are subsequently assigned to every pixel in an image to create pseudo-maps of ''single-frame'' diffusion and concentration as follows:

$$
D(x, y, f) = \sum_{i=1}^{m} (R_i(x, y, f) \times D_i) \text{ and}
$$

\n
$$
N(x, y, f) = \sum_{i=1}^{m} (R_i(x, y, f) \times N_i),
$$
\n(12)

respectively, where \times denotes an elementwise multiplication. Although Eq. 12 assumes the m ROIs are completely nonoverlapping, only a small adaptation is needed to allow also overlapping ROIs. Finally, and as will also be shown experimentally, the m ROIs may move from one frame to the next. Therefore, an average over the single-frame pseudo-maps is performed as follows to generate a representative calculation of the diffusion and concentration pseudo-maps:

$$
\overline{D(x,y)} = \frac{1}{F} \sum_{f=1}^{F} D(x,y,f) \text{ and}
$$

resp.
$$
\overline{N(x,y)} = \frac{1}{F} \sum_{f=1}^{F} N(x,y,f),
$$
 (13)

where F is the total number of frames minus any frames where, due to preprocessing stipulations (Eq. 10), the pixel was not assigned to a ROI.

MATERIALS AND METHODS

Plasmids, cell culture, and transfection

pKHIV^{Venus} encoding Gag. Venus was obtained from Barbara Müller (University of Heidelberg) and cloned as described previously ([21](#page-11-0)). eGFP-LEDGF/p75 was cloned as described previously [\(25\)](#page-11-0). pMyrPalm.mYFP was provided by Prof. R. Tsien (University of California San Diego, La Jolla, CA). PcsVenus and calreticulin-mRFP-KDEL/pcDNA3 plasmids were a gift of Prof. A. Miyawaki ([26\)](#page-11-0). HeLa cells (NIH Reagent program) were cultivated without antibiotics in low-glucose DMEM (Life Technologies, Darmstadt, Germany) supplemented with 10% heat-inactivated fetal bovine serum (complete medium) at 5% CO₂ and 37° C in a humidified atmosphere. For transfection, 3×10^4 cells per well were plated in complete medium in eight-well cover slips (Lab-Tek II Chambered Coverglass, Thermo Scientific, Langenselbold, Germany). Plasmid DNA (500 ng in total) was mixed with 1.5 μ L XtremeGene 9 transfection reagent (Roche Applied Science, Mannheim, Germany) in 50 μ L OptiMEM and incubated for 15–20 min at room temperature, before addition of 100 ng pKHIVFP plasmid 6–8 h after cell seeding. For cotransfections a 1:1 plasmid weight ratio was used. All imaging experiments were performed at room temperature.

Venus FP imaging experiment

Previously described imaging data of the Venus fluorescent protein freely diffusing in a 10-cP viscosity buffer, acquired on a home-built confocal laser-scanning microscope (2 μ W of 475-nm excitation at the sample) [\(13](#page-11-0)), was reanalyzed in this work. Imaging parameters were 200 frames, $12.5 \times 12.5 \ \mu \text{m}^2$, $300 \times 300 \text{ pixel}^2$, line time $\tau_l = 3.33 \text{ ms}$, pixel dwell time $\tau_p = 11.11 \mu s$, and pixel size $\delta r = 41.7 \text{ nm}$.

Membrane diffusion experiment

Previously described imaging data of cells coexpressing cytosolic Venus and mCherry fluorescent proteins and membrane-targeted MyrPalmmYFP, acquired on a home-built confocal laser-scanning microscope (0.8 μ W of 475-nm excitation at the sample) ([21\)](#page-11-0), was reanalyzed in this work. Imaging parameters were 100 frames, 300×300 pixel², line time τ_l = 3.33 ms, pixel dwell time τ_p = 11.11 μ s, and pixel size δr = 41.7 nm. Before per-frame intensity thresholding (Eq. 7), a rough ROI covering the cell was manually drawn on the first image of the image series and kept constant for all frames.

Other imaging experiments

The Gag and LEDGF/p75 imaging experiments were carried out on a commercial Olympus Fluoview FV1000 confocal microscope. Raster-scanning was performed in the center of the scan range during 200 frames with the following settings: 256×256 pixel², line time $\tau_l = 4.325$ ms, pixel dwell time $\tau_p = 12.5 \mu s$, and pixel size $\delta r = 50 \text{ nm}$ (i.e., zoom 16.4). Excitation light from a 488 nm Ar-ion laser (2% transmissivity, \sim 2 μ W in the sample) was reflected into a UPLSAPO-60XW objective (NA $= 1.2$) using a DM405/488/559/635 polychroic mirror. The optimal position of the objective cover slip correction collar was determined by maximizing the molecular brightness as measured by RICS of freely diffusing ATTO488-CA (ATTO-TEC, Siegen, Germany) at nM concentration in water. Emission was detected through a 130 μ m pinhole (automatic setting) and a BA505-540 emission filter onto a photomultiplier tube operating in pseudo-photon counting mode. To convert pseudo-counts to real counts, an image intensity rescaling parameter $S = 6$ was used [\(27,28](#page-11-0)). In the second imaging channel used for generating the ROI, 559-nm excitation (1% transmissivity) from a DPSS laser was used. Emission was separated from the other imaging channel using an SDM560 dichroic mirror and a BA575-675 emission filter. Before per-frame intensity thresholding (Eq. 7), a rough ROI covering the cytosol (Gag experiment) or nucleus (LEDGF/p75 experiment) was manually drawn on the first image of the image series and kept constant for all frames.

