

Unexpected changes in the population of coordination isomers for the lanthanide ion complexes of DOTMA-tetraglycinate

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Supporting Information

HPLC profiles

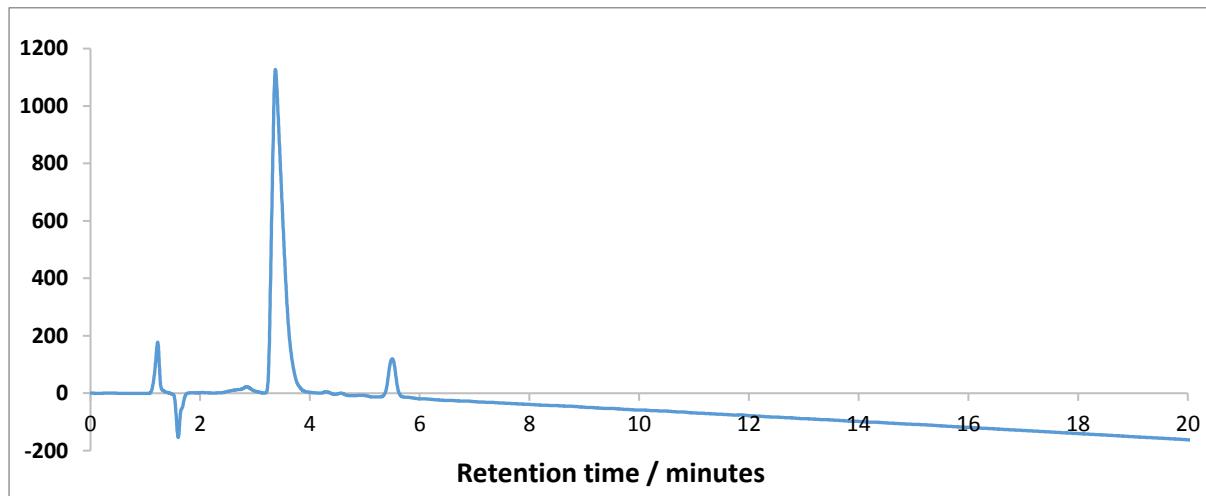


Figure S1: Analytical HPLC profile for DOTMA-Gly₄ (scheme 1); solvent gradient conditions - 98% Water (1% TFA): 2% ACN to 40% water (1% TFA): 60% ACN in 30 min, 215 nm.

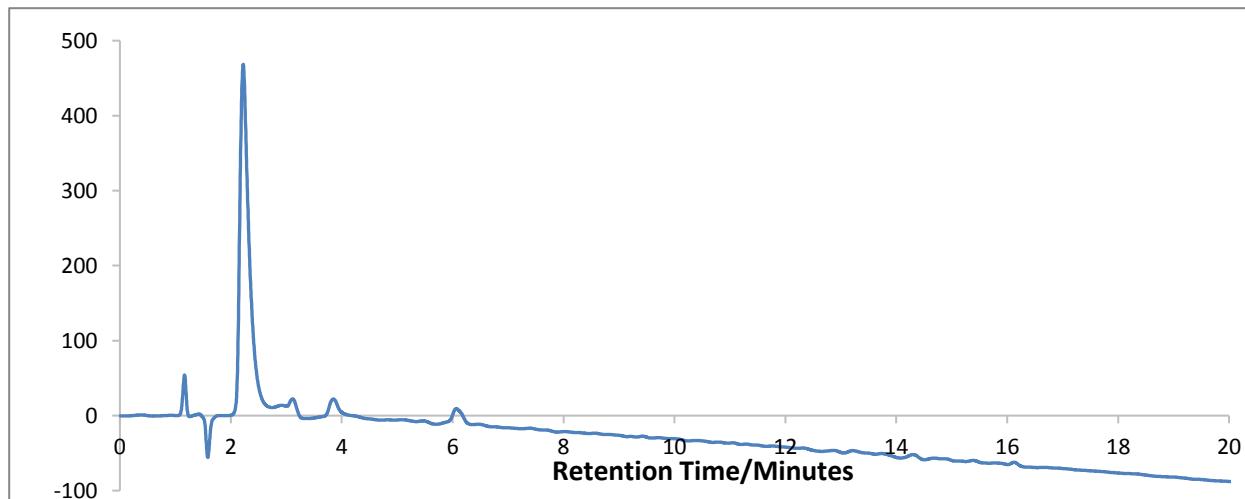


Figure S2: Analytical HPLC profile for ErDOTMA-Gly₄; solvent gradient conditions - 98% Water (1% TFA): 2% ACN to 40% water (1% TFA): 60% ACN in 30 min.

NMR Measurements ¹H NMR spectra and CEST spectra were recorded on a 400 MHz Bruker Avance III spectrometer. High resolution ¹H NMR samples were prepared either in D₂O or H₂O. Samples for studies were prepared by dissolving the appropriate amount of agent in water and the pH was adjusted to neutral pH.

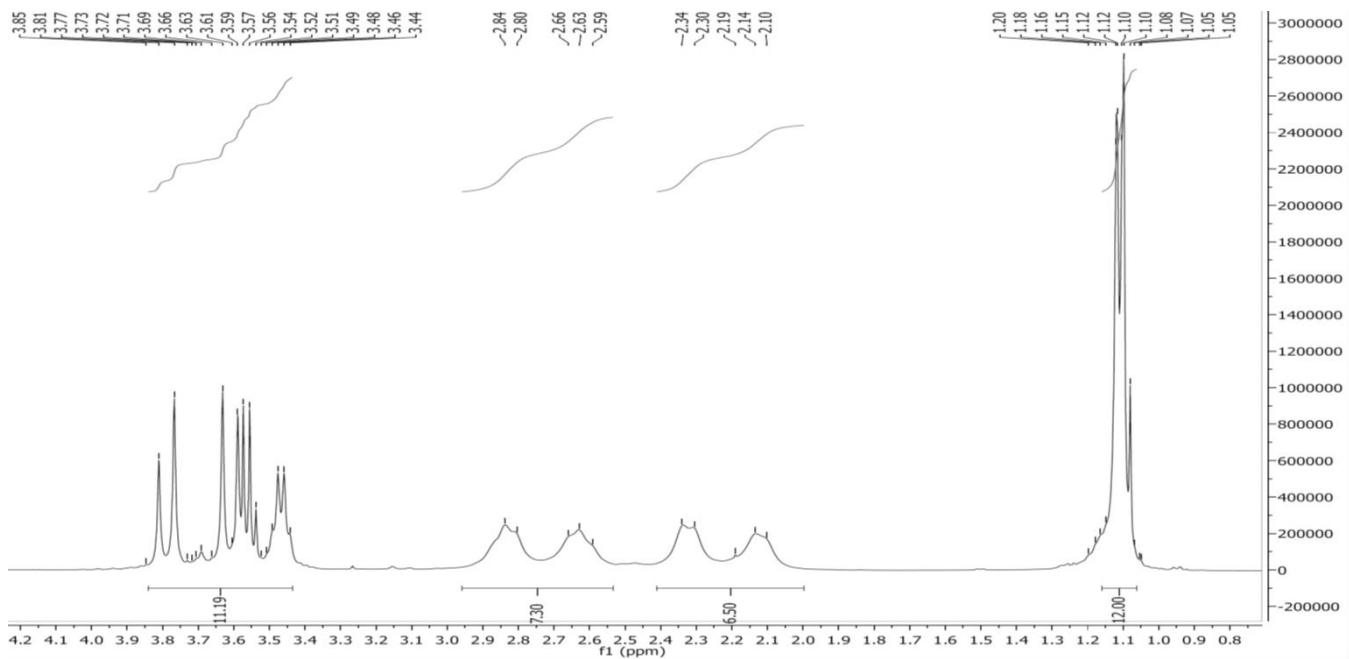


Figure S3. ^1H NMR spectra of the ethyl ester of DOTMA-(gly)₄.

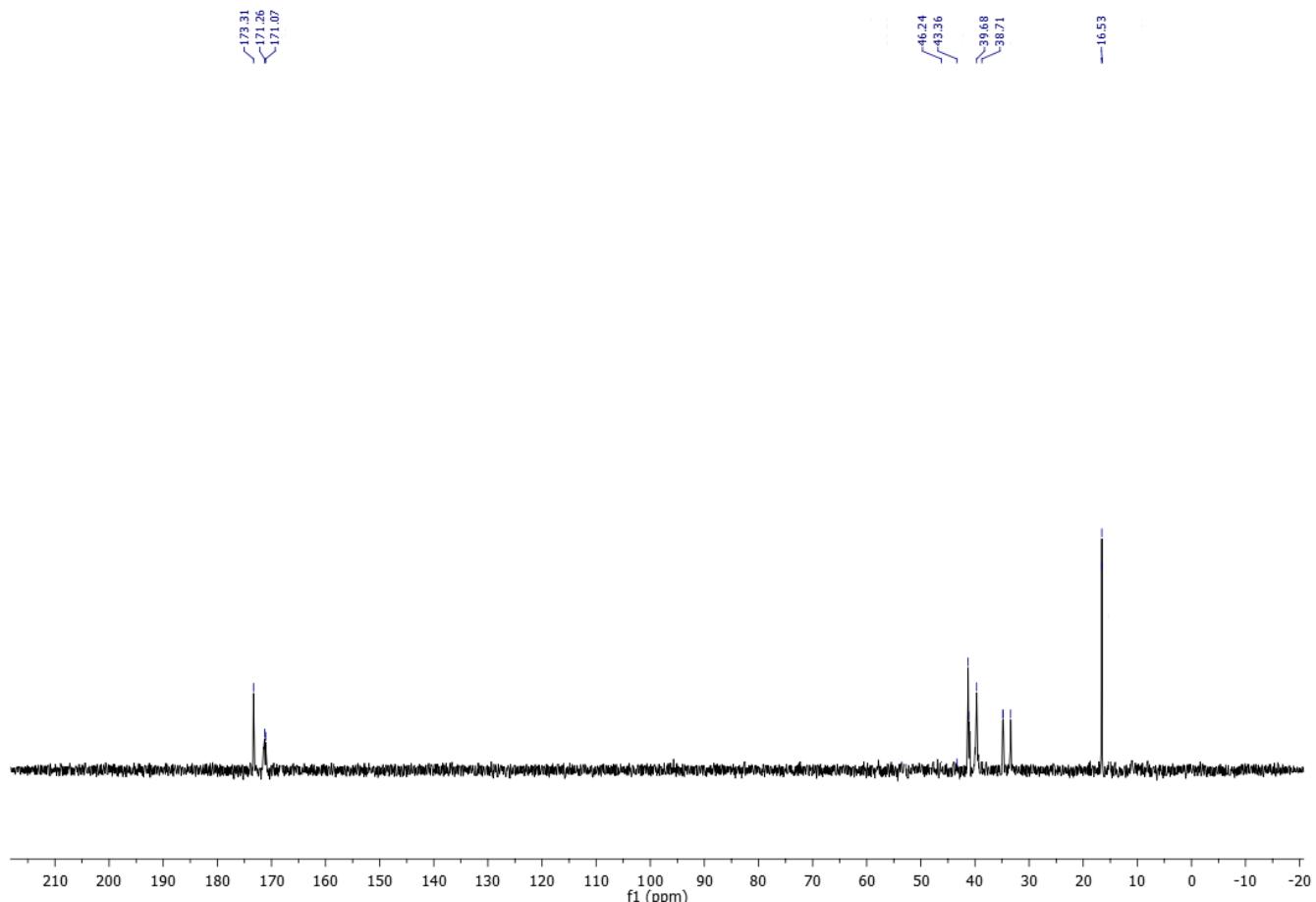


Figure S4. ^{13}C NMR spectra of the ethyl ester of DOTMA-(gly)₄.

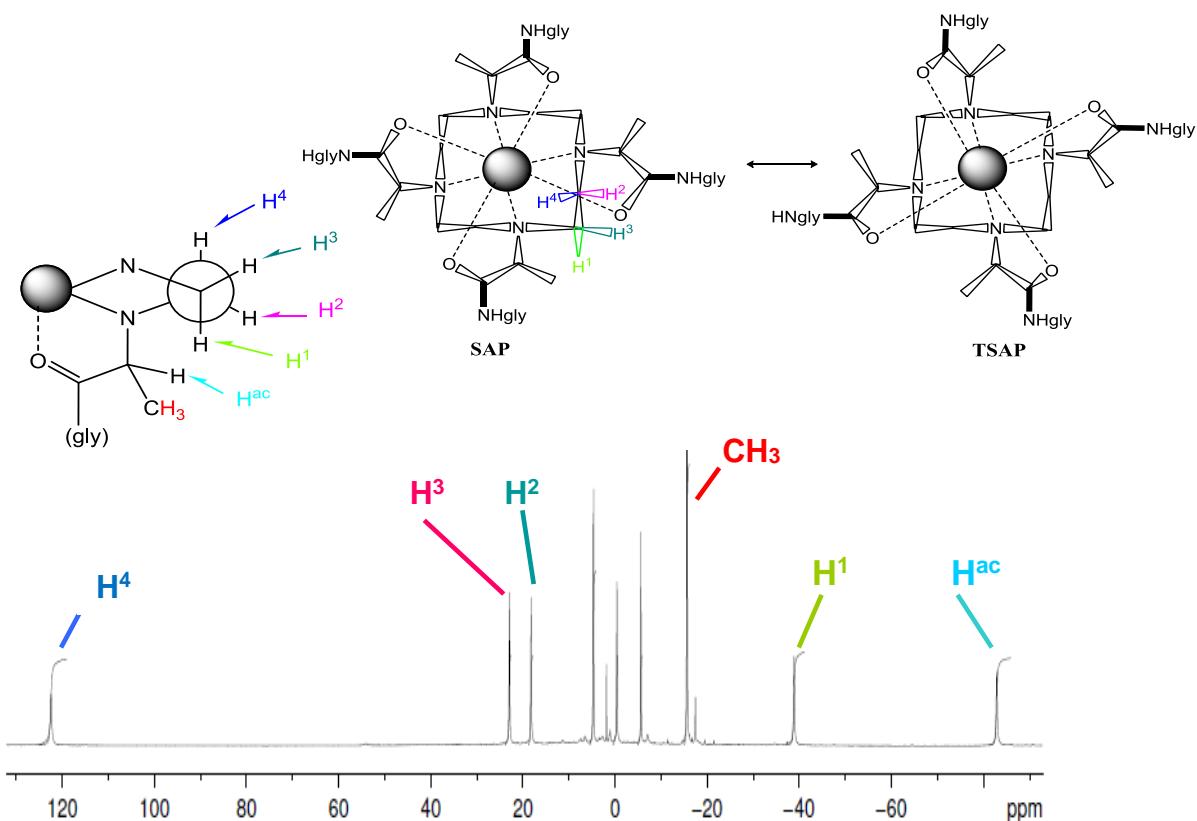


Figure S5. **Top:** A description of lanthanide coordination in the SAP and TSAP geometry isomers of the macrocyclic ring protons in the LnDOTMA-(gly)₄ complexes. **Bottom:** Assignment of the peaks in the ¹H NMR spectrum of YbDOTMA-(gly)₄. The spectrum was recorded in H₂O at 298 K (pH 7.4). The notation scheme H¹ and H⁴ for *axial* protons, H² and H³ for *equatorial* protons of macrocyclic ring and H^{ac} for an acetamide proton was used.

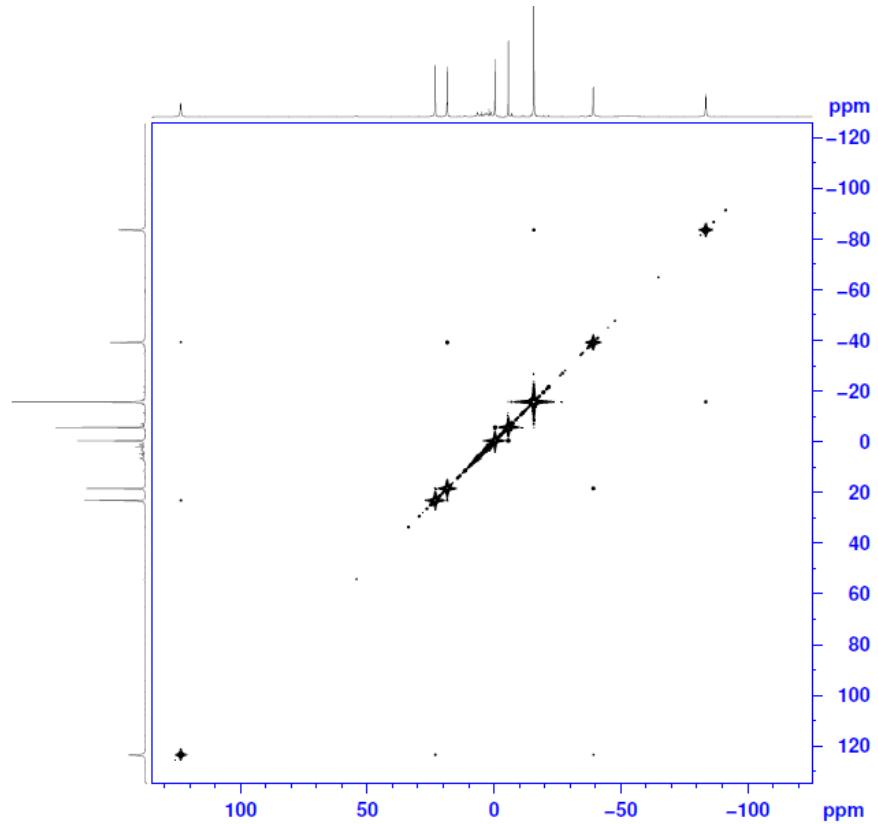


Figure S6. ¹H COSY spectrum of YbDOTMA-(gly)₄ recorded at 400 MHz and 298 K in D₂O (pD 7.4).

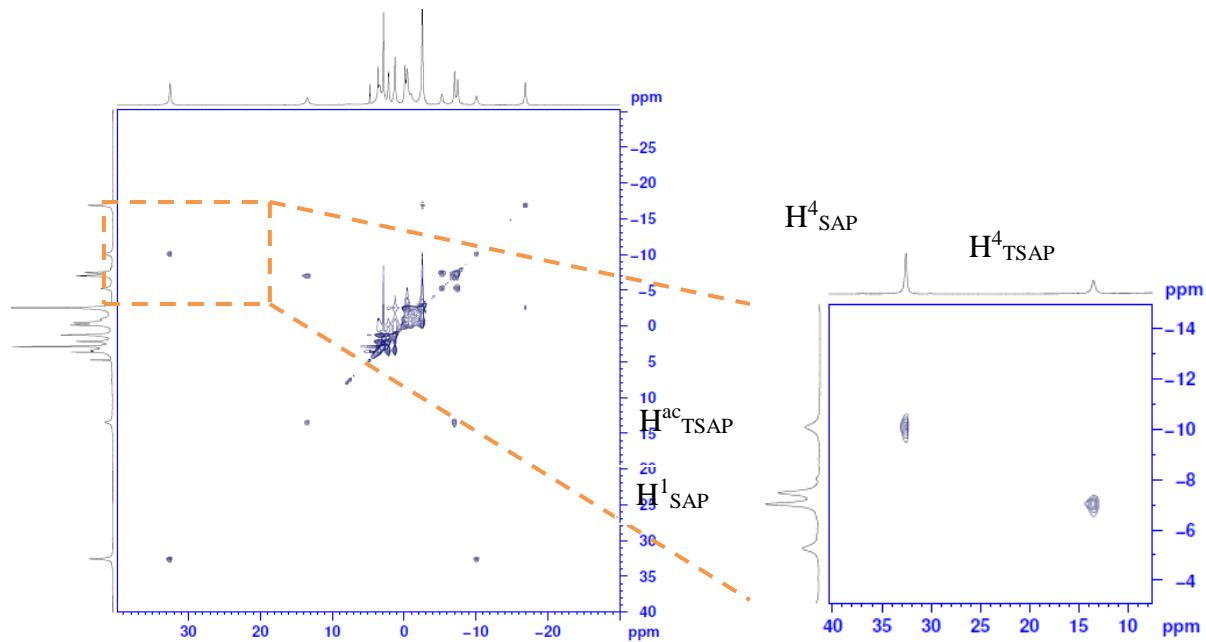


Figure S7. ¹H EXSY spectrum of EuDOTMA-(gly)₄ recorded at 400 MHz and 298 K in D₂O (pD 7.4). EXSY spectrum shows the SAP and TSAP transition of cyclen protons.

CH₃

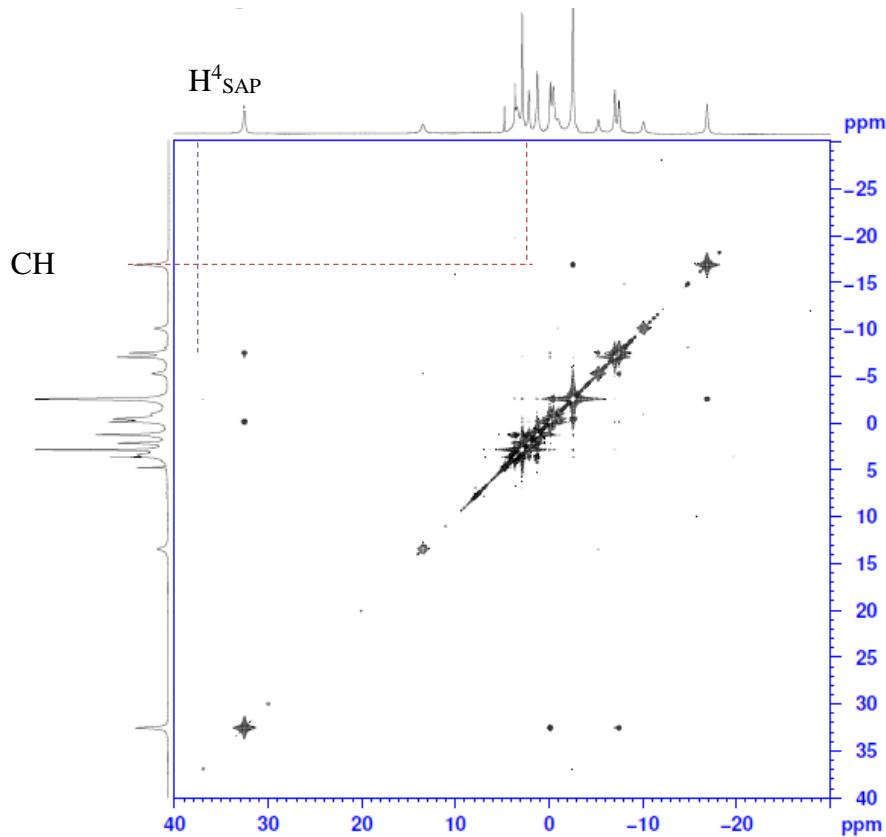


Figure S8. ¹H COSY spectrum of EuDOTMA-(gly)₄ recorded at 400 MHz and 298 K in D₂O (pD 7.4).

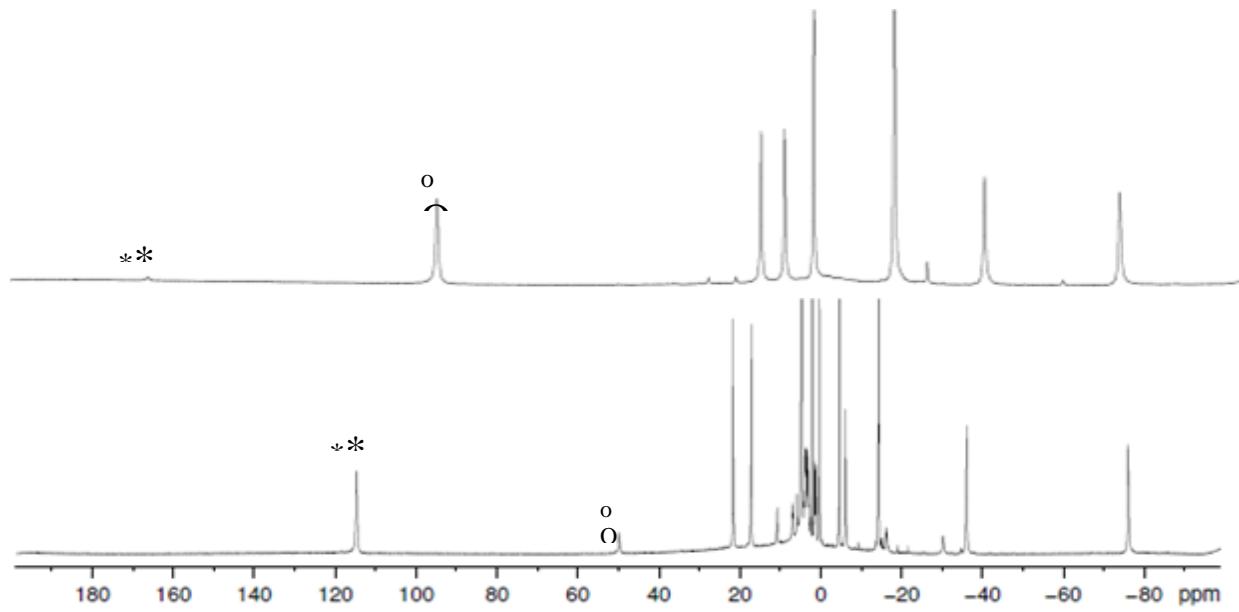


Figure S9. ¹H NMR spectra of YbDOTMA (Top) and YbDOTMA-(gly)₄ (Bottom). All spectra were recorded in D₂O at 298 K and 400 MHz. (*) is denoted for the axial H⁴ protons of the SAP isomer and (o) is for the H⁴ protons of the TSAP isomer.

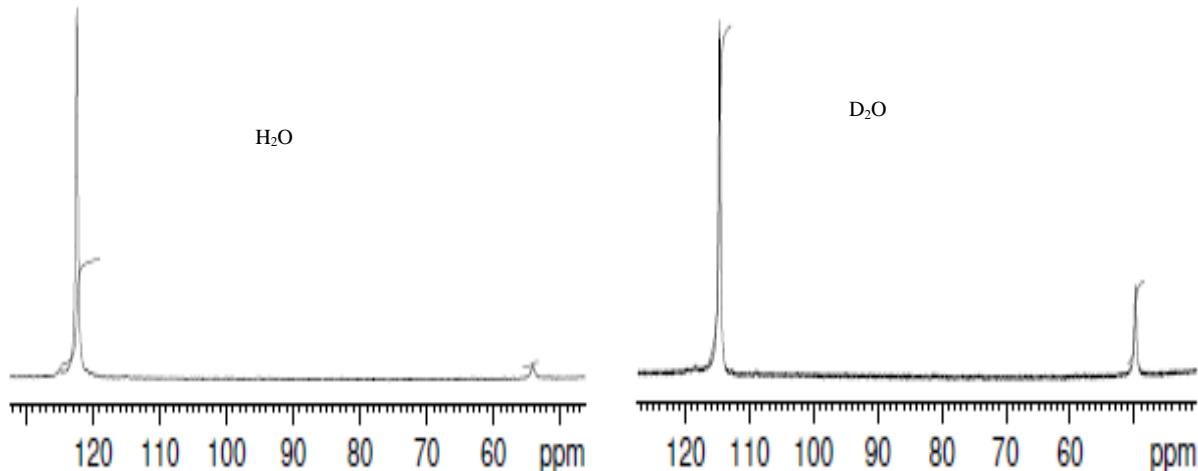


Figure S10. ^1H NMR spectra of YbDOTMA-(gly)_4 in H_2O and D_2O , focusing on the highly shifted H^4 resonances. The most highly shifted downfield resonance in each spectrum corresponds to the SAP isomer. The smaller resonance near 50-55 ppm reflects the TSAP isomer.

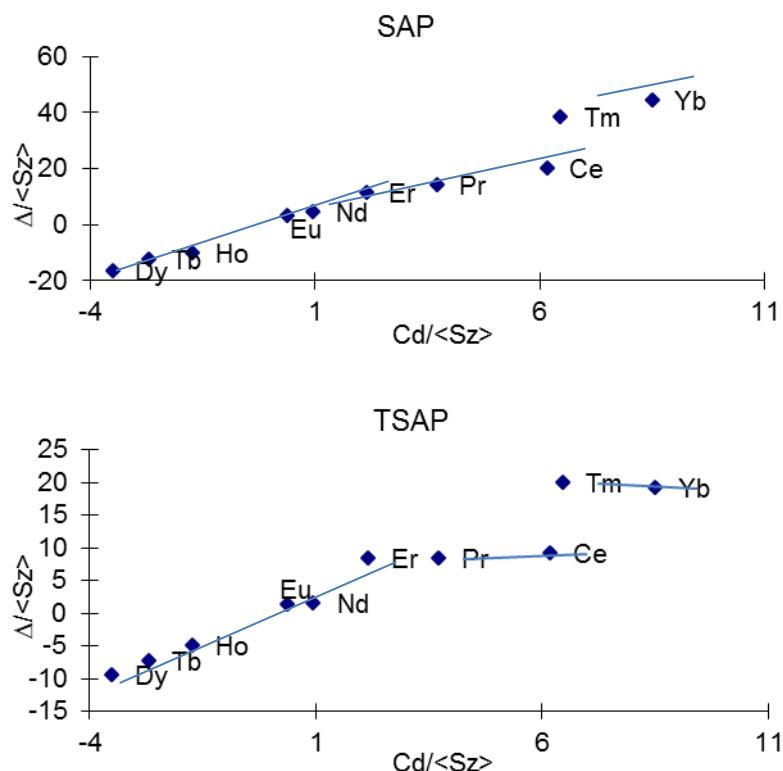


Figure S11. Plot of $<\text{S}_z>$ vs $\text{C}_d/<\text{S}_z>$ for the axial proton (H^4) of the SAP (left) isomeric forms in DOTMA-(gly)₄ chelates.

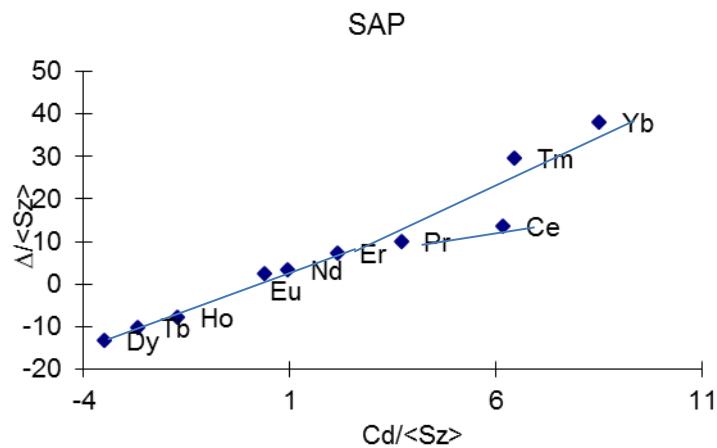


Figure S12. Plot of $\langle S_z \rangle$ vs $C_d/\langle S_z \rangle$ for the axial proton (H^4) of the DOTA-(gly)₄ chelates.

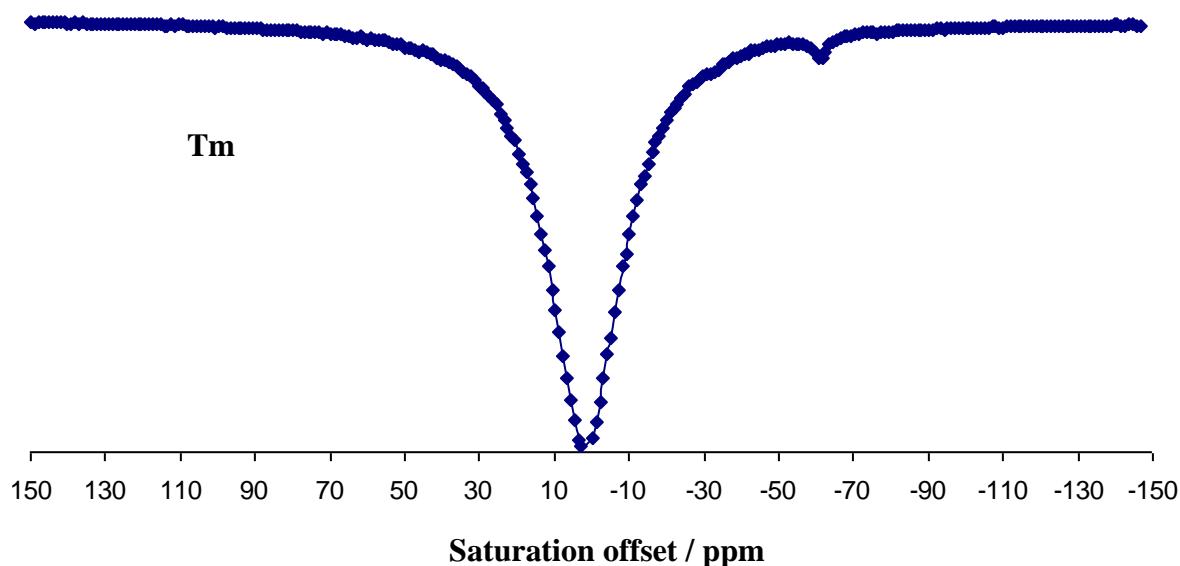


Figure S13. CEST spectra of 30 mM TmDOTMA-(gly)₄ complex at $B_1 = 800$ Hz (90% $D_2O + 10\%$ H_2O , 37°C)

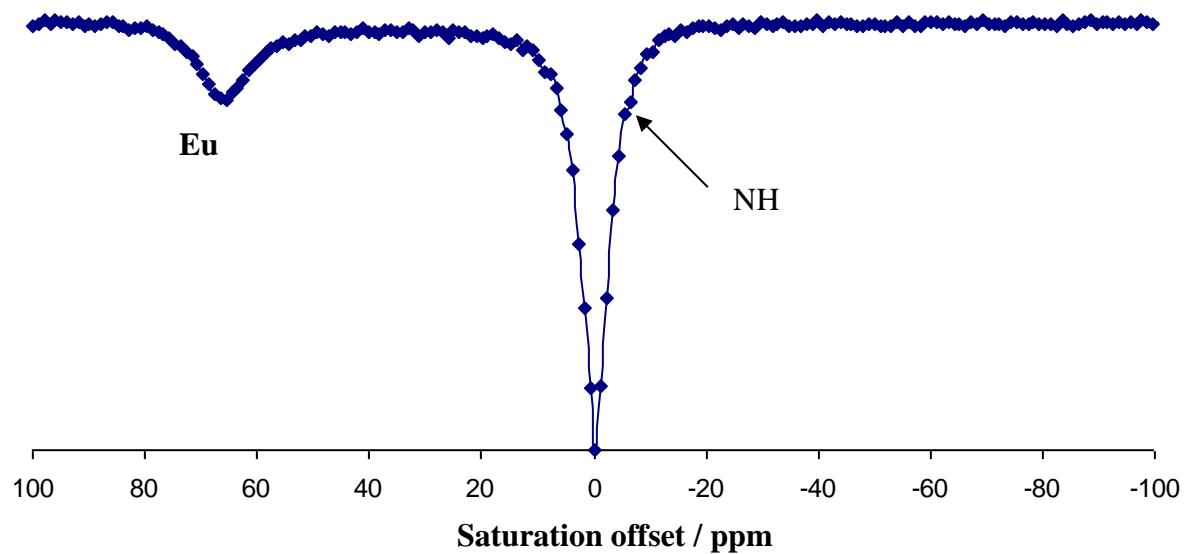


Figure S14. CEST spectra of 40 mM EuDOTMA-(gly)₄ complex at $B_1 = 400$ Hz

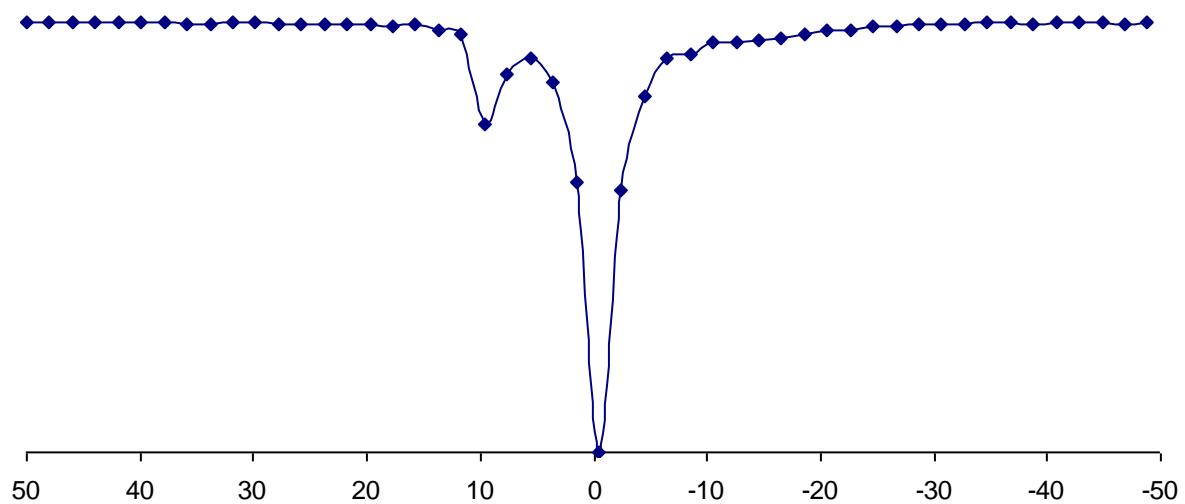


Figure S15. CEST spectra of 80mM SmDOTMA-(gly)₄ complex at $B_1 = 100$ Hz

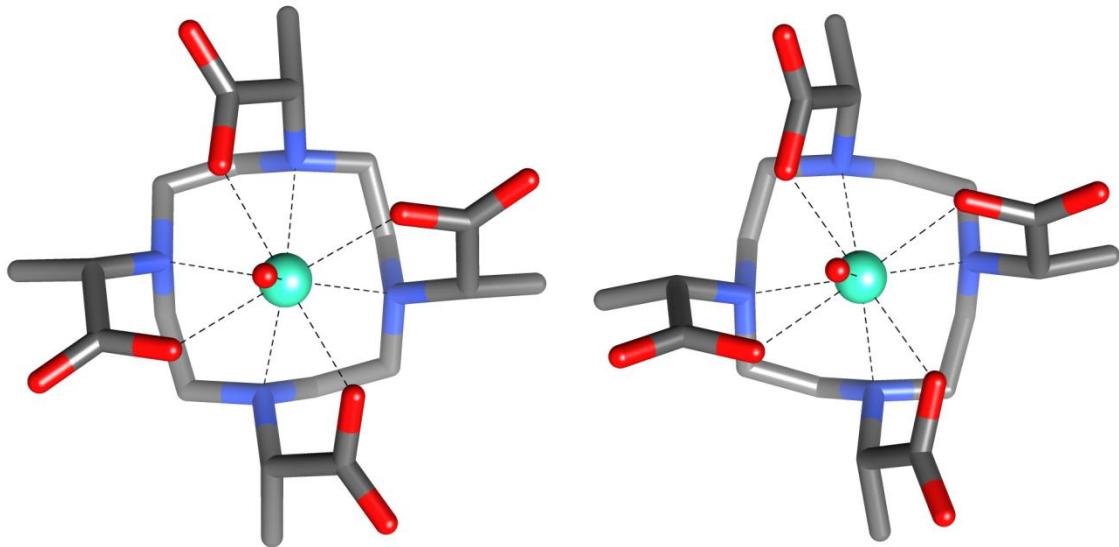


Figure S16. Optimized geometry of the SAP (left) and TSAP (right) isomers of $[\text{Gd}(\text{DOTMA})(\text{H}_2\text{O})]^-$ obtained with DFT calculations performed in aqueous solution at the TPSSh/LCRECP/6-31G(d,p) level. Hydrogen atoms were omitted for simplicity.

