

Supplementary Data

HPLC-based kinetics assay facilitates analysis of systems with multiple reaction products and thermal enzyme denaturation

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$$[\text{Gluc}]_t = K_m W(x)$$

Equation SD-1

$$W(x) \cong (1 + \varepsilon) \left(\ln \left\{ \frac{6 \cdot x}{5 \cdot \ln[(12/5) \cdot (x/\ln(1 + (12/5) \cdot x))]} \right\} \right) - \varepsilon \left(\ln \left\{ \frac{2 \cdot x}{\ln(1 + 2 \cdot x)} \right\} \right)$$

Equation SD-2

$$x = \left(\frac{[\text{Gluc}]_0}{K_m} \right) \exp \left(\frac{[\text{Gluc}]_0 - V_{\max} \cdot t}{K_m} \right)$$

Equation SD-3

$$Y = (K_m) \cdot ((1 + 0.4586887) \cdot (\ln((6 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))) / (5 \cdot \ln((12/5) \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))))) / \ln(1 + (12/5) \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))))) - (0.4586887 \cdot \ln((2 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))) / \ln(1 + (2 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))))))))$$

Equation SD-4. Textual definition of Equation SD-1 (with included Eq. SD-2 and Eq. SD-3) for use in calculating reaction progress curves for $[\text{Gluc}]_t$ in GraphPad Prism 6.0 and other nonlinear regression software. This equation is based on Equation 7 with the improved Lambert W function (Equations 10-11) in Goličnik, M. *Anal. Biochem.* **2010**, 406, 94–96. Initial variable values for nonlinear regression were $[\text{Gluc}]_0 = Y_0 = 500$, $K_m = KM = 1.0$, and $V_{\max} = VMAX = 8.0$.

$$[\text{ITC}]_t = [\text{nitrile}]_t = [\text{Gluc}]_0 - [\text{Gluc}]_t$$

Equation SD-5

$$Y = Y_0 - ((K_m) \cdot ((1 + 0.4586887) \cdot (\ln((6 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))) / (5 \cdot \ln((12/5) \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))))) / \ln(1 + (12/5) \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))))) - (0.4586887 \cdot \ln((2 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))) / \ln(1 + (2 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - (V_{\max} \cdot X))/K_m)))))))))$$

Equation SD-6. Textual definition of Eq. SD-5 (with included Eq. SD-1, Eq. SD-2, and Eq. SD-3) for use in calculating reaction progress curves for $[\text{ITC}]_t$ or $[\text{nitrile}]_t$ in GraphPad Prism 6.0 and other nonlinear regression software. This equation is based on Equation 7 from Goličnik, M. *Anal. Biochem.* **2010**, 406, 94–96. Initial variable values for nonlinear regression were $[\text{Gluc}]_0 = Y_0 = 500$, $K_m = KM = 1.0$, and $V_{\max} = VMAX = 8.0$.

$$V_0 = - \frac{d[\text{Gluc}]}{dt} = \frac{V_{\max} \cdot [\text{Gluc}]_0}{K_m + [\text{Gluc}]_0}$$

Equation SD-7. The Michaelis–Menten equation.

$$Y = (K_m) \cdot ((1 + 0.4586887) \cdot (\ln((6 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - ((V_{\max} \cdot (\exp(-K_D \cdot X))) \cdot X))/K_m)))) / (5 \cdot \ln((12/5) \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - ((V_{\max} \cdot (\exp(-K_D \cdot X))) \cdot X))/K_m)))))) / \ln(1 + (12/5) \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - ((V_{\max} \cdot (\exp(-K_D \cdot X))) \cdot X))/K_m)))))) - (0.4586887 \cdot \ln((2 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - ((V_0 \cdot (\exp(-K_D \cdot X))) \cdot X))/K_m)))) / \ln(1 + (2 \cdot ((Y_0/K_m) \cdot (\exp((Y_0 - ((V_{\max} \cdot (\exp(-K_D \cdot X))) \cdot X))/K_m)))))))))$$

Equation SD-8. Textual definition of Eq. SD-1 (with included Eq. SD-2, Eq. SD-3, and Eq. 1) for use in calculating reaction progress curves of $[\text{Gluc}]_t$ in GraphPad Prism 6.0 and other nonlinear regression software. This equation is based on Equation 7 with the improved Lambert W function (Equations 10-11) in Goličnik, M. *Anal. Biochem.* **2010**, 406, 94–96 and includes a term to account for the first-order denaturation of enzyme (Eq. 1). Initial variable values for nonlinear regression were $[\text{Gluc}]_0 = Y_0 = 250$, $K_m = KM = 500$, $V_{\max} = VMAX = 8.0$, and $k_d = KD = 1 \times 10^{-7}$. The following constraints were placed on nonlinear regression variables: $Y_0 = 0-400$, $KM = 0-1200$, $VMAX = 0-50$, and $KD = 0-0.1$.