RICS fitting

The mean of the SACF series was analyzed as before [\(21](#page-11-0)) by nonlinear least squares fitting with a two-component (one mobile and one immobile) model for Brownian diffusion in a three-dimensional (3D) Gaussian PSF as follows:

$$
G_{\text{fit}}(\xi, \psi) = A_{\text{mob}} G_{\text{fit}, \text{mob}}(\xi, \psi) + A_{\text{imm}} exp(-\delta r^2 \omega_{\text{imm}}^{-2} (\xi^2 + \psi^2)) + G(\infty),
$$

where

$$
G_{\text{fit},\text{mob}}(\xi,\psi) = \left(1 + \frac{4D(\tau_p\xi + \tau_l\psi)}{\omega_r^2}\right)^{-1} \times \left(1 + \frac{4D(\tau_p\xi + \tau_l\psi)}{\omega_z^2}\right)^{-\frac{1}{2}} \qquad (14)
$$

$$
\times \exp\left(-\frac{\delta r^2(\xi^2 + \psi^2)}{\omega_r^2 + 4D(\tau_p\xi + \tau_l\psi)}\right)
$$

is the time-dependent component of the correlation function ascribed to fast diffusing molecules. A_{mob} and A_{imm} are the amplitudes of the mobile and immobile component in the correlation function, respectively and $G(\infty)$ is a baseline correction term. The lateral and axial focus radii are denoted by ω_r and ω_z , respectively, defined as the distance from the focus center where the signal intensity decreases to $1/e^2$ of its initial value. The fraction of immobile molecules (on the RICS timescale) was described with a symmetrical 2D Gaussian function where ω_{imm} represents the half-width of the function at $1/e^2$ of the maximal intensity of the immobilized objects. When the objects are smaller than the diffraction limit, ω_{imm} becomes equal to ω_r . $N_{mob} = \gamma \frac{A_{mob}}{(A_{mob} + A_{jump})^2}$ is the average number of molecules in the point spread function (PSF) that are mobile on the RICS timescale, with $\gamma = 2^{-3/2}$ the shape factor for a 3D Gaussian. Goodness-of-fit parameters were the weighted residuals parameter r_w and reduced χ^2 parameter. Because of the strong autocorrelation of the shot noise at ($\xi = 0, \psi = 0$), $G(0,0)$ was not considered during fitting, and autocorrelation amplitudes were approximated by the average of $G(1,0)$ and $G(-1,0)$ for graphical representations.

Diffusion and concentration pseudo-maps

A freehand ROI was drawn around the nucleus of the cells, to exclude the cytosolic region a priori. Arbitrary ROIs were calculated using the H2B imaging channel and mapped onto the LEDGF/p75 channel. Moreover, in the H2B imaging channel, pixel intensities in each frame were rescaled such that the average image intensity in all frames was equal to that of the first frame. This procedure, which corrected the data for photobleaching, was important to render the threshold intensities applicable to all image frames.

RESULTS

Outlier-free fluctuation imaging

Many unwanted phenomena can give rise to confocal images with inhomogenously distributed fluorescence intensities: aspecific aggregation of molecules of interest, sticking of fluorophores to organelles, diffusing organelles lacking the molecule of interest, just to name a few. Although intrinsically part of the sample, when bright or dark artifacts move significantly from one frame to the next, they will adversely affect any quantitative (fluctuation) image analyses. A first application of the generalized ICS algorithm is cleaning up imaging data by removing fluorescent outliers before correlation and RICS analyses. As a proof-of-principle, we used a confocal image series of the freely diffusing Venus fluorescent protein at nM concentration in a buffer of roughly 10 times the viscosity of water. Fig. 2 A shows two frames: a clean frame and a frame in which a Venus aggregate coincidently diffused through the focal plane while the laser was scanning over it. We calculated the SACF of each frame (Fig. 2 B). Strikingly, although in the second frame, the aggregate was only detected in ~1% of all pixels, its SACF looks completely different than that of the clean frame. To mask out the aggregate, we employed an absolute intensity threshold $\langle I \rangle_{5 \times 5}$ < 150 kHz (Eq. 7). This selectively removed the aggregate from the image while leaving the rest of the image untouched (Fig. 2 C). Consequently, the threshold removed the high-count tail from the overall pixel intensity distribution histogram, while leaving the shape of the low-count part unchanged (Fig. $2 D$). To check whether the threshold held for all frames in the image series, we calculated all

FIGURE 2 Cleaning up image series before RICS analysis. (A) Two image frames from a 200-frame confocal image series of freely diffusing Venus fluorescent protein are shown. In the right image frame, a protein aggregate was in focus while the laser scanned over it. Scale bars represent $1 \mu m$. (B) SACFs were calculated from the frames in (A). The aggregate dictates the shape of the second SACF. (C) The frame containing the aggregate, with the pixels around which a 5×5 pixel² area exhibited an average intensity exceeding 150 kHz depicted in *red*. To avoid edge effects during thresholding, the borders of the image were also omitted from the ROI. The scale bar represents $1 \mu m$. (D) Intensity distribution histogram is provided of (black) all pixels in the frame containing the aggregate and (red) all pixels included in the arbitrary ROI of the same frame. For comparison, both the absolute photon counts and the count rate per pixel are displayed. (E) The amplitudes of the individual SACFs were calculated (black) using all image pixels with Eq. 2 or (red) using all pixels included in the arbitrary ROI with Eq. 6. Amplitudes were approximated by the correlation value at $\xi = 1$. For clarity, a break at 0.11–0.2 was introduced on the y-axis. (F) The averaged arbitrary-ROI SACF was fitted using Eq. 14 and color-coded using the weighted residuals goodness-of-fit parameter r_w . Fig. S1 contains further details on the fitting, as well as a comparison with the raw-data average SACF fitting. To see this figure in color, go online.

corresponding SACFs and plotted their amplitudes, approximated by the correlation value at $\xi = 1, \psi = 0$, as a function of frame number (Fig. $2 E$). Clearly, when an arbitrary ROI was used, the variation on the SACF amplitude decreased tremendously. Finally, when the individual, artifact-free SACFs were averaged and the average SACF was fitted using Eq. 14, a single diffusing species $(D = 7.7 \pm 0.3 \ \mu \text{m}^2/\text{s})$ was observed with the fit model yielding 100% amplitude of the mobile fraction and 0% for an immobile species (reduced $\chi^2 = 1.02$) [\(Fig. 2](#page-5-0) F). For comparison, Fig. S1 displays a RICS analysis of the raw imaging data, which is not described at all by Eq. 14 due to the presence of Venus aggregates. This proof-of-principle experiment clearly shows the generalized ICS algorithm can be used to specifically remove outliers from imaging data of freely diffusing Venus, resulting in RICS data that could be perfectly described by a single-component fit model.