Optimized geometries. Geometry optimizations of the $[\text{Gd}(\text{DOTMA})(\text{H}_2\text{O})]^-$ complex provide two energy minima that correspond to the capped square antiprismatic (SAP) and capped twisted-square antiprismatic diastereoisomers (TSAP, Figure S14). The structural parameters calculated both in the gas-phase and in aqueous solution are shown in Table S3. The distances between the Gd^{3+} ion and the donor atoms of the ligand calculated for the two isomers are quite similar. As observed previously for related systems, the inclusion of solvent effects (water) provokes an important shortening of the Ln-N distances,ⁱ which is also reflected in a shortening of the distance between the Gd^{3+} ion and the plane defined by the four N atoms of the macrocycle (Ln-P_N) and a lengthening of the distance to the plane defined by the four O atoms of the ligand coordinated to the metal ion (Ln-P_O). The structural parameters calculated in aqueous solution for the TSAP isomer present an excellent agreement with the values observed in the X-ray crystal structure reported by Woods et al.ⁱⁱ The main discrepancy between

the experimental and calculated geometries concerns the distance between the metal ion and the oxygen atom of the inner-sphere water molecule, which is overestimated by calculations by ~ 0.17 Å. However, this is not surprising considering that the Gd-O_{water} distances observed in the solid state have been shown to be very sensitive the environment of the coordinated water molecule. For instance, the Gd-O_{water} distances observed for different salts of the [Gd(DOTAM)(H₂O)]³⁺ complex were shown to differ up to 0.12 Å depending upon the anions present in the crystal lattice.ⁱⁱⁱ Furthermore, it has been recently shown that the accurate calculation of accurate Gd-O_{water} distances and ¹⁷O hyperfine coupling constants of coordinated water molecules requires the explicit inclusion of at least two second-sphere water molecules.^{iv} The Gd-O_{water} distances calculated for the SAP isomer are shorter than those obtained for the TSAP one, in line with the faster water exchange rates usually observed for SAP isomers in DOTA-like complexes.ⁱ

Table S1. Geometrical parameters of calculated structures for the two isomers of [Gd(DOTMA)(H₂O)]⁻ and [Gd(DOTMA-gly₄)(H₂O)]⁻.^a

| | DOTMA | | | | | DOTMA-gly ₄ | |
|---|-----------|-----------|-----------|-----------|---------------|------------------------|-----------|
| | SAP | | TSAP | | TSAP exptl | SAP | TSAP |
| | Gas-phase | Water | Gas-phase | Water | | Water | Water |
| Gd-N | 2.736(25) | 2.686(10) | 2.756(25) | 2.684(11) | 2.681(23) | 2.670(4) | 2.689(7) |
| Gd-O | 2.363(35) | 2.374(23) | 2.367(36) | 2.382(26) | 2.373(18) | 2.399(11) | 2.402(15) |
| Gd-Ow | 2.565 | 2.616 | 2.556 | 2.671 | 2.500 | 2.520 | 2.546 |
| ω^b | 39.6(4) | 38.4(4) | -28.0(4) | -26.8(3) | -26.2(8) | 38.3(6) | -25.9(8) |
| Gd-P _O ^c | 0.648 | 0.769 | 0.700 | 0.847 | 0.794 | 0.776 | 0.871 |
| Gd-P _N ^d | 1.702 | 1.611 | 1.755 | 1.630 | 1.663 | 1.572 | 1.618 |
| P _O -P _N ^e | 2.350 | 2.381 | 2.456 | 2.477 | 2.457 | 2.348 | 2.489 |

^a Distances (Å); The average values of bond distances to the oxygen atoms of the P_O (Gd-O) and P_N (Gd-N) planes are reported with standard deviations within parentheses; O_w, oxygen atom of the inner-sphere water molecule. ^b Mean twist angle (°) of the upper and lower planes. ^c Distance between the lanthanide and the least-squares plane defined by the coordinated oxygen atoms, P_O. ^d Distance between the lanthanide and the least-squares plane defined by the nitrogen atoms, P_N. ^e Distance between the centroids of the P_O and P_N planes.

The calculations performed for the Gd^{3+} complex were extended to several Ln^{3+} ions across the lanthanide series. The average Ln-O and Ln-N distances involving the eight donor atoms of the macrocycle decrease quadratically along the series as a consequence of the lanthanide contraction, in agreement with previous experimentalⁱⁱ and theoretical^{iii, iv, v} studies.

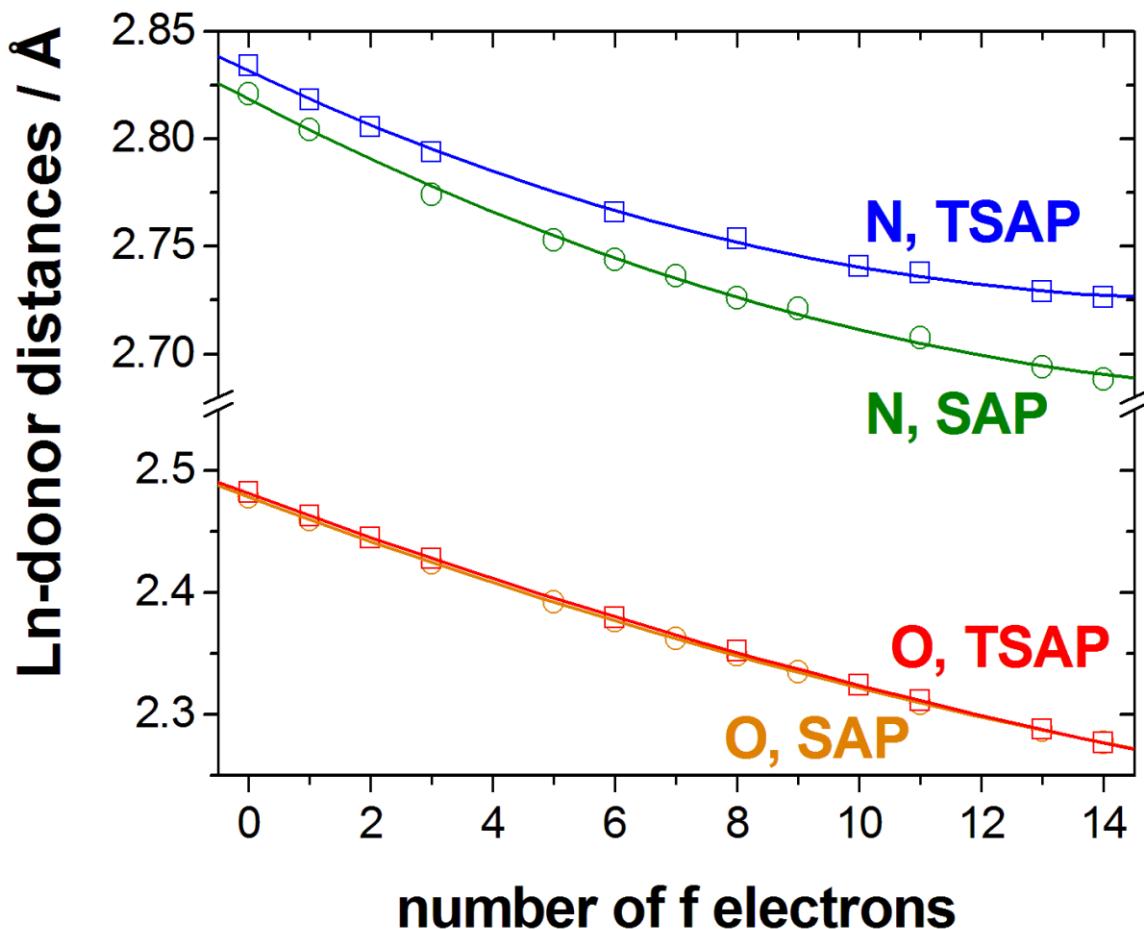


Figure S17. Variation of the average $\text{Ln}-\text{O}_{\text{amide}}$ and $\text{Ln}-\text{N}$ distances of the metal coordination environments for the $[\text{Ln}(\text{DOTMA})(\text{H}_2\text{O})]^\cdot$ complexes at the TPSSh/LCRECP/6-31G(d,p) level (results obtained in the gas-phase). The solid lines represent quadratic fits of the data to $y = a + bx + cx^2$ with $R^2 > 0.99$.

The relative energies of the SAP and TSAP isomers of $[\text{Ln}(\text{DOTMA})(\text{H}_2\text{O})]^\cdot$ were first investigated in the gas-phase (Figure S16, see also Table S4). According to our calculations the TSAP isomer is

more stable than the SAP one only for the light Ln^{3+} ions ($\text{Ln} = \text{La}, \text{Ce}$), which is in contrast with the experimental evidence. A stabilization of the SAP isomer occurs across the whole lanthanide series from La^{3+} to Lu^{3+} . To understand the reasons for this trend we calculated the counterpoise-corrected binding energies (BEs) of the ligands, as well as the relative strain energies (SEs) of the macrocyclic ligand across the series (Figure 17, see also Table S4). Our calculations provide positive relative binding energies (R_{BE}) calculated as $R_{\text{BE}} = \text{BE}_{\text{TSAP}} - \text{BE}_{\text{SAP}}$. The actual binding energies are negative, and therefore a positive binding energy indicates that the binding energy of the ligand is higher in the case of the SAP form, an effect that is magnified across the lanthanide series as the positive charge density of the metal ion increases. On the other hand, the relative strain energies $R_{\text{SE}} = \text{LE}_{\text{TSAP}} - \text{LE}_{\text{SAP}}$ (LE_{TSAP} and LE_{SAP} are the ligand energies with the ligand adopting the geometry observed for the TSAP and SAP isomer, respectively) are negative, which indicates that in the SAP isomer the ligand is more strained than in the TSAP form. The R_{SE} values do not experience an important variation along the lanthanide series ($< 0.5 \text{ kcal mol}^{-1}$), while the calculated R_{BEs} present a more important variation ($\sim 1.76 \text{ kcal mol}^{-1}$). The sum of the R_{SE} and R_{BE} values results in an increased stability of the SAP isomer across the series, as reflected by the relative free energies of the two isomers. Thus, the stabilization of the SAP form across the series is mainly the result of the higher binding energy of the ligand to the metal ion for this isomer, which further increases by increasing metal ion density.^{vi, vii}

Table S2. Relative free energies (ΔG°) for the SAP \rightleftharpoons TSAP equilibrium, relative binding energies (BE), relative strain energies of the ligands (SE), and hydration free energies ($\Delta G^\circ_{\text{hyd}}$) ($\text{kcal}\cdot\text{mol}^{-1}$).

| Ln | $\Delta G^{\circ\text{a,b}}$ | $\Delta G^{\circ\text{a,c}}$ | $\Delta G^{\circ\text{a,d}}$ | R_{SE} | R_{BE} | $\Delta G^\circ_{\text{hyd(SAP)}}$ | $\Delta G^\circ_{\text{hyd(TSAP)}}$ |
|----|------------------------------|------------------------------|------------------------------|-----------------|-----------------|------------------------------------|-------------------------------------|
| La | -0.30 | -3.66 | -3.16 | -4.24 | 4.44 | -80.03 | -83.39 |
| Ce | -0.15 | -3.54 | -3.32 | -4.19 | 4.60 | -80.63 | -84.03 |
| Nd | 0.14 | -3.60 | -4.03 | -4.32 | 5.08 | -79.80 | -83.54 |
| Eu | 0.34 | -3.11 | -2.97 | -3.84 | 5.11 | -79.97 | -83.42 |
| Tb | 0.73 | -2.88 | -2.61 | -4.00 | 5.67 | -79.48 | -83.09 |
| Er | 1.48 | -1.86 | -2.55 | -3.73 | 5.89 | -79.23 | -82.57 |
| Yb | 1.80 | -1.60 | -3.35 | -3.83 | 6.05 | -79.56 | -82.96 |
| Lu | 1.80 | -1.37 | -3.71 | -3.78 | 6.20 | -79.49 | -82.67 |

^a Relative free energies are defined as $\Delta G^\circ = G^\circ_{\text{TSAP}} - G^\circ_{\text{SAP}}$; Note that the actual values of the complex free energies are negative, and therefore a positive relative free energy indicates that the SAP isomer is more stable than the TSAP one. The

same holds for the relative strain energies, as the actual ligand energies are negative. ^b Values obtained from calculations in the gas-phase. ^c Values calculated in aqueous solution using geometries optimized in the gas phase. ^d Values obtained in solution using geometries optimized in solution. ^e Obtained using the geometries optimized in the gas phase.

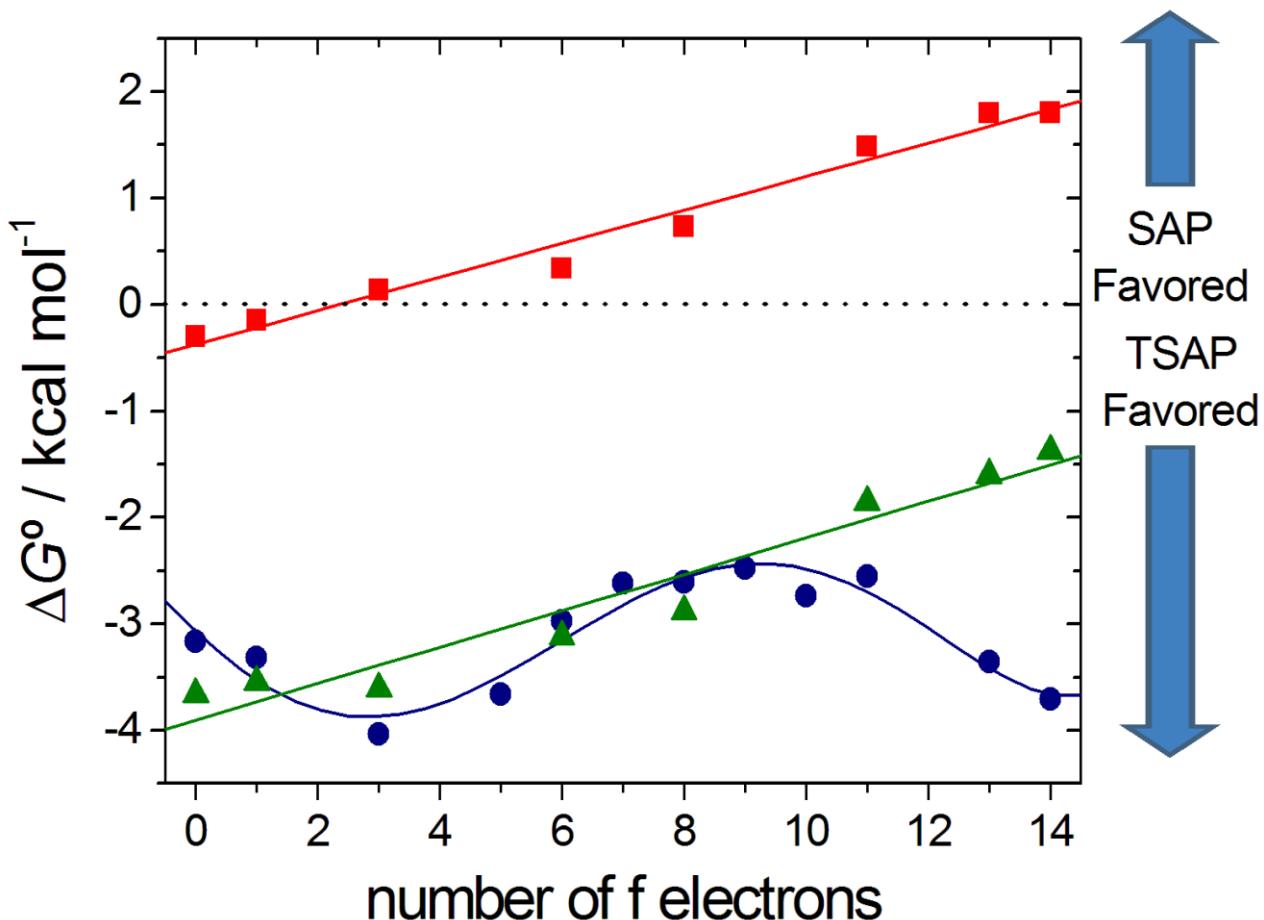


Figure S18. Relative energies of the SAP and TSAP isomers of $[\text{Ln}(\text{DOTMA})(\text{H}_2\text{O})]$ complexes calculated in the gas-phase (red squares), in aqueous solution using geometries optimized in the gas phase (green triangles) and in aqueous solution using geometries optimized in water (blue circles). The solid lines are used only as a guide for the eye.

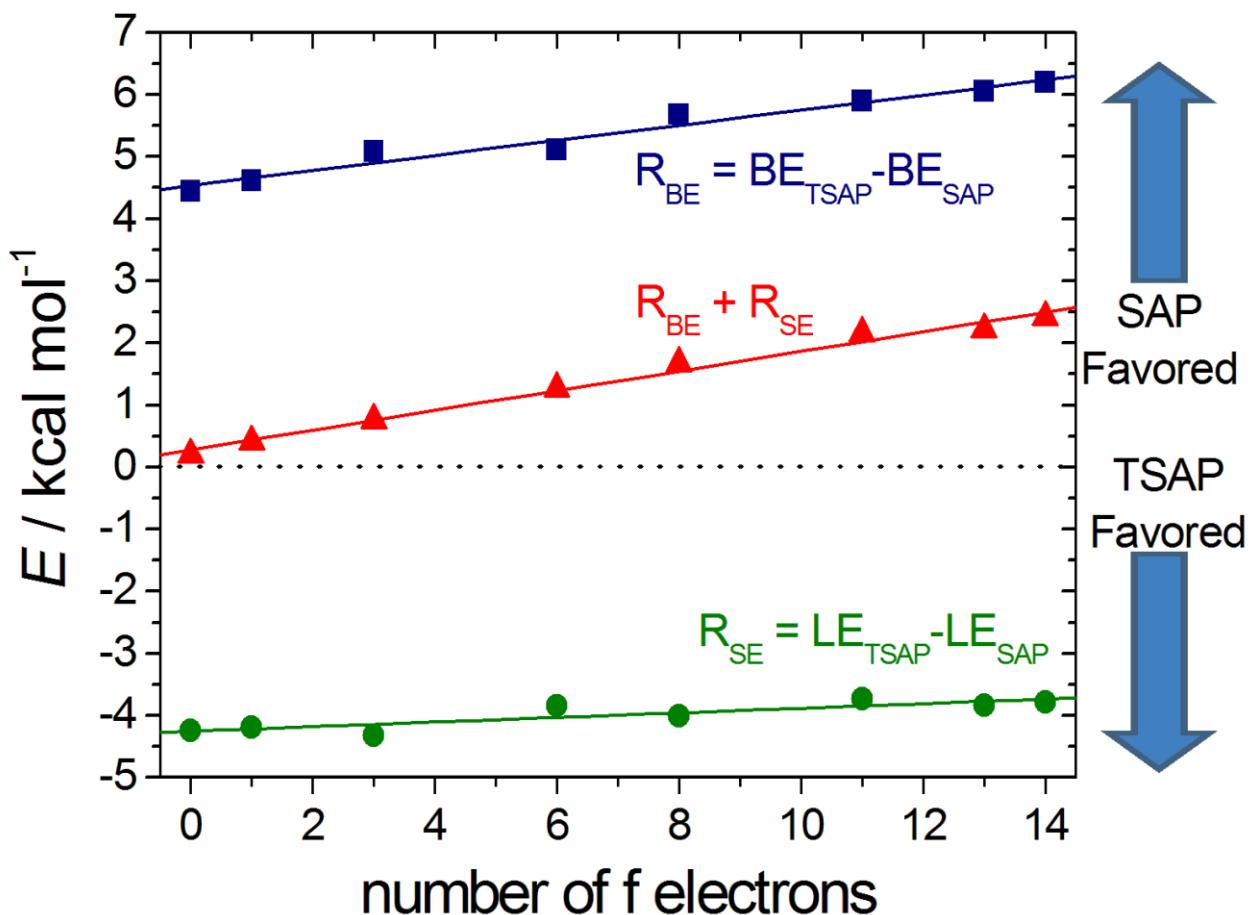


Figure S19. Relative energies binding energies (R_{BE}) and strain energies (R_{SE}) of the ligands in the SAP and TSAP isomers of $[\text{Ln(DOTMA)}(\text{H}_2\text{O})]^-$ complexes calculated in the gas-phase. The solid lines are used only as a guide for the eye.

The effects of the solvent on the relative energies of the SAP and TSAP isomers of $[\text{Ln(DOTMA)}(\text{H}_2\text{O})]^-$ were first evaluated by calculating the hydration free energies of the two isomers using the structures optimized in the gas-phase. The hydration free energies of the TSAP isomer are considerably more negative than those of the SAP form ($3.2 - 3.7 \text{ kcal mol}^{-1}$, Table 2), and therefore the inclusion of solvent effects provokes an important stabilization of the TSAP form, which becomes the most stable one along the whole lanthanide series from La^{3+} to Lu^{3+} . This is related to the higher dipole moment of the TSAP complexes ($26.3-26.8 D$ in aqueous solution at the TPSSh/LCRECP/6-31G(d,p)

level) compared with the SAP isomers ($21.1\text{-}22.6 D$). However, the hydration free energies of a given isomer do not change significantly across the series, and thus the SAP isomer becomes steadily more stable across the series. This is in contrast to the experimental trend, which shows a stabilization of the SAP isomer on proceeding to the right across the series with a maximum around Tb, with a stabilization of the TSAP isomer for the heaviest Ln^{3+} ions. Thus, we conclude that a structural change results in a significant change of the contributions related to the geometry relaxation passing from vacuo to solution. This is confirmed by the relative free energies of the two isomers obtained from geometry optimizations in aqueous solution, which show a bell-like shape with a maximum population of the SAP isomer around Tb (Figure 3).

Table S3. Yb^{3+} -induced paramagnetic shifts in Ybdota-(gly)_4 versus the geometric factors obtained from DFT calculations.^[a]

| | θ (°) | r (Å) | $(3\cos^2\theta - 1)/r^3$ | δ_{para} (ppm) |
|-------------|--------------|-------|---------------------------|------------------------------|
| H1ax | 22.93 | 3.744 | 0.0294 | 95.8 |
| H1eq | 45.57 | 4.459 | 0.00531 | 20.9 |
| H2ax | 67.14 | 3.721 | -0.0106 | -35.3 |
| H2eq | 47.11 | 4.467 | 0.00437 | 17.9 |
| H3ax | 87.49 | 3.588 | -0.0215 | -62.4 |
| H3eq | 72.88 | 4.382 | -0.00880 | -29.8 |
| H4a | 123.47 | 5.129 | -0.000649 | -3.1 |
| H4b | 108.68 | 5.207 | -0.00490 | -7.1 |

^[a] The diamagnetic contribution was assumed to be 3.0 ppm for all nuclei. Negative paramagnetic shifts correspond to shifts to higher field.

Table S4. Yb³⁺-induced paramagnetic shifts in Ybdotma-(gly)₄ versus the geometric factors obtained from DFT calculations.^[a]

| | θ (°) | r (Å) | $(3\cos^2\theta - 1)/r^3$ | δ_{para} (ppm) |
|-------------|--------------|-------|---------------------------|------------------------------|
| H1ax | 23.27 | 3.685 | 0.0306 | 119.5 |
| H1eq | 45.75 | 4.438 | 0.00527 | 19.9 |
| H2ax | 67.69 | 3.726 | -0.0110 | -41.9 |
| H2eq | 47.23 | 4.442 | 0.00432 | 15.2 |
| H3 | 89.71 | 3.456 | -0.0242 | -85.9 |
| H4a | 123.66 | 5.089 | -0.000595 | -3.4 |
| H4b | 108.15 | 5.149 | -0.00519 | -8.6 |
| Me | 73.36 | 5.346 | -0.00455 | -18.3 |

^[a] The diamagnetic contribution was assumed to be 3.0 ppm for all nuclei. Negative paramagnetic shifts correspond to shifts to higher field.

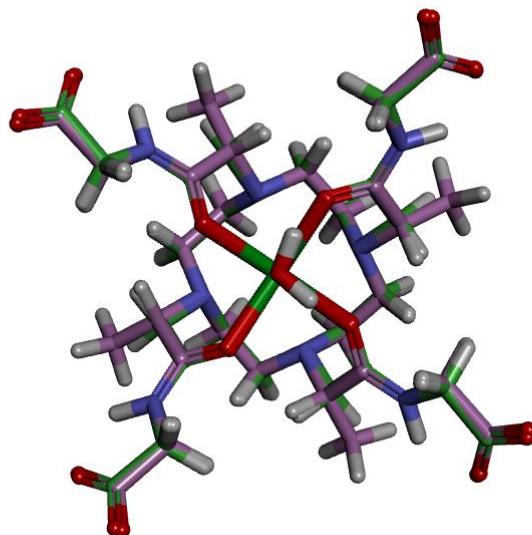


Figure S20. Overlay of the DFT structures obtained for the SAP isomers of YbDOTMA-(gly)₄ and YbDOTA-(gly)₄ complexes obtained with DFT calculations.

Table S5. [La(DOTMA)(H₂O)]⁺ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -2.120791 | 0.740775 | 0.880792 |
| 2 | 6 | -1.627660 | 1.632164 | 1.964225 |
| 3 | 6 | -0.584166 | 2.661298 | 1.527786 |
| 4 | 7 | 0.662987 | 2.059009 | 0.973243 |
| 5 | 6 | 1.483959 | 1.513698 | 2.086956 |
| 6 | 6 | 2.548637 | 0.501996 | 1.664653 |
| 7 | 7 | 1.985587 | -0.727388 | 1.035993 |
| 8 | 6 | 1.412882 | -1.608097 | 2.089454 |
| 9 | 6 | 0.407326 | -2.643277 | 1.583605 |
| 10 | 7 | -0.796726 | -2.047073 | 0.937116 |
| 11 | 6 | -1.701962 | -1.497433 | 1.981745 |
| 12 | 6 | -2.729420 | -0.482793 | 1.476852 |
| 13 | 6 | -3.109174 | 1.406743 | -0.035114 |
| 14 | 6 | -2.405057 | 2.402984 | -0.995534 |
| 15 | 8 | -1.296792 | 1.977483 | -1.513231 |
| 16 | 6 | 1.386499 | 3.083926 | 0.145325 |
| 17 | 6 | 2.413259 | 2.436396 | -0.818781 |
| 18 | 8 | 2.028239 | 1.323854 | -1.366927 |
| 19 | 6 | 3.047284 | -1.399530 | 0.210651 |
| 20 | 6 | 2.436027 | -2.415341 | -0.787983 |
| 21 | 8 | 1.363175 | -2.008639 | -1.398776 |
| 22 | 6 | -1.453695 | -3.071778 | 0.054915 |
| 23 | 6 | -2.417745 | -2.404630 | -0.961795 |
| 24 | 8 | -1.972618 | -1.318862 | -1.508323 |
| 25 | 1 | -1.205907 | 0.992647 | 2.743460 |
| 26 | 1 | -2.458523 | 2.172021 | 2.439016 |
| 27 | 1 | -1.003258 | 3.320058 | 0.764875 |
| 28 | 1 | -0.358641 | 3.288493 | 2.403395 |
| 29 | 1 | 0.795825 | 1.042605 | 2.793120 |
| 30 | 1 | 1.978000 | 2.322366 | 2.642787 |
| 31 | 1 | 3.237947 | 0.955804 | 0.949361 |
| 32 | 1 | 3.136499 | 0.249888 | 2.559872 |
| 33 | 1 | 0.930824 | -0.960972 | 2.826065 |
| 34 | 1 | 2.207186 | -2.139353 | 2.631353 |
| 35 | 1 | 0.883085 | -3.302336 | 0.854625 |
| 36 | 1 | 0.121716 | -3.268863 | 2.442463 |
| 37 | 1 | -1.071405 | -1.028270 | 2.740561 |
| 38 | 1 | -2.242114 | -2.303428 | 2.497564 |
| 39 | 1 | -3.367797 | -0.940872 | 0.719325 |
| 40 | 1 | -3.377594 | -0.223361 | 2.327227 |
| 41 | 1 | -3.444232 | 0.592951 | -0.690886 |
| 42 | 1 | 0.608382 | 3.470595 | -0.525495 |
| 43 | 1 | 3.427352 | -0.592842 | -0.429542 |
| 44 | 1 | -0.629039 | -3.449412 | -0.563221 |
| 45 | 8 | 0.957783 | -0.152082 | -3.334395 |
| 46 | 1 | 1.629438 | 0.496976 | -3.031057 |
| 47 | 1 | 1.324989 | -1.016927 | -3.050957 |
| 48 | 6 | -2.104100 | -4.251291 | 0.784524 |
| 49 | 1 | -3.015267 | -3.957550 | 1.311985 |
| 50 | 1 | -2.388681 | -5.004012 | 0.046116 |
| 51 | 1 | -1.413830 | -4.714093 | 1.496851 |
| 52 | 6 | 4.217384 | -1.997825 | 0.998155 |
| 53 | 1 | 4.992318 | -2.303850 | 0.292139 |
| 54 | 1 | 4.652020 | -1.268280 | 1.688422 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 55 | 1 | 3.924071 | -2.888112 | 1.560518 |
| 56 | 6 | 1.990156 | 4.257026 | 0.925097 |
| 57 | 1 | 2.859616 | 3.956469 | 1.515885 |
| 58 | 1 | 2.329852 | 5.011127 | 0.212320 |
| 59 | 1 | 1.253238 | 4.718970 | 1.589286 |
| 60 | 6 | -4.330317 | 2.025135 | 0.652269 |
| 61 | 1 | -4.075312 | 2.929673 | 1.210395 |
| 62 | 1 | -5.054481 | 2.313163 | -0.112941 |
| 63 | 1 | -4.813135 | 1.313324 | 1.329366 |
| 64 | 8 | 3.005246 | -3.496707 | -0.987818 |
| 65 | 8 | 3.479774 | 3.018940 | -1.055123 |
| 66 | 8 | -2.944695 | 3.491688 | -1.245300 |
| 67 | 8 | -3.500482 | -2.950864 | -1.222691 |
| 68 | 57 | -0.012777 | 0.001113 | -0.757818 |

E(RTPSSh) = -1710.8181719 Hartree

Zero-point correction = 0.560676 Hartree/particle

Sum of electronic and thermal Energies = -1710.221705 Hartree

Sum of electronic and thermal Enthalpies = -1710.220761 Hartree

Sum of electronic and thermal Free Energies = -1710.322691 Hartree

Table S6. [Ce(DOTMA)(H₂O)]⁺ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 2.062752 | 0.849897 | 0.895351 |
| 2 | 6 | 2.273546 | -0.139765 | 1.983869 |
| 3 | 6 | 2.189932 | -1.602921 | 1.546503 |
| 4 | 7 | 0.862772 | -1.979824 | 0.979457 |
| 5 | 6 | -0.119485 | -2.151905 | 2.083254 |
| 6 | 6 | -1.584558 | -2.078405 | 1.651245 |
| 7 | 7 | -1.962541 | -0.773624 | 1.034601 |
| 8 | 6 | -2.120319 | 0.254243 | 2.098726 |
| 9 | 6 | -2.057369 | 1.699152 | 1.600922 |
| 10 | 7 | -0.762388 | 2.047831 | 0.948142 |
| 11 | 6 | 0.276750 | 2.261285 | 1.990431 |
| 12 | 6 | 1.717701 | 2.175186 | 1.484691 |
| 13 | 6 | 3.245972 | 0.992000 | -0.020618 |
| 14 | 6 | 3.368113 | -0.219528 | -0.984181 |
| 15 | 8 | 2.250867 | -0.642037 | -1.485527 |
| 16 | 6 | 1.011565 | -3.205713 | 0.120705 |
| 17 | 6 | -0.190916 | -3.394050 | -0.840170 |
| 18 | 8 | -0.650675 | -2.300889 | -1.371498 |
| 19 | 6 | -3.201767 | -0.955117 | 0.200335 |
| 20 | 6 | -3.397686 | 0.210668 | -0.802587 |
| 21 | 8 | -2.316074 | 0.608344 | -1.404700 |
| 22 | 6 | -0.952467 | 3.236935 | 0.046189 |
| 23 | 6 | 0.207878 | 3.365882 | -0.977385 |
| 24 | 8 | 0.588834 | 2.254414 | -1.523574 |
| 25 | 1 | 1.515101 | 0.053097 | 2.746972 |
| 26 | 1 | 3.242813 | 0.016409 | 2.477184 |
| 27 | 1 | 2.948210 | -1.813484 | 0.789784 |
| 28 | 1 | 2.431929 | -2.221813 | 2.423315 |
| 29 | 1 | 0.081223 | -1.371926 | 2.822280 |
| 30 | 1 | 0.037170 | -3.106094 | 2.604407 |
| 31 | 1 | -1.801538 | -2.863099 | 0.923939 |
| 32 | 1 | -2.199898 | -2.285542 | 2.539302 |
| 33 | 1 | -1.327336 | 0.087729 | 2.832523 |
| 34 | 1 | -3.065533 | 0.116820 | 2.640934 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 35 | 1 | -2.854614 | 1.882842 | 0.877896 |
| 36 | 1 | -2.250617 | 2.354031 | 2.463427 |
| 37 | 1 | 0.118820 | 1.505777 | 2.764506 |
| 38 | 1 | 0.143048 | 3.232206 | 2.486486 |
| 39 | 1 | 1.894581 | 2.935691 | 0.721413 |
| 40 | 1 | 2.378166 | 2.412175 | 2.332187 |
| 41 | 1 | 2.966736 | 1.826526 | -0.676068 |
| 42 | 1 | 1.842379 | -2.950475 | -0.548961 |
| 43 | 1 | -2.959058 | -1.814149 | -0.437613 |
| 44 | 1 | -1.819919 | 2.960523 | -0.566050 |
| 45 | 8 | -0.715099 | -0.442579 | -3.310775 |
| 46 | 1 | -0.801489 | -1.384621 | -3.048620 |
| 47 | 1 | -1.576922 | -0.050853 | -3.051153 |
| 48 | 6 | -1.249780 | 4.561216 | 0.755711 |
| 49 | 1 | -0.377031 | 4.951824 | 1.285473 |
| 50 | 1 | -1.528206 | 5.303407 | 0.004533 |
| 51 | 1 | -2.079140 | 4.461362 | 1.463062 |
| 52 | 6 | -4.483825 | -1.265907 | 0.979691 |
| 53 | 1 | -5.265622 | -1.536398 | 0.266918 |
| 54 | 1 | -4.342834 | -2.104674 | 1.668397 |
| 55 | 1 | -4.846501 | -0.401852 | 1.542574 |
| 56 | 6 | 1.357988 | -4.498176 | 0.867172 |
| 57 | 1 | 0.518578 | -4.872527 | 1.459173 |
| 58 | 1 | 1.601986 | -5.267927 | 0.132229 |
| 59 | 1 | 2.223032 | -4.363289 | 1.523837 |
| 60 | 6 | 4.574590 | 1.323872 | 0.665482 |
| 61 | 1 | 4.967152 | 0.478784 | 1.237140 |
| 62 | 1 | 5.313202 | 1.563189 | -0.102477 |
| 63 | 1 | 4.478780 | 2.187926 | 1.330610 |
| 64 | 8 | -4.535478 | 0.649355 | -1.016593 |
| 65 | 8 | -0.598770 | -4.535596 | -1.091215 |
| 66 | 8 | 4.492259 | -0.668773 | -1.254584 |
| 67 | 8 | 0.657420 | 4.490007 | -1.247340 |
| 68 | 58 | 0.007030 | 0.006151 | -0.723895 |

E(RTPSSh) = -1711.4699447 Hartree

Zero-point correction = 0.560549 Hartree/particle

Sum of electronic and thermal Energies = -1710.873630 Hartree

Sum of electronic and thermal Enthalpies = -1710.872686 Hartree

Sum of electronic and thermal Free Energies = -1710.974039 Hartree

Table S7. [Pr(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 1.984962 | 0.996533 | 0.902548 |
| 2 | 6 | 2.273994 | 0.027021 | 1.991593 |
| 3 | 6 | 2.297336 | -1.437485 | 1.553055 |
| 4 | 7 | 1.001592 | -1.908122 | 0.983648 |
| 5 | 6 | 0.034717 | -2.155125 | 2.085704 |
| 6 | 6 | -1.429716 | -2.192214 | 1.649122 |
| 7 | 7 | -1.900101 | -0.918369 | 1.031863 |
| 8 | 6 | -2.143604 | 0.091022 | 2.096841 |
| 9 | 6 | -2.185093 | 1.536643 | 1.601005 |
| 10 | 7 | -0.916471 | 1.978471 | 0.953844 |
| 11 | 6 | 0.100571 | 2.267463 | 1.999290 |
| 12 | 6 | 1.543539 | 2.292013 | 1.493860 |
| 13 | 6 | 3.152329 | 1.224968 | -0.016509 |
| 14 | 6 | 3.353138 | 0.030009 | -0.986614 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 15 | 8 | 2.264842 | -0.473445 | -1.477422 |
| 16 | 6 | 1.240101 | -3.116055 | 0.120278 |
| 17 | 6 | 0.061183 | -3.379714 | -0.851012 |
| 18 | 8 | -0.475400 | -2.316588 | -1.371255 |
| 19 | 6 | -3.114301 | -1.190623 | 0.186595 |
| 20 | 6 | -3.383804 | -0.044251 | -0.820948 |
| 21 | 8 | -2.326229 | 0.439536 | -1.401961 |
| 22 | 6 | -1.188766 | 3.150533 | 0.051157 |
| 23 | 6 | -0.043953 | 3.353859 | -0.975860 |
| 24 | 8 | 0.421413 | 2.266784 | -1.505446 |
| 25 | 1 | 1.508136 | 0.164569 | 2.759350 |
| 26 | 1 | 3.231884 | 0.254876 | 2.478806 |
| 27 | 1 | 3.069974 | -1.591523 | 0.797166 |
| 28 | 1 | 2.582157 | -2.038961 | 2.429061 |
| 29 | 1 | 0.174981 | -1.362503 | 2.825238 |
| 30 | 1 | 0.261850 | -3.094964 | 2.607064 |
| 31 | 1 | -1.584591 | -2.990654 | 0.920742 |
| 32 | 1 | -2.031673 | -2.445118 | 2.534452 |
| 33 | 1 | -1.347124 | -0.017903 | 2.837520 |
| 34 | 1 | -3.080476 | -0.117584 | 2.630935 |
| 35 | 1 | -2.990471 | 1.661556 | 0.874440 |
| 36 | 1 | -2.430244 | 2.174750 | 2.463025 |
| 37 | 1 | -0.001171 | 1.500594 | 2.771530 |
| 38 | 1 | -0.106808 | 3.224395 | 2.497204 |
| 39 | 1 | 1.662439 | 3.065133 | 0.732042 |
| 40 | 1 | 2.185030 | 2.576351 | 2.341338 |
| 41 | 1 | 2.814739 | 2.041916 | -0.666852 |
| 42 | 1 | 2.056547 | -2.801245 | -0.542091 |
| 43 | 1 | -2.803571 | -2.030292 | -0.448010 |
| 44 | 1 | -2.037269 | 2.816268 | -0.558935 |
| 45 | 8 | -0.609973 | -0.445569 | -3.284512 |
| 46 | 1 | -0.636131 | -1.396781 | -3.043241 |
| 47 | 1 | -1.507614 | -0.124297 | -3.051910 |
| 48 | 6 | -1.571916 | 4.453368 | 0.759642 |
| 49 | 1 | -0.723460 | 4.906760 | 1.278787 |
| 50 | 1 | -1.910574 | 5.171050 | 0.009472 |
| 51 | 1 | -2.384573 | 4.297508 | 1.476266 |
| 52 | 6 | -4.377510 | -1.592660 | 0.954564 |
| 53 | 1 | -5.127410 | -1.932192 | 0.237093 |
| 54 | 1 | -4.178854 | -2.409864 | 1.654897 |
| 55 | 1 | -4.813109 | -0.753348 | 1.502998 |
| 56 | 6 | 1.668406 | -4.385527 | 0.863600 |
| 57 | 1 | 0.850123 | -4.822794 | 1.441965 |
| 58 | 1 | 1.977400 | -5.131180 | 0.128322 |
| 59 | 1 | 2.512383 | -4.192748 | 1.533152 |
| 60 | 6 | 4.457555 | 1.643130 | 0.667392 |
| 61 | 1 | 4.910905 | 0.822654 | 1.229879 |
| 62 | 1 | 5.174027 | 1.940337 | -0.101242 |
| 63 | 1 | 4.304250 | 2.492618 | 1.340553 |
| 64 | 8 | -4.548914 | 0.300886 | -1.058271 |
| 65 | 8 | -0.259253 | -4.544926 | -1.119596 |
| 66 | 8 | 4.504408 | -0.332805 | -1.271465 |
| 67 | 8 | 0.316057 | 4.505056 | -1.264672 |
| 68 | 59 | 0.007925 | 0.007684 | -0.703798 |

