

Supplementary Table 11A: Top 50 SNPs in tests of $\mathcal{I}_0^{(g)}$. Tests of $\mathcal{I}_0^{(g)}$ and $\mathcal{M}_0^{(g)}$ were performed for G×R and Main effect models, respectively, for 488,200 SNPs of the learning performance scores over the PING sample (n=479). Both models included covariates for status of learning problem diagnosis and first two PCs of genotype data. Learning performance scores were, by construction, uncorrelated with age, sex, household income, and parental education. CHR, POS, MAF, and MA are chromosome, position, minor allele frequency (within PING sample), and minor allele, respectively, for given SNP. SNPs were genotyped with the Illumina Human660W-Quad Beadchip array and their positions correspond to HG build 19. F-tests of $\mathcal{I}_0^{(g)}$ were performed with statistic having 2 and 472 df. F-tests of $\mathcal{M}_0^{(g)}$ were performed with statistic having 1 and 474 df. F-tests of $\mathcal{M}_{0;PNC}^{(g)}$ were performed with statistic having 1 and 2,322 df. Information gain are for respective G×R and Main effect models over the PING sample (n=479). It represents in the increase in adjusted R² for respective model fit over that of the non-genetic base model including only the covariates.

Rank	SNP	CHR	POS	MAF	MA	P-values		Information Gain		Estimates				Standard errors			
						$\mathcal{I}_0^{(g)}$	$\mathcal{M}_0^{(g)}$	GxR	Main	α_g	β_g	γ_g	θ_g	α_g	β_g	γ_g	θ_g
1	rs11633708	15	87050708	0.47	G	3.49E-08	2.28E-06	7.9	4.3	-0.807	-0.899	0.437	-0.198	0.179	0.219	0.135	0.041
2	rs4243100	15	87037559	0.45	A	4.01E-08	6.54E-05	7.8	3.0	0.244	1.025	-0.534	0.168	0.173	0.214	0.132	0.042
3	rs11853362	15	87057124	0.44	A	1.70E-07	7.66E-05	7.3	2.9	-0.898	-1.001	0.514	-0.172	0.182	0.223	0.137	0.043
4	rs11632104	15	87049894	0.45	A	2.04E-07	2.95E-04	7.2	2.4	0.241	1.009	-0.532	0.152	0.174	0.215	0.133	0.042
5	rs4887473	15	87053206	0.45	A	2.04E-07	2.95E-04	7.2	2.4	0.241	1.009	-0.532	0.152	0.174	0.215	0.133	0.042
6	rs2011905	15	87053846	0.45	A	2.11E-07	3.08E-04	7.2	2.4	0.239	1.007	-0.531	0.152	0.174	0.215	0.133	0.042
7	rs6496338	15	86993635	0.48	G	1.79E-06	1.15E-04	6.4	2.8	-0.747	-0.878	0.441	-0.167	0.166	0.227	0.140	0.043
8	rs4887466	15	86995749	0.48	G	1.79E-06	1.15E-04	6.4	2.8	-0.747	-0.878	0.441	-0.167	0.166	0.227	0.140	0.043
9	rs9920533	15	60673192	0.10	A	5.71E-06	1.13E-05	6.0	3.7	-1.172	-0.429	0.477	0.319	0.437	0.378	0.235	0.072
10	rs8042879	15	87093955	0.45	G	9.29E-06	1.03E-05	5.8	3.7	-0.604	-0.620	0.272	-0.191	0.185	0.223	0.138	0.043
11	rs17260000	1	209057061	0.13	G	9.90E-06	9.36E-06	5.7	3.7	0.401	0.335	-0.401	-0.283	0.382	0.331	0.212	0.063
12	rs1533046	2	22594727	0.45	A	1.20E-05	5.06E-06	5.7	4.0	-0.582	-0.241	0.272	0.194	0.188	0.214	0.135	0.042
13	rs10517873	4	166850443	0.09	G	1.32E-05	3.68E-01	5.6	0.0	-2.401	-1.728	1.158	0.067	0.457	0.389	0.246	0.074
14	rs1110413	5	76223856	0.15	A	1.34E-05	2.71E-03	5.6	1.6	0.959	1.336	-0.740	0.185	0.382	0.332	0.212	0.061
15	rs10220773	15	86903044	0.48	A	1.52E-05	7.84E-04	5.6	2.1	-0.732	-0.838	0.423	-0.151	0.167	0.232	0.143	0.045
16	rs12482611	21	39417989	0.10	A	1.87E-05	2.83E-01	5.5	0.0	1.781	1.839	-1.137	0.074	0.471	0.392	0.250	0.069
17	rs10281072	7	11535903	0.08	G	2.08E-05	1.77E-04	5.5	2.6	-1.833	-1.553	0.815	-0.302	0.563	0.460	0.294	0.080
18	rs1341458	1	241583612	0.48	C	2.13E-05	2.19E-01	5.4	0.1	0.420	0.955	-0.640	-0.053	0.188	0.226	0.141	0.043
19	rs6536942	4	166986194	0.08	G	2.95E-05	2.51E-05	5.3	3.4	-0.925	-0.870	0.328	-0.338	0.486	0.419	0.260	0.079
20	rs10749321	10	121207961	0.41	A	3.09E-05	1.35E-01	5.3	0.3	-1.077	-0.875	0.603	0.065	0.205	0.227	0.141	0.044
21	rs9406769	9	19995895	0.16	A	4.37E-05	4.75E-05	5.2	3.1	0.379	0.850	-0.398	0.230	0.316	0.292	0.181	0.056
22	rs13142383	4	133561788	0.37	G	4.63E-05	6.63E-06	5.1	3.9	-0.250	0.245	-0.034	0.196	0.206	0.229	0.144	0.043
23	rs13134454	4	133530329	0.37	G	4.86E-05	6.93E-06	5.1	3.9	-0.204	0.297	-0.068	0.194	0.203	0.225	0.141	0.043
24	rs12054223	3	137528884	0.07	G	4.97E-05	2.32E-02	5.1	0.8	1.584	1.790	-1.022	0.192	0.512	0.428	0.270	0.084
25	rs6665593	1	2140261	0.14	A	5.09E-05	2.57E-04	5.1	2.5	-1.084	-0.946	0.457	-0.223	0.340	0.309	0.193	0.061