Simultaneously measuring diffusion in the cytosol and membrane

In a next experiment, we used absolute intensity thresholding in live cells to discern between species diffusing in the cell membrane and the cytosol. We coexpressed cytosolic Venus together with a membrane targeted MyrPalm-mYFP in HeLa cells (Fig. 3 A). We avoided imaging near the bottom and top cell membrane by an mCherry coexpression control and z-stacking (Fig. S2). We defined two arbitrary ROIs using Eq. 7 for selecting the membrane $(\langle I \rangle_{5 \times 5}$ > 300 kHz) and cytosol ($\langle I \rangle_{5 \times 5}$ < 300 kHz). By doing this, two complete pixel intensity distribution histograms were obtained, each one representing the molecules in the respective ROIs (Fig. $3 \, B$). After preprocessing the image series using Eq. 9 (Fig. 3 C) and calculating the SACF of each image frame, the average SACF was obtained for the membrane and cytosolic ROI (Fig. 3 D, top and bottom graphs, respectively). In the membrane ROI, a circular SACF shape was observed, indicative of slower mobility. After fitting, a diffusion constant of $D = 0.3 \pm 0.1 \ \mu \text{m}^2/\text{s}$ was obtained in the membrane ROI (Fig. 3 E, top graph), which is what is expected for the membrane-bound MyrPalm-mYFP protein ([29\)](#page-11-0). In the cytosol ROI, on the other hand, a line-shaped SACF was observed, with a corresponding diffusion constant of $D = 30 \pm 7 \mu \text{m}^2/\text{s}$ (Fig. 3, D) and E , *bottom graphs*), which in turn agrees with the expected value for fluorescent proteins diffusing freely in the cytosol $(21,25)$. Together, this experiment shows that arbitrary-region RICS can be used to simultaneously quantify diffusion in different compartments of the cell, as long

FIGURE 3 Absolute intensity thresholding for region-specific RICS analysis. (A) One image frame from a 100-frame confocal image series of a HeLa cell coexpressing cytosolic Venus fluorescent protein and membrane-targeted MyrPalm-YFP is shown. Scale bar represents 1μ m. (B) Intensity distribution histogram is provided of (black) all pixels in the frame, (red) an arbitrary ROI with $\langle I \rangle_{5\times5}$ > 300 kHz, and (green) an arbitrary ROI with $\langle I \rangle_{5\times5}$ < 300 kHz. For comparison, both the absolute photon count and the count rate per pixel are displayed. (C) The data from (A), were preprocessed using Eq. 9, and intensitythresholded to select (top image) the membrane or (bottom image) the cytosol. (D) SACFs were calculated from the preprocessed ROI in (C). The inset is a top view of the SACFs. (E) The average arbitrary-ROI SACF was fitted using Eq. 14 and color-coded using the weighted residuals goodness-of-fit parameter r_w . Fig. S2 contains further details on the experiment. Results for a representative cell are shown. The average error on the SACF data (% error on a data point relative to the SACF amplitude) was 3–4%, the error on D was 10–25%, and the reduced χ^2 fit quality parameter was 1.9–2.4. To see this figure in color, go online.

as the ROIs can be discerned on the basis of the absolute fluorescence intensity.

Mobility near complex subcellular structures

It would be of great interest to be able to measure the diffusion of proteins in different subcellular structures or organelles within a living cell. With the exception of the nucleus, this has not possible with RICS as the organelles are limited in size and are poorly described by rectangular ROIs. With ARICS, this becomes possible. When subcellular regions cannot be easily distinguished via the absolute fluorescence intensity as described above, a second channel can be used to image the subcellular structures or organelles. The ROI can then be generated from the fluorescence channel of the marker and then mapped back onto the image series of the molecule of interest. We used dual-color ARICS to study diffusion of the HIV-1 Gag, the protein that constitutes the protein shell of HIV-1 virions, near the ER. Previously, it had been shown that, under some conditions, the incorrect assembly of Gag can occur in the ER ([30\)](#page-11-0). Also, bridging conduits between macrophage cells that allow for cell-tocell transfer of HIV consists of ER membranes ([31\)](#page-11-0). For the dual-color ARICS experiments, HIV-1 Gag was labeled with Venus and the ER membrane was labeled by fusing mRFP to an ER-targeting peptide (calreticulin-mRFP-KDEL). A typical confocal image of HeLa cells expressing Gag (as part of the MA-Venus-CA-NC-p6 construct) is shown in [Fig. 4](#page-8-0) A. The Gag protein is present in the cytosol but not in the nucleus. In the cytosol, regions with less Gag staining are visible (top left region in Fig. $4A$), which might correspond to the ER, but a reference image series of the ER was needed to confirm this. The image in Fig. $4 \, B$ corre-sponds to the image in [Fig. 4](#page-8-0) A, and shows the typical structure of the ER surrounding the nucleus, and staining densely in some cytosolic regions, but not in others. Based on intensity thresholding in the red imaging channel, we could define two ROIs: one staining only dimly in the ER imaging channel [\(Fig. 4](#page-8-0) C, left) and one staining very intensely in the ER imaging channel (Fig. $4 \, C$, *right*). These regions were consequently mapped onto the Gag imaging channel ([Fig. 4](#page-8-0) D) and a RICS analysis was performed (Fig. 4, E) and F). Visually, the SACFs in cytosolic regions mostly devoid of ER membranes (Fig. $4 E$, *left*) and enriched in ER membranes [\(Fig. 4](#page-8-0) E, right) looked similar. After analyzing 10 cells, average diffusion coefficients of $D =$ $3.5 \pm 0.3 \ \mu \text{m}^2/\text{s}$ ($F_{mob} = 74 \pm 1\%$) and $D = 3.7 \pm 1\%$ 0.3 μ m²/s ($F_{mob} = 72 \pm 3\%$) were obtained respectively ([Fig. 4](#page-8-0) F). This can be interpreted in different ways: 1) the mobility of Gag in the cytosol and in the ER is similar, 2) the mobility of Gag near the ER as observed with ARICS is not decreased by interactions with the ER, or 3) diffusion in or interaction with the ER is not picked up at all by ARICS. To investigate whether ARICS is principally sensitive for diffusion inside confined areas, we performed simulations (Fig. S3). In brief, ARICS provided qualitative information on diffusion for confinements of similar size as the PSF, in that the SACFs got distorted from the freely diffusing species. For compartments that were significantly larger than the PSF, the algorithm could even extract correct diffusion constants. Although interpretations 1) and 2) cannot be ruled out, a complete absence of experimental SACF distortion suggests that Gag does not interact with or localize in the ER lumen at all, and the latter is likely also too small to affect the SACFs.

Taken together, molecular mobility can, in principle, be studied in or at particular subcellular structures using RICS by generating a dynamic arbitrary ROI of the structure in a second imaging channel and mapping this ROI onto the image series of the molecule of interest. For the mobility of Gag in or close to ER membranes, a significant difference could not be observed relative to regions with low/no ER staining.