E(RTPSSh) = -1712.105256 Hartree

Zero-point correction = 0.560304 Hartree/particle

Sum of electronic and thermal Energies = -1711.509237 Hartree

Sum of electronic and thermal Enthalpies = -1711.508293 Hartree

Sum of electronic and thermal Free Energies = -1711.609495 Hartree

Table S8. [Nd(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 1.927246 | 1.090421 | 0.906949 |
| 2 | 6 | 2.268969 | 0.139211 | 1.996101 |
| 3 | 6 | 2.364393 | -1.321178 | 1.556331 |
| 4 | 7 | 1.093261 | -1.851540 | 0.984405 |
| 5 | 6 | 0.141948 | -2.151266 | 2.086467 |
| 6 | 6 | -1.318242 | -2.260370 | 1.649101 |
| 7 | 7 | -1.849075 | -1.010657 | 1.031564 |
| 8 | 6 | -2.145060 | -0.016603 | 2.097923 |
| 9 | 6 | -2.257345 | 1.425126 | 1.602727 |
| 10 | 7 | -1.010756 | 1.926598 | 0.956892 |
| 11 | 6 | -0.012333 | 2.269575 | 2.003516 |
| 12 | 6 | 1.427077 | 2.363952 | 1.498287 |
| 13 | 6 | 3.079647 | 1.372522 | -0.016802 |
| 14 | 6 | 3.327286 | 0.188714 | -0.988456 |
| 15 | 8 | 2.259016 | -0.364352 | -1.469460 |
| 16 | 6 | 1.390468 | -3.042680 | 0.116017 |
| 17 | 6 | 0.223978 | -3.356967 | -0.853422 |
| 18 | 8 | -0.366272 | -2.317070 | -1.362605 |
| 19 | 6 | -3.045902 | -1.340624 | 0.182993 |
| 20 | 6 | -3.365541 | -0.203745 | -0.818515 |
| 21 | 8 | -2.328154 | 0.332652 | -1.389859 |
| 22 | 6 | -1.336561 | 3.081512 | 0.049777 |
| 23 | 6 | -0.201112 | 3.329969 | -0.976070 |
| 24 | 8 | 0.315385 | 2.260949 | -1.494578 |
| 25 | 1 | 1.499106 | 0.239337 | 2.765712 |
| 26 | 1 | 3.215578 | 0.415485 | 2.480175 |
| 27 | 1 | 3.144713 | -1.436390 | 0.801544 |
| 28 | 1 | 2.676919 | -1.910050 | 2.431480 |
| 29 | 1 | 0.243293 | -1.354183 | 2.827630 |
| 30 | 1 | 0.416230 | -3.079923 | 2.605212 |
| 31 | 1 | -1.433423 | -3.065504 | 0.920752 |
| 32 | 1 | -1.907965 | -2.542608 | 2.533872 |
| 33 | 1 | -1.344706 | -0.087301 | 2.839080 |
| 34 | 1 | -3.070952 | -0.272125 | 2.630839 |
| 35 | 1 | -3.067314 | 1.510740 | 0.875601 |
| 36 | 1 | -2.534310 | 2.050549 | 2.464525 |
| 37 | 1 | -0.077394 | 1.500453 | 2.777501 |
| 38 | 1 | -0.267759 | 3.216331 | 2.498521 |
| 39 | 1 | 1.508381 | 3.141843 | 0.736491 |
| 40 | 1 | 2.055104 | 2.678832 | 2.345126 |
| 41 | 1 | 2.703820 | 2.174428 | -0.664891 |
| 42 | 1 | 2.190088 | -2.685652 | -0.545696 |
| 43 | 1 | -2.692525 | -2.161433 | -0.454057 |
| 44 | 1 | -2.168600 | 2.707270 | -0.559748 |
| 45 | 8 | -0.581005 | -0.460649 | -3.263210 |
| 46 | 1 | -0.565042 | -1.411972 | -3.020984 |
| 47 | 1 | -1.491599 | -0.178762 | -3.029606 |
| 48 | 6 | -1.778789 | 4.368861 | 0.751927 |
| 49 | 1 | -0.951623 | 4.864372 | 1.266920 |
| 50 | 1 | -2.152229 | 5.065625 | -0.001392 |
| 51 | 1 | -2.581864 | 4.178909 | 1.471123 |
| 52 | 6 | -4.290347 | -1.806829 | 0.945195 |
| 53 | 1 | -5.018490 | -2.186046 | 0.225205 |
| 54 | 1 | -4.052366 | -2.611617 | 1.647602 |
| 55 | 1 | -4.771384 | -0.990519 | 1.490272 |
| 56 | 6 | 1.879925 | -4.293578 | 0.852878 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 57 | 1 | 1.082619 | -4.775107 | 1.425291 |
| 58 | 1 | 2.228747 | -5.018313 | 0.114553 |
| 59 | 1 | 2.710798 | -4.062576 | 1.526665 |
| 60 | 6 | 4.368662 | 1.847039 | 0.660907 |
| 61 | 1 | 4.861215 | 1.046568 | 1.219250 |
| 62 | 1 | 5.066832 | 2.176754 | -0.111253 |
| 63 | 1 | 4.181630 | 2.687908 | 1.336344 |
| 64 | 8 | -4.544239 | 0.081482 | -1.067811 |
| 65 | 8 | -0.040108 | -4.534028 | -1.131153 |
| 66 | 8 | 4.491138 | -0.123420 | -1.282580 |
| 67 | 8 | 0.107764 | 4.493691 | -1.274088 |
| 68 | 60 | 0.006747 | 0.009684 | -0.692115 |

E(RTPSSh) = -1712.72839 Hartree

Zero-point correction = 0.561232 Hartree/particle

Sum of electronic and thermal Energies = -1712.131757 Hartree

Sum of electronic and thermal Enthalpies = -1712.130813 Hartree

Sum of electronic and thermal Free Energies = -1712.230381 Hartree

Table S9. [Sm(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.813819 | 2.038407 | 0.924143 |
| 2 | 6 | 1.672061 | 1.508939 | 2.016329 |
| 3 | 6 | 2.664692 | 0.435144 | 1.572398 |
| 4 | 7 | 2.006556 | -0.768439 | 0.988873 |
| 5 | 6 | 1.462209 | -1.614667 | 2.083155 |
| 6 | 6 | 0.387993 | -2.604402 | 1.635856 |
| 7 | 7 | -0.803948 | -1.947172 | 1.028515 |
| 8 | 6 | -1.647237 | -1.359547 | 2.102395 |
| 9 | 6 | -2.646086 | -0.313390 | 1.609208 |
| 10 | 7 | -1.991758 | 0.859257 | 0.963018 |
| 11 | 6 | -1.442694 | 1.758597 | 2.011428 |
| 12 | 6 | -0.370758 | 2.725964 | 1.511323 |
| 13 | 6 | 1.542305 | 2.975968 | 0.002424 |
| 14 | 6 | 2.462259 | 2.202688 | -0.976915 |
| 15 | 8 | 1.962941 | 1.106132 | -1.454027 |
| 16 | 6 | 2.981146 | -1.499147 | 0.108488 |
| 17 | 6 | 2.262632 | -2.449554 | -0.879541 |
| 18 | 8 | 1.145491 | -1.995662 | -1.364644 |
| 19 | 6 | -1.542966 | -2.940503 | 0.176226 |
| 20 | 6 | -2.479023 | -2.239309 | -0.837969 |
| 21 | 8 | -1.993936 | -1.161018 | -1.377744 |
| 22 | 6 | -2.964568 | 1.545956 | 0.045832 |
| 23 | 6 | -2.227745 | 2.448800 | -0.976121 |
| 24 | 8 | -1.141305 | 1.944757 | -1.471288 |
| 25 | 1 | 1.008017 | 1.097691 | 2.780515 |
| 26 | 1 | 2.231759 | 2.316970 | 2.507020 |
| 27 | 1 | 3.347681 | 0.841244 | 0.823148 |
| 28 | 1 | 3.275166 | 0.164010 | 2.446390 |
| 29 | 1 | 1.048602 | -0.944042 | 2.840355 |
| 30 | 1 | 2.262390 | -2.175715 | 2.584507 |
| 31 | 1 | 0.798503 | -3.296822 | 0.897805 |
| 32 | 1 | 0.101705 | -3.203895 | 2.512658 |
| 33 | 1 | -0.974508 | -0.904623 | 2.834583 |
| 34 | 1 | -2.198412 | -2.140589 | 2.643527 |
| 35 | 1 | -3.330067 | -0.758323 | 0.883357 |
| 36 | 1 | -3.254574 | -0.000027 | 2.470265 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 37 | 1 | -1.026065 | 1.123954 | 2.797118 |
| 38 | 1 | -2.240463 | 2.342958 | 2.489741 |
| 39 | 1 | -0.787958 | 3.385380 | 0.747580 |
| 40 | 1 | -0.076099 | 3.363316 | 2.358198 |
| 41 | 1 | 0.748868 | 3.376483 | -0.641026 |
| 42 | 1 | 3.384685 | -0.711661 | -0.540617 |
| 43 | 1 | -0.757543 | -3.376379 | -0.453926 |
| 44 | 1 | -3.367987 | 0.728789 | -0.565001 |
| 45 | 8 | -0.137089 | -0.600217 | -3.224853 |
| 46 | 1 | 0.463471 | -1.346119 | -3.007928 |
| 47 | 1 | -1.028545 | -0.960085 | -3.030592 |
| 48 | 6 | -4.124559 | 2.270482 | 0.735223 |
| 49 | 1 | -3.799830 | 3.183249 | 1.241411 |
| 50 | 1 | -4.851941 | 2.565558 | -0.024028 |
| 51 | 1 | -4.629246 | 1.622982 | 1.459433 |
| 52 | 6 | -2.250378 | -4.068498 | 0.934478 |
| 53 | 1 | -2.585826 | -4.816488 | 0.213066 |
| 54 | 1 | -1.577216 | -4.556432 | 1.646295 |
| 55 | 1 | -3.136502 | -3.716207 | 1.469216 |
| 56 | 6 | 4.142513 | -2.187018 | 0.833591 |
| 57 | 1 | 3.820635 | -3.077396 | 1.380350 |
| 58 | 1 | 4.873776 | -2.512045 | 0.090698 |
| 59 | 1 | 4.640287 | -1.504413 | 1.529442 |
| 60 | 6 | 2.266252 | 4.141208 | 0.683804 |
| 61 | 1 | 3.161891 | 3.814397 | 1.218634 |
| 62 | 1 | 2.589539 | 4.848082 | -0.083169 |
| 63 | 1 | 1.609037 | 4.669997 | 1.381592 |
| 64 | 8 | -3.573048 | -2.746597 | -1.117320 |
| 65 | 8 | 2.792448 | -3.522769 | -1.194374 |
| 66 | 8 | 3.564491 | 2.681250 | -1.283807 |
| 67 | 8 | -2.721558 | 3.540859 | -1.294580 |
| 68 | 62 | 0.000134 | 0.014221 | -0.666469 |

E(RTPSSh) = -1713.9504937 Hartree

Zero-point correction = 0.561384 Hartree/particle

Sum of electronic and thermal Energies = -1713.353788 Hartree

Sum of electronic and thermal Enthalpies = -1713.352843 Hartree

Sum of electronic and thermal Free Energies = -1713.452667 Hartree

Table S10. [Eu(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.788212 | 2.043332 | 0.927382 |
| 2 | 6 | 1.656354 | 1.528114 | 2.018732 |
| 3 | 6 | 2.659115 | 0.464346 | 1.574191 |
| 4 | 7 | 2.011290 | -0.744771 | 0.990679 |
| 5 | 6 | 1.477786 | -1.596627 | 2.085860 |
| 6 | 6 | 0.417159 | -2.600216 | 1.637262 |
| 7 | 7 | -0.780585 | -1.956145 | 1.027179 |
| 8 | 6 | -1.634509 | -1.384628 | 2.101102 |
| 9 | 6 | -2.643383 | -0.348391 | 1.608543 |
| 10 | 7 | -1.998505 | 0.831092 | 0.965688 |
| 11 | 6 | -1.460073 | 1.732663 | 2.017678 |
| 12 | 6 | -0.402967 | 2.716154 | 1.517939 |
| 13 | 6 | 1.502114 | 2.987339 | 0.001362 |
| 14 | 6 | 2.424669 | 2.221163 | -0.980364 |
| 15 | 8 | 1.938121 | 1.113251 | -1.443940 |
| 16 | 6 | 2.990625 | -1.465114 | 0.107609 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 17 | 6 | 2.277993 | -2.415466 | -0.883760 |
| 18 | 8 | 1.151721 | -1.972040 | -1.357324 |
| 19 | 6 | -1.503338 | -2.954429 | 0.167295 |
| 20 | 6 | -2.441605 | -2.258918 | -0.848007 |
| 21 | 8 | -1.969549 | -1.167326 | -1.372503 |
| 22 | 6 | -2.975507 | 1.511176 | 0.048534 |
| 23 | 6 | -2.243477 | 2.414415 | -0.975707 |
| 24 | 8 | -1.149127 | 1.918696 | -1.461269 |
| 25 | 1 | 0.999079 | 1.112645 | 2.786536 |
| 26 | 1 | 2.208289 | 2.344366 | 2.504495 |
| 27 | 1 | 3.337389 | 0.877195 | 0.824459 |
| 28 | 1 | 3.273098 | 0.198419 | 2.447321 |
| 29 | 1 | 1.054358 | -0.929670 | 2.841033 |
| 30 | 1 | 2.284865 | -2.145964 | 2.589159 |
| 31 | 1 | 0.837600 | -3.287935 | 0.900494 |
| 32 | 1 | 0.135565 | -3.203013 | 2.513291 |
| 33 | 1 | -0.968941 | -0.925169 | 2.836677 |
| 34 | 1 | -2.177585 | -2.174731 | 2.637268 |
| 35 | 1 | -3.321174 | -0.798946 | 0.880474 |
| 36 | 1 | -3.256774 | -0.042071 | 2.468655 |
| 37 | 1 | -1.031543 | 1.099404 | 2.798271 |
| 38 | 1 | -2.264799 | 2.302884 | 2.501369 |
| 39 | 1 | -0.830265 | 3.371661 | 0.756515 |
| 40 | 1 | -0.114143 | 3.355707 | 2.365106 |
| 41 | 1 | 0.701867 | 3.377842 | -0.639555 |
| 42 | 1 | 3.387980 | -0.672590 | -0.539044 |
| 43 | 1 | -0.709792 | -3.377449 | -0.461558 |
| 44 | 1 | -3.374997 | 0.691106 | -0.560697 |
| 45 | 8 | -0.123777 | -0.565176 | -3.206952 |
| 46 | 1 | 0.483805 | -1.307681 | -2.998864 |
| 47 | 1 | -1.011518 | -0.937127 | -3.018284 |
| 48 | 6 | -4.138457 | 2.231305 | 0.737329 |
| 49 | 1 | -3.817892 | 3.146602 | 1.241644 |
| 50 | 1 | -4.867747 | 2.521295 | -0.022020 |
| 51 | 1 | -4.639293 | 1.582647 | 1.463196 |
| 52 | 6 | -2.201277 | -4.093674 | 0.917152 |
| 53 | 1 | -2.525421 | -4.841952 | 0.190901 |
| 54 | 1 | -1.525667 | -4.577212 | 1.629655 |
| 55 | 1 | -3.093358 | -3.753577 | 1.449885 |
| 56 | 6 | 4.156951 | -2.147695 | 0.829559 |
| 57 | 1 | 3.841210 | -3.041513 | 1.374311 |
| 58 | 1 | 4.889445 | -2.466039 | 0.085005 |
| 59 | 1 | 4.650976 | -1.463853 | 1.526885 |
| 60 | 6 | 2.216752 | 4.161262 | 0.677342 |
| 61 | 1 | 3.118135 | 3.844986 | 1.208847 |
| 62 | 1 | 2.529080 | 4.870021 | -0.092425 |
| 63 | 1 | 1.556972 | 4.684262 | 1.377088 |
| 64 | 8 | -3.523544 | -2.782202 | -1.144272 |
| 65 | 8 | 2.818686 | -3.479557 | -1.210913 |
| 66 | 8 | 3.516482 | 2.714132 | -1.301447 |
| 67 | 8 | -2.747460 | 3.498662 | -1.304999 |
| 68 | 63 | -0.000058 | 0.014392 | -0.650342 |

E(RTPSSh) = -1714.5481586 Hartree

Zero-point correction = 0.561636 Hartree/particle

Sum of electronic and thermal Energies = -1713.951299 Hartree

Sum of electronic and thermal Enthalpies = -1713.950354 Hartree

Sum of electronic and thermal Free Energies = -1714.049723 Hartree

Table S11. [Gd(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.818456 | 2.026390 | 0.931962 |
| 2 | 6 | 1.681101 | 1.498938 | 2.021370 |
| 3 | 6 | 2.667188 | 0.421088 | 1.574199 |
| 4 | 7 | 1.998000 | -0.775430 | 0.989585 |
| 5 | 6 | 1.452546 | -1.620490 | 2.084331 |
| 6 | 6 | 0.377239 | -2.608025 | 1.635787 |
| 7 | 7 | -0.809704 | -1.944559 | 1.025782 |
| 8 | 6 | -1.658320 | -1.364438 | 2.099998 |
| 9 | 6 | -2.648992 | -0.309997 | 1.609380 |
| 10 | 7 | -1.983672 | 0.859189 | 0.968818 |
| 11 | 6 | -1.434559 | 1.753441 | 2.021310 |
| 12 | 6 | -0.360597 | 2.719210 | 1.523560 |
| 13 | 6 | 1.545049 | 2.956343 | 0.002173 |
| 14 | 6 | 2.449238 | 2.172609 | -0.981879 |
| 15 | 8 | 1.946568 | 1.067220 | -1.433766 |
| 16 | 6 | 2.961469 | -1.510935 | 0.102693 |
| 17 | 6 | 2.227582 | -2.442803 | -0.889822 |
| 18 | 8 | 1.104782 | -1.979261 | -1.352480 |
| 19 | 6 | -1.545467 | -2.927822 | 0.160957 |
| 20 | 6 | -2.466253 | -2.213067 | -0.855945 |
| 21 | 8 | -1.979318 | -1.119906 | -1.363473 |
| 22 | 6 | -2.945486 | 1.553899 | 0.047490 |
| 23 | 6 | -2.193653 | 2.439721 | -0.976641 |
| 24 | 8 | -1.103719 | 1.925453 | -1.452752 |
| 25 | 1 | 1.020332 | 1.090569 | 2.789729 |
| 26 | 1 | 2.244701 | 2.307261 | 2.507080 |
| 27 | 1 | 3.351362 | 0.823890 | 0.824319 |
| 28 | 1 | 3.277629 | 0.143666 | 2.446246 |
| 29 | 1 | 1.037524 | -0.948839 | 2.839917 |
| 30 | 1 | 2.252009 | -2.181099 | 2.587442 |
| 31 | 1 | 0.786756 | -3.302400 | 0.899057 |
| 32 | 1 | 0.086370 | -3.206466 | 2.511751 |
| 33 | 1 | -0.988822 | -0.918543 | 2.840557 |
| 34 | 1 | -2.215560 | -2.148440 | 2.630485 |
| 35 | 1 | -3.334448 | -0.747078 | 0.880194 |
| 36 | 1 | -3.257361 | 0.005084 | 2.469913 |
| 37 | 1 | -1.018730 | 1.115608 | 2.804767 |
| 38 | 1 | -2.231800 | 2.337176 | 2.501387 |
| 39 | 1 | -0.776170 | 3.383299 | 0.762887 |
| 40 | 1 | -0.060724 | 3.352594 | 2.371519 |
| 41 | 1 | 0.749450 | 3.359574 | -0.636642 |
| 42 | 1 | 3.372386 | -0.724139 | -0.542414 |
| 43 | 1 | -0.757091 | -3.362417 | -0.466453 |
| 44 | 1 | -3.357545 | 0.739667 | -0.561164 |
| 45 | 8 | -0.131439 | -0.526152 | -3.188131 |
| 46 | 1 | 0.461176 | -1.283367 | -2.991053 |
| 47 | 1 | -1.026207 | -0.883251 | -3.003716 |
| 48 | 6 | -4.098012 | 2.296574 | 0.729940 |
| 49 | 1 | -3.763673 | 3.207472 | 1.233316 |
| 50 | 1 | -4.819249 | 2.597038 | -0.032981 |
| 51 | 1 | -4.612971 | 1.658815 | 1.455659 |
| 52 | 6 | -2.264959 | -4.058177 | 0.904129 |
| 53 | 1 | -2.597952 | -4.798552 | 0.173895 |
| 54 | 1 | -1.599750 | -4.554919 | 1.617426 |
| 55 | 1 | -3.153542 | -3.706238 | 1.435095 |
| 56 | 6 | 4.116445 | -2.218137 | 0.819283 |
| 57 | 1 | 3.785562 | -3.107363 | 1.362612 |
| 58 | 1 | 4.840580 | -2.547940 | 0.071636 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 59 | 1 | 4.625444 | -1.545847 | 1.517152 |
| 60 | 6 | 2.282691 | 4.119268 | 0.672521 |
| 61 | 1 | 3.179302 | 3.788867 | 1.203589 |
| 62 | 1 | 2.606185 | 4.819052 | -0.100768 |
| 63 | 1 | 1.634160 | 4.657025 | 1.371655 |
| 64 | 8 | -3.549921 | -2.723038 | -1.169168 |
| 65 | 8 | 2.749894 | -3.512461 | -1.229186 |
| 66 | 8 | 3.544215 | 2.650775 | -1.315357 |
| 67 | 8 | -2.679141 | 3.529933 | -1.314841 |
| 68 | 64 | 0.000285 | 0.015272 | -0.632233 |

E(RTPSSh) = -1715.1389338 Hartree

Zero-point correction = 0.561731 Hartree/particle

Sum of electronic and thermal Energies = -1714.542048 Hartree

Sum of electronic and thermal Enthalpies = -1714.541104 Hartree

Sum of electronic and thermal Free Energies = -1714.640142 Hartree

Table S12. [Tb(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.786927 | 2.030056 | 0.936306 |
| 2 | 6 | 1.657366 | 1.518721 | 2.027339 |
| 3 | 6 | 2.657781 | 0.455073 | 1.579733 |
| 4 | 7 | 2.002851 | -0.748502 | 0.994054 |
| 5 | 6 | 1.475587 | -1.603993 | 2.088852 |
| 6 | 6 | 0.414616 | -2.604657 | 1.637274 |
| 7 | 7 | -0.778670 | -1.953122 | 1.027592 |
| 8 | 6 | -1.635359 | -1.390976 | 2.103766 |
| 9 | 6 | -2.641447 | -0.352375 | 1.612971 |
| 10 | 7 | -1.989793 | 0.824413 | 0.973053 |
| 11 | 6 | -1.457162 | 1.725305 | 2.028098 |
| 12 | 6 | -0.399987 | 2.707850 | 1.529019 |
| 13 | 6 | 1.500433 | 2.969672 | 0.005981 |
| 14 | 6 | 2.412024 | 2.197318 | -0.979366 |
| 15 | 8 | 1.924635 | 1.081575 | -1.422733 |
| 16 | 6 | 2.973629 | -1.467997 | 0.101722 |
| 17 | 6 | 2.249504 | -2.402600 | -0.894704 |
| 18 | 8 | 1.118570 | -1.950468 | -1.349521 |
| 19 | 6 | -1.499967 | -2.942487 | 0.157072 |
| 20 | 6 | -2.425815 | -2.236497 | -0.860663 |
| 21 | 8 | -1.952520 | -1.132670 | -1.358253 |
| 22 | 6 | -2.960329 | 1.507246 | 0.051552 |
| 23 | 6 | -2.219874 | 2.400283 | -0.973840 |
| 24 | 8 | -1.118949 | 1.902006 | -1.441620 |
| 25 | 1 | 1.002192 | 1.103794 | 2.797253 |
| 26 | 1 | 2.209396 | 2.336577 | 2.510147 |
| 27 | 1 | 3.336026 | 0.868007 | 0.830040 |
| 28 | 1 | 3.272498 | 0.184238 | 2.450790 |
| 29 | 1 | 1.053819 | -0.940296 | 2.847867 |
| 30 | 1 | 2.285135 | -2.154125 | 2.587263 |
| 31 | 1 | 0.834593 | -3.291305 | 0.899199 |
| 32 | 1 | 0.129451 | -3.209710 | 2.510522 |
| 33 | 1 | -0.971949 | -0.935540 | 2.843879 |
| 34 | 1 | -2.179071 | -2.185079 | 2.633303 |
| 35 | 1 | -3.319626 | -0.799656 | 0.883219 |
| 36 | 1 | -3.255377 | -0.044766 | 2.472170 |
| 37 | 1 | -1.030143 | 1.092374 | 2.809859 |
| 38 | 1 | -2.264235 | 2.294306 | 2.509226 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 39 | 1 | -0.826784 | 3.364964 | 0.768609 |
| 40 | 1 | -0.107388 | 3.346285 | 2.375627 |
| 41 | 1 | 0.698754 | 3.362838 | -0.631150 |
| 42 | 1 | 3.373544 | -0.672939 | -0.539829 |
| 43 | 1 | -0.704279 | -3.364720 | -0.469435 |
| 44 | 1 | -3.362786 | 0.687631 | -0.555887 |
| 45 | 8 | -0.123015 | -0.494951 | -3.172075 |
| 46 | 1 | 0.477049 | -1.247459 | -2.980545 |
| 47 | 1 | -1.013537 | -0.863429 | -2.989602 |
| 48 | 65 | 0.000516 | 0.016652 | -0.627476 |
| 49 | 6 | -4.120940 | 2.237435 | 0.733635 |
| 50 | 1 | -3.796950 | 3.153323 | 1.234740 |
| 51 | 1 | -4.846091 | 2.528050 | -0.029384 |
| 52 | 1 | -4.627993 | 1.595318 | 1.461069 |
| 53 | 6 | -2.208646 | -4.083488 | 0.894048 |
| 54 | 1 | -2.530081 | -4.825582 | 0.160376 |
| 55 | 1 | -1.540880 | -4.574500 | 1.608897 |
| 56 | 1 | -3.103544 | -3.743320 | 1.422066 |
| 57 | 6 | 4.137942 | -2.165594 | 0.812397 |
| 58 | 1 | 3.818732 | -3.063049 | 1.349115 |
| 59 | 1 | 4.865764 | -2.480747 | 0.061973 |
| 60 | 1 | 4.638927 | -1.492255 | 1.515056 |
| 61 | 6 | 2.224960 | 4.141090 | 0.675680 |
| 62 | 1 | 3.127816 | 3.821708 | 1.202897 |
| 63 | 1 | 2.536526 | 4.846367 | -0.097524 |
| 64 | 1 | 1.572043 | 4.669213 | 1.378071 |
| 65 | 8 | -3.499139 | -2.761029 | -1.184449 |
| 66 | 8 | 2.784609 | -3.462248 | -1.244565 |
| 67 | 8 | 3.496414 | 2.691934 | -1.322687 |
| 68 | 8 | -2.723129 | 3.479003 | -1.322141 |

E(RTPSSh) = -1715.7276619 Hartree

Zero-point correction = 0.561876 Hartree/particle

Sum of electronic and thermal Energies = -1715.130694 Hartree

Sum of electronic and thermal Enthalpies = -1715.129750 Hartree

Sum of electronic and thermal Free Energies = -1715.228536 Hartree

Table S13. [Dy(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.993739 | 1.930999 | 0.936948 |
| 2 | 6 | 1.811140 | 1.335179 | 2.026046 |
| 3 | 6 | 2.692359 | 0.174085 | 1.574010 |
| 4 | 7 | 1.907287 | -0.951344 | 0.992778 |
| 5 | 6 | 1.291749 | -1.739312 | 2.092047 |
| 6 | 6 | 0.138682 | -2.630499 | 1.640159 |
| 7 | 7 | -0.978439 | -1.859129 | 1.025867 |
| 8 | 6 | -1.781988 | -1.219209 | 2.100305 |
| 9 | 6 | -2.666973 | -0.077124 | 1.609370 |
| 10 | 7 | -1.886761 | 1.021782 | 0.975074 |
| 11 | 6 | -1.262133 | 1.856755 | 2.034085 |
| 12 | 6 | -0.113732 | 2.729009 | 1.533899 |
| 13 | 6 | 1.797747 | 2.790470 | 0.002928 |
| 14 | 6 | 2.615737 | 1.926768 | -0.987715 |
| 15 | 8 | 2.020678 | 0.855540 | -1.407489 |
| 16 | 6 | 2.791198 | -1.776201 | 0.101246 |
| 17 | 6 | 1.967740 | -2.620198 | -0.898566 |
| 18 | 8 | 0.888617 | -2.048721 | -1.344905 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 19 | 6 | -1.791500 | -2.765374 | 0.146154 |
| 20 | 6 | -2.631292 | -1.964088 | -0.874730 |
| 21 | 8 | -2.051983 | -0.901570 | -1.350439 |
| 22 | 6 | -2.775027 | 1.811093 | 0.055351 |
| 23 | 6 | -1.941627 | 2.612424 | -0.973088 |
| 24 | 8 | -0.891039 | 2.003334 | -1.423874 |
| 25 | 1 | 1.120137 | 0.989921 | 2.799325 |
| 26 | 1 | 2.445987 | 2.093022 | 2.504577 |
| 27 | 1 | 3.403646 | 0.513593 | 0.818383 |
| 28 | 1 | 3.280406 | -0.161360 | 2.440816 |
| 29 | 1 | 0.933021 | -1.028269 | 2.840658 |
| 30 | 1 | 2.039663 | -2.362413 | 2.600773 |
| 31 | 1 | 0.489802 | -3.356118 | 0.903562 |
| 32 | 1 | -0.209445 | -3.202270 | 2.512802 |
| 33 | 1 | -1.081960 | -0.843474 | 2.850945 |
| 34 | 1 | -2.411866 | -1.956076 | 2.616702 |
| 35 | 1 | -3.385012 | -0.446259 | 0.874176 |
| 36 | 1 | -3.247996 | 0.294115 | 2.466282 |
| 37 | 1 | -0.896132 | 1.179073 | 2.809640 |
| 38 | 1 | -2.006512 | 2.500273 | 2.522124 |
| 39 | 1 | -0.473609 | 3.426100 | 0.774318 |
| 40 | 1 | 0.246412 | 3.333167 | 2.379421 |
| 41 | 1 | 1.038062 | 3.265947 | -0.629191 |
| 42 | 1 | 3.280236 | -1.030552 | -0.537434 |
| 43 | 1 | -1.038761 | -3.264452 | -0.476461 |
| 44 | 1 | -3.269876 | 1.042046 | -0.549777 |
| 45 | 8 | -0.170863 | -0.446943 | -3.155723 |
| 46 | 1 | 0.337979 | -1.265145 | -2.970394 |
| 47 | 1 | -1.097529 | -0.710264 | -2.970119 |
| 48 | 66 | 0.003389 | 0.016353 | -0.606321 |
| 49 | 6 | -3.844556 | 2.668485 | 0.739292 |
| 50 | 1 | -3.419688 | 3.543849 | 1.238068 |
| 51 | 1 | -4.535195 | 3.036069 | -0.022444 |
| 52 | 1 | -4.417594 | 2.088171 | 1.469695 |
| 53 | 6 | -2.619280 | -3.831138 | 0.871820 |
| 54 | 1 | -3.006401 | -4.534440 | 0.131792 |
| 55 | 1 | -2.010977 | -4.389760 | 1.590133 |
| 56 | 1 | -3.480467 | -3.405058 | 1.393707 |
| 57 | 6 | 3.867771 | -2.602672 | 0.812351 |
| 58 | 1 | 3.448725 | -3.456250 | 1.352321 |
| 59 | 1 | 4.553012 | -3.000923 | 0.061445 |
| 60 | 1 | 4.444371 | -1.989994 | 1.512556 |
| 61 | 6 | 2.644440 | 3.880482 | 0.667558 |
| 62 | 1 | 3.507643 | 3.470446 | 1.198966 |
| 63 | 1 | 3.030191 | 4.543084 | -0.109849 |
| 64 | 1 | 2.051109 | 4.479746 | 1.365744 |
| 65 | 8 | -3.741956 | -2.385401 | -1.222815 |
| 66 | 8 | 2.387861 | -3.727116 | -1.259516 |
| 67 | 8 | 3.733542 | 2.317415 | -1.357483 |
| 68 | 8 | -2.334675 | 3.730387 | -1.339738 |

E(RTPSSh) = -1716.3144319 Hartree
Zero-point correction = 0.561910 Hartree/particle
Sum of electronic and thermal Energies = -1715.717432 Hartree
Sum of electronic and thermal Enthalpies = -1715.716487 Hartree
Sum of electronic and thermal Free Energies = -1715.815096 Hartree

Table S14. [Ho(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center | Atomic | Coordinates (Angstroms) |
|--------|--------|-------------------------|
|--------|--------|-------------------------|

| Number | Number | X | Y | Z |
|--------|--------|-----------|-----------|-----------|
| 1 | 7 | 0.760296 | 2.030523 | 0.942174 |
| 2 | 6 | 1.639990 | 1.534634 | 2.032958 |
| 3 | 6 | 2.651186 | 0.483403 | 1.583010 |
| 4 | 7 | 2.0044313 | -0.723868 | 0.996950 |
| 5 | 6 | 1.489491 | -1.584248 | 2.093478 |
| 6 | 6 | 0.444574 | -2.599720 | 1.639834 |
| 7 | 7 | -0.753035 | -1.959583 | 1.027442 |
| 8 | 6 | -1.620476 | -1.416470 | 2.104668 |
| 9 | 6 | -2.636504 | -0.388394 | 1.614977 |
| 10 | 7 | -1.992490 | 0.793723 | 0.978183 |
| 11 | 6 | -1.472779 | 1.697399 | 2.037356 |
| 12 | 6 | -0.431664 | 2.695729 | 1.537988 |
| 13 | 6 | 1.460097 | 2.975374 | 0.007397 |
| 14 | 6 | 2.369224 | 2.207954 | -0.982490 |
| 15 | 8 | 1.895002 | 1.078368 | -1.403965 |
| 16 | 6 | 2.978015 | -1.433860 | 0.101070 |
| 17 | 6 | 2.256415 | -2.362502 | -0.901026 |
| 18 | 8 | 1.114973 | -1.918446 | -1.337447 |
| 19 | 6 | -1.458852 | -2.951936 | 0.148679 |
| 20 | 6 | -2.381676 | -2.248450 | -0.871799 |
| 21 | 8 | -1.921693 | -1.128134 | -1.344744 |
| 22 | 6 | -2.966267 | 1.469936 | 0.055841 |
| 23 | 6 | -2.229153 | 2.359308 | -0.973411 |
| 24 | 8 | -1.116260 | 1.871437 | -1.422897 |
| 25 | 1 | 0.992155 | 1.112358 | 2.805242 |
| 26 | 1 | 2.181849 | 2.361137 | 2.512361 |
| 27 | 1 | 3.323652 | 0.904075 | 0.832584 |
| 28 | 1 | 3.270343 | 0.216298 | 2.452036 |
| 29 | 1 | 1.055136 | -0.924268 | 2.848790 |
| 30 | 1 | 2.306466 | -2.120086 | 2.595370 |
| 31 | 1 | 0.875328 | -3.280760 | 0.902841 |
| 32 | 1 | 0.163455 | -3.208825 | 2.511513 |
| 33 | 1 | -0.965090 | -0.956458 | 2.848762 |
| 34 | 1 | -2.154896 | -2.220800 | 2.628161 |
| 35 | 1 | -3.309017 | -0.840984 | 0.883379 |
| 36 | 1 | -3.254872 | -0.086911 | 2.473143 |
| 37 | 1 | -1.033036 | 1.067361 | 2.814596 |
| 38 | 1 | -2.287660 | 2.251059 | 2.523095 |
| 39 | 1 | -0.868684 | 3.347974 | 0.779308 |
| 40 | 1 | -0.143972 | 3.337119 | 2.383946 |
| 41 | 1 | 0.651648 | 3.361578 | -0.624982 |
| 42 | 1 | 3.374898 | -0.633549 | -0.535449 |
| 43 | 1 | -0.655418 | -3.364134 | -0.474317 |
| 44 | 1 | -3.366704 | 0.647208 | -0.548284 |
| 45 | 8 | -0.113686 | -0.454144 | -3.146686 |
| 46 | 1 | 0.487584 | -1.206489 | -2.958964 |
| 47 | 1 | -1.003024 | -0.826096 | -2.965677 |
| 48 | 67 | 0.000817 | 0.017723 | -0.606462 |
| 49 | 6 | -4.128783 | 2.199204 | 0.735648 |
| 50 | 1 | -3.807796 | 3.118040 | 1.233388 |
| 51 | 1 | -4.854958 | 2.484443 | -0.028365 |
| 52 | 1 | -4.633473 | 1.558248 | 1.465800 |
| 53 | 6 | -2.162942 | -4.102211 | 0.875378 |
| 54 | 1 | -2.473097 | -4.843428 | 0.136004 |
| 55 | 1 | -1.495778 | -4.590876 | 1.592442 |
| 56 | 1 | -3.064099 | -3.772165 | 1.399157 |
| 57 | 6 | 4.144801 | -2.132085 | 0.806860 |
| 58 | 1 | 3.828672 | -3.032812 | 1.339963 |
| 59 | 1 | 4.872258 | -2.441722 | 0.053812 |
| 60 | 1 | 4.645003 | -1.460819 | 1.512099 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 61 | 6 | 2.179960 | 4.153273 | 0.670618 |
| 62 | 1 | 3.088156 | 3.842052 | 1.193602 |
| 63 | 1 | 2.481834 | 4.858872 | -0.106104 |
| 64 | 1 | 1.527130 | 4.678204 | 1.375527 |
| 65 | 8 | -3.439564 | -2.787611 | -1.221249 |
| 66 | 8 | 2.801109 | -3.409760 | -1.272750 |
| 67 | 8 | 3.438852 | 2.717404 | -1.349787 |
| 68 | 8 | -2.745016 | 3.425150 | -1.342631 |