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26	rs5766424	22	45502533	0.50	G	5.17E-05	3.70E-04	5.1	2.4	0.056	0.407	-0.366	-0.162	0.186	0.243	0.152	0.045
27	rs2279604	5	34687911	0.35	G	5.29E-05	6.01E-06	5.1	3.9	-0.378	-0.312	0.073	-0.206	0.226	0.240	0.152	0.045
28	rs6958208	7	48984046	0.24	G	5.44E-05	1.40E-04	5.1	2.7	-0.835	-0.320	0.339	0.195	0.278	0.267	0.170	0.051
29	rs1875341	4	7237092	0.44	A	5.70E-05	1.12E-01	5.1	0.3	-0.949	-0.981	0.582	-0.068	0.184	0.223	0.139	0.043
30	rs10771958	12	32638162	0.33	C	5.73E-05	6.01E-03	5.1	1.3	-0.971	-0.698	0.523	0.126	0.215	0.235	0.147	0.046
31	rs17793675	9	82869545	0.09	G	5.79E-05	5.45E-04	5.1	2.2	0.908	1.297	-0.667	0.261	0.464	0.392	0.249	0.075
32	rs9406760	9	19971287	0.47	A	5.86E-05	2.43E-02	5.1	0.8	0.260	0.911	-0.517	0.098	0.183	0.220	0.138	0.043
33	rs17050441	4	139402774	0.14	G	6.17E-05	5.07E-03	5.0	1.4	-1.441	-0.863	0.665	0.177	0.351	0.316	0.197	0.063
34	rs11726117	4	113353285	0.35	A	7.12E-05	6.52E-05	5.0	3.0	-0.545	-0.060	0.157	0.176	0.222	0.234	0.147	0.044
35	rs2003880	8	6788102	0.18	A	7.17E-05	5.93E-02	5.0	0.5	0.935	1.263	-0.742	0.105	0.329	0.297	0.187	0.056
36	rs699096	5	162100311	0.50	G	7.53E-05	7.51E-01	5.0	-0.2	-0.925	-0.964	0.622	0.014	0.173	0.225	0.141	0.044
37	rs17014035	1	206841857	0.20	C	7.76E-05	2.47E-02	4.9	0.8	-1.266	-0.881	0.623	0.116	0.274	0.265	0.164	0.052
38	rs2060060	15	86900992	0.49	G	7.99E-05	1.59E-03	4.9	1.8	-0.699	-0.767	0.387	-0.142	0.170	0.231	0.143	0.045
39	rs4609816	15	87102625	0.47	A	8.20E-05	4.25E-05	4.9	3.2	-0.534	-0.519	0.219	-0.174	0.181	0.220	0.136	0.042
40	rs9407951	9	19959158	0.50	G	8.47E-05	2.84E-02	4.9	0.8	-0.790	-0.881	0.500	-0.094	0.164	0.217	0.137	0.043
41	rs1032725	12	32641200	0.33	G	8.65E-05	6.96E-03	4.9	1.3	-0.947	-0.671	0.505	0.122	0.213	0.232	0.146	0.045
42	rs417342	4	139282314	0.39	G	8.65E-05	5.12E-02	4.9	0.6	0.290	0.897	-0.512	0.083	0.188	0.216	0.135	0.043
43	rs17484454	4	149209008	0.27	G	8.72E-05	4.96E-05	4.9	3.1	-0.721	-0.646	0.305	-0.192	0.258	0.253	0.165	0.047
44	rs7597588	2	216486659	0.11	A	8.97E-05	5.08E-04	4.9	2.2	-1.433	-0.769	0.630	0.239	0.439	0.382	0.237	0.068
45	rs1071501	16	54131681	0.18	G	9.02E-05	5.53E-03	4.9	1.4	0.822	1.172	-0.656	0.153	0.357	0.314	0.200	0.055
46	rs872072	14	20859013	0.45	A	9.45E-05	1.75E-03	4.9	1.8	-0.742	-0.542	0.425	0.139	0.178	0.228	0.140	0.044
47	rs1550883	8	94305178	0.13	G	9.49E-05	3.51E-02	4.9	0.7	-1.706	-1.389	0.794	-0.133	0.384	0.338	0.210	0.063
48	rs2339518	2	22598926	0.45	G	9.51E-05	4.15E-05	4.9	3.2	-0.579	-0.250	0.265	0.173	0.191	0.217	0.137	0.042
49	rs12771377	10	22717779	0.06	G	9.68E-05	7.37E-03	4.9	1.3	-2.065	-1.757	0.940	-0.253	0.545	0.466	0.288	0.094
50	rs12421046	11	36354576	0.06	C	9.68E-05	4.38E-05	4.9	3.2	0.631	0.366	-0.487	-0.396	0.592	0.487	0.309	0.096