Concentration and diffusion pseudo-maps

We exploited the generalized ICS algorithm to segment the image into several ROIs and map the mobility and concentrations of the different segments. As outlined in the Introduction, the ROIs are selected depending on a particular image characteristic. A RICS analysis is performed on each of the AROIs in each image and an average over the time series of the obtained RICS parameters is determined for each pixel in the image. We validated this approach using simulations (see the [Supporting Material](#page-10-0)) where the diffusion coefficient varied depending on the position of the particle in the image. Slower diffusion leads to a higher concentration of particles and hence to higher intensity. Using fluorescence intensity for segmentation of the image, we could reconstruct the diffusion map (Fig. S4).

To test this method experimentally, we performed a RICS experiment on cells coexpressing the transcriptional coactivator LEDGF/p75 fused to eGFP (Fig. 5 A) as well as the core histone H2B fused to mRFP as a marker of chromatin density ([Fig. 5](#page-9-0) B) (25) (25) . We calculated the whole-series cumulative pixel intensity histogram of the H2B image series ([Fig. 5](#page-9-0) C), from which we defined five threshold intensities (725 kHz, 959 kHz, 1075 kHz, 1209 kHz, and 1792 kHz) that divided each image in the image series into five ROIs, as illustrated in [Fig. 5](#page-9-0) D. In each frame, we then calculated five SACFs and averaged these over the whole image series. After fitting, it was clear that the $G(\xi,0)$ amplitude scaled inversely with the average fluorescence intensity of the mRFP-H2B protein. In other words, the eGFP-LEDGF/ p75 density followed the mRFP-H2B density (Fig. $5 E$). From the $G(0,\psi)$ shape, on the other hand, it was clear that at least the lowest-intensity ROI seemed to contain molecules of overall lower mobility (Fig. $5 F$). Using Eqs. 12 and 13, we then used the diffusion coefficients and number concentrations obtained from the five SACFs to create

FIGURE 4 Molecular mobility near complex cell organelles. (A and B) One image frame from a 200-frame two-color confocal image series of a HeLa cell coexpressing (A) Gag. Venus and (B) the endoplasmic reticulum marker calr-mRFP-KDEL are shown. Scale bars represent 1μ m. (C) The data from (B) was intensity-thresholded ($I_{threshold} = 500$ kHz) to select (left image) regions devoid of ER membranes or (right image) regions with dense ER staining. (D) Selected pixels from (C) were used to create region-specific ROIs in the Gag.Venus imaging channel. (E) SACFs were calculated from the ROIs in (D); y-axes are $\times 10^{-3}$. (F) The average arbitrary-ROI SACF was fitted using Eq. 14 and color-coded using the weighted residuals goodness-of-fit parameter r_w ; y-axes are $\times 10^{-3}$. Results for a representative cell are shown, but a total of 10 cells were analyzed, using values for $I_{threshold}$ that visually separated the cytosol from the ER. Errors on fit parameters are the mean plus SE. The average error on the SACF

pseudo-maps of diffusion [\(Fig. 5](#page-9-0) G) and concentration ([Fig. 5](#page-9-0) H). Several interesting features become obvious from this analysis: 1) The N map of LEDGF/p75 correlated with both the LEDGF/p75 and H2B intensity maps, suggesting that the intensity distribution in the intensity images is due to difference in concentration and not due to changes in the intrinsic fluorophore brightness. In addition, the concentration of LEDGF/p75 follows the chromatin density. This experiment can be viewed as a single-cell titration experiment as the segmentation leads to separate analyses for regions of different LEDGF/p75 concentrations. 2) Regions of low concentration, corresponding to the nucleoli as seen from the mRFP-H2B staining, correlated with regions of low mobility. 3) Other regions of low mobility correlated with regions of high eGFP-LEDGF/p75 concentration. As it is believed that LEDGF/p75 transiently interacts with DNA, slowing down its diffusion (25) (25) , the regions of lower mobility, corresponding to high chromatin densities, suggest that the affinity of eGFP-LEDGF/p75 for chromatin increases with concentration. 4) Lastly, the nucleoli are surrounded by regions of high mobility, suggesting a lower local viscosity in these regions. Since molecules naturally accumulate in regions of low mobility (the reader is referred to the simulation in Fig. S4), the absence of an excess LEDGF/p75 in the nucleolar regions suggests the protein has a hard time entering, or, is actively exported from these regions.

To compare the results from the ARICS analysis with other FFS methods, we calculated the concentration map using an number and brightness (N&B) analysis (Fig. S5). The overall distribution and magnitude of number concentrations obtained with N&B and ARICS is similar, but because no spatial averaging was used for the N&B analysis, the noise in the number concentration image is higher. In summary, by categorizing image pixels in different intensity regions of another imaging channel, pseudo-maps of diffusion and concentration could be obtained for the transcription factor LEDGF/p75, which revealed an interesting correlation between diffusion and concentration, information that would otherwise be completely hidden in the SACF.

DISCUSSION

The ability of RICS to extract biophysical information from fluorescence images makes it an exciting method for the biological and biophysical communities. Numerous studies of cytosolic or nuclear dynamics in cell types, such as HeLa cells, have been shown to be possible using RICS. However, accurate cellular RICS experiments are often difficult because of aggregates of high intensity or dark vesicles diffusing through the field of view. In addition, RICS is

data (% error on a data point relative to the SACF amplitude) was 1–4%, and the reduced χ^2 fit quality parameter was 1.7–3.5. To see this figure in color, go online.