E(RTPSSh) = -1716.8982644 Hartree

Zero-point correction = 0.562182 Hartree/particle

Sum of electronic and thermal Energies = -1716.301106 Hartree

Sum of electronic and thermal Enthalpies = -1716.300161 Hartree

Sum of electronic and thermal Free Energies = -1716.398395 Hartree

Table S15. [Er(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.744789 | 2.031318 | 0.944726 |
| 2 | 6 | 1.628339 | 1.543236 | 2.036048 |
| 3 | 6 | 2.646772 | 0.500297 | 1.584827 |
| 4 | 7 | 2.005618 | -0.709413 | 0.998168 |
| 5 | 6 | 1.497730 | -1.572846 | 2.095561 |
| 6 | 6 | 0.462180 | -2.596672 | 1.641005 |
| 7 | 7 | -0.738145 | -1.963152 | 1.027822 |
| 8 | 6 | -1.610333 | -1.428904 | 2.105788 |
| 9 | 6 | -2.633156 | -0.408358 | 1.616254 |
| 10 | 7 | -1.994722 | 0.776846 | 0.980275 |
| 11 | 6 | -1.482693 | 1.683459 | 2.040937 |
| 12 | 6 | -0.450262 | 2.689870 | 1.541116 |
| 13 | 6 | 1.438089 | 2.979494 | 0.008668 |
| 14 | 6 | 2.346969 | 2.215131 | -0.983000 |
| 15 | 8 | 1.878959 | 1.079772 | -1.395425 |
| 16 | 6 | 2.982007 | -1.413357 | 0.100835 |
| 17 | 6 | 2.263053 | -2.340024 | -0.904250 |
| 18 | 8 | 1.116127 | -1.901551 | -1.331756 |
| 19 | 6 | -1.436252 | -2.957843 | 0.146042 |
| 20 | 6 | -2.357711 | -2.256796 | -0.876615 |
| 21 | 8 | -1.904857 | -1.128985 | -1.338425 |
| 22 | 6 | -2.971265 | 1.447716 | 0.057202 |
| 23 | 6 | -2.236915 | 2.336711 | -0.973515 |
| 24 | 8 | -1.117606 | 1.855460 | -1.413787 |
| 25 | 1 | 0.983961 | 1.115112 | 2.808072 |
| 26 | 1 | 2.162889 | 2.374370 | 2.515530 |
| 27 | 1 | 3.315762 | 0.926092 | 0.834269 |
| 28 | 1 | 3.268405 | 0.235739 | 2.452842 |
| 29 | 1 | 1.056056 | -0.915411 | 2.848797 |
| 30 | 1 | 2.319022 | -2.100161 | 2.599401 |
| 31 | 1 | 0.898722 | -3.274164 | 0.904191 |
| 32 | 1 | 0.184043 | -3.208263 | 2.511878 |
| 33 | 1 | -0.958750 | -0.964223 | 2.850167 |
| 34 | 1 | -2.137980 | -2.238315 | 2.628292 |
| 35 | 1 | -3.302231 | -0.865006 | 0.884085 |
| 36 | 1 | -3.253976 | -0.110472 | 2.473874 |
| 37 | 1 | -1.036494 | 1.056276 | 2.816861 |
| 38 | 1 | -2.302220 | 2.229031 | 2.527893 |
| 39 | 1 | -0.892388 | 3.338797 | 0.782640 |
| 40 | 1 | -0.165858 | 3.333410 | 2.386504 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 41 | 1 | 0.626537 | 3.362092 | -0.621735 |
| 42 | 1 | 3.376528 | -0.609858 | -0.532949 |
| 43 | 1 | -0.628910 | -3.365654 | -0.474602 |
| 44 | 1 | -3.368732 | 0.622500 | -0.545284 |
| 45 | 8 | -0.107835 | -0.435634 | -3.135498 |
| 46 | 1 | 0.495960 | -1.186018 | -2.948469 |
| 47 | 1 | -0.995596 | -0.811626 | -2.955547 |
| 48 | 6 | -4.136415 | 2.174134 | 0.735484 |
| 49 | 1 | -3.818839 | 3.094758 | 1.232126 |
| 50 | 1 | -4.863093 | 2.455774 | -0.029376 |
| 51 | 1 | -4.639299 | 1.532529 | 1.466333 |
| 52 | 6 | -2.137838 | -4.111988 | 0.868892 |
| 53 | 1 | -2.442851 | -4.853283 | 0.127464 |
| 54 | 1 | -1.470771 | -4.599018 | 1.587181 |
| 55 | 1 | -3.041773 | -3.786353 | 1.390629 |
| 56 | 6 | 4.150708 | -2.110337 | 0.804566 |
| 57 | 1 | 3.836962 | -3.012894 | 1.335985 |
| 58 | 1 | 4.878466 | -2.416621 | 0.050440 |
| 59 | 1 | 4.649645 | -1.439389 | 1.511020 |
| 60 | 6 | 2.154628 | 4.160499 | 0.669838 |
| 61 | 1 | 3.065083 | 3.853321 | 1.191300 |
| 62 | 1 | 2.452141 | 4.866698 | -0.108011 |
| 63 | 1 | 1.501096 | 4.683329 | 1.375673 |
| 64 | 8 | -3.407610 | -2.803545 | -1.238047 |
| 65 | 8 | 2.813687 | -3.380394 | -1.286305 |
| 66 | 8 | 3.409604 | 2.731562 | -1.360640 |
| 67 | 8 | -2.760071 | 3.395396 | -1.352859 |
| 68 | 68 | 0.000834 | 0.018096 | -0.597155 |

E(RTPSSh) = -1717.4814698 Hartree

Zero-point correction = 0.562281 Hartree/particle

Sum of electronic and thermal Energies = -1716.884223 Hartree

Sum of electronic and thermal Enthalpies = -1716.883278 Hartree

Sum of electronic and thermal Free Energies = -1716.981486 Hartree

Table S16. [Tm(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.560163 | 2.081800 | 0.944585 |
| 2 | 6 | 1.482452 | 1.678422 | 2.038103 |
| 3 | 6 | 2.590083 | 0.734248 | 1.583883 |
| 4 | 7 | 2.054163 | -0.525793 | 0.997452 |
| 5 | 6 | 1.627843 | -1.429993 | 2.096642 |
| 6 | 6 | 0.690368 | -2.542788 | 1.642169 |
| 7 | 7 | -0.558918 | -2.016031 | 1.025954 |
| 8 | 6 | -1.479260 | -1.566900 | 2.103512 |
| 9 | 6 | -2.587223 | -0.641438 | 1.614058 |
| 10 | 7 | -2.052460 | 0.594403 | 0.979733 |
| 11 | 6 | -1.624358 | 1.542676 | 2.041654 |
| 12 | 6 | -0.687119 | 2.636219 | 1.540053 |
| 13 | 6 | 1.170842 | 3.085920 | 0.008370 |
| 14 | 6 | 2.133250 | 2.401099 | -0.990438 |
| 15 | 8 | 1.770664 | 1.222912 | -1.386398 |
| 16 | 6 | 3.087916 | -1.145024 | 0.100998 |
| 17 | 6 | 2.451920 | -2.124850 | -0.908985 |
| 18 | 8 | 1.265745 | -1.794703 | -1.324513 |
| 19 | 6 | -1.166394 | -3.067573 | 0.142490 |
| 20 | 6 | -2.136868 | -2.450832 | -0.888210 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 21 | 8 | -1.793516 | -1.279467 | -1.334048 |
| 22 | 6 | -3.083190 | 1.181829 | 0.058287 |
| 23 | 6 | -2.425398 | 2.123653 | -0.976078 |
| 24 | 8 | -1.262819 | 1.744465 | -1.401010 |
| 25 | 1 | 0.880846 | 1.191936 | 2.809758 |
| 26 | 1 | 1.937367 | 2.555438 | 2.517660 |
| 27 | 1 | 3.213544 | 1.219417 | 0.830524 |
| 28 | 1 | 3.236596 | 0.524170 | 2.448562 |
| 29 | 1 | 1.129090 | -0.816280 | 2.850841 |
| 30 | 1 | 2.493619 | -1.880294 | 2.600728 |
| 31 | 1 | 1.186883 | -3.178201 | 0.906321 |
| 32 | 1 | 0.464852 | -3.176325 | 2.512603 |
| 33 | 1 | -0.875912 | -1.050040 | 2.853985 |
| 34 | 1 | -1.933892 | -2.422588 | 2.620869 |
| 35 | 1 | -3.211747 | -1.153913 | 0.879785 |
| 36 | 1 | -3.233702 | -0.398983 | 2.470218 |
| 37 | 1 | -1.123869 | 0.958922 | 2.818278 |
| 38 | 1 | -2.489970 | 2.012000 | 2.528050 |
| 39 | 1 | -1.184671 | 3.240767 | 0.779474 |
| 40 | 1 | -0.458788 | 3.304706 | 2.382972 |
| 41 | 1 | 0.327950 | 3.405248 | -0.615606 |
| 42 | 1 | 3.417788 | -0.309837 | -0.527792 |
| 43 | 1 | -0.323418 | -3.408260 | -0.470227 |
| 44 | 1 | -3.416066 | 0.325067 | -0.538743 |
| 45 | 8 | -0.066518 | -0.415015 | -3.120031 |
| 46 | 1 | 0.593179 | -1.117530 | -2.937495 |
| 47 | 1 | -0.922626 | -0.860492 | -2.946794 |
| 48 | 69 | -0.001898 | 0.017853 | -0.580528 |
| 49 | 6 | -4.300442 | 1.815824 | 0.738197 |
| 50 | 1 | -4.057123 | 2.764568 | 1.224430 |
| 51 | 1 | -5.052375 | 2.029523 | -0.024353 |
| 52 | 1 | -4.743954 | 1.141496 | 1.478012 |
| 53 | 6 | -1.775254 | -4.274393 | 0.863652 |
| 54 | 1 | -2.006674 | -5.041819 | 0.122363 |
| 55 | 1 | -1.078247 | -4.700223 | 1.592378 |
| 56 | 1 | -2.710414 | -4.025115 | 1.372598 |
| 57 | 6 | 4.307674 | -1.747303 | 0.805914 |
| 58 | 1 | 4.067413 | -2.674521 | 1.333607 |
| 59 | 1 | 5.058311 | -1.991919 | 0.051757 |
| 60 | 1 | 4.750367 | -1.040798 | 1.515201 |
| 61 | 6 | 1.794224 | 4.319013 | 0.669625 |
| 62 | 1 | 2.728401 | 4.084881 | 1.187713 |
| 63 | 1 | 2.032664 | 5.047033 | -0.108545 |
| 64 | 1 | 1.103455 | 4.787141 | 1.378440 |
| 65 | 8 | -3.120719 | -3.097850 | -1.270101 |
| 66 | 8 | 3.097441 | -3.104296 | -1.304197 |
| 67 | 8 | 3.136962 | 3.013006 | -1.386570 |
| 68 | 8 | -3.041609 | 3.125382 | -1.370457 |

E(RTPSSh) = -1718.0612266 Hartree

Zero-point correction = 0.562381 Hartree/particle

Sum of electronic and thermal Energies = -1717.463864 Hartree

Sum of electronic and thermal Enthalpies = -1717.462920 Hartree

Sum of electronic and thermal Free Energies = -1717.561077 Hartree

Table S17. [Yb(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | X | Coordinates (Angstroms) | Y | Z |
|---------------|---------------|---|-------------------------|---|---|
| | | | | | |

| | | | | |
|----|---|-----------|-----------|-----------|
| 1 | 7 | 0.519596 | 2.088931 | 0.949207 |
| 2 | 6 | 1.450587 | 1.704343 | 2.042247 |
| 3 | 6 | 2.575231 | 0.779717 | 1.588399 |
| 4 | 7 | 2.061915 | -0.488921 | 1.001127 |
| 5 | 6 | 1.654901 | -1.402141 | 2.100198 |
| 6 | 6 | 0.738033 | -2.531525 | 1.644158 |
| 7 | 7 | -0.520128 | -2.025509 | 1.028914 |
| 8 | 6 | -1.449428 | -1.597473 | 2.107541 |
| 9 | 6 | -2.574019 | -0.691357 | 1.618513 |
| 10 | 7 | -2.060971 | 0.553163 | 0.983244 |
| 11 | 6 | -1.654362 | 1.510227 | 2.045809 |
| 12 | 6 | -0.736614 | 2.621029 | 1.545363 |
| 13 | 6 | 1.111490 | 3.101826 | 0.010997 |
| 14 | 6 | 2.083050 | 2.430503 | -0.987047 |
| 15 | 8 | 1.742474 | 1.242526 | -1.372400 |
| 16 | 6 | 3.103956 | -1.087818 | 0.101235 |
| 17 | 6 | 2.482252 | -2.068895 | -0.915683 |
| 18 | 8 | 1.285833 | -1.760899 | -1.319472 |
| 19 | 6 | -1.107005 | -3.083700 | 0.139387 |
| 20 | 6 | -2.086571 | -2.478131 | -0.888918 |
| 21 | 8 | -1.762986 | -1.297702 | -1.326506 |
| 22 | 6 | -3.099322 | 1.120586 | 0.058293 |
| 23 | 6 | -2.455414 | 2.069389 | -0.978162 |
| 24 | 8 | -1.280626 | 1.715012 | -1.391285 |
| 25 | 1 | 0.858934 | 1.208269 | 2.815352 |
| 26 | 1 | 1.890364 | 2.590113 | 2.519899 |
| 27 | 1 | 3.191505 | 1.276200 | 0.836560 |
| 28 | 1 | 3.224313 | 0.580291 | 2.453761 |
| 29 | 1 | 1.144945 | -0.799069 | 2.855342 |
| 30 | 1 | 2.530093 | -1.836054 | 2.602248 |
| 31 | 1 | 1.246225 | -3.156423 | 0.907208 |
| 32 | 1 | 0.523372 | -3.171143 | 2.512833 |
| 33 | 1 | -0.856759 | -1.070561 | 2.859483 |
| 34 | 1 | -1.887996 | -2.463329 | 2.621683 |
| 35 | 1 | -3.190229 | -1.215280 | 0.885419 |
| 36 | 1 | -3.223916 | -0.459124 | 2.474891 |
| 37 | 1 | -1.144369 | 0.936902 | 2.823745 |
| 38 | 1 | -2.529888 | 1.963223 | 2.529850 |
| 39 | 1 | -1.245045 | 3.217901 | 0.786039 |
| 40 | 1 | -0.519692 | 3.292410 | 2.389051 |
| 41 | 1 | 0.263024 | 3.405469 | -0.613069 |
| 42 | 1 | 3.422482 | -0.244803 | -0.522942 |
| 43 | 1 | -0.257554 | -3.405203 | -0.474858 |
| 44 | 1 | -3.416409 | 0.257434 | -0.537934 |
| 45 | 8 | -0.059055 | -0.399397 | -3.112482 |
| 46 | 1 | 0.613507 | -1.089548 | -2.929972 |
| 47 | 1 | -0.906768 | -0.860763 | -2.938896 |
| 48 | 6 | -4.328833 | 1.735888 | 0.733148 |
| 49 | 1 | -4.102053 | 2.687384 | 1.221646 |
| 50 | 1 | -5.079903 | 1.939340 | -0.032954 |
| 51 | 1 | -4.765973 | 1.054460 | 1.470234 |
| 52 | 6 | -1.694805 | -4.305414 | 0.852573 |
| 53 | 1 | -1.915204 | -5.070859 | 0.105818 |
| 54 | 1 | -0.989648 | -4.724843 | 1.577052 |
| 55 | 1 | -2.632856 | -4.075029 | 1.364855 |
| 56 | 6 | 4.332195 | -1.677207 | 0.802145 |
| 57 | 1 | 4.104883 | -2.610746 | 1.324164 |
| 58 | 1 | 5.086577 | -1.905857 | 0.046745 |
| 59 | 1 | 4.763739 | -0.968841 | 1.516410 |
| 60 | 6 | 1.715139 | 4.346172 | 0.668960 |
| 61 | 1 | 2.654248 | 4.128588 | 1.185018 |
| 62 | 1 | 1.939022 | 5.077062 | -0.110741 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 63 | 1 | 1.018469 | 4.803638 | 1.378957 |
| 64 | 8 | -3.058462 | -3.139033 | -1.277497 |
| 65 | 8 | 3.146569 | -3.027921 | -1.329091 |
| 66 | 8 | 3.071069 | 3.060324 | -1.394590 |
| 67 | 8 | -3.091097 | 3.053883 | -1.385212 |
| 68 | 70 | -0.001812 | 0.018067 | -0.572957 |

E(RTPSSh) = -1718.6447604 Hartree

Zero-point correction = 0.562353 Hartree/particle

Sum of electronic and thermal Energies = -1718.047409 Hartree

Sum of electronic and thermal Enthalpies = -1718.046465 Hartree

Sum of electronic and thermal Free Energies = -1718.144744 Hartree

Table S18. [Lu(DOTMA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.581246 | 2.066652 | 0.953409 |
| 2 | 6 | 1.498922 | 1.657242 | 2.047717 |
| 3 | 6 | 2.595586 | 0.701879 | 1.592238 |
| 4 | 7 | 2.040383 | -0.548232 | 1.003543 |
| 5 | 6 | 1.610220 | -1.449768 | 2.103190 |
| 6 | 6 | 0.661136 | -2.550550 | 1.645454 |
| 7 | 7 | -0.579552 | -2.003351 | 1.030157 |
| 8 | 6 | -1.495338 | -1.551348 | 2.110230 |
| 9 | 6 | -2.592188 | -0.613462 | 1.620154 |
| 10 | 7 | -2.037979 | 0.613757 | 0.986019 |
| 11 | 6 | -1.606012 | 1.557308 | 2.050048 |
| 12 | 6 | -0.657013 | 2.639997 | 1.548678 |
| 13 | 6 | 1.204641 | 3.059273 | 0.013243 |
| 14 | 6 | 2.150748 | 2.355873 | -0.987335 |
| 15 | 8 | 1.771263 | 1.178814 | -1.370833 |
| 16 | 6 | 3.063037 | -1.178571 | 0.102037 |
| 17 | 6 | 2.409605 | -2.139339 | -0.913919 |
| 18 | 8 | 1.221778 | -1.795122 | -1.314664 |
| 19 | 6 | -1.199946 | -3.043331 | 0.141722 |
| 20 | 6 | -2.155752 | -2.406636 | -0.889393 |
| 21 | 8 | -1.795876 | -1.234987 | -1.322553 |
| 22 | 6 | -3.057196 | 1.213860 | 0.059702 |
| 23 | 6 | -2.381801 | 2.139280 | -0.977540 |
| 24 | 8 | -1.218676 | 1.746592 | -1.389243 |
| 25 | 1 | 0.892774 | 1.176759 | 2.819830 |
| 26 | 1 | 1.961981 | 2.530567 | 2.526200 |
| 27 | 1 | 3.225701 | 1.180844 | 0.840386 |
| 28 | 1 | 3.239380 | 0.480158 | 2.455888 |
| 29 | 1 | 1.117474 | -0.832435 | 2.858503 |
| 30 | 1 | 2.473276 | -1.908206 | 2.604286 |
| 31 | 1 | 1.150454 | -3.189454 | 0.907698 |
| 32 | 1 | 0.425774 | -3.184547 | 2.512727 |
| 33 | 1 | -0.887059 | -1.040939 | 2.861240 |
| 34 | 1 | -1.957334 | -2.404753 | 2.624433 |
| 35 | 1 | -3.222784 | -1.118426 | 0.885854 |
| 36 | 1 | -3.236209 | -0.360943 | 2.475097 |
| 37 | 1 | -1.112112 | 0.968998 | 2.827602 |
| 38 | 1 | -2.468832 | 2.034027 | 2.533971 |
| 39 | 1 | -1.147334 | 3.250869 | 0.788440 |
| 40 | 1 | -0.418780 | 3.305802 | 2.390900 |
| 41 | 1 | 0.365407 | 3.390465 | -0.609259 |
| 42 | 1 | 3.406273 | -0.345444 | -0.522162 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 43 | 1 | -0.360923 | -3.395394 | -0.469848 |
| 44 | 1 | -3.402314 | 0.360743 | -0.535338 |
| 45 | 8 | -0.069545 | -0.391308 | -3.109447 |
| 46 | 1 | 0.579747 | -1.103168 | -2.925751 |
| 47 | 1 | -0.931719 | -0.824762 | -2.936522 |
| 48 | 71 | -0.001621 | 0.017545 | -0.570682 |
| 49 | 6 | -4.265710 | 1.870756 | 0.733294 |
| 50 | 1 | -4.008004 | 2.816107 | 1.218460 |
| 51 | 1 | -5.010445 | 2.095701 | -0.033002 |
| 52 | 1 | -4.724102 | 1.206109 | 1.472803 |
| 53 | 6 | -1.830728 | -4.242474 | 0.856588 |
| 54 | 1 | -2.072413 | -5.003146 | 0.111551 |
| 55 | 1 | -1.142836 | -4.682225 | 1.585665 |
| 56 | 1 | -2.763135 | -3.979906 | 1.363744 |
| 57 | 6 | 4.273113 | -1.806385 | 0.801154 |
| 58 | 1 | 4.017795 | -2.733046 | 1.322571 |
| 59 | 1 | 5.019139 | -2.057435 | 0.044564 |
| 60 | 1 | 4.727453 | -1.112412 | 1.515421 |
| 61 | 6 | 1.851086 | 4.282821 | 0.669456 |
| 62 | 1 | 2.783207 | 4.034028 | 1.184206 |
| 63 | 1 | 2.098288 | 5.005224 | -0.111138 |
| 64 | 1 | 1.171289 | 4.763953 | 1.380137 |
| 65 | 8 | -3.145357 | -3.037089 | -1.283476 |
| 66 | 8 | 3.042815 | -3.118602 | -1.328602 |
| 67 | 8 | 3.158216 | 2.952301 | -1.397415 |
| 68 | 8 | -2.984758 | 3.143183 | -1.386636 |

E(RTPSSh) = -1719.1985484 Hartree

Zero-point correction = 0.562662 Hartree/particle

Sum of electronic and thermal Energies = -1718.601020 Hartree

Sum of electronic and thermal Enthalpies = -1718.600076 Hartree

Sum of electronic and thermal Free Energies = -1718.697968 Hartree

Table S19. [La(DOTMA)(H₂O)]⁺ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.914280 | -0.886111 | 1.144210 |
| 2 | 6 | -1.272339 | -1.674306 | 2.228033 |
| 3 | 6 | -0.163612 | -2.607231 | 1.740963 |
| 4 | 7 | 0.982366 | -1.893400 | 1.113559 |
| 5 | 6 | 1.826187 | -1.253980 | 2.156474 |
| 6 | 6 | 2.732021 | -0.142390 | 1.627298 |
| 7 | 7 | 1.987124 | 0.994450 | 1.019820 |
| 8 | 6 | 1.396892 | 1.855364 | 2.074949 |
| 9 | 6 | 0.262909 | 2.754388 | 1.580525 |
| 10 | 7 | -0.904754 | 2.004004 | 1.040965 |
| 11 | 6 | -1.706917 | 1.423268 | 2.147488 |
| 12 | 6 | -2.633365 | 0.288267 | 1.711331 |
| 13 | 6 | -2.843004 | -1.721479 | 0.317403 |
| 14 | 6 | -3.245923 | -0.963228 | -0.977100 |
| 15 | 8 | -2.394092 | -0.078404 | -1.405030 |
| 16 | 6 | 1.771129 | -2.824257 | 0.244204 |
| 17 | 6 | 0.961370 | -3.212490 | -1.024063 |
| 18 | 8 | 0.004057 | -2.399794 | -1.361479 |
| 19 | 6 | 2.870681 | 1.759415 | 0.082470 |
| 20 | 6 | 3.208381 | 0.883956 | -1.159921 |
| 21 | 8 | 2.348048 | -0.039701 | -1.454716 |
| 22 | 6 | -1.725309 | 2.881216 | 0.145140 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 23 | 6 | -0.935965 | 3.202181 | -1.157345 |
| 24 | 8 | -0.039885 | 2.333393 | -1.506414 |
| 25 | 1 | -0.867673 | -0.967073 | 2.956456 |
| 26 | 1 | -2.011940 | -2.276781 | 2.773447 |
| 27 | 1 | -0.562755 | -3.302152 | 0.997623 |
| 28 | 1 | 0.169713 | -3.208285 | 2.599293 |
| 29 | 1 | 1.157909 | -0.851409 | 2.921799 |
| 30 | 1 | 2.455892 | -1.995342 | 2.667852 |
| 31 | 1 | 3.400674 | -0.543225 | 0.861178 |
| 32 | 1 | 3.364345 | 0.200929 | 2.458883 |
| 33 | 1 | 1.027543 | 1.198214 | 2.866518 |
| 34 | 1 | 2.159812 | 2.492449 | 2.544011 |
| 35 | 1 | 0.628334 | 3.407442 | 0.783653 |
| 36 | 1 | -0.039562 | 3.402905 | 2.415440 |
| 37 | 1 | -1.008149 | 1.058260 | 2.904463 |
| 38 | 1 | -2.315796 | 2.191269 | 2.644665 |
| 39 | 1 | -3.327532 | 0.648425 | 0.947227 |
| 40 | 1 | -3.237371 | -0.003885 | 2.582429 |
| 41 | 1 | -2.240844 | -2.567129 | -0.039899 |
| 42 | 1 | 2.607599 | -2.228058 | -0.141717 |
| 43 | 1 | 2.250481 | 2.575416 | -0.310346 |
| 44 | 1 | -2.568091 | 2.260601 | -0.185915 |
| 45 | 8 | -0.528723 | -0.599708 | -3.274954 |
| 46 | 1 | -0.360031 | -1.525791 | -2.988754 |
| 47 | 1 | -1.465625 | -0.446480 | -3.020160 |
| 48 | 57 | 0.010043 | 0.012492 | -0.642959 |
| 49 | 6 | 4.137574 | 2.360129 | 0.704540 |
| 50 | 1 | 4.798845 | 1.586074 | 1.105022 |
| 51 | 1 | 4.683506 | 2.888121 | -0.078937 |
| 52 | 1 | 3.906344 | 3.070828 | 1.503514 |
| 53 | 6 | -2.281489 | 4.157002 | 0.790372 |
| 54 | 1 | -1.481729 | 4.825807 | 1.121866 |
| 55 | 1 | -2.866783 | 4.689515 | 0.039067 |
| 56 | 1 | -2.931109 | 3.938296 | 1.643070 |
| 57 | 6 | -4.075727 | -2.270124 | 1.047968 |
| 58 | 1 | -4.727705 | -1.466645 | 1.403079 |
| 59 | 1 | -4.649075 | -2.873307 | 0.342288 |
| 60 | 1 | -3.803899 | -2.901845 | 1.898453 |
| 61 | 6 | 2.335874 | -4.069594 | 0.941913 |
| 62 | 1 | 1.540991 | -4.713726 | 1.329547 |
| 63 | 1 | 2.899004 | -4.644659 | 0.205183 |
| 64 | 1 | 3.008528 | -3.810956 | 1.764845 |
| 65 | 8 | -4.300667 | -1.270585 | -1.546152 |
| 66 | 8 | -1.234792 | 4.221934 | -1.795038 |
| 67 | 8 | 4.234175 | 1.142518 | -1.805133 |
| 68 | 8 | 1.294915 | -4.223289 | -1.655111 |

E(RTPSSh) = -1710.8237971 Hartree

Zero-point correction = 0.560730 Hartree/particle

Sum of electronic and thermal Energies = -1710.227515 Hartree

Sum of electronic and thermal Enthalpies = -1710.226571 Hartree

Sum of electronic and thermal Free Energies = -1710.327730 Hartree

Table S20. [Ce(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | -1.878037 | -0.955826 | 1.141257 |
| 2 | 6 | -1.216939 | -1.728383 | 2.224614 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 3 | 6 | -0.074024 | -2.618430 | 1.737579 |
| 4 | 7 | 1.043804 | -1.858464 | 1.113599 |
| 5 | 6 | 1.862890 | -1.194878 | 2.160211 |
| 6 | 6 | 2.729755 | -0.051541 | 1.634720 |
| 7 | 7 | 1.943976 | 1.057380 | 1.028347 |
| 8 | 6 | 1.327249 | 1.897321 | 2.085287 |
| 9 | 6 | 0.162272 | 2.754935 | 1.591866 |
| 10 | 7 | -0.974704 | 1.960979 | 1.049751 |
| 11 | 6 | -1.760305 | 1.354066 | 2.153517 |
| 12 | 6 | -2.643215 | 0.187071 | 1.712149 |
| 13 | 6 | -2.771469 | -1.818003 | 0.302714 |
| 14 | 6 | -3.189079 | -1.066395 | -0.990140 |
| 15 | 8 | -2.366098 | -0.146697 | -1.402006 |
| 16 | 6 | 1.865623 | -2.753361 | 0.237553 |
| 17 | 6 | 1.067324 | -3.159771 | -1.031522 |
| 18 | 8 | 0.088671 | -2.371127 | -1.365606 |
| 19 | 6 | 2.798656 | 1.852544 | 0.089439 |
| 20 | 6 | 3.147761 | 0.998594 | -1.164046 |
| 21 | 8 | 2.314040 | 0.050289 | -1.456588 |
| 22 | 6 | -1.821878 | 2.806998 | 0.148262 |
| 23 | 6 | -1.038647 | 3.148243 | -1.151790 |
| 24 | 8 | -0.116927 | 2.304344 | -1.495425 |
| 25 | 1 | -0.838182 | -1.010873 | 2.957004 |
| 26 | 1 | -1.938910 | -2.357454 | 2.763362 |
| 27 | 1 | -0.445970 | -3.327171 | 0.993177 |
| 28 | 1 | 0.281292 | -3.207960 | 2.595030 |
| 29 | 1 | 1.177869 | -0.815410 | 2.922573 |
| 30 | 1 | 2.515663 | -1.915537 | 2.672211 |
| 31 | 1 | 3.414602 | -0.426322 | 0.869679 |
| 32 | 1 | 3.347530 | 0.313411 | 2.467947 |
| 33 | 1 | 0.981648 | 1.227563 | 2.876918 |
| 34 | 1 | 2.068377 | 2.560665 | 2.552974 |
| 35 | 1 | 0.504385 | 3.422545 | 0.796674 |
| 36 | 1 | -0.165255 | 3.390465 | 2.427147 |
| 37 | 1 | -1.052537 | 1.013280 | 2.913517 |
| 38 | 1 | -2.398321 | 2.100196 | 2.647396 |
| 39 | 1 | -3.349472 | 0.523798 | 0.948434 |
| 40 | 1 | -3.237042 | -0.131940 | 2.580746 |
| 41 | 1 | -2.137999 | -2.639553 | -0.055673 |
| 42 | 1 | 2.678137 | -2.124033 | -0.146690 |
| 43 | 1 | 2.153778 | 2.654167 | -0.292379 |
| 44 | 1 | -2.641279 | 2.157263 | -0.184876 |
| 45 | 8 | -0.462670 | -0.560607 | -3.254586 |
| 46 | 1 | -0.266500 | -1.486134 | -2.984752 |
| 47 | 1 | -1.408254 | -0.446316 | -3.012363 |
| 48 | 6 | 4.054283 | 2.482629 | 0.705294 |
| 49 | 1 | 4.741974 | 1.723665 | 1.089975 |
| 50 | 1 | 4.576417 | 3.035019 | -0.077561 |
| 51 | 1 | 3.811053 | 3.176623 | 1.515204 |
| 52 | 6 | -2.422533 | 4.065342 | 0.787277 |
| 53 | 1 | -1.646619 | 4.759531 | 1.123183 |
| 54 | 1 | -3.019214 | 4.577988 | 0.031109 |
| 55 | 1 | -3.070268 | 3.827163 | 1.636094 |
| 56 | 6 | -3.989614 | -2.412194 | 1.021533 |
| 57 | 1 | -4.662285 | -1.632664 | 1.391137 |
| 58 | 1 | -4.546275 | -3.016215 | 0.303276 |
| 59 | 1 | -3.701459 | -3.051949 | 1.860560 |
| 60 | 6 | 2.476340 | -3.981480 | 0.926223 |
| 61 | 1 | 1.705846 | -4.652291 | 1.317750 |
| 62 | 1 | 3.051932 | -4.535446 | 0.182971 |
| 63 | 1 | 3.145961 | -3.703265 | 1.745175 |
| 64 | 8 | -4.223683 | -1.410078 | -1.575110 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 65 | 8 | -1.363437 | 4.157662 | -1.792901 |
| 66 | 8 | 4.157467 | 1.293921 | -1.819002 |
| 67 | 8 | 1.428804 | -4.157012 | -1.668286 |
| 68 | 58 | 0.006691 | 0.012471 | -0.624241 |

E(RTPSSh) = -1711.4756591 Hartree

Zero-point correction = 0.561012 Hartree/particle

Sum of electronic and thermal Energies = -1710.879121 Hartree

Sum of electronic and thermal Enthalpies = -1710.878177 Hartree

Sum of electronic and thermal Free Energies = -1710.979323 Hartree

Table S21. [Pr(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.886907 | -0.925272 | 1.140815 |
| 2 | 6 | -1.244894 | -1.712864 | 2.224052 |
| 3 | 6 | -0.115570 | -2.618456 | 1.736798 |
| 4 | 7 | 1.009644 | -1.870060 | 1.113187 |
| 5 | 6 | 1.842124 | -1.227090 | 2.161654 |
| 6 | 6 | 2.725269 | -0.096644 | 1.637309 |
| 7 | 7 | 1.951140 | 1.020827 | 1.032449 |
| 8 | 6 | 1.353952 | 1.869736 | 2.093138 |
| 9 | 6 | 0.203400 | 2.745952 | 1.601868 |
| 10 | 7 | -0.939969 | 1.965389 | 1.055216 |
| 11 | 6 | -1.737596 | 1.375086 | 2.159033 |
| 12 | 6 | -2.638596 | 0.223815 | 1.716038 |
| 13 | 6 | -2.788533 | -1.770041 | 0.293194 |
| 14 | 6 | -3.191086 | -1.000407 | -0.993033 |
| 15 | 8 | -2.349364 | -0.093265 | -1.395843 |
| 16 | 6 | 1.815610 | -2.771825 | 0.229125 |
| 17 | 6 | 1.001800 | -3.162364 | -1.034378 |
| 18 | 8 | 0.041534 | -2.349368 | -1.365401 |
| 19 | 6 | 2.811595 | 1.803292 | 0.087808 |
| 20 | 6 | 3.148787 | 0.935530 | -1.158641 |
| 21 | 8 | 2.294388 | 0.004762 | -1.449816 |
| 22 | 6 | -1.770997 | 2.820720 | 0.147421 |
| 23 | 6 | -0.974129 | 3.146032 | -1.147998 |
| 24 | 8 | -0.065337 | 2.284772 | -1.484943 |
| 25 | 1 | -0.857480 | -1.005639 | 2.961790 |
| 26 | 1 | -1.980169 | -2.331720 | 2.756416 |
| 27 | 1 | -0.496944 | -3.322230 | 0.992381 |
| 28 | 1 | 0.233676 | -3.213295 | 2.592999 |
| 29 | 1 | 1.166135 | -0.839510 | 2.928088 |
| 30 | 1 | 2.483413 | -1.961940 | 2.667760 |
| 31 | 1 | 3.405153 | -0.479905 | 0.871926 |
| 32 | 1 | 3.348401 | 0.261143 | 2.469546 |
| 33 | 1 | 0.998958 | 1.205043 | 2.885028 |
| 34 | 1 | 2.108647 | 2.518885 | 2.558922 |
| 35 | 1 | 0.555877 | 3.412547 | 0.810336 |
| 36 | 1 | -0.119662 | 3.382501 | 2.438054 |
| 37 | 1 | -1.036924 | 1.023202 | 2.920598 |
| 38 | 1 | -2.362718 | 2.133661 | 2.650387 |
| 39 | 1 | -3.341487 | 0.573297 | 0.955023 |
| 40 | 1 | -3.235496 | -0.091345 | 2.583882 |
| 41 | 1 | -2.163736 | -2.596203 | -0.069795 |
| 42 | 1 | 2.632369 | -2.150232 | -0.158127 |
| 43 | 1 | 2.172337 | 2.607249 | -0.298555 |
| 44 | 1 | -2.597357 | 2.181490 | -0.188469 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 45 | 8 | -0.451411 | -0.511595 | -3.240152 |
| 46 | 1 | -0.278528 | -1.445097 | -2.982797 |
| 47 | 1 | -1.396484 | -0.380069 | -3.004841 |
| 48 | 6 | 4.073870 | 2.425699 | 0.696845 |
| 49 | 1 | 4.753908 | 1.663834 | 1.089351 |
| 50 | 1 | 4.601112 | 2.963572 | -0.092739 |
| 51 | 1 | 3.838652 | 3.131492 | 1.498917 |
| 52 | 6 | -2.356751 | 4.089424 | 0.779327 |
| 53 | 1 | -1.573327 | 4.773551 | 1.118492 |
| 54 | 1 | -2.940745 | 4.608518 | 0.017604 |
| 55 | 1 | -3.014012 | 3.863411 | 1.624202 |
| 56 | 6 | -4.017305 | -2.353816 | 1.002283 |
| 57 | 1 | -4.683671 | -1.568772 | 1.371559 |
| 58 | 1 | -4.576522 | -2.948607 | 0.278253 |
| 59 | 1 | -3.741744 | -3.001233 | 1.839597 |
| 60 | 6 | 2.416311 | -4.009592 | 0.908691 |
| 61 | 1 | 1.641311 | -4.672385 | 1.304910 |
| 62 | 1 | 2.978209 | -4.568294 | 0.158470 |
| 63 | 1 | 3.097227 | -3.742690 | 1.722113 |
| 64 | 8 | -4.233684 | -1.314709 | -1.579961 |
| 65 | 8 | -1.275465 | 4.160077 | -1.793099 |
| 66 | 8 | 4.167218 | 1.203703 | -1.811563 |
| 67 | 8 | 1.332082 | -4.170869 | -1.670014 |
| 68 | 59 | 0.007136 | 0.011837 | -0.613218 |

E(RTPSSh) = -1712.1107368 Hartree

Zero-point correction = 0.561138 Hartree/particle

Sum of electronic and thermal Energies = -1711.514132 Hartree

Sum of electronic and thermal Enthalpies = -1711.513188 Hartree

Sum of electronic and thermal Free Energies = -1711.614117 Hartree

Table S22. [Nd(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.893867 | -0.913947 | 1.138262 |
| 2 | 6 | -1.264478 | -1.710181 | 2.222805 |
| 3 | 6 | -0.140357 | -2.621549 | 1.734679 |
| 4 | 7 | 0.990293 | -1.878438 | 1.114055 |
| 5 | 6 | 1.829867 | -1.247932 | 2.164529 |
| 6 | 6 | 2.717593 | -0.120828 | 1.642069 |
| 7 | 7 | 1.948152 | 1.001069 | 1.037843 |
| 8 | 6 | 1.358781 | 1.853748 | 2.099793 |
| 9 | 6 | 0.215392 | 2.738522 | 1.608553 |
| 10 | 7 | -0.930371 | 1.964241 | 1.057189 |
| 11 | 6 | -1.739649 | 1.383785 | 2.157936 |
| 12 | 6 | -2.644066 | 0.237593 | 1.710520 |
| 13 | 6 | -2.795667 | -1.747373 | 0.279920 |
| 14 | 6 | -3.174182 | -0.969554 | -1.008380 |
| 15 | 8 | -2.324048 | -0.061321 | -1.390516 |
| 16 | 6 | 1.786849 | -2.783877 | 0.225602 |
| 17 | 6 | 0.972434 | -3.149073 | -1.044550 |
| 18 | 8 | 0.015810 | -2.326283 | -1.362227 |
| 19 | 6 | 2.814264 | 1.777734 | 0.093653 |
| 20 | 6 | 3.137882 | 0.907380 | -1.153633 |
| 21 | 8 | 2.275840 | -0.018983 | -1.436892 |
| 22 | 6 | -1.748537 | 2.824162 | 0.142208 |
| 23 | 6 | -0.937586 | 3.136345 | -1.146855 |
| 24 | 8 | -0.034648 | 2.264090 | -1.471153 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 25 | 1 | -0.875113 | -1.007913 | 2.964735 |
| 26 | 1 | -2.007352 | -2.325536 | 2.748832 |
| 27 | 1 | -0.526218 | -3.319084 | 0.986845 |
| 28 | 1 | 0.204634 | -3.222408 | 2.588301 |
| 29 | 1 | 1.158189 | -0.861165 | 2.935373 |
| 30 | 1 | 2.468191 | -1.990095 | 2.663714 |
| 31 | 1 | 3.394925 | -0.507087 | 0.876120 |
| 32 | 1 | 3.342625 | 0.233632 | 2.474221 |
| 33 | 1 | 0.996872 | 1.190191 | 2.889545 |
| 34 | 1 | 2.119349 | 2.495033 | 2.566713 |
| 35 | 1 | 0.573974 | 3.404912 | 0.819740 |
| 36 | 1 | -0.106153 | 3.374969 | 2.445353 |
| 37 | 1 | -1.045869 | 1.027723 | 2.924078 |
| 38 | 1 | -2.361804 | 2.148509 | 2.643381 |
| 39 | 1 | -3.339785 | 0.591047 | 0.944964 |
| 40 | 1 | -3.247876 | -0.075508 | 2.574260 |
| 41 | 1 | -2.177539 | -2.580076 | -0.078496 |
| 42 | 1 | 2.615573 | -2.172678 | -0.152204 |
| 43 | 1 | 2.182973 | 2.588755 | -0.290626 |
| 44 | 1 | -2.577884 | 2.191298 | -0.197875 |
| 45 | 8 | -0.414342 | -0.461612 | -3.217634 |
| 46 | 1 | -0.257004 | -1.401003 | -2.972525 |
| 47 | 1 | -1.361019 | -0.323148 | -2.993124 |
| 48 | 60 | 0.009473 | 0.012587 | -0.592141 |
| 49 | 6 | 4.084169 | 2.384502 | 0.702398 |
| 50 | 1 | 4.756217 | 1.613870 | 1.091450 |
| 51 | 1 | 4.616267 | 2.920014 | -0.085587 |
| 52 | 1 | 3.857836 | 3.090042 | 1.507337 |
| 53 | 6 | -2.325497 | 4.100040 | 0.767473 |
| 54 | 1 | -1.537073 | 4.777053 | 1.109274 |
| 55 | 1 | -2.900924 | 4.623155 | 0.001935 |
| 56 | 1 | -2.989233 | 3.882289 | 1.609441 |
| 57 | 6 | -4.038960 | -2.318123 | 0.973858 |
| 58 | 1 | -4.703149 | -1.526527 | 1.332927 |
| 59 | 1 | -4.593923 | -2.909362 | 0.243607 |
| 60 | 1 | -3.779697 | -2.966197 | 1.815877 |
| 61 | 6 | 2.363924 | -4.037605 | 0.896266 |
| 62 | 1 | 1.576173 | -4.696404 | 1.273526 |
| 63 | 1 | 2.929758 | -4.592942 | 0.146410 |
| 64 | 1 | 3.036925 | -3.789268 | 1.722040 |
| 65 | 8 | -4.204958 | -1.280592 | -1.617373 |
| 66 | 8 | -1.219458 | 4.152682 | -1.797158 |
| 67 | 8 | 4.151707 | 1.170299 | -1.815841 |
| 68 | 8 | 1.298630 | -4.148039 | -1.696906 |