FIGURE 5 Diffusion and concentration pseudo-maps with ARICS. (A and B) One-frame images from a 200-frame two-color confocal image series of a HeLa cell coexpressing (A) eGFP-LEDGF/p75 and (B) a chromatin density marker mRFP-H2B are shown. Scale bars represent 1 μ m. (C) The cumulative pixel intensity histogram is provided of the complete mRFP-H2B image series for all pixels inside the nucleus. (D) Using intensity thresholding, each image can then be divided in five approximately equally sized ROIs, as displayed for the image frame from (B) . The legend indicates the upper intensity threshold per ROI. Black regions correspond to pixels that switched between different ROIs within the moving average and are excluded by the preprocessing algorithm (Eq. 9). (E and F) The five averaged arbitrary-ROI SACFs (symbols and error bars) were fitted using Eq. 14 (solid line) and the (E) $G(\xi,0)$ and (F) $G(0,\psi)$ values and fits are displayed. Top panels show the weighted residuals goodness-of-fit parameter. (G) From the ARICS analysis, a pseudo-diffusion map and (H) pseudo-concentration map of eGFP-LEDGF/p75 averaged over all frames are shown. Results for a representative cell are shown. The average error on the SACF data (% error on a data point relative to the SACF amplitude) was $1-4\%$, the error on parameters in the pseudo-maps were 5–15% for D and 1–3% for N, and the reduced χ^2 fit quality parameter was 1–2.5. To see this figure in color, go online.

difficult with smaller cell types (for example T-cells or even bacteria or yeast cells) and nearly impossible when trying to measure diffusion in small organelles as the ROI is too small or ill-shaped for classical RICS. ARICS can circumvent many of these difficulties. As for any fluctuation experiment, enough (adjacent) pixels need to be sampled for the SACF to have meaningful statistics. As a rule-of-thumb, the statistics are generally sufficient for fitting the SACF to simple models when the standard deviation is smaller than 5% and the SACF does not contain a significant negative offset.

The freedom to correlate virtually any shape of ROI using ARICS opens up a number of possibilities. One possibility is the automatic detection and removal of undesired spatial fluctuations within images. For example, in live-cell measurements at 37° C, cell components (organelles, vesicles, membranes) move significantly from frame to frame, leading to the situation where many frame contains artifacts from moving dim or bright objects. As the SACF is calculated on each frame separately, one could delete each frame where such an artifact is observed. However, this can be time consuming and throws out data unnecessarily. By including predetermined criteria (e.g., minimum and maximum acceptable pixel intensity, maximum acceptable fluctuation from the pixel average, etc.), these artifacts can be detected and removed from the analysis as we demonstrated in our proof-of-principle Venus imaging experiment.

The strength of ARICS is that ROIs can be selected using a myriad of conditions, making it very powerful, not just to clean up artifacts but to perform biophysical characterization of biomolecules in cells with subcellular resolution. For example, we exploited the difference in absolute fluorescence intensity to discern between diffusion in the membrane and from the cytosol. Another alternative is to use a second imaging channel to perform the segmentation, as we demonstrated for labeling of the ER membrane. Hence, one can consider a wide range of parameters that could be used to select the ROIs for the ARICS analysis.

An additional advantage of ARICS is the ability to automate the analysis and to perform batch analyses. How well the process can be automated depends on how well one can automate the selection criteria for the different ROIs. Thus, we implemented a relative thresholding of a small (e.g., 5×5) versus a larger (e.g., 10×10) subregion in the image (as outlined in the [Supporting Materials](#page-10-0)). In general, relative thresholds can be interesting for automated analysis, since they do not require a user-defined input of absolute intensities. Shape-sensitive ROI-generating algorithms for automatically detecting cells, nuclear membranes or cellular components ([32\)](#page-11-0) can also be implemented. Thus, ARICS holds promise for automated whole-cell and subcellular analysis by fluctuation methods.

We have also demonstrated the possibility of pseudomapping parameters using the ARICS method. To our knowledge, this is a versatile new way of looking at spatial correlation data. We deliberately termed it a pseudo-map, since it is based on the a priori definition of a number of ROIs between which the average properties are investigated. The quality of the pseudo-map depends on how well the ROIs are defined. When a particular parameter, such as *D*, varies largely within a single ROI, the pseudomap will still provide a single averaged value. Any image feature (intensity, intensity variance, but possibly also higher moments) in any imaging channel can be used as input for generating the different ROIs. For example, a molecular brightness map can be made by dividing the average intensity image by the N pseudo-map. In this way, molecular stoichiometries can be imaged using ARICS just as with the N&B method. Conversely, the stoichiometry from an N&B analysis can also be used to generate ROIs and the dynamics of molecules having a particular stoichiometry investigated using ARICS.

Pseudo-mapping can principally also be used for creating D or N maps from TICS or imaging FCS (light sheet or total internal reflection fluorescence (TIRF)-based) data, where similar image features can be used as we proposed above, recorded in the same or another imaging channel. In general, the values for D that have to be quantified determine which fluctuation imaging methods are best suited. In terms of excitation power, a higher density is typically used in the RICS method, but regions are illuminated only briefly (μs) pixel dwell times) in each frame, whereas a lower, but continuous density is typically used in TIRF and light sheet experiments. Finally, whereas the excitation light in confocal microscopy and light sheet microscopy travels throughout the cell $(-10 \mu m)$ thickness and \sim 20 μ m length, respectively), in TIRF microscopy only a thin $(200 nm)$ region is exposed to the excitation light.

In this work, we have described the principle of the ARICS approach and demonstrated some of its capabilities. However, there are a number of possibilities for extending the ARICS approach. ARICS can be extrapolated to a cross-correlation analysis of two or more channels or to other fluctuation analysis methods such as ICS, STICS, iMSD that analyze spatial fluctuations. The other spatial correlation methods will benefit from the same advantages as ARICS. The method can also be applied to other measuring modalities such as RICS combined with stimulated emission depletion microscopy (STED), which allows imaging dynamics on smaller spatial scales [\(33](#page-11-0)). Another extension of ARICS that we envision would be to give a statistical weight to the pixels within the ROIs. Fluorescence lifetime correlation spectroscopy [\(34](#page-11-0)), raster lifetime image correlation spectroscopy ([13\)](#page-11-0), and fluorescence spectral correlation spectroscopy [\(35](#page-11-0)) employ statistical filtering of fluorescence data during the correlation analysis. In a similar approach, the $R(x, y)$ filter does not have to be binary but can be used as a statistical filter for weighting the ARICS data.

RICS and FCS both have particular advantages. FCS has the advantage of higher temporal resolution and, as the excitation volume is typically diffraction-limited, site-specific dynamics can be probed such as inside cell organelles or on the membrane. RICS has the advantage that the excitation energy is distributed over a much larger region in the sample. Hence, RICS and other imaging methods typically suffer much less from photobleaching-related artifacts ([13\)](#page-11-0). Secondly, because spatial correlation methods are carried out on a whole region in a sample, rather than a single point, much shorter measurement times are needed for obtaining adequate statistics. With ARICS, it is now possible to also probe dynamics inside cell compartments or membranes with RICS. In addition, nondesired heterogeneities within the sample, such as bright aggregates or dark organelles diffusing through the image, can be easily removed, making reliable RICS measurements much easier to perform. Lastly, since the ROI mask can move along with the imaged region-of-interest, ARICS makes it possible to probing molecular properties in dynamic subimage regions.

CONCLUSIONS

In this work, we present the ARICS method, which employs a generalized algorithm for spatial correlation analyses and can be applied to arbitrary regions-of-interest of a fluorescence image series. The way we have implemented ARICS is compatible with the fast Fourier transfer algorithms used typically in ICS and is not computationally cumbersome. ARICS sprouted from the many challenges we encountered in performing high-quality RICS data at 37° C in living cells. To illustrate the power of ARICS, we employed ARICS to clean up image series during correlation analysis, to perform cell organelle-specific correlation analysis, and to generate diffusion and concentration pseudo-maps. ARICS can be combined with any spatial correlation method and can be easily expanded to provide new modalities of analyzing RICS data. Hence, ARICS is a powerful successor of the classical RICS method with new functionalities and offers many exciting possibilities for further development.

SUPPORTING MATERIAL

Supporting Material and Methods, Supporting Results, and five figures are available at [http://www.biophysj.org/biophysj/supplemental/S0006-3495](http://www.biophysj.org/biophysj/supplemental/S0006-3495(16)30810-4) [\(16\)30810-4](http://www.biophysj.org/biophysj/supplemental/S0006-3495(16)30810-4).

AUTHOR CONTRIBUTIONS

J.H. and T.D. designed the research. J.H. performed experiments and wrote the article. W.S. performed the simulations. All authors critically reviewed the article.

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Supplemental Information

Arbitrary-Region Raster Image Correlation Spectroscopy

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Supporting Materials and Methods

Intensity or intensity variance thresholding

Besides manually drawing the ROI or using an organelle-based ROI, the *R* mask can also be generated by thresholding images on the basis of intensity or the variance in intensity. Below, we discuss a few approaches to image thresholding.

Frame-averaged intensity: When structural heterogeneities in the imaged sample remain localized (static) over the course of the experiment, the frame-averaged intensity can be used as a threshold. The image of the average intensity over all frames, $\langle I \rangle_{\mathbf{r}}$, is then compared at each pixel with given thresholds, I_{min} and I_{max} , the minimal and maximal allowed pixel intensities, respectively, to generate *R*:

$$
for \quad \langle I(x,y)\rangle_F < I_{min} \quad \text{or} \quad \langle I(x,y)\rangle_F > I_{max}, \quad R(x,y) = 0
$$
\n
$$
for \quad I_{min} \leq \langle I(x,y)\rangle_F \leq I_{max}, \quad R(x,y) = 1
$$
\nEq.S1

Frame-averaged intensity thresholding performs well for separating regions in the sample with clear differences in intensity, for example between intra- and extracellular regions or between the cytosol and the nucleus.

Rolling-window frame-averaged intensity: When structural heterogeneities in the imaged sample move slowly but remain localized (static) over at least 2Δ*F*+1 frames, averaging over a sliding window of 2Δ*F*+1 frames can be performed. In this case, the average intensity image is calculated between frames (*f*- ΔF) and (*f*+ ΔF), $\langle I \rangle_{\Delta F}$, and the intensity at every pixel compared with the threshold intensities, I_{\min} and I_{\max} , to generate a frame-specific ROI mask of size *X*×*Y*×(*F*-2Δ*F*):

$$
for \quad \langle I(x,y)\rangle_{\Delta F} < I_{min} \quad \text{or} \quad \langle I(x,y)\rangle_{\Delta F} > I_{max}, \quad R(x,y) = 0
$$
\n
$$
for \quad I_{min} \leq \langle I(x,y)\rangle_{\Delta F} \leq I_{max}, \quad R(x,y) = 1 \quad \text{Eq.S2}
$$

Due to the window necessary for performing the rolling average, the first and last Δ*F* frames in the image are ignored for calculation of the SACF. The total I_{min} and I_{max} can be (*i*) absolute numbers, (*ii*) defined relatively to $\langle I \rangle_{\mathbf{r}}$:

$$
\begin{aligned}\n\text{for} \quad & \langle I(x,y) \rangle_{\Delta F} < \langle I(x,y) \rangle_{F} / c & \text{or} \quad & \langle I(x,y) \rangle_{\Delta F} > c \langle I(x,y) \rangle_{F}, \qquad R(x,y) = 0 \\
\text{for} \quad & \langle I \rangle(x,y)_{F} / c \leq \langle I(x,y) \rangle_{\Delta F} \leq c \langle I(x,y) \rangle_{F}, \qquad R(x,y) = 1 & \text{Eq.S3}\n\end{aligned}
$$

where *c* defines the strictness of the threshold, *(iii)* defined relatively to $\langle I \rangle_{\mathbf{A}\mathbf{E}^2}$, the average intensity image between frames (f - $\Delta F2$) and (f + $\Delta F2$) with $\Delta F2 > \Delta F$:

$$
\begin{aligned}\n\text{for} \quad & \langle I(x,y) \rangle_{\Delta F} < \langle I(x,y) \rangle_{\Delta F2}/c \quad \text{or} \quad \langle I(x,y) \rangle_{\Delta F} > c \langle I(x,y) \rangle_{\Delta F2}, \quad R(x,y) = 0 \\
\text{for} \quad & \langle I(x,y) \rangle_{\Delta F2}/c \le \langle I(x,y) \rangle_{\Delta F} \le c \langle I(x,y) \rangle_{\Delta F2}, \quad R(x,y) = 1 \\
& \qquad \text{Eq.S4}\n\end{aligned}
$$

or (*iv*) defined relatively to the mean intensity in any other region surrounding the pixel. A rolling window-averaged intensity thresholding performs well for excluding slowly moving bright (*e.g*. aggregates or oligomers) or dim (*e.g*. non-fluorescent cell organelles) regions from ICS analysis.