E(RTPSSh) = -1712.7334131 Hartree
Zero-point correction = 0.561120 Hartree/particle
Sum of electronic and thermal Energies = -1712.136829 Hartree
Sum of electronic and thermal Enthalpies = -1712.135885 Hartree
Sum of electronic and thermal Free Energies = -1712.236808 Hartree

Table S23. [Sm(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | -1.721883 | -1.203526 | 1.133408 |
| 2 | 6 | -0.983300 | -1.898035 | 2.217766 |
| 3 | 6 | 0.271966 | -2.614938 | 1.727580 |
| 4 | 7 | 1.266120 | -1.693267 | 1.112139 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 5 | 6 | 1.994608 | -0.947062 | 2.169036 |
| 6 | 6 | 2.693408 | 0.306556 | 1.650245 |
| 7 | 7 | 1.752152 | 1.287617 | 1.042403 |
| 8 | 6 | 1.042355 | 2.041510 | 2.105699 |
| 9 | 6 | -0.226273 | 2.731768 | 1.612294 |
| 10 | 7 | -1.227364 | 1.778568 | 1.057706 |
| 11 | 6 | -1.939378 | 1.082895 | 2.158473 |
| 12 | 6 | -2.650186 | -0.190313 | 1.707278 |
| 13 | 6 | -2.475634 | -2.161745 | 0.262639 |
| 14 | 6 | -2.955033 | -1.437188 | -1.021370 |
| 15 | 8 | -2.251885 | -0.401023 | -1.375410 |
| 16 | 6 | 2.194598 | -2.453942 | 0.215455 |
| 17 | 6 | 1.437468 | -2.930052 | -1.051961 |
| 18 | 8 | 0.369105 | -2.253342 | -1.358174 |
| 19 | 6 | 2.481761 | 2.185719 | 0.090828 |
| 20 | 6 | 2.940139 | 1.358505 | -1.141640 |
| 21 | 8 | 2.215740 | 0.319367 | -1.420210 |
| 22 | 6 | -2.166356 | 2.490487 | 0.131823 |
| 23 | 6 | -1.393661 | 2.930204 | -1.141378 |
| 24 | 8 | -0.373175 | 2.195131 | -1.457327 |
| 25 | 1 | -0.712200 | -1.149405 | 2.966689 |
| 26 | 1 | -1.622758 | -2.627012 | 2.734433 |
| 27 | 1 | 0.002687 | -3.360967 | 0.975779 |
| 28 | 1 | 0.711066 | -3.157206 | 2.577066 |
| 29 | 1 | 1.269207 | -0.670990 | 2.938691 |
| 30 | 1 | 2.739804 | -1.582810 | 2.666964 |
| 31 | 1 | 3.427504 | 0.033318 | 0.888239 |
| 32 | 1 | 3.249339 | 0.758862 | 2.483779 |
| 33 | 1 | 0.788565 | 1.332405 | 2.897884 |
| 34 | 1 | 1.695465 | 2.795105 | 2.567008 |
| 35 | 1 | 0.022719 | 3.448004 | 0.825177 |
| 36 | 1 | -0.650286 | 3.307037 | 2.447590 |
| 37 | 1 | -1.201404 | 0.838709 | 2.926873 |
| 38 | 1 | -2.674626 | 1.742392 | 2.639903 |
| 39 | 1 | -3.391588 | 0.050771 | 0.941301 |
| 40 | 1 | -3.197904 | -0.600135 | 2.567792 |
| 41 | 1 | -1.733696 | -2.885693 | -0.096660 |
| 42 | 1 | 2.913551 | -1.716926 | -0.163065 |
| 43 | 1 | 1.728011 | 2.877864 | -0.304826 |
| 44 | 1 | -2.871447 | 1.727931 | -0.221686 |
| 45 | 8 | -0.304017 | -0.441112 | -3.177978 |
| 46 | 1 | -0.010332 | -1.352214 | -2.954315 |
| 47 | 1 | -1.262857 | -0.453539 | -2.963093 |
| 48 | 6 | 3.635592 | 2.995710 | 0.692698 |
| 49 | 1 | 4.419098 | 2.347522 | 1.096291 |
| 50 | 1 | 4.080602 | 3.597557 | -0.101517 |
| 51 | 1 | 3.296384 | 3.669023 | 1.485536 |
| 52 | 6 | -2.955336 | 3.651512 | 0.747419 |
| 53 | 1 | -2.294346 | 4.445831 | 1.106326 |
| 54 | 1 | -3.594785 | 4.078368 | -0.027130 |
| 55 | 1 | -3.590571 | 3.324328 | 1.575748 |
| 56 | 6 | -3.621660 | -2.922629 | 0.940181 |
| 57 | 1 | -4.401313 | -2.245682 | 1.301363 |
| 58 | 1 | -4.074502 | -3.584282 | 0.199799 |
| 59 | 1 | -3.271836 | -3.532245 | 1.778026 |
| 60 | 6 | 2.964635 | -3.605304 | 0.874312 |
| 61 | 1 | 2.291859 | -4.381032 | 1.251608 |
| 62 | 1 | 3.606383 | -4.061404 | 0.118603 |
| 63 | 1 | 3.595595 | -3.259271 | 1.697941 |
| 64 | 8 | -3.917250 | -1.893574 | -1.650077 |
| 65 | 8 | -1.804585 | 3.903570 | -1.788363 |
| 66 | 8 | 3.919088 | 1.746748 | -1.794327 |

| | | | | |
|----|----|----------|-----------|-----------|
| 67 | 8 | 1.899317 | -3.868707 | -1.711490 |
| 68 | 62 | 0.007717 | 0.014865 | -0.565502 |

E(RTPSSh) = -1713.9543252 Hartree
 Zero-point correction = 0.560421 Hartree/particle
 Sum of electronic and thermal Energies = -1713.358334 Hartree
 Sum of electronic and thermal Enthalpies = -1713.357390 Hartree
 Sum of electronic and thermal Free Energies = -1713.458503 Hartree

Table S24. [Eu(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.749346 | -1.154337 | 1.135006 |
| 2 | 6 | -1.035055 | -1.874909 | 2.218637 |
| 3 | 6 | 0.201087 | -2.622808 | 1.728416 |
| 4 | 7 | 1.216681 | -1.725360 | 1.112354 |
| 5 | 6 | 1.970032 | -1.003875 | 2.168986 |
| 6 | 6 | 2.701046 | 0.230416 | 1.649631 |
| 7 | 7 | 1.784183 | 1.236021 | 1.044953 |
| 8 | 6 | 1.099390 | 2.009247 | 2.110450 |
| 9 | 6 | -0.149931 | 2.733114 | 1.617829 |
| 10 | 7 | -1.174202 | 1.805537 | 1.062854 |
| 11 | 6 | -1.906155 | 1.132156 | 2.164164 |
| 12 | 6 | -2.651391 | -0.119945 | 1.712009 |
| 13 | 6 | -2.527921 | -2.086439 | 0.258448 |
| 14 | 6 | -2.977403 | -1.343254 | -1.024678 |
| 15 | 8 | -2.245843 | -0.322291 | -1.366527 |
| 16 | 6 | 2.119659 | -2.508913 | 0.209777 |
| 17 | 6 | 1.341040 | -2.958857 | -1.053079 |
| 18 | 8 | 0.290263 | -2.250112 | -1.349473 |
| 19 | 6 | 2.534574 | 2.113359 | 0.090514 |
| 20 | 6 | 2.957789 | 1.274508 | -1.145751 |
| 21 | 8 | 2.209571 | 0.248590 | -1.410218 |
| 22 | 6 | -2.092069 | 2.542110 | 0.135619 |
| 23 | 6 | -1.309016 | 2.948033 | -1.141544 |
| 24 | 8 | -0.300920 | 2.190367 | -1.444358 |
| 25 | 1 | -0.745899 | -1.138194 | 2.972833 |
| 26 | 1 | -1.697125 | -2.588211 | 2.728719 |
| 27 | 1 | -0.087180 | -3.361996 | 0.976820 |
| 28 | 1 | 0.627344 | -3.175740 | 2.577489 |
| 29 | 1 | 1.255613 | -0.709777 | 2.942440 |
| 30 | 1 | 2.698555 | -1.662616 | 2.661640 |
| 31 | 1 | 3.425074 | -0.062238 | 0.885162 |
| 32 | 1 | 3.271319 | 0.667467 | 2.481527 |
| 33 | 1 | 0.827219 | 1.307481 | 2.903175 |
| 34 | 1 | 1.774825 | 2.743986 | 2.570130 |
| 35 | 1 | 0.118077 | 3.442441 | 0.830722 |
| 36 | 1 | -0.559720 | 3.319086 | 2.452717 |
| 37 | 1 | -1.175695 | 0.867023 | 2.933004 |
| 38 | 1 | -2.622027 | 1.813358 | 2.644784 |
| 39 | 1 | -3.387292 | 0.142108 | 0.947612 |
| 40 | 1 | -3.208404 | -0.517734 | 2.572114 |
| 41 | 1 | -1.807301 | -2.831563 | -0.099867 |
| 42 | 1 | 2.856583 | -1.791513 | -0.171021 |
| 43 | 1 | 1.799938 | 2.828370 | -0.299857 |
| 44 | 1 | -2.822307 | 1.801564 | -0.212706 |
| 45 | 8 | -0.305470 | -0.420102 | -3.168989 |
| 46 | 1 | -0.044624 | -1.339876 | -2.940087 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 47 | 1 | -1.263567 | -0.397321 | -2.952064 |
| 48 | 6 | 3.716912 | 2.886489 | 0.685273 |
| 49 | 1 | 4.479531 | 2.214341 | 1.089710 |
| 50 | 1 | 4.178950 | 3.468336 | -0.114143 |
| 51 | 1 | 3.402772 | 3.574694 | 1.475733 |
| 52 | 6 | -2.840747 | 3.732492 | 0.745669 |
| 53 | 1 | -2.153053 | 4.505647 | 1.100661 |
| 54 | 1 | -3.464556 | 4.176798 | -0.031832 |
| 55 | 1 | -3.486973 | 3.431352 | 1.575479 |
| 56 | 6 | -3.701286 | -2.812586 | 0.927826 |
| 57 | 1 | -4.462726 | -2.112563 | 1.283909 |
| 58 | 1 | -4.168872 | -3.460174 | 0.184156 |
| 59 | 1 | -3.376035 | -3.432933 | 1.767764 |
| 60 | 6 | 2.860033 | -3.683851 | 0.861052 |
| 61 | 1 | 2.167703 | -4.440615 | 1.241475 |
| 62 | 1 | 3.482677 | -4.156829 | 0.099696 |
| 63 | 1 | 3.506956 | -3.358347 | 1.680768 |
| 64 | 8 | -3.945307 | -1.771035 | -1.664709 |
| 65 | 8 | -1.701154 | 3.918870 | -1.803894 |
| 66 | 8 | 3.933717 | 1.642086 | -1.814824 |
| 67 | 8 | 1.769609 | -3.908734 | -1.718958 |
| 68 | 63 | 0.009837 | 0.015256 | -0.552773 |

E(RTPSSh) = -1714.5519019 Hartree

Zero-point correction = 0.561011 Hartree/particle

Sum of electronic and thermal Energies = -1713.955534 Hartree

Sum of electronic and thermal Enthalpies = -1713.954590 Hartree

Sum of electronic and thermal Free Energies = -1714.054459 Hartree

Table S25. [Gd(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.438246 | -1.523052 | 1.136097 |
| 2 | 6 | -0.580698 | -2.063353 | 2.220228 |
| 3 | 6 | 0.794155 | -2.510273 | 1.731851 |
| 4 | 7 | 1.576212 | -1.405143 | 1.114999 |
| 5 | 6 | 2.146940 | -0.531847 | 2.171008 |
| 6 | 6 | 2.577352 | 0.836941 | 1.651743 |
| 7 | 7 | 1.455061 | 1.607016 | 1.050048 |
| 8 | 6 | 0.612866 | 2.204701 | 2.114624 |
| 9 | 6 | -0.769510 | 2.623679 | 1.622319 |
| 10 | 7 | -1.556110 | 1.488002 | 1.068210 |
| 11 | 6 | -2.114815 | 0.664777 | 2.168260 |
| 12 | 6 | -2.553017 | -0.724774 | 1.714525 |
| 13 | 6 | -1.977062 | -2.603424 | 0.252155 |
| 14 | 6 | -2.574906 | -1.976907 | -1.032534 |
| 15 | 8 | -2.099943 | -0.810452 | -1.362594 |
| 16 | 6 | 2.630913 | -1.957487 | 0.207455 |
| 17 | 6 | 1.970826 | -2.561800 | -1.057761 |
| 18 | 8 | 0.783964 | -2.110761 | -1.343783 |
| 19 | 6 | 1.983113 | 2.631152 | 0.092644 |
| 20 | 6 | 2.569585 | 1.907821 | -1.150000 |
| 21 | 8 | 2.082030 | 0.731850 | -1.395768 |
| 22 | 6 | -2.616893 | 1.995605 | 0.140856 |
| 23 | 6 | -1.944967 | 2.554715 | -1.141623 |
| 24 | 8 | -0.785505 | 2.051606 | -1.430245 |
| 25 | 1 | -0.467835 | -1.278638 | 2.972937 |
| 26 | 1 | -1.064458 | -2.907872 | 2.730588 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 27 | 1 | 0.684807 | -3.297848 | 0.981776 |
| 28 | 1 | 1.335152 | -2.948892 | 2.582406 |
| 29 | 1 | 1.384324 | -0.409172 | 2.944644 |
| 30 | 1 | 3.006579 | -1.007928 | 2.663197 |
| 31 | 1 | 3.346257 | 0.717625 | 0.884229 |
| 32 | 1 | 3.035377 | 1.392602 | 2.482317 |
| 33 | 1 | 0.511673 | 1.461766 | 2.910320 |
| 34 | 1 | 1.101967 | 3.076090 | 2.572138 |
| 35 | 1 | -0.670598 | 3.374075 | 0.833554 |
| 36 | 1 | -1.302087 | 3.102007 | 2.456637 |
| 37 | 1 | -1.343348 | 0.574876 | 2.937675 |
| 38 | 1 | -2.968491 | 1.162596 | 2.649111 |
| 39 | 1 | -3.330946 | -0.638730 | 0.951304 |
| 40 | 1 | -3.002677 | -1.241035 | 2.574634 |
| 41 | 1 | -1.102525 | -3.162619 | -0.100780 |
| 42 | 1 | 3.184626 | -1.088507 | -0.166451 |
| 43 | 1 | 1.103785 | 3.165769 | -0.286494 |
| 44 | 1 | -3.165849 | 1.108721 | -0.197260 |
| 45 | 8 | -0.183992 | -0.448430 | -3.160994 |
| 46 | 1 | 0.273628 | -1.288412 | -2.934810 |
| 47 | 1 | -1.123728 | -0.642358 | -2.951480 |
| 48 | 64 | 0.005629 | 0.017452 | -0.537450 |
| 49 | 6 | 2.969293 | 3.648007 | 0.678646 |
| 50 | 1 | 3.869806 | 3.164264 | 1.068483 |
| 51 | 1 | 3.276630 | 4.322470 | -0.122517 |
| 52 | 1 | 2.518337 | 4.243792 | 1.477714 |
| 53 | 6 | -3.611524 | 2.994154 | 0.743882 |
| 54 | 1 | -3.115579 | 3.906934 | 1.086929 |
| 55 | 1 | -4.321746 | 3.276874 | -0.035061 |
| 56 | 1 | -4.169981 | 2.563859 | 1.580543 |
| 57 | 6 | -2.956911 | -3.584094 | 0.908715 |
| 58 | 1 | -3.862799 | -3.081993 | 1.261033 |
| 59 | 1 | -3.255607 | -4.317468 | 0.157789 |
| 60 | 1 | -2.503087 | -4.117413 | 1.749154 |
| 61 | 6 | 3.622801 | -2.937091 | 0.847572 |
| 62 | 1 | 3.125362 | -3.836616 | 1.222172 |
| 63 | 1 | 4.334223 | -3.246952 | 0.080196 |
| 64 | 1 | 4.180287 | -2.477857 | 1.669197 |
| 65 | 8 | -3.411168 | -2.614723 | -1.683876 |
| 66 | 8 | -2.551558 | 3.395289 | -1.820905 |
| 67 | 8 | 3.416228 | 2.491992 | -1.840697 |
| 68 | 8 | 2.601769 | -3.382838 | -1.733870 |

E(RTPSSh) = -1715.1427197 Hartree

Zero-point correction = 0.561633 Hartree/particle

Sum of electronic and thermal Energies = -1714.545835 Hartree

Sum of electronic and thermal Enthalpies = -1714.544891 Hartree

Sum of electronic and thermal Free Energies = -1714.644311 Hartree

Table S26. [Tb(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | -1.361218 | -1.586820 | 1.136151 |
| 2 | 6 | -0.484508 | -2.093792 | 2.221305 |
| 3 | 6 | 0.910044 | -2.471343 | 1.732446 |
| 4 | 7 | 1.635212 | -1.326966 | 1.117275 |
| 5 | 6 | 2.168522 | -0.432224 | 2.174607 |
| 6 | 6 | 2.530760 | 0.955655 | 1.656149 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 7 | 7 | 1.371165 | 1.667874 | 1.052924 |
| 8 | 6 | 0.505472 | 2.230473 | 2.117449 |
| 9 | 6 | -0.895156 | 2.579881 | 1.625241 |
| 10 | 7 | -1.621795 | 1.405013 | 1.070372 |
| 11 | 6 | -2.148253 | 0.560344 | 2.170070 |
| 12 | 6 | -2.516427 | -0.847763 | 1.714163 |
| 13 | 6 | -1.846516 | -2.687785 | 0.245469 |
| 14 | 6 | -2.473443 | -2.081615 | -1.034446 |
| 15 | 8 | -2.047392 | -0.894742 | -1.358957 |
| 16 | 6 | 2.713085 | -1.827328 | 0.206278 |
| 17 | 6 | 2.077764 | -2.459740 | -1.057222 |
| 18 | 8 | 0.872165 | -2.057951 | -1.340804 |
| 19 | 6 | 1.851594 | 2.713332 | 0.092780 |
| 20 | 6 | 2.476507 | 2.011531 | -1.142842 |
| 21 | 8 | 2.036593 | 0.816394 | -1.387849 |
| 22 | 6 | -2.702705 | 1.861607 | 0.138720 |
| 23 | 6 | -2.051148 | 2.455490 | -1.137759 |
| 24 | 8 | -0.870092 | 2.002678 | -1.423132 |
| 25 | 1 | -0.410909 | -1.310154 | 2.980210 |
| 26 | 1 | -0.930252 | -2.963558 | 2.723701 |
| 27 | 1 | 0.838560 | -3.261453 | 0.980519 |
| 28 | 1 | 1.473971 | -2.884882 | 2.580560 |
| 29 | 1 | 1.404138 | -0.347477 | 2.951795 |
| 30 | 1 | 3.051493 | -0.868909 | 2.661953 |
| 31 | 1 | 3.305764 | 0.874438 | 0.889789 |
| 32 | 1 | 2.959416 | 1.534800 | 2.486216 |
| 33 | 1 | 0.440378 | 1.486891 | 2.916436 |
| 34 | 1 | 0.954442 | 3.125574 | 2.570204 |
| 35 | 1 | -0.833165 | 3.334464 | 0.836715 |
| 36 | 1 | -1.452852 | 3.030607 | 2.458417 |
| 37 | 1 | -1.378433 | 0.507538 | 2.944731 |
| 38 | 1 | -3.027090 | 1.019052 | 2.644316 |
| 39 | 1 | -3.295922 | -0.798263 | 0.949375 |
| 40 | 1 | -2.941604 | -1.388979 | 2.571260 |
| 41 | 1 | -0.945902 | -3.202358 | -0.109982 |
| 42 | 1 | 3.224837 | -0.932860 | -0.167540 |
| 43 | 1 | 0.948763 | 3.203423 | -0.291518 |
| 44 | 1 | -3.206615 | 0.949912 | -0.203842 |
| 45 | 8 | -0.154321 | -0.429207 | -3.144265 |
| 46 | 1 | 0.335956 | -1.251027 | -2.919767 |
| 47 | 1 | -1.086267 | -0.664166 | -2.943496 |
| 48 | 65 | 0.004773 | 0.018586 | -0.534929 |
| 49 | 6 | 2.787040 | 3.777209 | 0.677806 |
| 50 | 1 | 3.705342 | 3.336677 | 1.077208 |
| 51 | 1 | 3.069917 | 4.458566 | -0.126530 |
| 52 | 1 | 2.305007 | 4.358699 | 1.469289 |
| 53 | 6 | -3.745404 | 2.811061 | 0.739238 |
| 54 | 1 | -3.293927 | 3.745532 | 1.085164 |
| 55 | 1 | -4.465105 | 3.061582 | -0.042010 |
| 56 | 1 | -4.286803 | 2.354423 | 1.573128 |
| 57 | 6 | -2.780135 | -3.716667 | 0.894922 |
| 58 | 1 | -3.710181 | -3.259689 | 1.245602 |
| 59 | 1 | -3.041224 | -4.460319 | 0.140069 |
| 60 | 1 | -2.304813 | -4.231709 | 1.734813 |
| 61 | 6 | 3.749636 | -2.762260 | 0.841880 |
| 62 | 1 | 3.294466 | -3.685390 | 1.212700 |
| 63 | 1 | 4.474156 | -3.035886 | 0.072969 |
| 64 | 1 | 4.286448 | -2.281781 | 1.665134 |
| 65 | 8 | -3.284531 | -2.749030 | -1.687248 |
| 66 | 8 | -2.687610 | 3.275736 | -1.813908 |
| 67 | 8 | 3.308126 | 2.624191 | -1.826994 |
| 68 | 8 | 2.740043 | -3.254507 | -1.734565 |

E(RTPSSh) = -1715.7308748 Hartree
 Zero-point correction = 0.561381 Hartree/particle
 Sum of electronic and thermal Energies = -1715.134223 Hartree
 Sum of electronic and thermal Enthalpies = -1715.133279 Hartree
 Sum of electronic and thermal Free Energies = -1715.232692 Hartree

Table S27. [Dy(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.338908 | -1.602055 | 1.136612 |
| 2 | 6 | -0.458725 | -2.101230 | 2.222242 |
| 3 | 6 | 0.940048 | -2.460045 | 1.732829 |
| 4 | 7 | 1.648180 | -1.304681 | 1.118397 |
| 5 | 6 | 2.172765 | -0.406445 | 2.176761 |
| 6 | 6 | 2.516969 | 0.985433 | 1.658256 |
| 7 | 7 | 1.347094 | 1.680698 | 1.055060 |
| 8 | 6 | 0.477001 | 2.234750 | 2.120274 |
| 9 | 6 | -0.927267 | 2.566191 | 1.627559 |
| 10 | 7 | -1.636488 | 1.381172 | 1.071778 |
| 11 | 6 | -2.155270 | 0.531865 | 2.171410 |
| 12 | 6 | -2.504979 | -0.880023 | 1.714273 |
| 13 | 6 | -1.808999 | -2.706486 | 0.242341 |
| 14 | 6 | -2.436419 | -2.102672 | -1.037664 |
| 15 | 8 | -2.026442 | -0.907048 | -1.351170 |
| 16 | 6 | 2.729929 | -1.790029 | 0.204125 |
| 17 | 6 | 2.097043 | -2.423696 | -1.059223 |
| 18 | 8 | 0.884017 | -2.037053 | -1.332904 |
| 19 | 6 | 1.813852 | 2.729764 | 0.092195 |
| 20 | 6 | 2.441916 | 2.030020 | -1.142323 |
| 21 | 8 | 2.014712 | 0.828678 | -1.379332 |
| 22 | 6 | -2.720461 | 1.823964 | 0.136993 |
| 23 | 6 | -2.069952 | 2.421212 | -1.137815 |
| 24 | 8 | -0.882399 | 1.980519 | -1.415213 |
| 25 | 1 | -0.395164 | -1.318666 | 2.983176 |
| 26 | 1 | -0.894996 | -2.977544 | 2.721603 |
| 27 | 1 | 0.878486 | -3.249977 | 0.979886 |
| 28 | 1 | 1.510839 | -2.866711 | 2.579607 |
| 29 | 1 | 1.408490 | -0.331354 | 2.955056 |
| 30 | 1 | 3.061539 | -0.833750 | 2.661900 |
| 31 | 1 | 3.292699 | 0.914066 | 0.891665 |
| 32 | 1 | 2.937821 | 1.571330 | 2.487502 |
| 33 | 1 | 0.420966 | 1.491310 | 2.920060 |
| 34 | 1 | 0.916234 | 3.135584 | 2.571202 |
| 35 | 1 | -0.874446 | 3.321618 | 0.839190 |
| 36 | 1 | -1.492336 | 3.008997 | 2.459939 |
| 37 | 1 | -1.386402 | 0.488323 | 2.947583 |
| 38 | 1 | -3.040431 | 0.980765 | 2.643294 |
| 39 | 1 | -3.283952 | -0.839647 | 0.948477 |
| 40 | 1 | -2.923745 | -1.428462 | 2.569875 |
| 41 | 1 | -0.902046 | -3.210951 | -0.111277 |
| 42 | 1 | 3.231476 | -0.889227 | -0.168141 |
| 43 | 1 | 0.905350 | 3.209792 | -0.291211 |
| 44 | 1 | -3.213791 | 0.906517 | -0.205442 |
| 45 | 8 | -0.146493 | -0.416752 | -3.135998 |
| 46 | 1 | 0.349555 | -1.233699 | -2.906560 |
| 47 | 1 | -1.076054 | -0.657088 | -2.930754 |
| 48 | 6 | 2.740287 | 3.803819 | 0.672732 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 49 | 1 | 3.663475 | 3.373158 | 1.071596 |
| 50 | 1 | 3.015103 | 4.485850 | -0.133855 |
| 51 | 1 | 2.254194 | 4.382670 | 1.463683 |
| 52 | 6 | -3.773998 | 2.764060 | 0.733022 |
| 53 | 1 | -3.332861 | 3.703746 | 1.078112 |
| 54 | 1 | -4.494456 | 3.005688 | -0.050357 |
| 55 | 1 | -4.312673 | 2.303683 | 1.566642 |
| 56 | 6 | -2.734753 | -3.746054 | 0.885876 |
| 57 | 1 | -3.670475 | -3.299209 | 1.234465 |
| 58 | 1 | -2.985665 | -4.490358 | 0.128190 |
| 59 | 1 | -2.257344 | -4.258464 | 1.726207 |
| 60 | 6 | 3.777138 | -2.716591 | 0.834307 |
| 61 | 1 | 3.331969 | -3.644898 | 1.204316 |
| 62 | 1 | 4.501925 | -2.981299 | 0.062497 |
| 63 | 1 | 4.311784 | -2.232973 | 1.657152 |
| 64 | 8 | -3.232512 | -2.777806 | -1.700774 |
| 65 | 8 | -2.711029 | 3.233187 | -1.819541 |
| 66 | 8 | 3.263515 | 2.648477 | -1.833238 |
| 67 | 8 | 2.765585 | -3.205558 | -1.745240 |
| 68 | 66 | 0.004203 | 0.019019 | -0.524394 |

E(RTPSSh) = -1716.3170192 Hartree

Zero-point correction = 0.561261 Hartree/particle

Sum of electronic and thermal Energies = -1715.720433 Hartree

Sum of electronic and thermal Enthalpies = -1715.719489 Hartree

Sum of electronic and thermal Free Energies = -1715.819036 Hartree

Table S28. [Ho(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.318696 | -1.615109 | 1.135821 |
| 2 | 6 | -0.435704 | -2.106650 | 2.221913 |
| 3 | 6 | 0.966111 | -2.449715 | 1.732095 |
| 4 | 7 | 1.659184 | -1.284856 | 1.118297 |
| 5 | 6 | 2.174800 | -0.384256 | 2.178439 |
| 6 | 6 | 2.504129 | 1.010536 | 1.660051 |
| 7 | 7 | 1.325660 | 1.691078 | 1.056469 |
| 8 | 6 | 0.452582 | 2.237119 | 2.123266 |
| 9 | 6 | -0.954441 | 2.553044 | 1.630188 |
| 10 | 7 | -1.648112 | 1.359314 | 1.073261 |
| 11 | 6 | -2.158281 | 0.505940 | 2.173435 |
| 12 | 6 | -2.493483 | -0.908221 | 1.714519 |
| 13 | 6 | -1.776854 | -2.722285 | 0.238940 |
| 14 | 6 | -2.405623 | -2.119181 | -1.039964 |
| 15 | 8 | -2.007148 | -0.917457 | -1.344966 |
| 16 | 6 | 2.744467 | -1.757978 | 0.202121 |
| 17 | 6 | 2.112993 | -2.393309 | -1.060344 |
| 18 | 8 | 0.895620 | -2.015869 | -1.328104 |
| 19 | 6 | 1.781807 | 2.743278 | 0.092102 |
| 20 | 6 | 2.411909 | 2.045206 | -1.141823 |
| 21 | 8 | 1.993778 | 0.839570 | -1.373269 |
| 22 | 6 | -2.735266 | 1.790999 | 0.137115 |
| 23 | 6 | -2.086056 | 2.391538 | -1.136239 |
| 24 | 8 | -0.893758 | 1.960363 | -1.408094 |
| 25 | 1 | -0.380325 | -1.324498 | 2.983850 |
| 26 | 1 | -0.863732 | -2.988039 | 2.719558 |
| 27 | 1 | 0.912788 | -3.239627 | 0.978592 |
| 28 | 1 | 1.542833 | -2.850245 | 2.577705 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 29 | 1 | 1.409682 | -0.317227 | 2.956555 |
| 30 | 1 | 3.067819 | -0.803549 | 2.662804 |
| 31 | 1 | 3.280934 | 0.947322 | 0.893881 |
| 32 | 1 | 2.917726 | 1.602167 | 2.488774 |
| 33 | 1 | 0.404569 | 1.493294 | 2.923094 |
| 34 | 1 | 0.883677 | 3.142583 | 2.572778 |
| 35 | 1 | -0.909384 | 3.309326 | 0.842240 |
| 36 | 1 | -1.526027 | 2.988502 | 2.461893 |
| 37 | 1 | -1.388762 | 0.469501 | 2.949204 |
| 38 | 1 | -3.047754 | 0.946484 | 2.645196 |
| 39 | 1 | -3.272654 | -0.874505 | 0.948709 |
| 40 | 1 | -2.906020 | -1.463550 | 2.568627 |
| 41 | 1 | -0.865288 | -3.218739 | -0.114180 |
| 42 | 1 | 3.238046 | -0.852403 | -0.169228 |
| 43 | 1 | 0.869313 | 3.216431 | -0.290062 |
| 44 | 1 | -3.220718 | 0.869393 | -0.205191 |
| 45 | 8 | -0.139669 | -0.401692 | -3.128041 |
| 46 | 1 | 0.361066 | -1.215665 | -2.898938 |
| 47 | 1 | -1.067392 | -0.648076 | -2.922611 |
| 48 | 67 | 0.003629 | 0.019551 | -0.516276 |
| 49 | 6 | 2.702245 | 3.824140 | 0.669379 |
| 50 | 1 | 3.629321 | 3.400462 | 1.066642 |
| 51 | 1 | 2.970545 | 4.507024 | -0.138702 |
| 52 | 1 | 2.214076 | 4.400656 | 1.460802 |
| 53 | 6 | -3.796623 | 2.723778 | 0.730533 |
| 54 | 1 | -3.363731 | 3.668407 | 1.072459 |
| 55 | 1 | -4.519637 | 2.956635 | -0.053188 |
| 56 | 1 | -4.330890 | 2.261403 | 1.565913 |
| 57 | 6 | -2.696501 | -3.769495 | 0.878613 |
| 58 | 1 | -3.636206 | -3.329802 | 1.225491 |
| 59 | 1 | -2.940209 | -4.514771 | 0.119504 |
| 60 | 1 | -2.217494 | -4.279293 | 1.719621 |
| 61 | 6 | 3.799166 | -2.678181 | 0.828890 |
| 62 | 1 | 3.361376 | -3.610944 | 1.196403 |
| 63 | 1 | 4.525757 | -2.935062 | 0.056109 |
| 64 | 1 | 4.330344 | -2.192913 | 1.653020 |
| 65 | 8 | -3.192747 | -2.798438 | -1.709514 |
| 66 | 8 | -2.731182 | 3.196872 | -1.822019 |
| 67 | 8 | 3.227623 | 2.667138 | -1.836577 |
| 68 | 8 | 2.784816 | -3.168165 | -1.751058 |

E(RTPSSh) = -1716.9009134 Hartree

Zero-point correction = 0.561363 Hartree/particle

Sum of electronic and thermal Energies = -1716.304245 Hartree

Sum of electronic and thermal Enthalpies = -1716.303301 Hartree

Sum of electronic and thermal Free Energies = -1716.402755 Hartree

Table S29. [Er(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | -1.315479 | -1.614070 | 1.136947 |
| 2 | 6 | -0.434131 | -2.108161 | 2.222816 |
| 3 | 6 | 0.967398 | -2.449556 | 1.732032 |
| 4 | 7 | 1.657484 | -1.282838 | 1.118826 |
| 5 | 6 | 2.175545 | -0.385002 | 2.179684 |
| 6 | 6 | 2.503190 | 1.010004 | 1.661813 |
| 7 | 7 | 1.322812 | 1.687619 | 1.059115 |
| 8 | 6 | 0.451794 | 2.234635 | 2.126630 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 9 | 6 | -0.954853 | 2.550251 | 1.633308 |
| 10 | 7 | -1.645728 | 1.355559 | 1.075502 |
| 11 | 6 | -2.157864 | 0.503595 | 2.175474 |
| 12 | 6 | -2.491722 | -0.910324 | 1.716014 |
| 13 | 6 | -1.771906 | -2.719100 | 0.236831 |
| 14 | 6 | -2.397430 | -2.110078 | -1.040185 |
| 15 | 8 | -1.997936 | -0.906430 | -1.336706 |
| 16 | 6 | 2.740281 | -1.753719 | 0.198698 |
| 17 | 6 | 2.102303 | -2.385429 | -1.061747 |
| 18 | 8 | 0.884042 | -2.005089 | -1.321782 |
| 19 | 6 | 1.776452 | 2.738406 | 0.092169 |
| 20 | 6 | 2.403242 | 2.035833 | -1.140228 |
| 21 | 8 | 1.982499 | 0.830011 | -1.366010 |
| 22 | 6 | -2.730702 | 1.786103 | 0.136475 |
| 23 | 6 | -2.075887 | 2.383083 | -1.135204 |
| 24 | 8 | -0.882871 | 1.949679 | -1.400855 |
| 25 | 1 | -0.379250 | -1.327816 | 2.986635 |
| 26 | 1 | -0.862715 | -2.990680 | 2.718043 |
| 27 | 1 | 0.914168 | -3.238728 | 0.977714 |
| 28 | 1 | 1.545769 | -2.850140 | 2.576451 |
| 29 | 1 | 1.412030 | -0.319051 | 2.959487 |
| 30 | 1 | 3.069464 | -0.805415 | 2.661503 |
| 31 | 1 | 3.279422 | 0.947802 | 0.894958 |
| 32 | 1 | 2.916417 | 1.602667 | 2.489940 |
| 33 | 1 | 0.404044 | 1.491407 | 2.927069 |
| 34 | 1 | 0.883780 | 3.140181 | 2.575198 |
| 35 | 1 | -0.909800 | 3.306856 | 0.845639 |
| 36 | 1 | -1.527946 | 2.984692 | 2.464469 |
| 37 | 1 | -1.389596 | 0.467485 | 2.952540 |
| 38 | 1 | -3.048023 | 0.944691 | 2.645451 |
| 39 | 1 | -3.270727 | -0.876859 | 0.950014 |
| 40 | 1 | -2.903569 | -1.467219 | 2.569404 |
| 41 | 1 | -0.859917 | -3.214445 | -0.116331 |
| 42 | 1 | 3.232355 | -0.847514 | -0.172735 |
| 43 | 1 | 0.863172 | 3.210010 | -0.289634 |
| 44 | 1 | -3.215425 | 0.864282 | -0.205862 |
| 45 | 8 | -0.140150 | -0.387644 | -3.121958 |
| 46 | 1 | 0.357548 | -1.203067 | -2.892717 |
| 47 | 1 | -1.068139 | -0.629972 | -2.913545 |
| 48 | 6 | 2.697861 | 3.820587 | 0.665080 |
| 49 | 1 | 3.624992 | 3.397946 | 1.063348 |
| 50 | 1 | 2.966041 | 4.500598 | -0.145518 |
| 51 | 1 | 2.210250 | 4.399990 | 1.454701 |
| 52 | 6 | -3.792731 | 2.720755 | 0.725452 |
| 53 | 1 | -3.359890 | 3.664859 | 1.068960 |
| 54 | 1 | -4.512380 | 2.954519 | -0.061147 |
| 55 | 1 | -4.330851 | 2.259177 | 1.558799 |
| 56 | 6 | -2.693030 | -3.767969 | 0.871349 |
| 57 | 1 | -3.632456 | -3.329134 | 1.220113 |
| 58 | 1 | -2.937215 | -4.509337 | 0.108517 |
| 59 | 1 | -2.214730 | -4.282361 | 1.709984 |
| 60 | 6 | 3.797035 | -2.675325 | 0.819546 |
| 61 | 1 | 3.360581 | -3.608014 | 1.188850 |
| 62 | 1 | 4.519392 | -2.932334 | 0.042784 |
| 63 | 1 | 4.332836 | -2.190798 | 1.641117 |
| 64 | 8 | -3.182920 | -2.784731 | -1.716124 |
| 65 | 8 | -2.716297 | 3.188234 | -1.825534 |
| 66 | 8 | 3.218783 | 2.653267 | -1.839121 |
| 67 | 8 | 2.768375 | -3.160194 | -1.757992 |
| 68 | 68 | 0.003522 | 0.019610 | -0.508740 |

E(RTPSSh) = -1717.4839164 Hartree

Zero-point correction = 0.561501 Hartree/particle
 Sum of electronic and thermal Energies = -1716.887141 Hartree
 Sum of electronic and thermal Enthalpies = -1716.886196 Hartree
 Sum of electronic and thermal Free Energies = -1716.985548 Hartree