Spatial-averaged intensity: When structural heterogeneities in the imaged sample are dynamic from one frame to the next, the spatially averaged intensity image, $\langle I \rangle_{\mathcal{M}}$, where ΔL is the size of the spatial averaging window in each dimension in pixels, is useful. Again, every pixel is compared with I_{min} and I_{max} , to generate R with size (X -*ΔL*)×(*Y-ΔL*)×*F*:

$$
for \quad \langle I(x,y)\rangle_{\Delta L} < I_{min} \quad \text{or} \quad \langle I(x,y)\rangle_{\Delta L} > I_{max}, \quad R(x,y) = 0
$$
\n
$$
for \quad I_{min} \le \langle I(x,y)\rangle_{\Delta L} \le I_{max}, \quad R(x,y) = 1 \tag{Eq. S5}
$$

We found it best to define I_{min} and I_{max} relatively to a larger spatially average image, $\langle I \rangle_{\Delta L2}$, where $\Delta L2 > \Delta L$ is the averaging window size per dimension.

$$
\begin{aligned}\n\text{for} \quad & \langle I(x,y) \rangle_{\Delta L} < \langle I(x,y) \rangle_{\Delta L2}/c \quad \text{or} \quad \langle I(x,y) \rangle_{\Delta L} > c \langle I(x,y) \rangle_{\Delta l2}, \quad R(x,y) = 0 \\
\text{for} \quad & \langle I(x,y) \rangle_{\Delta l2}/c \le \langle I(x,y) \rangle_{\Delta l} \le c \langle I(x,y) \rangle_{\Delta L2}, \quad R(x,y) = 1\n\end{aligned}\n\quad \text{Eq.S6}
$$

Typical values were $\Delta L2 = 30$, $\Delta L = 10$ and $c = 1.5$.

Space-averaged intensity variance: Lastly, the spatial variance image, $\sigma_{\rm M}^2$, where ΔL is the side length of the square in which the variance is calculated, can be compared with, the minimal and maximal allowed variance, σ_{min}^2 and σ_{max}^2 respectively, to generate *R* with a size of (*X-ΔL*)×(*Y-ΔL*)×*F*:

$$
for \quad \sigma_{\Delta L}^2 < \sigma_{min}^2 \quad or \quad \sigma_{\Delta L}^2 > \sigma_{max}^2, \qquad R(x, y) = 0
$$
\n
$$
for \quad \sigma_{min}^2 \le \sigma_{\Delta L}^2 \le \sigma_{max}^2, \qquad R(x, y) = 1 \qquad \qquad \text{Eq.S7}
$$

We found it best to define σ_{min}^2 and σ_{max}^2 relatively to σ_{AL2}^2 , where $\Delta L2 > \Delta L$:

$$
for \quad \sigma_{\Delta L}^2 < \sigma_{\Delta L 2}^2/c \quad \text{or} \quad \sigma_{\Delta L}^2 > c \sigma_{\Delta L 2}^2, \qquad R(x, y) = 0
$$
\n
$$
for \quad \sigma_{\Delta L 2}^2/c \le \sigma_{\Delta L}^2 \le c \sigma_{\Delta L 2}^2, \qquad R(x, y) = 1 \qquad \qquad \text{Eq.S8}
$$

Typical values were $\Delta L2 = 30$, $\Delta L = 10$ and $c = 1.5$. Since the $\sigma_{\Delta L2}^2 / \sigma_{\Delta L}^2$ ratio is typically larger than the $\langle I \rangle_{\Delta L2}/\langle I \rangle_{\Delta L}$ ratio, variance-based thresholding can be slightly more sensitive. Intensity and variance thresholding allow removal of dynamic bright (*e.g.* fluorescent aggregates or oligomers) or dim (*e.g.* non-fluorescent vesicles) regions from ICS analysis.

Simulations for confined diffusion

Random motion of particles was simulated using a pseudo-random number generator based on the commonly used Mersenne Twister algorithm (1). The smallest simulation interval was set to 1 µs. Random photon emission was also ensured by the pseudo-random number generator, based on the particle's brightness and its position relative to the focus. The focus shape was approximated by a 2D Gaussian with a focal size *ω^r* of 200 nm. The restriction to 2D movement was done to increase the local concentration and thus reduce the total calculation time of the simulation. The molecular brightness was 100 kHz. During the simulation, the focus position was moved to emulate the raster scanning. The total area scanned was 250×250 pixels or 12.5 μ m × 12.5 μ m, with pixel, line and frame times of 12 μ s, 3 ms and 750 ms, respectively. Consequently, the pixel size was 50 nm. In total, 2000 particles per condition were simulated for a total of 100 frames. Upon exiting the simulation box, particles were reentered on the opposite side. Since this might lead to artifacts in the correlation function, the simulation box was increased to $15 \mu m$ per dimension, thus limiting the border effects. For each simulation two different particle types were simulated. The first type of particles was confined to small round compartments and moved with a diffusion coefficient of $2 \mu m^2/s$. The rest of the particles diffused freely around these confinements with $D = 10 \mu m^2/s$.

Simulations for diffusion pseudo-maps

The same algorithms as in the previous section were employed, with the exception that the diffusion coefficient or, more precisely, the step sizes of the particles depended on their spatial position, defined by an input diffusion map. This spatial diffusion distribution was generated using a map of random numbers that was smoothed with a Gaussian blur and rescaled to an appropriate diffusion range (Fig. S4*A*). The resolution of the map was 5 nm. The molecular brightness of the particles was 10 kHz for the channel used for correlation analysis and 100 kHz for the one used for generating the ROIs.

Supporting Results

Diffusion in confinements

In order to test the minimal size of compartments in/around which diffusion can still be accurately quantified with ARICS, simulations with known parameters were employed. Four different diameters of circular confinements were simulated: 200 nm, 400 nm, 800 nm, and 1600 nm (Fig. S3*A, from top to bottom*), corresponding to 1, 2 4, and 8 times the focus size. The confinements covered approximately 10% of the total image area. Concentration inside and outside were chosen such that the brightness inside the confinements was 4-5 times higher than in the surrounding space. The average count rate of all simulations was in the range of 75-80 kHz. Pixels with an average count rate of 70 kHz and less were attributed to the free component (Fig. S3*A*, *red regions*), while all pixels with more than 100 kHz were assumed to belong to the confinements (Fig. S3*A*, *blue regions*). The intermediate border regions with 70-100 kHz were omitted from further analysis.

SACFs for diffusion outside the confinements showed a similar shape for all conditions (Fig. S3*B*). Quantitatively, a deviation of *D* from the simulated value was more pronounced at smaller confinement sizes, but always less than 10% (Fig. S3*D*). Additionally, the reflective nature of the confinements might further contribute to the decreased diffusion.

SACFs for confined diffusion, on the other hand, were more affected by the confinement size (Fig. S3*C*). The SACFs exhibited a 300-500-nm dip along the fast scanning axis, with the depth decreasing for larger sizes and almost vanishing at confinement diameters that were 8 times the focus size. This dip is most likely caused by the confinement and the reflective borders and not by the ARICS algorithm itself. Quantitatively, for confinement sizes up to 400 nm, *D* was larger than the set value (Fig S3*D*). This is again caused by problems in correctly assigning the pixels so that the correlation functions still contain contributions from the freely diffusion component. Interestingly, in the simulations with confinements that were four time larger than the focus (800 nm), the individual compartments were large enough that miss-assignment no longer contributed to the correlation function, but small enough such that the confinement still significantly affected the mobility. This lead to an apparent *D* that was even lower than expected. For the largest sizes (1600 nm), the diffusion coefficient can be recovered to within less than 5% of the expected value.

Together, these results show that ARICS can reliably probe diffusion in compartments down to a factor of 4-8 times the focus size, which in practice means 600-1200 nm for a realistic focus size of 150 nm. This limit can be further decreased by decreasing the focus size, *e.g.* by using STED-RICS (2). However, another limit to the quantitative analysis, not specific to the ARICS algorithm, is the actual influence of confinements of the diffusion itself.

Diffusion pseudo-maps

In order to test the validity of the diffusion pseudo-map generation procedure, simulations with known parameters were employed. The differences in the diffusion coefficients in the different parts of the simulated image resulted in corresponding differences in concentration and, therefore, also in count rate (Fig. S4*A*). Just as described in the Results part of the main text, these differences in signal intensity were used to sort the pixels into five ROIs. A separate channel with higher brightness was used for this segmentation, to limit crosstalk between the selection procedure and the correlations. The segmentation was based on the count rate in a 5×5 pixel and 5-frame moving average (Fig. S4*B*). The additional averaging over multiple frames was needed due to the low concentrations and strong concentration fluctuations. The original diffusion map and the pseudo diffusion map generated using ARICS are shown in Fig. S4*C* and *D*. There is excellent agreement between the two images. However, as the map has gradual diffusion coefficients but the algorithm only divides the images into only five ROIs, the complete gradient was not recovered. Especially for the highest and the lowest intensity regions, the gradient was flattened by this undersampling. This shows that for each system the number and threshold of the ROIs need to be adjusted individually to ensure a good recovery of the underlying features, while at the same time limit the change of miss-assignment of the individual pixels (especially important when the diffusion and the signal intensity are not strictly correlated).

Supporting Figures

Fig. S1 | Further analysis of the data from Fig 2. (*A*) The average raw-data SACF, color-coded according to the correlation value. (*B*) Best fit of the data from panel *A* to Eq. 14, color-coded using the weighted residuals goodness-of-fit parameter r_w . The best fit does not provide reliable results (see *red data* panels *E* and *F*) because the error on the average SACF is very large. Hence, r_w and the reduced $\chi^2 = 1.39$ are still relatively small. (*C*) The average arbitrary-ROI SACF, color-coded according to the correlation value. (*D*) Best fit of the data from panel *C* to Eq. 14, color-coded using the weighted residuals goodness-of-fit parameter r_w (reduced $\chi^2 = 1.02$). (*E* and *F*) Experimental *G*(*ξ*,0) (*symbols* in panel *E*) and *G*(0,*ψ*) (*symbols* in panel *F*), standard deviation (*error bars*) and *G*fit(*ξ*,0) (*solid lines* in panel *E*) and *G*fit(0,*ψ*) (*solid lines* in panel *F*) corresponding to the data in panels *A* and *B* (*red*) and panels *C* and *D* (*blue*). The average arbitrary-ROI SACF has a much lower error and is described excellently by the fit model. (*Plot on the upper panel*) Weighted residuals *r*w.

Fig. S2 | Further information on Fig. 3. (*A*) Dual-color confocal image of the HeLa cell co-expressing Venus, MyrPalm-mYFP and mCherry. The *pink arrow* points towards the location where the *z*-scan shown in panel *B* was performed. The *pink square* marks the region shown in panel *C* used for the RICS analysis. The scale bar is 5 µm. (*B*) Axial *z*-scan, clearly illustrating the enrichment of MyrPalm-mYFP at the bottom and top cell membrane. The *black arrow* points to the middle of the cell, where imaging for RICS was performed. (*C*) Zoom-in of the *pink square* in panel *A*. Scale bar is 1 μ m.

Fig. S3 | Simulations for different confinement sizes. (*A*) Images of samples containing confinements of varying diameter: (*from top to bottom*) 200 nm, 400 nm, 800 nm and 1600 nm, corresponding to 1, 2, 4 and 8 times the focus size, respectively. Blue regions contain the pixels in the confinements, red regions encompass the surrounding area. Gray pixels at the borders were omitted from further analysis. Scale bars are $2 \mu m$. (*B*) SACFs calculated only using pixels from the surrounding area. (*C*) SACFs calculated with pixels in the confinements. In panels *B* and *C*, the fast scanning axis is shown in on the left, the slow scanning axis on the right. Points show the data, including the s.e.m., solid lines depict the fit. (*D*) Extracted *D* values for different confinement sizes for the free (*red squares*) and confined (*blue circles*) components. Error bars indicate the s.d. of five measurements. Dashed lines show the values used for the simulation.

Fig. S4 | Simulations for diffusion pseudo-map analysis. (*A*) Average fluorescence intensity image of the simulated experiment with 5000 particles with a molecular brightness of 10 kHz. (*B*) Single frame segmented into 5 ROIs. Maximum intensities for selection of the respective ROIs are given in the legend. (*C*) Diffusion map used for the simulations. (*D*) A pseudo-diffusion map reconstructed from the ROI segmentation procedure. The scale bar corresponds to 2 μ m. The color table used for panels *C* and *D* is shown to the right.

Fig. S5 | Comparative analysis of the eGFP-LEDGF/p75 imaging data in Fig. 5 with the Number & Brightness method. (*A*) pixel intensity image averaged over all frames. (*B*) Epsilon (brightness) image. (*C*) The pixel intensity distribution histogram. (*D*) Number image, illustrating similar concentrations as with the ROI segmentation method (*E*). The pointillism-like appearance of the n image is because of low statistics. For the N&B analysis, pixel intensities were pre-processed using a spacetime moving average (3-pixel radius and $\Delta F = 3$) as reported before (3). n and epsilon images were median-filtered (3-by-3).

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