Table S30. [Tm(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.435419 | -1.506241 | 1.139962 |
| 2 | 6 | -0.595459 | -2.067634 | 2.226046 |
| 3 | 6 | 0.775564 | -2.515930 | 1.735651 |
| 4 | 7 | 1.552001 | -1.405990 | 1.122076 |
| 5 | 6 | 2.139874 | -0.551257 | 2.181882 |
| 6 | 6 | 2.573263 | 0.814369 | 1.663637 |
| 7 | 7 | 1.447971 | 1.579352 | 1.062145 |
| 8 | 6 | 0.622942 | 2.192939 | 2.129444 |
| 9 | 6 | -0.755806 | 2.614623 | 1.637581 |
| 10 | 7 | -1.533875 | 1.476051 | 1.079965 |
| 11 | 6 | -2.112535 | 0.666858 | 2.179170 |
| 12 | 6 | -2.554443 | -0.716357 | 1.719078 |
| 13 | 6 | -1.973037 | -2.571801 | 0.237902 |
| 14 | 6 | -2.545527 | -1.913223 | -1.038521 |
| 15 | 8 | -2.051837 | -0.743491 | -1.329281 |
| 16 | 6 | 2.593514 | -1.957349 | 0.199687 |
| 17 | 6 | 1.906086 | -2.531355 | -1.061875 |
| 18 | 8 | 0.718895 | -2.058531 | -1.314645 |
| 19 | 6 | 1.979126 | 2.592007 | 0.094473 |
| 20 | 6 | 2.544626 | 1.842782 | -1.139295 |
| 21 | 8 | 2.027661 | 0.674426 | -1.362659 |
| 22 | 6 | -2.581776 | 1.986297 | 0.139325 |
| 23 | 6 | -1.883342 | 2.524866 | -1.134213 |
| 24 | 8 | -0.729111 | 1.996949 | -1.398405 |
| 25 | 1 | -0.480186 | -1.292079 | 2.988392 |
| 26 | 1 | -1.091475 | -2.913662 | 2.722059 |
| 27 | 1 | 0.662298 | -3.298987 | 0.981484 |
| 28 | 1 | 1.321265 | -2.959318 | 2.580439 |
| 29 | 1 | 1.383688 | -0.427235 | 2.962036 |
| 30 | 1 | 2.999312 | -1.039286 | 2.662760 |
| 31 | 1 | 3.341677 | 0.693107 | 0.895872 |
| 32 | 1 | 3.031565 | 1.373397 | 2.491451 |
| 33 | 1 | 0.519352 | 1.455817 | 2.930375 |
| 34 | 1 | 1.123957 | 3.062486 | 2.577410 |
| 35 | 1 | -0.655064 | 3.366505 | 0.850368 |
| 36 | 1 | -1.293570 | 3.090951 | 2.469495 |
| 37 | 1 | -1.349218 | 0.570836 | 2.956222 |
| 38 | 1 | -2.965404 | 1.176561 | 2.648859 |
| 39 | 1 | -3.328716 | -0.623326 | 0.953073 |
| 40 | 1 | -3.007968 | -1.240219 | 2.572333 |
| 41 | 1 | -1.101116 | -3.135360 | -0.113685 |
| 42 | 1 | 3.156436 | -1.091945 | -0.168026 |
| 43 | 1 | 1.104385 | 3.133610 | -0.284569 |
| 44 | 1 | -3.137201 | 1.103948 | -0.199179 |
| 45 | 8 | -0.173298 | -0.370627 | -3.118958 |
| 46 | 1 | 0.258269 | -1.223182 | -2.891864 |
| 47 | 1 | -1.115159 | -0.537945 | -2.897366 |
| 48 | 69 | 0.007194 | 0.018833 | -0.506423 |
| 49 | 6 | 2.984283 | 3.599261 | 0.663268 |
| 50 | 1 | 3.878437 | 3.105774 | 1.055304 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 51 | 1 | 3.299311 | 4.258118 | -0.147956 |
| 52 | 1 | 2.547236 | 4.212962 | 1.456471 |
| 53 | 6 | -3.568501 | 3.003001 | 0.723888 |
| 54 | 1 | -3.064594 | 3.914032 | 1.059535 |
| 55 | 1 | -4.270834 | 3.285106 | -0.062488 |
| 56 | 1 | -4.137194 | 2.588938 | 1.561865 |
| 57 | 6 | -2.973115 | -3.548909 | 0.867396 |
| 58 | 1 | -3.877213 | -3.041237 | 1.216026 |
| 59 | 1 | -3.271641 | -4.267404 | 0.101989 |
| 60 | 1 | -2.536427 | -4.100288 | 1.705224 |
| 61 | 6 | 3.575303 | -2.961905 | 0.814987 |
| 62 | 1 | 3.067886 | -3.859892 | 1.179418 |
| 63 | 1 | 4.276039 | -3.270074 | 0.037023 |
| 64 | 1 | 4.146334 | -2.524196 | 1.639089 |
| 65 | 8 | -3.379743 | -2.521293 | -1.719043 |
| 66 | 8 | -2.458542 | 3.374673 | -1.828461 |
| 67 | 8 | 3.405761 | 2.391464 | -1.840400 |
| 68 | 8 | 2.508733 | -3.350557 | -1.764694 |

E(RTPSSh) = -1718.0634798 Hartree

Zero-point correction = 0.562082 Hartree/particle

Sum of electronic and thermal Energies = -1717.466376 Hartree

Sum of electronic and thermal Enthalpies = -1717.465432 Hartree

Sum of electronic and thermal Free Energies = -1717.563984 Hartree

Table S31. [Yb(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 1.991233 | -0.095141 | -1.261722 |
| 2 | 6 | 1.721010 | -1.065938 | -2.350449 |
| 3 | 6 | 1.041816 | -2.333180 | -1.842216 |
| 4 | 7 | -0.256999 | -2.054336 | -1.169276 |
| 5 | 6 | -1.321373 | -1.820671 | -2.177031 |
| 6 | 6 | -2.541882 | -1.122834 | -1.586157 |
| 7 | 7 | -2.205036 | 0.193658 | -0.978216 |
| 8 | 6 | -2.079305 | 1.231455 | -2.032126 |
| 9 | 6 | -1.332599 | 2.469700 | -1.547019 |
| 10 | 7 | 0.038717 | 2.155457 | -1.059435 |
| 11 | 6 | 0.967840 | 1.991786 | -2.206263 |
| 12 | 6 | 2.249052 | 1.259776 | -1.823180 |
| 13 | 6 | 3.134502 | -0.516754 | -0.391229 |
| 14 | 6 | 3.127904 | 0.339650 | 0.897788 |
| 15 | 8 | 1.956951 | 0.770918 | 1.276301 |
| 16 | 6 | -0.600415 | -3.167988 | -0.227608 |
| 17 | 6 | 0.315228 | -3.096307 | 1.018805 |
| 18 | 8 | 0.853576 | -1.933318 | 1.255127 |
| 19 | 6 | -3.220597 | 0.558343 | 0.062707 |
| 20 | 6 | -3.026838 | -0.353308 | 1.301685 |
| 21 | 8 | -1.837783 | -0.855450 | 1.447212 |
| 22 | 6 | 0.501526 | 3.204036 | -0.094533 |
| 23 | 6 | -0.273799 | 3.048292 | 1.239473 |
| 24 | 8 | -0.749103 | 1.863069 | 1.477446 |
| 25 | 1 | 1.082479 | -0.571233 | -3.087327 |
| 26 | 1 | 2.643122 | -1.343424 | -2.878911 |
| 27 | 1 | 1.688685 | -2.835394 | -1.117885 |
| 28 | 1 | 0.908003 | -3.022922 | -2.686737 |
| 29 | 1 | -0.892750 | -1.204738 | -2.972021 |
| 30 | 1 | -1.640964 | -2.759177 | -2.650316 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 31 | 1 | -2.984608 | -1.746937 | -0.805629 |
| 32 | 1 | -3.297938 | -1.011480 | -2.375412 |
| 33 | 1 | -1.546497 | 0.784324 | -2.876175 |
| 34 | 1 | -3.062273 | 1.536253 | -2.416498 |
| 35 | 1 | -1.879926 | 2.934723 | -0.722825 |
| 36 | 1 | -1.302020 | 3.202641 | -2.364906 |
| 37 | 1 | 0.438718 | 1.434719 | -2.984264 |
| 38 | 1 | 1.233103 | 2.961514 | -2.649467 |
| 39 | 1 | 2.791639 | 1.834118 | -1.067346 |
| 40 | 1 | 2.897798 | 1.203671 | -2.707922 |
| 41 | 1 | 2.889045 | -1.526766 | -0.043332 |
| 42 | 1 | -1.597442 | -2.933229 | 0.160372 |
| 43 | 1 | -2.942122 | 1.557616 | 0.415690 |
| 44 | 1 | 1.534188 | 2.940656 | 0.160043 |
| 45 | 8 | 1.398795 | -0.626214 | 3.683040 |
| 46 | 1 | 1.221342 | -1.316548 | 3.009728 |
| 47 | 1 | 1.715227 | 0.094083 | 3.103374 |
| 48 | 6 | -4.678617 | 0.585814 | -0.408597 |
| 49 | 1 | -5.018205 | -0.398039 | -0.744914 |
| 50 | 1 | -5.303030 | 0.879875 | 0.436718 |
| 51 | 1 | -4.833820 | 1.305091 | -1.218195 |
| 52 | 6 | 0.472380 | 4.646256 | -0.612313 |
| 53 | 1 | -0.542717 | 4.973505 | -0.854813 |
| 54 | 1 | 0.850258 | 5.298563 | 0.176894 |
| 55 | 1 | 1.102453 | 4.775724 | -1.497296 |
| 56 | 6 | 4.512206 | -0.538317 | -1.061004 |
| 57 | 1 | 4.812804 | 0.454265 | -1.408767 |
| 58 | 1 | 5.245709 | -0.865465 | -0.321969 |
| 59 | 1 | 4.544849 | -1.230584 | -1.907478 |
| 60 | 6 | -0.624374 | -4.575261 | -0.835860 |
| 61 | 1 | 0.359518 | -4.877954 | -1.205808 |
| 62 | 1 | -0.915320 | -5.278483 | -0.053584 |
| 63 | 1 | -1.345123 | -4.653767 | -1.655002 |
| 64 | 8 | 4.183596 | 0.528286 | 1.511701 |
| 65 | 8 | -0.363190 | 4.020344 | 2.000051 |
| 66 | 8 | -3.973374 | -0.518967 | 2.081394 |
| 67 | 8 | 0.454122 | -4.099005 | 1.727010 |
| 68 | 70 | -0.018290 | 0.004896 | 0.392415 |

E(RTPSSh) = -1718.6478812 Hartree

Zero-point correction = 0.561624 Hartree/particle

Sum of electronic and thermal Energies = -1718.050811 Hartree

Sum of electronic and thermal Enthalpies = -1718.049867 Hartree

Sum of electronic and thermal Free Energies = -1718.150084 Hartree

Table S32. [Lu(DOTMA)(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 1.888166 | -0.686745 | -1.237762 |
| 2 | 6 | 1.355764 | -1.540933 | -2.329287 |
| 3 | 6 | 0.326360 | -2.547089 | -1.827176 |
| 4 | 7 | -0.837318 | -1.892171 | -1.168668 |
| 5 | 6 | -1.781428 | -1.369222 | -2.187748 |
| 6 | 6 | -2.740322 | -0.332357 | -1.611837 |
| 7 | 7 | -2.028918 | 0.825078 | -1.001846 |
| 8 | 6 | -1.600305 | 1.778186 | -2.056459 |
| 9 | 6 | -0.522704 | 2.739047 | -1.567659 |
| 10 | 7 | 0.688542 | 2.030668 | -1.068427 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 11 | 6 | 1.540120 | 1.600175 | -2.205109 |
| 12 | 6 | 2.543897 | 0.525007 | -1.803343 |
| 13 | 6 | 2.846079 | -1.423677 | -0.352232 |
| 14 | 6 | 3.060557 | -0.613688 | 0.948575 |
| 15 | 8 | 2.076606 | 0.172070 | 1.288958 |
| 16 | 6 | -1.499335 | -2.847353 | -0.223111 |
| 17 | 6 | -0.616085 | -3.029068 | 1.034590 |
| 18 | 8 | 0.248810 | -2.079051 | 1.257486 |
| 19 | 6 | -2.895169 | 1.473375 | 0.036458 |
| 20 | 6 | -2.988027 | 0.538421 | 1.269529 |
| 21 | 8 | -1.992584 | -0.282641 | 1.424820 |
| 22 | 6 | 1.430758 | 2.898914 | -0.098013 |
| 23 | 6 | 0.627512 | 2.983505 | 1.224718 |
| 24 | 8 | -0.180375 | 1.991692 | 1.453525 |
| 25 | 1 | 0.899445 | -0.881172 | -3.072712 |
| 26 | 1 | 2.160246 | -2.080458 | -2.847204 |
| 27 | 1 | 0.788937 | -3.214816 | -1.095789 |
| 28 | 1 | 0.002848 | -3.170484 | -2.671837 |
| 29 | 1 | -1.189228 | -0.922004 | -2.990716 |
| 30 | 1 | -2.365430 | -2.177379 | -2.649070 |
| 31 | 1 | -3.358749 | -0.789559 | -0.835289 |
| 32 | 1 | -3.420392 | -0.001760 | -2.408605 |
| 33 | 1 | -1.222092 | 1.190637 | -2.897336 |
| 34 | 1 | -2.448982 | 2.359076 | -2.442265 |
| 35 | 1 | -0.913838 | 3.347290 | -0.748107 |
| 36 | 1 | -0.267529 | 3.427268 | -2.384847 |
| 37 | 1 | 0.879720 | 1.219724 | -2.989423 |
| 38 | 1 | 2.083758 | 2.447632 | -2.644485 |
| 39 | 1 | 3.224971 | 0.919690 | -1.044288 |
| 40 | 1 | 3.155377 | 0.269927 | -2.679558 |
| 41 | 1 | 2.315826 | -2.323493 | -0.020420 |
| 42 | 1 | -2.389653 | -2.329212 | 0.148149 |
| 43 | 1 | -2.331212 | 2.340808 | 0.397011 |
| 44 | 1 | 2.334848 | 2.341300 | 0.168735 |
| 45 | 8 | 0.933459 | -0.818332 | 3.645704 |
| 46 | 1 | 0.624162 | -1.487479 | 2.999184 |
| 47 | 1 | 1.519065 | -0.285222 | 3.071819 |
| 48 | 71 | -0.011869 | 0.011555 | 0.382104 |
| 49 | 6 | -4.274723 | 1.938705 | -0.441679 |
| 50 | 1 | -4.890960 | 1.104227 | -0.788832 |
| 51 | 1 | -4.789823 | 2.401221 | 0.402118 |
| 52 | 1 | -4.201446 | 2.677050 | -1.245769 |
| 53 | 6 | 1.835006 | 4.283541 | -0.616064 |
| 54 | 1 | 0.964387 | 4.900352 | -0.856647 |
| 55 | 1 | 2.393117 | 4.792360 | 0.171709 |
| 56 | 1 | 2.473277 | 4.218299 | -1.502171 |
| 57 | 6 | 4.173867 | -1.834503 | -0.997130 |
| 58 | 1 | 4.758490 | -0.967090 | -1.316605 |
| 59 | 1 | 4.761643 | -2.373465 | -0.252021 |
| 60 | 1 | 4.023401 | -2.491995 | -1.858186 |
| 61 | 6 | -1.923775 | -4.194284 | -0.820285 |
| 62 | 1 | -1.065757 | -4.777835 | -1.166140 |
| 63 | 1 | -2.423689 | -4.769536 | -0.039156 |
| 64 | 1 | -2.619940 | -4.068398 | -1.654423 |
| 65 | 8 | 4.094238 | -0.776640 | 1.604885 |
| 66 | 8 | 0.817410 | 3.939926 | 1.986098 |
| 67 | 8 | -3.952952 | 0.643311 | 2.036837 |
| 68 | 8 | -0.792574 | -4.010826 | 1.762971 |

E(RTPSSh) = -1719.2010682 Hartree

Zero-point correction = 0.561134 Hartree/particle

Sum of electronic and thermal Energies = -1718.604389 Hartree

Sum of electronic and thermal Enthalpies = -1718.603445 Hartree
 Sum of electronic and thermal Free Energies = -1718.703875 Hartree

Table S33. [La(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 2.080002 | -0.641511 | 1.574643 |
| 2 | 6 | 1.581235 | -1.549085 | 2.648928 |
| 3 | 6 | 0.591251 | -2.616757 | 2.187004 |
| 4 | 7 | -0.655953 | -2.059508 | 1.576956 |
| 5 | 6 | -1.548282 | -1.549096 | 2.659037 |
| 6 | 6 | -2.627190 | -0.566315 | 2.205463 |
| 7 | 7 | -2.080892 | 0.676364 | 1.576644 |
| 8 | 6 | -1.581737 | 1.587943 | 2.647469 |
| 9 | 6 | -0.592758 | 2.655619 | 2.182920 |
| 10 | 7 | 0.653336 | 2.098381 | 1.572004 |
| 11 | 6 | 1.545860 | 1.587730 | 2.652752 |
| 12 | 6 | 2.624329 | 0.605431 | 2.197977 |
| 13 | 6 | 3.153569 | -1.263475 | 0.720193 |
| 14 | 6 | 2.524055 | -2.252403 | -0.267106 |
| 15 | 8 | 1.414339 | -1.953231 | -0.814899 |
| 16 | 6 | -1.296829 | -3.127055 | 0.729188 |
| 17 | 6 | -2.297290 | -2.483907 | -0.238156 |
| 18 | 8 | -2.009138 | -1.364455 | -0.765596 |
| 19 | 6 | -3.149241 | 1.297105 | 0.715641 |
| 20 | 6 | -2.509291 | 2.275464 | -0.276975 |
| 21 | 8 | -1.393557 | 1.974783 | -0.807918 |
| 22 | 6 | 1.294052 | 3.162813 | 0.722149 |
| 23 | 6 | 2.281429 | 2.514148 | -0.255328 |
| 24 | 8 | 1.984780 | 1.394858 | -0.777814 |
| 25 | 1 | 1.112635 | -0.920649 | 3.409736 |
| 26 | 1 | 2.414287 | -2.053519 | 3.154453 |
| 27 | 1 | 1.055865 | -3.275979 | 1.451505 |
| 28 | 1 | 0.352442 | -3.235832 | 3.062521 |
| 29 | 1 | -0.907635 | -1.067592 | 3.401422 |
| 30 | 1 | -2.040146 | -2.377729 | 3.184041 |
| 31 | 1 | -3.299335 | -1.038849 | 1.487296 |
| 32 | 1 | -3.230924 | -0.320458 | 3.089839 |
| 33 | 1 | -1.112312 | 0.961967 | 3.409865 |
| 34 | 1 | -2.415132 | 2.092850 | 3.152135 |
| 35 | 1 | -1.059046 | 3.314126 | 1.447918 |
| 36 | 1 | -0.353534 | 3.275766 | 3.057819 |
| 37 | 1 | 0.906239 | 1.106349 | 3.396141 |
| 38 | 1 | 2.039243 | 2.415519 | 3.177927 |
| 39 | 1 | 3.292601 | 1.077198 | 1.475647 |
| 40 | 1 | 3.231910 | 0.363384 | 3.080678 |
| 41 | 1 | 3.485979 | -0.440941 | 0.073887 |
| 42 | 1 | -0.486469 | -3.465329 | 0.070224 |
| 43 | 1 | -3.485732 | 0.471572 | 0.075331 |
| 44 | 1 | 0.480770 | 3.508348 | 0.070851 |
| 45 | 8 | 0.076050 | -0.415575 | -2.720476 |
| 46 | 1 | 0.620737 | -1.217608 | -2.807191 |
| 47 | 1 | -0.764254 | -0.617966 | -3.161475 |
| 48 | 7 | 3.381999 | 3.165178 | -0.573212 |
| 49 | 7 | -3.163626 | 3.371381 | -0.601644 |
| 50 | 7 | -3.398926 | -3.138712 | -0.543693 |
| 51 | 7 | 3.177038 | -3.353120 | -0.573663 |
| 52 | 1 | 3.678906 | 4.080683 | -0.187919 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 53 | 1 | -4.075591 | 3.673306 | -0.210976 |
| 54 | 1 | -3.688641 | -4.056142 | -0.156786 |
| 55 | 1 | 4.084409 | -3.656300 | -0.171537 |
| 56 | 6 | 2.796293 | -4.345191 | -1.571423 |
| 57 | 1 | 2.686672 | -3.880986 | -2.556852 |
| 58 | 6 | 4.375048 | 2.770252 | -1.564114 |
| 59 | 1 | 3.910256 | 2.634821 | -2.545958 |
| 60 | 6 | -2.779205 | 4.352526 | -1.608518 |
| 61 | 1 | -1.832301 | 4.834165 | -1.343126 |
| 62 | 6 | -4.401873 | -2.748576 | -1.526562 |
| 63 | 1 | -3.945263 | -2.608800 | -2.511654 |
| 64 | 1 | 4.852356 | 1.825279 | -1.284186 |
| 65 | 1 | 1.841728 | -4.814065 | -1.311068 |
| 66 | 1 | -4.883105 | -1.807115 | -1.241579 |
| 67 | 1 | -2.652196 | 3.875427 | -2.585544 |
| 68 | 6 | -5.453564 | -3.907268 | -1.563643 |
| 69 | 8 | -5.212815 | -4.864051 | -0.762822 |
| 70 | 8 | -6.399084 | -3.759039 | -2.366624 |
| 71 | 6 | 3.942144 | -5.411536 | -1.586628 |
| 72 | 8 | 4.883295 | -5.185182 | -0.763232 |
| 73 | 8 | 3.800332 | -6.351943 | -2.396356 |
| 74 | 6 | 5.434108 | 3.921989 | -1.607458 |
| 75 | 8 | 5.205908 | 4.879444 | -0.803790 |
| 76 | 8 | 6.372946 | 3.768540 | -2.417426 |
| 77 | 6 | -3.933290 | 5.408892 | -1.653935 |
| 78 | 8 | -4.880998 | 5.190472 | -0.835974 |
| 79 | 8 | -3.791013 | 6.336281 | -2.478852 |
| 80 | 6 | 1.850802 | 4.373208 | 1.484654 |
| 81 | 1 | 2.771410 | 4.144304 | 2.028021 |
| 82 | 1 | 2.061750 | 5.182616 | 0.780297 |
| 83 | 1 | 1.114021 | 4.754860 | 2.195391 |
| 84 | 6 | -4.365692 | 1.853016 | 1.468695 |
| 85 | 1 | -5.175979 | 2.046513 | 0.760336 |
| 86 | 1 | -4.740848 | 1.121852 | 2.188711 |
| 87 | 1 | -4.147183 | 2.783035 | 2.000196 |
| 88 | 6 | -1.838288 | -4.343051 | 1.493546 |
| 89 | 1 | -2.753414 | -4.120695 | 2.048673 |
| 90 | 1 | -2.053794 | -5.150262 | 0.788082 |
| 91 | 1 | -1.091409 | -4.724617 | 2.193557 |
| 92 | 6 | 4.372175 | -1.806681 | 1.478823 |
| 93 | 1 | 4.157404 | -2.731610 | 2.020601 |
| 94 | 1 | 5.182429 | -2.004851 | 0.771777 |
| 95 | 1 | 4.745278 | -1.066521 | 2.190497 |
| 96 | 57 | -0.003425 | 0.012275 | -0.137353 |

E(RTPSSh) = -2542.8414576 Hartree

Zero-point correction = 0.780436 Hartree/particle

Sum of electronic and thermal Energies = -2542.007278 Hartree

Sum of electronic and thermal Enthalpies = -2542.006334 Hartree

Sum of electronic and thermal Free Energies = -2542.153601 Hartree

Table S34. [Ce(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | 2.092702 | -0.576430 | 1.597003 |
| 2 | 6 | 1.618153 | -1.493096 | 2.674670 |
| 3 | 6 | 0.662110 | -2.591513 | 2.214232 |
| 4 | 7 | -0.597538 | -2.070279 | 1.597441 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 5 | 6 | -1.512774 | -1.595274 | 2.676926 |
| 6 | 6 | -2.613816 | -0.639436 | 2.220724 |
| 7 | 7 | -2.094821 | 0.615848 | 1.594011 |
| 8 | 6 | -1.622250 | 1.539234 | 2.667065 |
| 9 | 6 | -0.666495 | 2.636574 | 2.202935 |
| 10 | 7 | 0.592372 | 2.113306 | 1.587895 |
| 11 | 6 | 1.506316 | 1.641093 | 2.668701 |
| 12 | 6 | 2.608026 | 0.684632 | 2.216314 |
| 13 | 6 | 3.179568 | -1.173571 | 0.742138 |
| 14 | 6 | 2.571573 | -2.168709 | -0.251171 |
| 15 | 8 | 1.447370 | -1.897109 | -0.784439 |
| 16 | 6 | -1.199042 | -3.151687 | 0.738265 |
| 17 | 6 | -2.208102 | -2.534498 | -0.236338 |
| 18 | 8 | -1.949011 | -1.402145 | -0.754272 |
| 19 | 6 | -3.174547 | 1.210444 | 0.728880 |
| 20 | 6 | -2.552940 | 2.194531 | -0.268761 |
| 21 | 8 | -1.423885 | 1.919089 | -0.785305 |
| 22 | 6 | 1.195118 | 3.188220 | 0.723338 |
| 23 | 6 | 2.189987 | 2.559574 | -0.259244 |
| 24 | 8 | 1.922265 | 1.425102 | -0.765980 |
| 25 | 1 | 1.128065 | -0.875076 | 3.430606 |
| 26 | 1 | 2.464494 | -1.969415 | 3.185454 |
| 27 | 1 | 1.148014 | -3.240997 | 1.483967 |
| 28 | 1 | 0.436882 | -3.213101 | 3.091462 |
| 29 | 1 | -0.892843 | -1.104141 | 3.430598 |
| 30 | 1 | -1.986464 | -2.442263 | 3.189124 |
| 31 | 1 | -3.271268 | -1.127806 | 1.499661 |
| 32 | 1 | -3.226945 | -0.408853 | 3.102692 |
| 33 | 1 | -1.132691 | 0.925578 | 3.426942 |
| 34 | 1 | -2.470078 | 2.016998 | 3.174128 |
| 35 | 1 | -1.152997 | 3.284078 | 1.471417 |
| 36 | 1 | -0.441556 | 3.260931 | 3.078521 |
| 37 | 1 | 0.886246 | 1.152148 | 3.423722 |
| 38 | 1 | 1.980496 | 2.488836 | 3.179464 |
| 39 | 1 | 3.263448 | 1.170459 | 1.491597 |
| 40 | 1 | 3.222740 | 0.460306 | 3.098759 |
| 41 | 1 | 3.496347 | -0.341560 | 0.100481 |
| 42 | 1 | -0.372601 | -3.460671 | 0.085187 |
| 43 | 1 | -3.493448 | 0.374559 | 0.093499 |
| 44 | 1 | 0.366013 | 3.503977 | 0.077304 |
| 45 | 8 | 0.004945 | -0.430417 | -2.657388 |
| 46 | 1 | 0.635600 | -1.168365 | -2.737978 |
| 47 | 1 | -0.853165 | -0.796954 | -2.928734 |
| 48 | 7 | 3.264289 | 3.241333 | -0.600302 |
| 49 | 7 | -3.235041 | 3.266910 | -0.613802 |
| 50 | 7 | -3.282731 | -3.222124 | -0.562469 |
| 51 | 7 | 3.255934 | -3.243123 | -0.580557 |
| 52 | 1 | 3.539538 | 4.169169 | -0.227817 |
| 53 | 1 | -4.158614 | 3.548613 | -0.234998 |
| 54 | 1 | -3.549747 | -4.151350 | -0.185981 |
| 55 | 1 | 4.176809 | -3.523750 | -0.192230 |
| 56 | 6 | 2.898420 | -4.230733 | -1.591323 |
| 57 | 1 | 2.762525 | -3.754084 | -2.567478 |
| 58 | 6 | 4.255602 | 2.866843 | -1.600872 |
| 59 | 1 | 3.782466 | 2.710813 | -2.575661 |
| 60 | 6 | -2.869237 | 4.246061 | -1.629549 |
| 61 | 1 | -1.938375 | 4.757034 | -1.362358 |
| 62 | 6 | -4.282220 | -2.859443 | -1.559442 |
| 63 | 1 | -3.814751 | -2.699747 | -2.536405 |
| 64 | 1 | 4.763078 | 1.938044 | -1.320123 |
| 65 | 1 | 1.963392 | -4.736496 | -1.329217 |
| 66 | 1 | -4.798518 | -1.935879 | -1.277589 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 67 | 1 | -2.720962 | 3.760986 | -2.599618 |
| 68 | 6 | -5.293828 | -4.052433 | -1.618588 |
| 69 | 8 | -5.032992 | -5.004754 | -0.818610 |
| 70 | 8 | -6.231086 | -3.931711 | -2.435482 |
| 71 | 6 | 4.080032 | -5.256446 | -1.636189 |
| 72 | 8 | 5.020645 | -5.012142 | -0.817269 |
| 73 | 8 | 3.962783 | -6.186589 | -2.461427 |
| 74 | 6 | 5.280194 | 4.048291 | -1.666383 |
| 75 | 8 | 5.032868 | 5.006043 | -0.868685 |
| 76 | 8 | 6.213871 | 3.914828 | -2.485682 |
| 77 | 6 | -4.051741 | 5.269281 | -1.697133 |
| 78 | 8 | -5.000259 | 5.033725 | -0.884864 |
| 79 | 8 | -3.927905 | 6.190683 | -2.531595 |
| 80 | 6 | 1.723541 | 4.420786 | 1.470179 |
| 81 | 1 | 2.658139 | 4.225742 | 2.002844 |
| 82 | 1 | 1.899019 | 5.231511 | 0.757691 |
| 83 | 1 | 0.984036 | 4.783704 | 2.187990 |
| 84 | 6 | -4.402760 | 1.746237 | 1.477490 |
| 85 | 1 | -5.218728 | 1.911213 | 0.768487 |
| 86 | 1 | -4.759083 | 1.015118 | 2.207131 |
| 87 | 1 | -4.205946 | 2.687828 | 1.997024 |
| 88 | 6 | -1.709801 | -4.388285 | 1.490491 |
| 89 | 1 | -2.638983 | -4.199794 | 2.034702 |
| 90 | 1 | -1.888659 | -5.199127 | 0.779015 |
| 91 | 1 | -0.959326 | -4.747552 | 2.198492 |
| 92 | 6 | 4.407537 | -1.696428 | 1.500169 |
| 93 | 1 | 4.213267 | -2.633931 | 2.027934 |
| 94 | 1 | 5.226529 | -1.864116 | 0.795358 |
| 95 | 1 | 4.757969 | -0.956908 | 2.224023 |
| 96 | 58 | -0.003313 | 0.013412 | -0.088462 |

E(RTPSSh) = -2543.4937071 Hartree

Zero-point correction = 0.780811 Hartree/particle

Sum of electronic and thermal Energies = -2542.659361 Hartree

Sum of electronic and thermal Enthalpies = -2542.658417 Hartree

Sum of electronic and thermal Free Energies = -2542.804370 Hartree

Table S35. [Pr(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 2.103071 | -0.525558 | 1.608697 |
| 2 | 6 | 1.650112 | -1.453832 | 2.688390 |
| 3 | 6 | 0.717247 | -2.573561 | 2.229797 |
| 4 | 7 | -0.554226 | -2.082811 | 1.610134 |
| 5 | 6 | -1.485734 | -1.629798 | 2.687663 |
| 6 | 6 | -2.605622 | -0.697403 | 2.227982 |
| 7 | 7 | -2.114134 | 0.568659 | 1.599142 |
| 8 | 6 | -1.665546 | 1.509563 | 2.669990 |
| 9 | 6 | -0.731818 | 2.625344 | 2.203072 |
| 10 | 7 | 0.539933 | 2.128921 | 1.589987 |
| 11 | 6 | 1.469790 | 1.686626 | 2.672619 |
| 12 | 6 | 2.590310 | 0.749453 | 2.224193 |
| 13 | 6 | 3.199493 | -1.099844 | 0.752531 |
| 14 | 6 | 2.604810 | -2.099315 | -0.243504 |
| 15 | 8 | 1.469965 | -1.851165 | -0.763344 |
| 16 | 6 | -1.128195 | -3.175261 | 0.748161 |
| 17 | 6 | -2.137810 | -2.574794 | -0.235201 |
| 18 | 8 | -1.898949 | -1.434292 | -0.743958 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 19 | 6 | -3.202285 | 1.135933 | 0.728389 |
| 20 | 6 | -2.591761 | 2.121337 | -0.273323 |
| 21 | 8 | -1.454647 | 1.862833 | -0.778942 |
| 22 | 6 | 1.116006 | 3.209612 | 0.716225 |
| 23 | 6 | 2.117021 | 2.590692 | -0.265236 |
| 24 | 8 | 1.869342 | 1.447188 | -0.760521 |
| 25 | 1 | 1.146834 | -0.845417 | 3.442895 |
| 26 | 1 | 2.507517 | -1.911424 | 3.197059 |
| 27 | 1 | 1.217364 | -3.215488 | 1.502590 |
| 28 | 1 | 0.505446 | -3.197210 | 3.108648 |
| 29 | 1 | -0.878916 | -1.125530 | 3.442723 |
| 30 | 1 | -1.942843 | -2.487963 | 3.195499 |
| 31 | 1 | -3.252092 | -1.200701 | 1.507333 |
| 32 | 1 | -3.224963 | -0.479309 | 3.108487 |
| 33 | 1 | -1.163886 | 0.909585 | 3.432355 |
| 34 | 1 | -2.525417 | 1.971145 | 3.170883 |
| 35 | 1 | -1.230946 | 3.261403 | 1.470170 |
| 36 | 1 | -0.521579 | 3.256567 | 3.077041 |
| 37 | 1 | 0.862360 | 1.190535 | 3.432656 |
| 38 | 1 | 1.927606 | 2.549245 | 3.172325 |
| 39 | 1 | 3.236834 | 1.245397 | 1.498448 |
| 40 | 1 | 3.208996 | 0.542250 | 3.107769 |
| 41 | 1 | 3.502718 | -0.261183 | 0.113490 |
| 42 | 1 | -0.291793 | -3.469910 | 0.101814 |
| 43 | 1 | -3.505137 | 0.290711 | 0.098186 |
| 44 | 1 | 0.278847 | 3.504339 | 0.071270 |
| 45 | 8 | -0.012532 | -0.380518 | -2.602461 |
| 46 | 1 | 0.653707 | -1.082416 | -2.710755 |
| 47 | 1 | -0.860987 | -0.800881 | -2.822973 |
| 48 | 7 | 3.179060 | 3.287196 | -0.618854 |
| 49 | 7 | -3.288374 | 3.180866 | -0.633280 |
| 50 | 7 | -3.194341 | -3.282505 | -0.580656 |
| 51 | 7 | 3.309822 | -3.156317 | -0.590122 |
| 52 | 1 | 3.434107 | 4.215906 | -0.246124 |
| 53 | 1 | -4.212319 | 3.443777 | -0.253836 |
| 54 | 1 | -3.440924 | -4.212084 | -0.202908 |
| 55 | 1 | 4.234532 | -3.411081 | -0.205032 |
| 56 | 6 | 2.953768 | -4.142693 | -1.602173 |
| 57 | 1 | 2.804795 | -3.661709 | -2.574349 |
| 58 | 6 | 4.173523 | 2.906194 | -1.613431 |
| 59 | 1 | 3.702524 | 2.744535 | -2.588441 |
| 60 | 6 | -2.915943 | 4.160813 | -1.645437 |
| 61 | 1 | -1.983039 | 4.665184 | -1.373338 |
| 62 | 6 | -4.188463 | -2.922220 | -1.583481 |
| 63 | 1 | -3.713735 | -2.758394 | -2.556345 |
| 64 | 1 | 4.676238 | 1.977341 | -1.324776 |
| 65 | 1 | 2.024721 | -4.656262 | -1.334438 |
| 66 | 1 | -4.707717 | -2.000012 | -1.303001 |
| 67 | 1 | -2.765631 | 3.676234 | -2.615578 |
| 68 | 6 | -5.199241 | -4.110230 | -1.660650 |
| 69 | 8 | -4.952984 | -5.074127 | -0.871583 |
| 70 | 8 | -6.132285 | -3.979776 | -2.484184 |
| 71 | 6 | 4.135624 | -5.161404 | -1.670451 |
| 72 | 8 | 5.092872 | -4.923885 | -0.870651 |
| 73 | 8 | 4.007290 | -6.090954 | -2.498103 |
| 74 | 6 | 5.204243 | 4.076728 | -1.691466 |
| 75 | 8 | 4.968625 | 5.050655 | -0.911672 |
| 76 | 8 | 6.141136 | 3.924668 | -2.507195 |
| 77 | 6 | -4.085288 | 5.192852 | -1.724508 |
| 78 | 8 | -5.051322 | 4.969257 | -0.931401 |
| 79 | 8 | -3.940119 | 6.118900 | -2.553673 |
| 80 | 6 | 1.622350 | 4.458363 | 1.451034 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 81 | 1 | 2.559709 | 4.286181 | 1.986307 |
| 82 | 1 | 1.781173 | 5.266390 | 0.731744 |
| 83 | 1 | 0.875495 | 4.812478 | 2.165507 |
| 84 | 6 | -4.442088 | 1.655540 | 1.468966 |
| 85 | 1 | -5.258946 | 1.800719 | 0.756807 |
| 86 | 1 | -4.786920 | 0.922038 | 2.201605 |
| 87 | 1 | -4.263787 | 2.602848 | 1.984422 |
| 88 | 6 | -1.623071 | -4.420376 | 1.496637 |
| 89 | 1 | -2.559737 | -4.248856 | 2.033171 |
| 90 | 1 | -1.778796 | -5.236169 | 0.785556 |
| 91 | 1 | -0.871626 | -4.762906 | 2.211763 |
| 92 | 6 | 4.436498 | -1.605036 | 1.507713 |
| 93 | 1 | 4.258999 | -2.547709 | 2.031753 |
| 94 | 1 | 5.259296 | -1.753290 | 0.803154 |
| 95 | 1 | 4.772175 | -0.862163 | 2.235021 |
| 96 | 59 | -0.005672 | 0.010748 | -0.039447 |

E(RTPSSh) = -2544.1515271 Hartree

Zero-point correction = 0.781745 Hartree/particle

Sum of electronic and thermal Energies = -2543.316451 Hartree

Sum of electronic and thermal Enthalpies = -2543.315506 Hartree

Sum of electronic and thermal Free Energies = -2543.460710 Hartree

Table S36. [Nd(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 2.094268 | -0.566499 | 1.603985 |
| 2 | 6 | 1.627905 | -1.488125 | 2.683098 |
| 3 | 6 | 0.678206 | -2.592062 | 2.220965 |
| 4 | 7 | -0.582964 | -2.075263 | 1.602125 |
| 5 | 6 | -1.505246 | -1.612106 | 2.682754 |
| 6 | 6 | -2.610412 | -0.661381 | 2.225279 |
| 7 | 7 | -2.094900 | 0.596471 | 1.599614 |
| 8 | 6 | -1.631467 | 1.525049 | 2.674357 |
| 9 | 6 | -0.681050 | 2.627323 | 2.209004 |
| 10 | 7 | 0.580084 | 2.108278 | 1.593119 |
| 11 | 6 | 1.501816 | 1.649228 | 2.675395 |
| 12 | 6 | 2.607200 | 0.696286 | 2.222798 |
| 13 | 6 | 3.174133 | -1.160978 | 0.740755 |
| 14 | 6 | 2.549034 | -2.140896 | -0.255936 |
| 15 | 8 | 1.420064 | -1.858597 | -0.770798 |
| 16 | 6 | -1.177915 | -3.150615 | 0.733047 |
| 17 | 6 | -2.170566 | -2.520133 | -0.248395 |
| 18 | 8 | -1.899889 | -1.383972 | -0.751338 |
| 19 | 6 | -3.169632 | 1.187338 | 0.727826 |
| 20 | 6 | -2.534040 | 2.159074 | -0.271431 |
| 21 | 8 | -1.402338 | 1.873044 | -0.774222 |
| 22 | 6 | 1.176362 | 3.177223 | 0.718337 |
| 23 | 6 | 2.159468 | 2.535074 | -0.266046 |
| 24 | 8 | 1.883588 | 1.396480 | -0.757657 |
| 25 | 1 | 1.131717 | -0.872454 | 3.436220 |
| 26 | 1 | 2.477861 | -1.958196 | 3.192803 |
| 27 | 1 | 1.168225 | -3.240669 | 1.492716 |
| 28 | 1 | 0.453718 | -3.214808 | 3.097253 |
| 29 | 1 | -0.889426 | -1.117446 | 3.436693 |
| 30 | 1 | -1.973797 | -2.464321 | 3.190043 |
| 31 | 1 | -3.265280 | -1.152319 | 1.503536 |
| 32 | 1 | -3.226629 | -0.433530 | 3.105454 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 33 | 1 | -1.136737 | 0.913935 | 3.432210 |
| 34 | 1 | -2.483231 | 1.997094 | 3.179232 |
| 35 | 1 | -1.170529 | 3.273602 | 1.478433 |
| 36 | 1 | -0.457557 | 3.253177 | 3.083477 |
| 37 | 1 | 0.885980 | 1.158295 | 3.431829 |
| 38 | 1 | 1.971368 | 2.503018 | 3.179244 |
| 39 | 1 | 3.261626 | 1.183592 | 1.498188 |
| 40 | 1 | 3.223535 | 0.474028 | 3.104326 |
| 41 | 1 | 3.493703 | -0.326931 | 0.103798 |
| 42 | 1 | -0.346916 | -3.459842 | 0.086686 |
| 43 | 1 | -3.489875 | 0.349776 | 0.095999 |
| 44 | 1 | 0.344015 | 3.490798 | 0.076116 |
| 45 | 8 | -0.029286 | -0.297090 | -2.580162 |
| 46 | 1 | 0.632358 | -0.993362 | -2.737870 |
| 47 | 1 | -0.883850 | -0.707871 | -2.796001 |
| 48 | 7 | 3.236606 | 3.205404 | -0.624278 |
| 49 | 7 | -3.202692 | 3.236472 | -0.631222 |
| 50 | 7 | -3.247445 | -3.195004 | -0.596054 |
| 51 | 7 | 3.220198 | -3.218683 | -0.605970 |
| 52 | 1 | 3.514856 | 4.127696 | -0.252770 |
| 53 | 1 | -4.119422 | 3.522505 | -0.251605 |
| 54 | 1 | -3.522344 | -4.116676 | -0.219090 |
| 55 | 1 | 4.135117 | -3.504141 | -0.220076 |
| 56 | 6 | 2.824156 | -4.197474 | -1.610653 |
| 57 | 1 | 2.695594 | -3.718462 | -2.586713 |
| 58 | 6 | 4.221614 | 2.795949 | -1.617135 |
| 59 | 1 | 3.747840 | 2.646285 | -2.592713 |
| 60 | 6 | -2.800161 | 4.210968 | -1.637257 |
| 61 | 1 | -1.853075 | 4.685833 | -1.361173 |
| 62 | 6 | -4.236985 | -2.794963 | -1.588474 |
| 63 | 1 | -3.766200 | -2.648064 | -2.565940 |
| 64 | 1 | 4.697969 | 1.853907 | -1.326679 |
| 65 | 1 | 1.874233 | -4.669341 | -1.339491 |
| 66 | 1 | -4.716627 | -1.853627 | -1.301254 |
| 67 | 1 | -2.663003 | 3.727892 | -2.610086 |
| 68 | 6 | -5.294553 | -3.941951 | -1.657126 |
| 69 | 8 | -5.076955 | -4.917829 | -0.874556 |
| 70 | 8 | -6.231420 | -3.771397 | -2.468953 |
| 71 | 6 | 3.961768 | -5.265659 | -1.670759 |
| 72 | 8 | 4.929252 | -5.062055 | -0.874137 |
| 73 | 8 | 3.792815 | -6.196045 | -2.490264 |
| 74 | 6 | 5.285109 | 3.936707 | -1.694969 |
| 75 | 8 | 5.074799 | 4.919170 | -0.918784 |
| 76 | 8 | 6.219926 | 3.755350 | -2.507111 |
| 77 | 6 | -3.937645 | 5.278231 | -1.711768 |
| 78 | 8 | -4.911256 | 5.079569 | -0.921430 |
| 79 | 8 | -3.762771 | 6.204177 | -2.535343 |
| 80 | 6 | 1.713784 | 4.413453 | 1.451839 |
| 81 | 1 | 2.648318 | 4.219391 | 1.984580 |
| 82 | 1 | 1.890095 | 5.217228 | 0.731789 |
| 83 | 1 | 0.977348 | 4.785469 | 2.168041 |
| 84 | 6 | -4.398697 | 1.734223 | 1.466295 |
| 85 | 1 | -5.209189 | 1.901743 | 0.751692 |
| 86 | 1 | -4.763901 | 1.006888 | 2.195223 |
| 87 | 1 | -4.199646 | 2.675344 | 1.985480 |
| 88 | 6 | -1.703239 | -4.388235 | 1.472661 |
| 89 | 1 | -2.634460 | -4.197486 | 2.012239 |
| 90 | 1 | -1.881243 | -5.193817 | 0.755101 |
| 91 | 1 | -0.959635 | -4.755827 | 2.183560 |
| 92 | 6 | 4.402098 | -1.699058 | 1.487429 |
| 93 | 1 | 4.203642 | -2.636773 | 2.012920 |
| 94 | 1 | 5.215369 | -1.869545 | 0.776755 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 95 | 1 | 4.762877 | -0.965430 | 2.212136 |
| 96 | 60 | -0.000923 | 0.011064 | -0.026247 |

E(RTPSSh) = -2544.7743983 Hartree
 Zero-point correction = 0.782050 Hartree/particle
 Sum of electronic and thermal Energies = -2543.939091 Hartree
 Sum of electronic and thermal Enthalpies = -2543.938147 Hartree
 Sum of electronic and thermal Free Energies = -2544.082530 Hartree

Table S37. [Sm(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 2.092101 | -0.545250 | 1.628448 |
| 2 | 6 | 1.643699 | -1.474947 | 2.708247 |
| 3 | 6 | 0.704019 | -2.585544 | 2.244955 |
| 4 | 7 | -0.559142 | -2.074125 | 1.626362 |
| 5 | 6 | -1.488695 | -1.629372 | 2.708560 |
| 6 | 6 | -2.600760 | -0.688470 | 2.251093 |
| 7 | 7 | -2.091053 | 0.571940 | 1.626528 |
| 8 | 6 | -1.643983 | 1.506911 | 2.702742 |
| 9 | 6 | -0.704372 | 2.616496 | 2.236174 |
| 10 | 7 | 0.558419 | 2.103308 | 1.619359 |
| 11 | 6 | 1.488336 | 1.661725 | 2.702029 |
| 12 | 6 | 2.600194 | 0.718984 | 2.247514 |
| 13 | 6 | 3.170988 | -1.127728 | 0.756542 |
| 14 | 6 | 2.544095 | -2.098503 | -0.246195 |
| 15 | 8 | 1.403728 | -1.821181 | -0.738893 |
| 16 | 6 | -1.142379 | -3.148999 | 0.749514 |
| 17 | 6 | -2.126127 | -2.517974 | -0.238704 |
| 18 | 8 | -1.860710 | -1.370976 | -0.720596 |
| 19 | 6 | -3.166106 | 1.151996 | 0.748512 |
| 20 | 6 | -2.530130 | 2.115638 | -0.256662 |
| 21 | 8 | -1.387897 | 1.835962 | -0.738847 |
| 22 | 6 | 1.142246 | 3.172030 | 0.736324 |
| 23 | 6 | 2.116955 | 2.528958 | -0.254214 |
| 24 | 8 | 1.847376 | 1.379644 | -0.724172 |
| 25 | 1 | 1.145138 | -0.867489 | 3.466594 |
| 26 | 1 | 2.502234 | -1.936948 | 3.210770 |
| 27 | 1 | 1.199149 | -3.228648 | 1.515327 |
| 28 | 1 | 0.482961 | -3.212372 | 3.119088 |
| 29 | 1 | -0.880477 | -1.132807 | 3.467523 |
| 30 | 1 | -1.948836 | -2.490358 | 3.208531 |
| 31 | 1 | -3.249950 | -1.184076 | 1.527397 |
| 32 | 1 | -3.221130 | -0.464932 | 3.129332 |
| 33 | 1 | -1.145687 | 0.902845 | 3.464028 |
| 34 | 1 | -2.503571 | 1.970042 | 3.202440 |
| 35 | 1 | -1.199586 | 3.257212 | 1.504583 |
| 36 | 1 | -0.483765 | 3.246164 | 3.108482 |
| 37 | 1 | 0.880654 | 1.168165 | 3.463438 |
| 38 | 1 | 1.949752 | 2.523941 | 3.198820 |
| 39 | 1 | 3.248508 | 1.211685 | 1.521093 |
| 40 | 1 | 3.221125 | 0.499672 | 3.126412 |
| 41 | 1 | 3.485170 | -0.287130 | 0.126094 |
| 42 | 1 | -0.304879 | -3.453582 | 0.109901 |
| 43 | 1 | -3.482436 | 0.308685 | 0.122911 |
| 44 | 1 | 0.303070 | 3.480167 | 0.100898 |
| 45 | 8 | -0.037856 | -0.244829 | -2.499944 |
| 46 | 1 | 0.629484 | -0.933811 | -2.665833 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 47 | 1 | -0.891199 | -0.670832 | -2.691502 |
| 48 | 7 | 3.178315 | 3.208614 | -0.640170 |
| 49 | 7 | -3.208596 | 3.177317 | -0.643243 |
| 50 | 7 | -3.187274 | -3.201831 | -0.614405 |
| 51 | 7 | 3.224013 | -3.160773 | -0.624467 |
| 52 | 1 | 3.446969 | 4.141268 | -0.287720 |
| 53 | 1 | -4.136149 | 3.453160 | -0.282690 |
| 54 | 1 | -3.453430 | -4.133745 | -0.256249 |
| 55 | 1 | 4.149753 | -3.437372 | -0.258076 |
| 56 | 6 | 2.831382 | -4.126198 | -1.643267 |
| 57 | 1 | 2.676545 | -3.629669 | -2.606615 |
| 58 | 6 | 4.150070 | 2.803743 | -1.647812 |
| 59 | 1 | 3.658772 | 2.628896 | -2.610390 |
| 60 | 6 | -2.811604 | 4.137835 | -1.664741 |
| 61 | 1 | -1.880604 | 4.641148 | -1.384349 |
| 62 | 6 | -4.163315 | -2.806499 | -1.621930 |
| 63 | 1 | -3.675022 | -2.635148 | -2.586696 |
| 64 | 1 | 4.652855 | 1.876850 | -1.353210 |
| 65 | 1 | 1.896541 | -4.624177 | -1.366500 |
| 66 | 1 | -4.668822 | -1.880027 | -1.330884 |
| 67 | 1 | -2.647399 | 3.636288 | -2.623865 |
| 68 | 6 | -5.195034 | -3.974186 | -1.729671 |
| 69 | 8 | -4.973404 | -4.956690 | -0.956505 |
| 70 | 8 | -6.118330 | -3.811108 | -2.558262 |
| 71 | 6 | 3.990166 | -5.168597 | -1.743997 |
| 72 | 8 | 4.965627 | -4.961413 | -0.958063 |
| 73 | 8 | 3.827775 | -6.084891 | -2.580429 |
| 74 | 6 | 5.187332 | 3.965291 | -1.765799 |
| 75 | 8 | 4.973884 | 4.954168 | -0.998636 |
| 76 | 8 | 6.107530 | 3.791768 | -2.596077 |
| 77 | 6 | -3.971975 | 5.176571 | -1.781293 |
| 78 | 8 | -4.952922 | 4.973734 | -1.001125 |
| 79 | 8 | -3.805530 | 6.087303 | -2.623321 |
| 80 | 6 | 1.681260 | 4.413032 | 1.460606 |
| 81 | 1 | 2.625351 | 4.227205 | 1.979199 |
| 82 | 1 | 1.839971 | 5.217756 | 0.737512 |
| 83 | 1 | 0.952585 | 4.779729 | 2.187515 |
| 84 | 6 | -4.398834 | 1.700616 | 1.479665 |
| 85 | 1 | -5.211075 | 1.851632 | 0.763367 |
| 86 | 1 | -4.758295 | 0.980858 | 2.218999 |
| 87 | 1 | -4.206864 | 2.650567 | 1.985179 |
| 88 | 6 | -1.670322 | -4.390808 | 1.480346 |
| 89 | 1 | -2.611864 | -4.207853 | 2.004481 |
| 90 | 1 | -1.829779 | -5.197971 | 0.760201 |
| 91 | 1 | -0.935391 | -4.752375 | 2.203360 |
| 92 | 6 | 4.403979 | -1.668086 | 1.493289 |
| 93 | 1 | 4.213721 | -2.615139 | 2.004832 |
| 94 | 1 | 5.217749 | -1.821405 | 0.779273 |
| 95 | 1 | 4.760153 | -0.942493 | 2.228389 |
| 96 | 62 | -0.000325 | 0.012526 | 0.028995 |

E(RTPSSh) = -2545.9974591 Hartree

Zero-point correction = 0.782634 Hartree/particle

Sum of electronic and thermal Energies = -2545.161819 Hartree

Sum of electronic and thermal Enthalpies = -2545.160875 Hartree

Sum of electronic and thermal Free Energies = -2545.304276 Hartree

Table S38. [Eu(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center | Atomic | Coordinates (Angstroms) |
|--------|--------|-------------------------|
|--------|--------|-------------------------|

| Number | Number | X | Y | Z |
|--------|--------|-----------|-----------|-----------|
| 1 | 7 | 2.092667 | -0.530070 | 1.642756 |
| 2 | 6 | 1.654223 | -1.464488 | 2.722497 |
| 3 | 6 | 0.722760 | -2.580814 | 2.258120 |
| 4 | 7 | -0.542619 | -2.075341 | 1.639681 |
| 5 | 6 | -1.476302 | -1.641420 | 2.722629 |
| 6 | 6 | -2.594378 | -0.708453 | 2.265465 |
| 7 | 7 | -2.091045 | 0.554766 | 1.641930 |
| 8 | 6 | -1.653439 | 1.492997 | 2.719149 |
| 9 | 6 | -0.722425 | 2.608941 | 2.252319 |
| 10 | 7 | 0.542496 | 2.102271 | 1.634954 |
| 11 | 6 | 1.476670 | 1.670282 | 2.717811 |
| 12 | 6 | 2.594561 | 0.736125 | 2.262294 |
| 13 | 6 | 3.172965 | -1.104075 | 0.767563 |
| 14 | 6 | 2.548312 | -2.071416 | -0.238927 |
| 15 | 8 | 1.401256 | -1.800550 | -0.720064 |
| 16 | 6 | -1.117685 | -3.151205 | 0.759218 |
| 17 | 6 | -2.098504 | -2.522158 | -0.232254 |
| 18 | 8 | -1.839540 | -1.368677 | -0.702663 |
| 19 | 6 | -3.167847 | 1.127498 | 0.761803 |
| 20 | 6 | -2.534266 | 2.088070 | -0.246942 |
| 21 | 8 | -1.386131 | 1.814724 | -0.718654 |
| 22 | 6 | 1.118030 | 3.172672 | 0.748944 |
| 23 | 6 | 2.089963 | 2.532000 | -0.245082 |
| 24 | 8 | 1.826929 | 1.376813 | -0.704351 |
| 25 | 1 | 1.152050 | -0.861933 | 3.482413 |
| 26 | 1 | 2.517510 | -1.920061 | 3.222713 |
| 27 | 1 | 1.222136 | -3.219578 | 1.527622 |
| 28 | 1 | 0.505015 | -3.210344 | 3.131095 |
| 29 | 1 | -0.872581 | -1.141816 | 3.483229 |
| 30 | 1 | -1.929646 | -2.507575 | 3.219845 |
| 31 | 1 | -3.239341 | -1.207761 | 1.540561 |
| 32 | 1 | -3.217206 | -0.489116 | 3.142977 |
| 33 | 1 | -1.151111 | 0.892883 | 3.480944 |
| 34 | 1 | -2.517560 | 1.948942 | 3.217594 |
| 35 | 1 | -1.222129 | 3.245790 | 1.520423 |
| 36 | 1 | -0.504944 | 3.240615 | 3.123906 |
| 37 | 1 | 0.873566 | 1.172758 | 3.480313 |
| 38 | 1 | 1.931217 | 2.537157 | 3.212782 |
| 39 | 1 | 3.238531 | 1.233493 | 1.535215 |
| 40 | 1 | 3.218039 | 0.519895 | 3.140097 |
| 41 | 1 | 3.483286 | -0.259436 | 0.140891 |
| 42 | 1 | -0.276377 | -3.451593 | 0.122878 |
| 43 | 1 | -3.481144 | 0.280777 | 0.139565 |
| 44 | 1 | 0.274955 | 3.476840 | 0.117003 |
| 45 | 8 | -0.034577 | -0.224708 | -2.461376 |
| 46 | 1 | 0.637226 | -0.910367 | -2.623939 |
| 47 | 1 | -0.885516 | -0.658750 | -2.646405 |
| 48 | 63 | -0.000077 | 0.013113 | 0.056944 |
| 49 | 7 | 3.140924 | 3.219436 | -0.645160 |
| 50 | 7 | -3.220774 | 3.139090 | -0.647950 |
| 51 | 7 | -3.148943 | -3.213742 | -0.622872 |
| 52 | 7 | 3.236197 | -3.122656 | -0.632652 |
| 53 | 1 | 3.401271 | 4.158421 | -0.303107 |
| 54 | 1 | -4.155094 | 3.406276 | -0.298275 |
| 55 | 1 | -3.407348 | -4.151956 | -0.275116 |
| 56 | 1 | 4.168924 | -3.391084 | -0.277653 |
| 57 | 6 | 2.849765 | -4.079855 | -1.661502 |
| 58 | 1 | 2.677294 | -3.572308 | -2.616044 |
| 59 | 6 | 4.104832 | 2.821588 | -1.663031 |
| 60 | 1 | 3.602852 | 2.629583 | -2.616751 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 61 | 6 | -2.831093 | 4.090638 | -1.680536 |
| 62 | 1 | -1.912360 | 4.615634 | -1.399356 |
| 63 | 6 | -4.118024 | -2.824545 | -1.639430 |
| 64 | 1 | -3.620291 | -2.637707 | -2.596448 |
| 65 | 1 | 4.628049 | 1.906369 | -1.367445 |
| 66 | 1 | 1.926407 | -4.597931 | -1.383065 |
| 67 | 1 | -4.641788 | -1.908660 | -1.347195 |
| 68 | 1 | -2.648517 | 3.577247 | -2.629980 |
| 69 | 6 | -5.129881 | -4.007384 | -1.769622 |
| 70 | 8 | -4.903024 | -4.992147 | -1.000817 |
| 71 | 8 | -6.044564 | -3.852537 | -2.609144 |
| 72 | 6 | 4.025241 | -5.100720 | -1.787800 |
| 73 | 8 | 5.003793 | -4.888577 | -1.007005 |
| 74 | 8 | 3.871117 | -6.007185 | -2.636331 |
| 75 | 6 | 5.120093 | 3.999759 | -1.806243 |
| 76 | 8 | 4.901264 | 4.991180 | -1.043854 |
| 77 | 8 | 6.030411 | 3.835242 | -2.649093 |
| 78 | 6 | -4.009116 | 5.105943 | -1.824200 |
| 79 | 8 | -4.992560 | 4.898770 | -1.048312 |
| 80 | 8 | -3.852183 | 6.005026 | -2.680417 |
| 81 | 6 | 1.655033 | 4.416566 | 1.469788 |
| 82 | 1 | 2.604070 | 4.236360 | 1.981245 |
| 83 | 1 | 1.803314 | 5.222745 | 0.746109 |
| 84 | 1 | 0.929390 | 4.778367 | 2.202221 |
| 85 | 6 | -4.402859 | 1.674642 | 1.490284 |
| 86 | 1 | -5.216875 | 1.815770 | 0.773997 |
| 87 | 1 | -4.757381 | 0.958051 | 2.235119 |
| 88 | 1 | -4.215840 | 2.629279 | 1.988725 |
| 89 | 6 | -1.643920 | -4.396229 | 1.485899 |
| 90 | 1 | -2.590560 | -4.219123 | 2.002784 |
| 91 | 1 | -1.792760 | -5.204487 | 0.764722 |
| 92 | 1 | -0.912234 | -4.753209 | 2.214521 |
| 93 | 6 | 4.408925 | -1.642987 | 1.500464 |
| 94 | 1 | 4.224315 | -2.595162 | 2.004462 |
| 95 | 1 | 5.224053 | -1.785603 | 0.785791 |
| 96 | 1 | 4.760321 | -0.920885 | 2.241329 |

E(RTPSSh) = -2546.5947156 Hartree

Zero-point correction = 0.782749 Hartree/particle

Sum of electronic and thermal Energies = -2545.758986 Hartree

Sum of electronic and thermal Enthalpies = -2545.758042 Hartree

Sum of electronic and thermal Free Energies = -2545.901914 Hartree

Table S39. [Gd(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | 2.099857 | -0.495023 | 1.667631 |
| 2 | 6 | 1.678419 | -1.437343 | 2.747110 |
| 3 | 6 | 0.765489 | -2.568641 | 2.281997 |
| 4 | 7 | -0.507958 | -2.083713 | 1.664008 |
| 5 | 6 | -1.450038 | -1.667888 | 2.746651 |
| 6 | 6 | -2.582350 | -0.752385 | 2.289118 |
| 7 | 7 | -2.098931 | 0.518973 | 1.666656 |
| 8 | 6 | -1.678519 | 1.465149 | 2.743572 |
| 9 | 6 | -0.766045 | 2.596027 | 2.275909 |
| 10 | 7 | 0.506978 | 2.109708 | 1.659081 |
| 11 | 6 | 1.449466 | 1.695916 | 2.741742 |
| 12 | 6 | 2.581775 | 0.779264 | 2.286133 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 13 | 6 | 3.187044 | -1.050847 | 0.790340 |
| 14 | 6 | 2.574422 | -2.018929 | -0.222087 |
| 15 | 8 | 1.418175 | -1.766369 | -0.691353 |
| 16 | 6 | -1.064080 | -3.166399 | 0.780853 |
| 17 | 6 | -2.045458 | -2.549517 | -0.216962 |
| 18 | 8 | -1.804581 | -1.387178 | -0.675445 |
| 19 | 6 | -3.182649 | 1.073387 | 0.784310 |
| 20 | 6 | -2.560964 | 2.034507 | -0.230564 |
| 21 | 8 | -1.404208 | 1.778897 | -0.691002 |
| 22 | 6 | 1.063744 | 3.186735 | 0.770034 |
| 23 | 6 | 2.036868 | 2.557787 | -0.229671 |
| 24 | 8 | 1.793155 | 1.393313 | -0.675965 |
| 25 | 1 | 1.167085 | -0.843851 | 3.508201 |
| 26 | 1 | 2.549789 | -1.878834 | 3.245909 |
| 27 | 1 | 1.275176 | -3.197727 | 1.550227 |
| 28 | 1 | 0.558670 | -3.202983 | 3.154153 |
| 29 | 1 | -0.855662 | -1.160472 | 3.509549 |
| 30 | 1 | -1.890037 | -2.542556 | 3.240884 |
| 31 | 1 | -3.217672 | -1.261389 | 1.562449 |
| 32 | 1 | -3.210104 | -0.543961 | 3.165777 |
| 33 | 1 | -1.167076 | 0.874167 | 3.506589 |
| 34 | 1 | -2.550758 | 1.907019 | 3.240534 |
| 35 | 1 | -1.276035 | 3.223069 | 1.542622 |
| 36 | 1 | -0.559435 | 3.232589 | 3.146573 |
| 37 | 1 | 0.855603 | 1.190623 | 3.506484 |
| 38 | 1 | 1.890476 | 2.571447 | 3.233658 |
| 39 | 1 | 3.216273 | 1.286346 | 1.557440 |
| 40 | 1 | 3.209889 | 0.573990 | 3.163265 |
| 41 | 1 | 3.487988 | -0.199312 | 0.168599 |
| 42 | 1 | -0.215522 | -3.457005 | 0.149796 |
| 43 | 1 | -3.486519 | 0.219620 | 0.167206 |
| 44 | 1 | 0.213506 | 3.480842 | 0.143092 |
| 45 | 8 | -0.030112 | -0.208973 | -2.417566 |
| 46 | 1 | 0.651956 | -0.885628 | -2.575971 |
| 47 | 1 | -0.874669 | -0.659075 | -2.594371 |
| 48 | 7 | 3.066943 | 3.264712 | -0.649489 |
| 49 | 7 | -3.266283 | 3.065654 | -0.649950 |
| 50 | 7 | -3.075762 | -3.259884 | -0.626642 |
| 51 | 7 | 3.281395 | -3.050033 | -0.634461 |
| 52 | 1 | 3.305471 | 4.215576 | -0.324631 |
| 53 | 1 | -4.211640 | 3.312730 | -0.315387 |
| 54 | 1 | -3.312716 | -4.210004 | -0.296086 |
| 55 | 1 | 4.225649 | -3.298057 | -0.295202 |
| 56 | 6 | 2.913318 | -3.995261 | -1.680930 |
| 57 | 1 | 2.707362 | -3.470896 | -2.619550 |
| 58 | 6 | 4.018283 | 2.885575 | -1.686108 |
| 59 | 1 | 3.498818 | 2.658433 | -2.622530 |
| 60 | 6 | -2.894995 | 4.004502 | -1.700746 |
| 61 | 1 | -1.999893 | 4.569270 | -1.420245 |
| 62 | 6 | -4.031928 | -2.889600 | -1.662295 |
| 63 | 1 | -3.516385 | -2.666657 | -2.601927 |
| 64 | 1 | 4.583793 | 1.995997 | -1.389964 |
| 65 | 1 | 2.014045 | -4.553809 | -1.401748 |
| 66 | 1 | -4.598677 | -1.999986 | -1.368927 |
| 67 | 1 | -2.680118 | 3.474104 | -2.633889 |
| 68 | 6 | -4.993431 | -4.107882 | -1.839806 |
| 69 | 8 | -4.751911 | -5.095112 | -1.078635 |
| 70 | 8 | -5.888222 | -3.974599 | -2.704064 |
| 71 | 6 | 4.123041 | -4.968885 | -1.850467 |
| 72 | 8 | 5.103761 | -4.743069 | -1.076243 |
| 73 | 8 | 3.990007 | -5.856539 | -2.722078 |
| 74 | 6 | 4.983784 | 4.098581 | -1.875762 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 75 | 8 | 4.749908 | 5.092707 | -1.121394 |
| 76 | 8 | 5.874902 | 3.955196 | -2.742626 |
| 77 | 6 | -4.106203 | 4.972878 | -1.886931 |
| 78 | 8 | -5.091565 | 4.752768 | -1.117056 |
| 79 | 8 | -3.970037 | 5.852593 | -2.766467 |
| 80 | 6 | 1.589709 | 4.437219 | 1.487919 |
| 81 | 1 | 2.547089 | 4.270325 | 1.988180 |
| 82 | 1 | 1.717168 | 5.247793 | 0.765230 |
| 83 | 1 | 0.866579 | 4.785448 | 2.229450 |
| 84 | 6 | -4.423845 | 1.609962 | 1.510400 |
| 85 | 1 | -5.241997 | 1.731875 | 0.795334 |
| 86 | 1 | -4.765601 | 0.895487 | 2.263268 |
| 87 | 1 | -4.249415 | 2.572122 | 1.998799 |
| 88 | 6 | -1.579547 | -4.417706 | 1.504760 |
| 89 | 1 | -2.534881 | -4.253937 | 2.009865 |
| 90 | 1 | -1.706917 | -5.230640 | 0.784772 |
| 91 | 1 | -0.850769 | -4.760578 | 2.243093 |
| 92 | 6 | 4.429104 | -1.579059 | 1.520986 |
| 93 | 1 | 4.257179 | -2.538841 | 2.014882 |
| 94 | 1 | 5.248507 | -1.702198 | 0.807619 |
| 95 | 1 | 4.767397 | -0.859045 | 2.270018 |
| 96 | 64 | -0.000114 | 0.013810 | 0.092362 |

E(RTPSSh) = -2547.1848096 Hartree

Zero-point correction = 0.782524 Hartree/particle

Sum of electronic and thermal Energies = -2546.349186 Hartree

Sum of electronic and thermal Enthalpies = -2546.348242 Hartree

Sum of electronic and thermal Free Energies = -2546.492923 Hartree

Table S40. [Tb(DOTMA-(gly)₄(H₂O)]⁺ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.462196 | 2.108049 | 1.683115 |
| 2 | 6 | 1.411078 | 1.718875 | 2.768353 |
| 3 | 6 | 2.561342 | 0.826565 | 2.312074 |
| 4 | 7 | 2.099226 | -0.454109 | 1.692589 |
| 5 | 6 | 1.702667 | -1.404751 | 2.773040 |
| 6 | 6 | 0.813972 | -2.552931 | 2.305090 |
| 7 | 7 | -0.465617 | -2.086623 | 1.686460 |
| 8 | 6 | -1.415447 | -1.695844 | 2.770642 |
| 9 | 6 | -2.565171 | -0.804576 | 2.311376 |
| 10 | 7 | -2.101191 | 0.473735 | 1.689290 |
| 11 | 6 | -1.706798 | 1.427606 | 2.768122 |
| 12 | 6 | -0.817888 | 2.575516 | 2.299170 |
| 13 | 6 | 1.000196 | 3.191383 | 0.790339 |
| 14 | 6 | 1.972841 | 2.572192 | -0.214457 |
| 15 | 8 | 1.749655 | 1.396544 | -0.641535 |
| 16 | 6 | 3.193056 | -0.989462 | 0.811274 |
| 17 | 6 | 2.590933 | -1.954829 | -0.208442 |
| 18 | 8 | 1.423563 | -1.720653 | -0.659975 |
| 19 | 6 | -1.001852 | -3.175186 | 0.798708 |
| 20 | 6 | -1.980867 | -2.567569 | -0.205485 |
| 21 | 8 | -1.757888 | -1.394400 | -0.645279 |
| 22 | 6 | -3.190917 | 1.008016 | 0.802304 |
| 23 | 6 | -2.578531 | 1.967426 | -0.218215 |
| 24 | 8 | -1.410977 | 1.730141 | -0.660756 |
| 25 | 1 | 0.827482 | 1.201882 | 3.533222 |
| 26 | 1 | 1.831679 | 2.605071 | 3.258858 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 27 | 1 | 3.184592 | 1.346429 | 1.582652 |
| 28 | 1 | 3.194958 | 0.631081 | 3.187370 |
| 29 | 1 | 1.179793 | -0.823009 | 3.535385 |
| 30 | 1 | 2.584705 | -1.826950 | 3.269602 |
| 31 | 1 | 1.336361 | -3.169672 | 1.571703 |
| 32 | 1 | 0.616674 | -3.194227 | 3.174263 |
| 33 | 1 | -0.832345 | -1.176992 | 3.534590 |
| 34 | 1 | -1.835711 | -2.581320 | 3.262643 |
| 35 | 1 | -3.188117 | -1.326007 | 1.582760 |
| 36 | 1 | -3.199784 | -0.606668 | 3.185422 |
| 37 | 1 | -1.184825 | 0.847929 | 3.532693 |
| 38 | 1 | -2.590163 | 1.850101 | 3.262065 |
| 39 | 1 | -1.339658 | 3.190359 | 1.563782 |
| 40 | 1 | -0.621867 | 3.218696 | 3.167292 |
| 41 | 1 | 0.142852 | 3.475651 | 0.168926 |
| 42 | 1 | 3.484165 | -0.129844 | 0.196385 |
| 43 | 1 | -0.145461 | -3.456141 | 0.174270 |
| 44 | 1 | -3.484212 | 0.146584 | 0.191148 |
| 45 | 8 | -0.020612 | -0.173089 | -2.354613 |
| 46 | 1 | 0.660823 | -0.850714 | -2.511842 |
| 47 | 1 | -0.864841 | -0.620747 | -2.538343 |
| 48 | 7 | -3.300590 | 2.976455 | -0.661828 |
| 49 | 7 | -2.989083 | -3.294225 | -0.640287 |
| 50 | 7 | 3.315600 | -2.962505 | -0.646444 |
| 51 | 7 | 2.979783 | 3.296872 | -0.659156 |
| 52 | 1 | -4.255861 | 3.206317 | -0.343447 |
| 53 | 1 | -3.207831 | -4.254721 | -0.327569 |
| 54 | 1 | 4.270317 | -3.192584 | -0.324017 |
| 55 | 1 | 3.198519 | 4.258425 | -0.352300 |
| 56 | 6 | 3.919343 | 2.929258 | -1.710631 |
| 57 | 1 | 3.386424 | 2.671859 | -2.631512 |
| 58 | 6 | -2.940002 | 3.902831 | -1.727384 |
| 59 | 1 | -2.698115 | 3.358770 | -2.645912 |
| 60 | 6 | -3.932323 | -2.934507 | -1.691469 |
| 61 | 1 | -4.531614 | -2.066799 | -1.397119 |
| 62 | 6 | 2.960224 | -3.893070 | -1.710395 |
| 63 | 1 | 2.724701 | -3.352496 | -2.632683 |
| 64 | 1 | -2.064321 | 4.497551 | -1.447475 |
| 65 | 1 | 4.517665 | 2.061657 | -1.413739 |
| 66 | 1 | 2.082390 | -4.485335 | -1.432445 |
| 67 | 1 | -3.402415 | -2.681058 | -2.615196 |
| 68 | 6 | 4.196034 | -4.825112 | -1.920740 |
| 69 | 8 | 5.179058 | -4.591536 | -1.151773 |
| 70 | 8 | 4.078608 | -5.691830 | -2.815287 |
| 71 | 6 | 4.843834 | 4.167057 | -1.940278 |
| 72 | 8 | 4.598123 | 5.165276 | -1.195153 |
| 73 | 8 | 5.718745 | 4.036623 | -2.825472 |
| 74 | 6 | -4.174185 | 4.833787 | -1.950147 |
| 75 | 8 | -5.162578 | 4.605493 | -1.186565 |
| 76 | 8 | -4.050995 | 5.695900 | -2.848778 |
| 77 | 6 | -4.853541 | -4.176967 | -1.910248 |
| 78 | 8 | -4.602787 | -5.168050 | -1.157154 |
| 79 | 8 | -5.729920 | -4.056329 | -2.794941 |
| 80 | 6 | -4.439642 | 1.535409 | 1.522383 |
| 81 | 1 | -4.279274 | 2.505741 | 1.999289 |
| 82 | 1 | -5.259535 | 1.636931 | 0.806141 |
| 83 | 1 | -4.771132 | 0.824823 | 2.283565 |
| 84 | 6 | -1.509360 | -4.433148 | 1.516917 |
| 85 | 1 | -1.615571 | -5.248404 | 0.796144 |
| 86 | 1 | -0.785425 | -4.765242 | 2.264965 |
| 87 | 1 | -2.473533 | -4.282738 | 2.009161 |
| 88 | 6 | 4.441800 | -1.509317 | 1.536715 |

| | | | | |
|----|----|-----------|-----------|----------|
| 89 | 1 | 4.283448 | -2.477819 | 2.017931 |
| 90 | 1 | 5.263805 | -1.611179 | 0.822999 |
| 91 | 1 | 4.768818 | -0.793957 | 2.295236 |
| 92 | 6 | 1.516821 | 4.448513 | 1.503628 |
| 93 | 1 | 2.482453 | 4.294965 | 1.992107 |
| 94 | 1 | 1.623876 | 5.261724 | 0.780618 |
| 95 | 1 | 0.797485 | 4.785621 | 2.254021 |
| 96 | 66 | -0.000247 | 0.013594 | 0.132652 |

E(RTPSSh) = -2547.7748475 Hartree

Zero-point correction = 0.782674 Hartree/particle

Sum of electronic and thermal Energies = -2546.939179 Hartree

Sum of electronic and thermal Enthalpies = -2546.938235 Hartree

Sum of electronic and thermal Free Energies = -2547.082011 Hartree

Table S41. [Dy(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.462196 | 2.108049 | 1.683115 |
| 2 | 6 | 1.411078 | 1.718875 | 2.768353 |
| 3 | 6 | 2.561342 | 0.826565 | 2.312074 |
| 4 | 7 | 2.099226 | -0.454109 | 1.692589 |
| 5 | 6 | 1.702667 | -1.404751 | 2.773040 |
| 6 | 6 | 0.813972 | -2.552931 | 2.305090 |
| 7 | 7 | -0.465617 | -2.086623 | 1.686460 |
| 8 | 6 | -1.415447 | -1.695844 | 2.770642 |
| 9 | 6 | -2.565171 | -0.804576 | 2.311376 |
| 10 | 7 | -2.101191 | 0.473735 | 1.689290 |
| 11 | 6 | -1.706798 | 1.427606 | 2.768122 |
| 12 | 6 | -0.817888 | 2.575516 | 2.299170 |
| 13 | 6 | 1.000196 | 3.191383 | 0.790339 |
| 14 | 6 | 1.972841 | 2.572192 | -0.214457 |
| 15 | 8 | 1.749655 | 1.396544 | -0.641535 |
| 16 | 6 | 3.193056 | -0.989462 | 0.811274 |
| 17 | 6 | 2.590933 | -1.954829 | -0.208442 |
| 18 | 8 | 1.423563 | -1.720653 | -0.659975 |
| 19 | 6 | -1.001852 | -3.175186 | 0.798708 |
| 20 | 6 | -1.980867 | -2.567569 | -0.205485 |
| 21 | 8 | -1.757888 | -1.394400 | -0.645279 |
| 22 | 6 | -3.190917 | 1.008016 | 0.802304 |
| 23 | 6 | -2.578531 | 1.967426 | -0.218215 |
| 24 | 8 | -1.410977 | 1.730141 | -0.660756 |
| 25 | 1 | 0.827482 | 1.201882 | 3.533222 |
| 26 | 1 | 1.831679 | 2.605071 | 3.258858 |
| 27 | 1 | 3.184592 | 1.346429 | 1.582652 |
| 28 | 1 | 3.194958 | 0.631081 | 3.187370 |
| 29 | 1 | 1.179793 | -0.823009 | 3.535385 |
| 30 | 1 | 2.584705 | -1.826950 | 3.269602 |
| 31 | 1 | 1.336361 | -3.169672 | 1.571703 |
| 32 | 1 | 0.616674 | -3.194227 | 3.174263 |
| 33 | 1 | -0.832345 | -1.176992 | 3.534590 |
| 34 | 1 | -1.835711 | -2.581320 | 3.262643 |
| 35 | 1 | -3.188117 | -1.326007 | 1.582760 |
| 36 | 1 | -3.199784 | -0.606668 | 3.185422 |
| 37 | 1 | -1.184825 | 0.847929 | 3.532693 |
| 38 | 1 | -2.590163 | 1.850101 | 3.262065 |
| 39 | 1 | -1.339658 | 3.190359 | 1.563782 |
| 40 | 1 | -0.621867 | 3.218696 | 3.167292 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 41 | 1 | 0.142852 | 3.475651 | 0.168926 |
| 42 | 1 | 3.484165 | -0.129844 | 0.196385 |
| 43 | 1 | -0.145461 | -3.456141 | 0.174270 |
| 44 | 1 | -3.484212 | 0.146584 | 0.191148 |
| 45 | 8 | -0.020612 | -0.173089 | -2.354613 |
| 46 | 1 | 0.660823 | -0.850714 | -2.511842 |
| 47 | 1 | -0.864841 | -0.620747 | -2.538343 |
| 48 | 7 | -3.300590 | 2.976455 | -0.661828 |
| 49 | 7 | -2.989083 | -3.294225 | -0.640287 |
| 50 | 7 | 3.315600 | -2.962505 | -0.646444 |
| 51 | 7 | 2.979783 | 3.296872 | -0.659156 |
| 52 | 1 | -4.255861 | 3.206317 | -0.343447 |
| 53 | 1 | -3.207831 | -4.254721 | -0.327569 |
| 54 | 1 | 4.270317 | -3.192584 | -0.324017 |
| 55 | 1 | 3.198519 | 4.258425 | -0.352300 |
| 56 | 6 | 3.919343 | 2.929258 | -1.710631 |
| 57 | 1 | 3.386424 | 2.671859 | -2.631512 |
| 58 | 6 | -2.940002 | 3.902831 | -1.727384 |
| 59 | 1 | -2.698115 | 3.358770 | -2.645912 |
| 60 | 6 | -3.932323 | -2.934507 | -1.691469 |
| 61 | 1 | -4.531614 | -2.066799 | -1.397119 |
| 62 | 6 | 2.960224 | -3.893070 | -1.710395 |
| 63 | 1 | 2.724701 | -3.352496 | -2.632683 |
| 64 | 1 | -2.064321 | 4.497551 | -1.447475 |
| 65 | 1 | 4.517665 | 2.061657 | -1.413739 |
| 66 | 1 | 2.082390 | -4.485335 | -1.432445 |
| 67 | 1 | -3.402415 | -2.681058 | -2.615196 |
| 68 | 6 | 4.196034 | -4.825112 | -1.920740 |
| 69 | 8 | 5.179058 | -4.591536 | -1.151773 |
| 70 | 8 | 4.078608 | -5.691830 | -2.815287 |
| 71 | 6 | 4.843834 | 4.167057 | -1.940278 |
| 72 | 8 | 4.598123 | 5.165276 | -1.195153 |
| 73 | 8 | 5.718745 | 4.036623 | -2.825472 |
| 74 | 6 | -4.174185 | 4.833787 | -1.950147 |
| 75 | 8 | -5.162578 | 4.605493 | -1.186565 |
| 76 | 8 | -4.050995 | 5.695900 | -2.848778 |
| 77 | 6 | -4.853541 | -4.176967 | -1.910248 |
| 78 | 8 | -4.602787 | -5.168050 | -1.157154 |
| 79 | 8 | -5.729920 | -4.056329 | -2.794941 |
| 80 | 6 | -4.439642 | 1.535409 | 1.522383 |
| 81 | 1 | -4.279274 | 2.505741 | 1.999289 |
| 82 | 1 | -5.259535 | 1.636931 | 0.806141 |
| 83 | 1 | -4.771132 | 0.824823 | 2.283565 |
| 84 | 6 | -1.509360 | -4.433148 | 1.516917 |
| 85 | 1 | -1.615571 | -5.248404 | 0.796144 |
| 86 | 1 | -0.785425 | -4.765242 | 2.264965 |
| 87 | 1 | -2.473533 | -4.282738 | 2.009161 |
| 88 | 6 | 4.441800 | -1.509317 | 1.536715 |
| 89 | 1 | 4.283448 | -2.477819 | 2.017931 |
| 90 | 1 | 5.263805 | -1.611179 | 0.822999 |
| 91 | 1 | 4.768818 | -0.793957 | 2.295236 |
| 92 | 6 | 1.516821 | 4.448513 | 1.503628 |
| 93 | 1 | 2.482453 | 4.294965 | 1.992107 |
| 94 | 1 | 1.623876 | 5.261724 | 0.780618 |
| 95 | 1 | 0.797485 | 4.785621 | 2.254021 |
| 96 | 66 | -0.000247 | 0.013594 | 0.132652 |

E(RTPSSh) = -2548.3611382 Hartree

Zero-point correction = 0.782441 Hartree/particle

Sum of electronic and thermal Energies = -2547.525645 Hartree

Sum of electronic and thermal Enthalpies = -2547.524701 Hartree

Sum of electronic and thermal Free Energies = -2547.668697 Hartree

Table S42. [Ho(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.421790 | 2.110654 | 1.692702 |
| 2 | 6 | 1.375666 | 1.741808 | 2.779863 |
| 3 | 6 | 2.542771 | 0.871355 | 2.324214 |
| 4 | 7 | 2.102852 | -0.416340 | 1.703914 |
| 5 | 6 | 1.726988 | -1.374594 | 2.784137 |
| 6 | 6 | 0.859137 | -2.537764 | 2.314139 |
| 7 | 7 | -0.427226 | -2.091688 | 1.695188 |
| 8 | 6 | -1.383384 | -1.721248 | 2.780102 |
| 9 | 6 | -2.549330 | -0.851802 | 2.319968 |
| 10 | 7 | -2.106891 | 0.433752 | 1.697875 |
| 11 | 6 | -1.734504 | 1.394857 | 2.777210 |
| 12 | 6 | -0.865826 | 2.557905 | 2.307636 |
| 13 | 6 | 0.942275 | 3.201017 | 0.798006 |
| 14 | 6 | 1.920840 | 2.594522 | -0.208255 |
| 15 | 8 | 1.717957 | 1.411996 | -0.626381 |
| 16 | 6 | 3.204236 | -0.931576 | 0.820116 |
| 17 | 6 | 2.615701 | -1.901533 | -0.202606 |
| 18 | 8 | 1.441026 | -1.687463 | -0.645523 |
| 19 | 6 | -0.944726 | -3.187273 | 0.805052 |
| 20 | 6 | -1.928088 | -2.592505 | -0.201951 |
| 21 | 8 | -1.724206 | -1.412479 | -0.632940 |
| 22 | 6 | -3.203355 | 0.948269 | 0.807592 |
| 23 | 6 | -2.603098 | 1.913550 | -0.214023 |
| 24 | 8 | -1.428344 | 1.695909 | -0.647587 |
| 25 | 1 | 0.800717 | 1.216138 | 3.545226 |
| 26 | 1 | 1.778884 | 2.636876 | 3.268840 |
| 27 | 1 | 3.155888 | 1.403222 | 1.594711 |
| 28 | 1 | 3.180401 | 0.686766 | 3.198946 |
| 29 | 1 | 1.196397 | -0.803551 | 3.549071 |
| 30 | 1 | 2.617971 | -1.781508 | 3.277415 |
| 31 | 1 | 1.393028 | -3.143279 | 1.579541 |
| 32 | 1 | 0.672112 | -3.184703 | 3.181402 |
| 33 | 1 | -0.809914 | -1.193671 | 3.545229 |
| 34 | 1 | -1.786965 | -2.615524 | 3.270139 |
| 35 | 1 | -3.161088 | -1.385081 | 1.590297 |
| 36 | 1 | -3.189236 | -0.665010 | 3.192587 |
| 37 | 1 | -1.205672 | 0.825606 | 3.544727 |
| 38 | 1 | -2.627373 | 1.801817 | 3.267019 |
| 39 | 1 | -1.398138 | 3.161807 | 1.570599 |
| 40 | 1 | -0.681042 | 3.206382 | 3.174269 |
| 41 | 1 | 0.079711 | 3.472544 | 0.178235 |
| 42 | 1 | 3.481854 | -0.065506 | 0.208124 |
| 43 | 1 | -0.082400 | -3.455663 | 0.183370 |
| 44 | 1 | -3.482221 | 0.080820 | 0.198282 |
| 45 | 8 | -0.015933 | -0.160315 | -2.329951 |
| 46 | 1 | 0.673897 | -0.829773 | -2.485785 |
| 47 | 1 | -0.854432 | -0.619176 | -2.512466 |
| 48 | 7 | -3.340897 | 2.906284 | -0.668258 |
| 49 | 7 | -2.919042 | -3.335174 | -0.648904 |
| 50 | 7 | 3.357376 | -2.891089 | -0.652979 |
| 51 | 7 | 2.910637 | 3.335551 | -0.664270 |
| 52 | 1 | -4.302555 | 3.119840 | -0.357702 |
| 53 | 1 | -3.121923 | -4.301654 | -0.343795 |
| 54 | 1 | 4.318389 | -3.105033 | -0.338025 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 55 | 1 | 3.111898 | 4.303617 | -0.365929 |
| 56 | 6 | 3.849447 | 2.979813 | -1.720532 |
| 57 | 1 | 3.314793 | 2.704100 | -2.635072 |
| 58 | 6 | -2.990896 | 3.832927 | -1.737152 |
| 59 | 1 | -2.732328 | 3.288055 | -2.650632 |
| 60 | 6 | -3.860600 | -2.987173 | -1.705591 |
| 61 | 1 | -4.478553 | -2.132677 | -1.411256 |
| 62 | 6 | 3.014271 | -3.819553 | -1.722858 |
| 63 | 1 | 2.763461 | -3.275923 | -2.639321 |
| 64 | 1 | -2.128787 | 4.446203 | -1.455186 |
| 65 | 1 | 4.468474 | 2.127419 | -1.422059 |
| 66 | 1 | 2.149527 | -4.430992 | -1.445451 |
| 67 | 1 | -3.328229 | -2.718455 | -2.623579 |
| 68 | 6 | 4.266658 | -4.725720 | -1.947642 |
| 69 | 8 | 5.249291 | -4.479434 | -1.182173 |
| 70 | 8 | 4.160826 | -5.587107 | -2.848735 |
| 71 | 6 | 4.745735 | 4.234957 | -1.966970 |
| 72 | 8 | 4.485397 | 5.233261 | -1.226976 |
| 73 | 8 | 5.615508 | 4.116250 | -2.858838 |
| 74 | 6 | -4.241103 | 4.738633 | -1.973960 |
| 75 | 8 | -5.230144 | 4.495971 | -1.215696 |
| 76 | 8 | -4.128129 | 5.597417 | -2.877096 |
| 77 | 6 | -4.756418 | -4.245467 | -1.938838 |
| 78 | 8 | -4.492687 | -5.236169 | -1.189710 |
| 79 | 8 | -5.628011 | -4.135934 | -2.829649 |
| 80 | 6 | -4.461606 | 1.458621 | 1.523418 |
| 81 | 1 | -4.318174 | 2.433685 | 1.996052 |
| 82 | 1 | -5.281959 | 1.543110 | 0.805515 |
| 83 | 1 | -4.782449 | 0.746085 | 2.287389 |
| 84 | 6 | -1.437026 | -4.453003 | 1.520251 |
| 85 | 1 | -1.526717 | -5.269615 | 0.798795 |
| 86 | 1 | -0.711978 | -4.774096 | 2.272056 |
| 87 | 1 | -2.405996 | -4.317670 | 2.007408 |
| 88 | 6 | 4.461458 | -1.435327 | 1.542331 |
| 89 | 1 | 4.319200 | -2.408948 | 2.018213 |
| 90 | 1 | 5.284798 | -1.519653 | 0.827886 |
| 91 | 1 | 4.776939 | -0.718818 | 2.304691 |
| 92 | 6 | 1.442797 | 4.466072 | 1.508831 |
| 93 | 1 | 2.412963 | 4.327811 | 1.992863 |
| 94 | 1 | 1.533634 | 5.280785 | 0.785325 |
| 95 | 1 | 0.721669 | 4.791993 | 2.262485 |
| 96 | 67 | -0.000406 | 0.013639 | 0.148922 |

E(RTPSSh) = -2548.9451695 Hartree

Zero-point correction = 0.781951 Hartree/particle

Sum of electronic and thermal Energies = -2548.110041 Hartree

Sum of electronic and thermal Enthalpies = -2548.109097 Hartree

Sum of electronic and thermal Free Energies = -2548.253789 Hartree

Table S43. [Tm(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | 0.383432 | 2.101856 | 1.701972 |
| 2 | 6 | 1.340905 | 1.758366 | 2.791895 |
| 3 | 6 | 2.521585 | 0.909481 | 2.335410 |
| 4 | 7 | 2.093047 | -0.381066 | 1.715770 |
| 5 | 6 | 1.738860 | -1.341074 | 2.799144 |
| 6 | 6 | 0.895140 | -2.518772 | 2.326594 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 7 | 7 | -0.393215 | -2.085368 | 1.705931 |
| 8 | 6 | -1.354455 | -1.738754 | 2.791705 |
| 9 | 6 | -2.533386 | -0.892087 | 2.327406 |
| 10 | 7 | -2.101958 | 0.395973 | 1.705938 |
| 11 | 6 | -1.752984 | 1.359987 | 2.787933 |
| 12 | 6 | -0.907260 | 2.537061 | 2.316262 |
| 13 | 6 | 0.889317 | 3.194254 | 0.799270 |
| 14 | 6 | 1.874607 | 2.595128 | -0.204811 |
| 15 | 8 | 1.691347 | 1.403646 | -0.607851 |
| 16 | 6 | 3.197989 | -0.884142 | 0.827773 |
| 17 | 6 | 2.618297 | -1.855947 | -0.198035 |
| 18 | 8 | 1.435918 | -1.657305 | -0.630602 |
| 19 | 6 | -0.895144 | -3.184302 | 0.809298 |
| 20 | 6 | -1.880084 | -2.598389 | -0.200955 |
| 21 | 8 | -1.689832 | -1.411494 | -0.622055 |
| 22 | 6 | -3.200664 | 0.897165 | 0.809013 |
| 23 | 6 | -2.606903 | 1.865896 | -0.213010 |
| 24 | 8 | -1.424507 | 1.662982 | -0.634702 |
| 25 | 1 | 0.777047 | 1.224263 | 3.560191 |
| 26 | 1 | 1.725628 | 2.663244 | 3.278333 |
| 27 | 1 | 3.123976 | 1.453012 | 1.605271 |
| 28 | 1 | 3.164399 | 0.731653 | 3.207929 |
| 29 | 1 | 1.196550 | -0.779924 | 3.563699 |
| 30 | 1 | 2.637870 | -1.728279 | 3.294357 |
| 31 | 1 | 1.442852 | -3.112362 | 1.592026 |
| 32 | 1 | 0.714350 | -3.171780 | 3.190810 |
| 33 | 1 | -0.793438 | -1.201523 | 3.559839 |
| 34 | 1 | -1.740121 | -2.642097 | 3.280176 |
| 35 | 1 | -3.132260 | -1.437908 | 1.595923 |
| 36 | 1 | -3.180926 | -0.712044 | 3.195988 |
| 37 | 1 | -1.213818 | 0.801365 | 3.556564 |
| 38 | 1 | -2.654684 | 1.747846 | 3.277704 |
| 39 | 1 | -1.452000 | 3.128862 | 1.578104 |
| 40 | 1 | -0.729788 | 3.191842 | 3.179840 |
| 41 | 1 | 0.021684 | 3.451572 | 0.180302 |
| 42 | 1 | 3.467584 | -0.012906 | 0.219346 |
| 43 | 1 | -0.026388 | -3.442040 | 0.191847 |
| 44 | 1 | -3.469109 | 0.024505 | 0.202254 |
| 45 | 8 | -0.012831 | -0.142773 | -2.312619 |
| 46 | 1 | 0.675638 | -0.812481 | -2.473194 |
| 47 | 1 | -0.852216 | -0.596949 | -2.502269 |
| 48 | 7 | -3.354966 | 2.844888 | -0.676678 |
| 49 | 7 | -2.855822 | -3.352069 | -0.658834 |
| 50 | 7 | 3.372268 | -2.829041 | -0.659791 |
| 51 | 7 | 2.848846 | 3.348441 | -0.670778 |
| 52 | 1 | -4.327709 | 3.054311 | -0.383617 |
| 53 | 1 | -3.056617 | -4.328751 | -0.369290 |
| 54 | 1 | 4.344839 | -3.038464 | -0.362182 |
| 55 | 1 | 3.043462 | 4.327841 | -0.390570 |
| 56 | 6 | 3.794091 | 3.006056 | -1.726173 |
| 57 | 1 | 3.265924 | 2.711339 | -2.638476 |
| 58 | 6 | -3.017624 | 3.775546 | -1.746668 |
| 59 | 1 | -2.742683 | 3.234799 | -2.657765 |
| 60 | 6 | -3.797702 | -3.019277 | -1.720693 |
| 61 | 1 | -4.435864 | -2.178949 | -1.428634 |
| 62 | 6 | 3.045375 | -3.758025 | -1.734845 |
| 63 | 1 | 2.779337 | -3.215620 | -2.647751 |
| 64 | 1 | -2.171356 | 4.409363 | -1.461998 |
| 65 | 1 | 4.435031 | 2.171734 | -1.422659 |
| 66 | 1 | 2.197135 | -4.392727 | -1.458671 |
| 67 | 1 | -3.266582 | -2.738757 | -2.635881 |
| 68 | 6 | 4.326822 | -4.628790 | -1.961464 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 69 | 8 | 5.296083 | -4.349828 | -1.188350 |
| 70 | 8 | 4.248899 | -5.487983 | -2.864338 |
| 71 | 6 | 4.655916 | 4.289046 | -1.974956 |
| 72 | 8 | 4.362522 | 5.274779 | -1.228699 |
| 73 | 8 | 5.525154 | 4.196593 | -2.867448 |
| 74 | 6 | -4.294395 | 4.649503 | -1.984689 |
| 75 | 8 | -5.272209 | 4.374025 | -1.221304 |
| 76 | 8 | -4.205641 | 5.509213 | -2.886650 |
| 77 | 6 | -4.662117 | -4.303975 | -1.953362 |
| 78 | 8 | -4.369907 | -5.279732 | -1.193408 |
| 79 | 8 | -5.530296 | -4.221879 | -2.847272 |
| 80 | 6 | -4.465475 | 1.399995 | 1.518594 |
| 81 | 1 | -4.330710 | 2.378775 | 1.986454 |
| 82 | 1 | -5.283051 | 1.476348 | 0.796565 |
| 83 | 1 | -4.784847 | 0.688994 | 2.284808 |
| 84 | 6 | -1.380106 | -4.456675 | 1.517894 |
| 85 | 1 | -1.457973 | -5.271196 | 0.792625 |
| 86 | 1 | -0.658250 | -4.774347 | 2.274399 |
| 87 | 1 | -2.354544 | -4.331556 | 1.997269 |
| 88 | 6 | 4.459360 | -1.382604 | 1.546563 |
| 89 | 1 | 4.323679 | -2.360479 | 2.016001 |
| 90 | 1 | 5.281923 | -1.458581 | 0.830248 |
| 91 | 1 | 4.771802 | -0.668898 | 2.312992 |
| 92 | 6 | 1.377861 | 4.468285 | 1.502374 |
| 93 | 1 | 2.351902 | 4.342556 | 1.982448 |
| 94 | 1 | 1.458338 | 5.279508 | 0.773663 |
| 95 | 1 | 0.656690 | 4.791374 | 2.257406 |
| 96 | 69 | -0.000706 | 0.014471 | 0.141891 |

E(RTPSSh) = -2550.0860564 Hartree

Zero-point correction = 0.782014 Hartree/particle

Sum of electronic and thermal Energies = -2549.251264 Hartree

Sum of electronic and thermal Enthalpies = -2549.250319 Hartree

Sum of electronic and thermal Free Energies = -2549.393187 Hartree

Table S44. [Yb(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.310352 | 2.109248 | 1.709231 |
| 2 | 6 | 1.278930 | 1.802774 | 2.800005 |
| 3 | 6 | 2.487343 | 0.994346 | 2.342759 |
| 4 | 7 | 2.100283 | -0.310045 | 1.724941 |
| 5 | 6 | 1.782151 | -1.281163 | 2.808957 |
| 6 | 6 | 0.979196 | -2.486204 | 2.334464 |
| 7 | 7 | -0.322258 | -2.093791 | 1.713986 |
| 8 | 6 | -1.295594 | -1.784049 | 2.799612 |
| 9 | 6 | -2.501781 | -0.978059 | 2.333089 |
| 10 | 7 | -2.111106 | 0.323563 | 1.713029 |
| 11 | 6 | -1.799536 | 1.299188 | 2.795462 |
| 12 | 6 | -0.994047 | 2.503548 | 2.322206 |
| 13 | 6 | 0.780058 | 3.215189 | 0.803083 |
| 14 | 6 | 1.780592 | 2.644112 | -0.201808 |
| 15 | 8 | 1.637481 | 1.444052 | -0.595416 |
| 16 | 6 | 3.218931 | -0.776907 | 0.834217 |
| 17 | 6 | 2.667165 | -1.762579 | -0.193419 |
| 18 | 8 | 1.476052 | -1.602611 | -0.618134 |
| 19 | 6 | -0.786822 | -3.206248 | 0.813730 |
| 20 | 6 | -1.785830 | -2.648890 | -0.198454 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 21 | 8 | -1.635344 | -1.453168 | -0.610683 |
| 22 | 6 | -3.222828 | 0.788118 | 0.812145 |
| 23 | 6 | -2.656342 | 1.772331 | -0.210107 |
| 24 | 8 | -1.464971 | 1.608494 | -0.623481 |
| 25 | 1 | 0.734936 | 1.250608 | 3.569737 |
| 26 | 1 | 1.631688 | 2.721885 | 3.283811 |
| 27 | 1 | 3.069122 | 1.557528 | 1.610582 |
| 28 | 1 | 3.138029 | 0.838894 | 3.213676 |
| 29 | 1 | 1.221050 | -0.740160 | 3.574344 |
| 30 | 1 | 2.694905 | -1.636764 | 3.302555 |
| 31 | 1 | 1.547178 | -3.059015 | 1.598545 |
| 32 | 1 | 0.819894 | -3.147313 | 3.196727 |
| 33 | 1 | -0.755372 | -1.228336 | 3.569382 |
| 34 | 1 | -1.649642 | -2.701471 | 3.285628 |
| 35 | 1 | -3.079393 | -1.543768 | 1.599391 |
| 36 | 1 | -3.157941 | -0.820000 | 3.199437 |
| 37 | 1 | -1.242477 | 0.761015 | 3.565804 |
| 38 | 1 | -2.715545 | 1.655552 | 3.282439 |
| 39 | 1 | -1.558320 | 3.074514 | 1.582091 |
| 40 | 1 | -0.838749 | 3.166463 | 3.183814 |
| 41 | 1 | -0.096334 | 3.444842 | 0.185499 |
| 42 | 1 | 3.461703 | 0.103381 | 0.227436 |
| 43 | 1 | 0.091298 | -3.436168 | 0.198396 |
| 44 | 1 | -3.462627 | -0.093537 | 0.206264 |
| 45 | 8 | -0.008396 | -0.131958 | -2.294471 |
| 46 | 1 | 0.697302 | -0.783595 | -2.454574 |
| 47 | 1 | -0.835457 | -0.608268 | -2.483860 |
| 48 | 7 | -3.434083 | 2.723385 | -0.683025 |
| 49 | 7 | -2.731891 | -3.433058 | -0.667239 |
| 50 | 7 | 3.451127 | -2.706644 | -0.665317 |
| 51 | 7 | 2.725806 | 3.427304 | -0.678204 |
| 52 | 1 | -4.415389 | 2.901058 | -0.397435 |
| 53 | 1 | -2.899827 | -4.418327 | -0.385735 |
| 54 | 1 | 4.432249 | -2.884359 | -0.374949 |
| 55 | 1 | 2.887424 | 4.415129 | -0.406590 |
| 56 | 6 | 3.679017 | 3.109547 | -1.734236 |
| 57 | 1 | 3.158733 | 2.790228 | -2.642756 |
| 58 | 6 | -3.121201 | 3.661576 | -1.753974 |
| 59 | 1 | -2.822888 | 3.127752 | -2.661766 |
| 60 | 6 | -3.680222 | -3.126090 | -1.731246 |
| 61 | 1 | -4.348448 | -2.310462 | -1.436404 |
| 62 | 6 | 3.149648 | -3.641459 | -1.742864 |
| 63 | 1 | 2.860031 | -3.104643 | -2.651878 |
| 64 | 1 | -2.298386 | 4.324157 | -1.466053 |
| 65 | 1 | 4.349033 | 2.300026 | -1.426394 |
| 66 | 1 | 2.325291 | -4.306053 | -1.464621 |
| 67 | 1 | -3.155528 | -2.821400 | -2.642403 |
| 68 | 6 | 4.458569 | -4.467321 | -1.980546 |
| 69 | 8 | 5.422177 | -4.159029 | -1.211521 |
| 70 | 8 | 4.404191 | -5.324844 | -2.886664 |
| 71 | 6 | 4.496080 | 4.419205 | -1.994961 |
| 72 | 8 | 4.170300 | 5.400430 | -1.256269 |
| 73 | 8 | 5.366614 | 4.348735 | -2.888142 |
| 74 | 6 | -4.424700 | 4.492213 | -2.002188 |
| 75 | 8 | -5.397434 | 4.186919 | -1.243686 |
| 76 | 8 | -4.358501 | 5.351751 | -2.906192 |
| 77 | 6 | -4.498886 | -4.438332 | -1.975690 |
| 78 | 8 | -4.175801 | -5.408482 | -1.221095 |
| 79 | 8 | -5.366156 | -4.379839 | -2.872268 |
| 80 | 6 | -4.503928 | 1.254710 | 1.517226 |
| 81 | 1 | -4.399587 | 2.239208 | 1.980910 |
| 82 | 1 | -5.322019 | 1.302961 | 0.793398 |

| | | | | |
|----|----|-----------|-----------|----------|
| 83 | 1 | -4.802713 | 0.537490 | 2.285932 |
| 84 | 6 | -1.236672 | -4.493558 | 1.518472 |
| 85 | 1 | -1.285198 | -5.309551 | 0.792339 |
| 86 | 1 | -0.510123 | -4.789351 | 2.279334 |
| 87 | 1 | -2.217530 | -4.398052 | 1.991589 |
| 88 | 6 | 4.495176 | -1.240776 | 1.549898 |
| 89 | 1 | 4.388376 | -2.224430 | 2.014777 |
| 90 | 1 | 5.319092 | -1.289169 | 0.832780 |
| 91 | 1 | 4.786669 | -0.521464 | 2.319334 |
| 92 | 6 | 1.233076 | 4.504248 | 1.502533 |
| 93 | 1 | 2.213353 | 4.408158 | 1.976773 |
| 94 | 1 | 1.284544 | 5.316967 | 0.772911 |
| 95 | 1 | 0.506713 | 4.805540 | 2.261580 |
| 96 | 70 | -0.001338 | 0.014745 | 0.154291 |

E(RTPSSh) = -2550.6693165 Hartree

Zero-point correction = 0.782274 Hartree/particle

Sum of electronic and thermal Energies = -2549.834377 Hartree

Sum of electronic and thermal Enthalpies = -2549.833433 Hartree

Sum of electronic and thermal Free Energies = -2549.975698 Hartree

Table S45. [Lu(DOTMA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.265920 | 2.111109 | 1.710223 |
| 2 | 6 | 1.241176 | 1.828352 | 2.801408 |
| 3 | 6 | 2.465826 | 1.045614 | 2.343312 |
| 4 | 7 | 2.103239 | -0.266204 | 1.726348 |
| 5 | 6 | 1.808622 | -1.243671 | 2.810976 |
| 6 | 6 | 1.031694 | -2.464821 | 2.335030 |
| 7 | 7 | -0.277067 | -2.096775 | 1.714947 |
| 8 | 6 | -1.256672 | -1.811011 | 2.801296 |
| 9 | 6 | -2.479325 | -1.031184 | 2.334020 |
| 10 | 7 | -2.113628 | 0.278055 | 1.714765 |
| 11 | 6 | -1.825277 | 1.259956 | 2.797749 |
| 12 | 6 | -1.045782 | 2.480623 | 2.323229 |
| 13 | 6 | 0.713315 | 3.224428 | 0.801581 |
| 14 | 6 | 1.723204 | 2.669767 | -0.202829 |
| 15 | 8 | 1.604319 | 1.464964 | -0.589882 |
| 16 | 6 | 3.228692 | -0.711387 | 0.833043 |
| 17 | 6 | 2.692119 | -1.705210 | -0.194533 |
| 18 | 8 | 1.496437 | -1.567057 | -0.614260 |
| 19 | 6 | -0.719483 | -3.216141 | 0.812056 |
| 20 | 6 | -1.726578 | -2.674788 | -0.200489 |
| 21 | 8 | -1.598328 | -1.474633 | -0.607620 |
| 22 | 6 | -3.233009 | 0.720600 | 0.812240 |
| 23 | 6 | -2.682898 | 1.713823 | -0.209835 |
| 24 | 8 | -1.486783 | 1.573098 | -0.617841 |
| 25 | 1 | 0.710515 | 1.265155 | 3.572420 |
| 26 | 1 | 1.573488 | 2.756011 | 3.283259 |
| 27 | 1 | 3.035004 | 1.620547 | 1.610196 |
| 28 | 1 | 3.120936 | 0.903217 | 3.213098 |
| 29 | 1 | 1.236022 | -0.716145 | 3.577211 |
| 30 | 1 | 2.729776 | -1.578832 | 3.303182 |
| 31 | 1 | 1.611748 | -3.024466 | 1.598202 |
| 32 | 1 | 0.885400 | -3.130820 | 3.195790 |
| 33 | 1 | -0.729824 | -1.243857 | 3.571944 |
| 34 | 1 | -1.589837 | -2.736965 | 3.285805 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 35 | 1 | -3.043994 | -1.608841 | 1.599344 |
| 36 | 1 | -3.140052 | -0.886601 | 3.199204 |
| 37 | 1 | -1.256676 | 0.735113 | 3.568817 |
| 38 | 1 | -2.749538 | 1.595850 | 3.283592 |
| 39 | 1 | -1.622155 | 3.038893 | 1.582590 |
| 40 | 1 | -0.903316 | 3.147917 | 3.183625 |
| 41 | 1 | -0.167768 | 3.436537 | 0.184510 |
| 42 | 1 | 3.454697 | 0.173662 | 0.226835 |
| 43 | 1 | 0.163430 | -3.428996 | 0.197544 |
| 44 | 1 | -3.455892 | -0.165738 | 0.206855 |
| 45 | 8 | -0.006084 | -0.117865 | -2.283816 |
| 46 | 1 | 0.712302 | -0.755095 | -2.445189 |
| 47 | 1 | -0.823863 | -0.610999 | -2.470543 |
| 48 | 7 | -3.477443 | 2.648281 | -0.687778 |
| 49 | 7 | -2.656397 | -3.474988 | -0.674389 |
| 50 | 7 | 3.491615 | -2.633710 | -0.671087 |
| 51 | 7 | 2.651405 | 3.469631 | -0.684847 |
| 52 | 1 | -4.462813 | 2.808035 | -0.405421 |
| 53 | 1 | -2.807406 | -4.463880 | -0.395662 |
| 54 | 1 | 4.476582 | -2.794716 | -0.383726 |
| 55 | 1 | 2.794549 | 4.461454 | -0.417304 |
| 56 | 6 | 3.612228 | 3.164978 | -1.737866 |
| 57 | 1 | 3.099583 | 2.835580 | -2.647163 |
| 58 | 6 | -3.178258 | 3.593079 | -1.756860 |
| 59 | 1 | -2.870494 | 3.065687 | -2.665284 |
| 60 | 6 | -3.611141 | -3.181413 | -1.736481 |
| 61 | 1 | -4.290919 | -2.376085 | -1.439809 |
| 62 | 6 | 3.202814 | -3.574817 | -1.746675 |
| 63 | 1 | 2.903658 | -3.044198 | -2.656255 |
| 64 | 1 | -2.366495 | 4.268264 | -1.466909 |
| 65 | 1 | 4.294310 | 2.366953 | -1.426590 |
| 66 | 1 | 2.389281 | -4.251613 | -1.466031 |
| 67 | 1 | -3.092867 | -2.868467 | -2.648540 |
| 68 | 6 | 4.523958 | -4.380805 | -1.985109 |
| 69 | 8 | 5.484612 | -4.054601 | -1.219790 |
| 70 | 8 | 4.480497 | -5.242074 | -2.888206 |
| 71 | 6 | 4.408799 | 4.487037 | -1.999487 |
| 72 | 8 | 4.063192 | 5.465366 | -1.265999 |
| 73 | 8 | 5.284574 | 4.427557 | -2.888293 |
| 74 | 6 | -4.494591 | 4.403152 | -2.005423 |
| 75 | 8 | -5.463747 | 4.079866 | -1.249803 |
| 76 | 8 | -4.440352 | 5.266065 | -2.906962 |
| 77 | 6 | -4.410491 | -4.505633 | -1.980410 |
| 78 | 8 | -4.069717 | -5.472021 | -1.228776 |
| 79 | 8 | -5.281672 | -4.458652 | -2.873805 |
| 80 | 6 | -4.522937 | 1.165393 | 1.515090 |
| 81 | 1 | -4.436736 | 2.152956 | 1.975960 |
| 82 | 1 | -5.341106 | 1.196810 | 0.790435 |
| 83 | 1 | -4.809130 | 0.444918 | 2.285530 |
| 84 | 6 | -1.148034 | -4.512271 | 1.513612 |
| 85 | 1 | -1.179630 | -5.327965 | 0.786216 |
| 86 | 1 | -0.418644 | -4.795816 | 2.276413 |
| 87 | 1 | -2.131988 | -4.434904 | 1.983575 |
| 88 | 6 | 4.513922 | -1.154456 | 1.545583 |
| 89 | 1 | 4.424937 | -2.141137 | 2.007805 |
| 90 | 1 | 5.337428 | -1.186499 | 0.827079 |
| 91 | 1 | 4.793722 | -0.432143 | 2.316545 |
| 92 | 6 | 1.144127 | 4.522528 | 1.498060 |
| 93 | 1 | 2.127548 | 4.445087 | 1.969161 |
| 94 | 1 | 1.178269 | 5.335056 | 0.767218 |
| 95 | 1 | 0.414610 | 4.811140 | 2.258995 |
| 96 | 71 | -0.001153 | 0.015517 | 0.159928 |

E(RTPSSh) = -2551.223034 Hartree
 Zero-point correction = 0.782361 Hartree/particle
 Sum of electronic and thermal Energies = -2550.388051 Hartree
 Sum of electronic and thermal Enthalpies = -2550.387107 Hartree
 Sum of electronic and thermal Free Energies = -2550.529304 Hartree

Table S46. [La(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.103298 | -1.857872 | 1.884380 |
| 2 | 6 | -0.127138 | -2.196801 | 2.956747 |
| 3 | 6 | 1.313925 | -2.340860 | 2.473001 |
| 4 | 7 | 1.873925 | -1.085634 | 1.886295 |
| 5 | 6 | 2.197301 | -0.113317 | 2.967407 |
| 6 | 6 | 2.345072 | 1.330112 | 2.491723 |
| 7 | 7 | 1.096238 | 1.887350 | 1.889247 |
| 8 | 6 | 0.120365 | 2.228950 | 2.960362 |
| 9 | 6 | -1.320790 | 2.368936 | 2.475952 |
| 10 | 7 | -1.874430 | 1.112895 | 1.884955 |
| 11 | 6 | -2.207476 | 0.142304 | 2.963357 |
| 12 | 6 | -2.353231 | -1.300742 | 2.486272 |
| 13 | 6 | -1.431119 | -3.044119 | 1.021245 |
| 14 | 6 | -2.223798 | -2.517906 | -0.186976 |
| 15 | 8 | -1.951239 | -1.363779 | -0.650500 |
| 16 | 6 | 3.073631 | -1.402740 | 1.038395 |
| 17 | 6 | 2.572778 | -2.167813 | -0.197150 |
| 18 | 8 | 1.425283 | -1.890148 | -0.676016 |
| 19 | 6 | 1.422990 | 3.067994 | 1.019597 |
| 20 | 6 | 2.207222 | 2.531363 | -0.190916 |
| 21 | 8 | 1.945952 | 1.368197 | -0.633479 |
| 22 | 6 | -3.061105 | 1.428513 | 1.019263 |
| 23 | 6 | -2.535429 | 2.19062 | -0.204362 |
| 24 | 8 | -1.376593 | 1.931760 | -0.656078 |
| 25 | 1 | -0.188900 | -1.409783 | 3.711264 |
| 26 | 1 | -0.406257 | -3.123092 | 3.473752 |
| 27 | 1 | 1.375516 | -3.123082 | 1.711233 |
| 28 | 1 | 1.920137 | -2.677204 | 3.324562 |
| 29 | 1 | 1.400661 | -0.177714 | 3.711515 |
| 30 | 1 | 3.117134 | -0.393767 | 3.495327 |
| 31 | 1 | 3.139169 | 1.397220 | 1.743289 |
| 32 | 1 | 2.666305 | 1.933915 | 3.350875 |
| 33 | 1 | 0.182617 | 1.444402 | 3.717587 |
| 34 | 1 | 0.398149 | 3.157635 | 3.474249 |
| 35 | 1 | -1.384627 | 3.153471 | 1.717006 |
| 36 | 1 | -1.929525 | 2.699998 | 3.327864 |
| 37 | 1 | -1.416556 | 0.206533 | 3.713718 |
| 38 | 1 | -3.131528 | 0.422989 | 3.484083 |
| 39 | 1 | -3.146146 | -1.367481 | 1.736396 |
| 40 | 1 | -2.675228 | -1.905921 | 3.344037 |
| 41 | 1 | -0.476275 | -3.390103 | 0.604896 |
| 42 | 1 | 3.429408 | -0.441092 | 0.647715 |
| 43 | 1 | 0.466692 | 3.415572 | 0.608208 |
| 44 | 1 | -3.409561 | 0.467254 | 0.620717 |
| 45 | 8 | -0.031286 | -0.379519 | -2.463817 |
| 46 | 1 | 0.610195 | -1.110188 | -2.533969 |
| 47 | 1 | -0.897496 | -0.787741 | -2.636402 |
| 48 | 7 | -3.313610 | 3.095973 | -0.770500 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 49 | 7 | 3.110524 | 3.304824 | -0.753967 |
| 50 | 7 | 3.356049 | -3.067033 | -0.749836 |
| 51 | 7 | -3.141667 | -3.287146 | -0.729795 |
| 52 | 1 | -4.254849 | 3.381480 | -0.441414 |
| 53 | 1 | 3.391432 | 4.249121 | -0.430390 |
| 54 | 1 | 4.287613 | -3.363815 | -0.401419 |
| 55 | 1 | -3.430604 | -4.225141 | -0.392758 |
| 56 | 6 | -3.945134 | -2.989089 | -1.908794 |
| 57 | 1 | -3.307009 | -2.832734 | -2.784707 |
| 58 | 6 | -3.019453 | 3.877707 | -1.964879 |
| 59 | 1 | -2.853563 | 3.222814 | -2.826419 |
| 60 | 6 | 3.907729 | 2.998618 | -1.934973 |
| 61 | 1 | 3.264247 | 2.824174 | -2.803395 |
| 62 | 6 | 3.081215 | -3.844003 | -1.952089 |
| 63 | 1 | 2.947820 | -3.186660 | -2.817559 |
| 64 | 1 | -4.537303 | -2.081214 | -1.755390 |
| 65 | 1 | -2.117257 | 4.480981 | -1.821124 |
| 66 | 1 | 4.508928 | 2.097878 | -1.774203 |
| 67 | 1 | 2.167485 | -4.434696 | -1.831581 |
| 68 | 6 | -4.263514 | 4.796952 | -2.202835 |
| 69 | 8 | -5.195296 | 4.654209 | -1.350377 |
| 70 | 8 | -4.198957 | 5.558088 | -3.191371 |
| 71 | 6 | 4.830562 | 4.239811 | -2.173786 |
| 72 | 8 | 4.677947 | 5.180170 | -1.332608 |
| 73 | 8 | 5.603916 | 4.165063 | -3.152156 |
| 74 | 6 | 4.319508 | -4.779316 | -2.158319 |
| 75 | 8 | 4.269735 | -5.540797 | -3.147034 |
| 76 | 8 | 5.231274 | -4.645819 | -1.283048 |
| 77 | 6 | -4.879675 | -4.226420 | -2.123132 |
| 78 | 8 | -4.727352 | -5.155391 | -1.269269 |
| 79 | 8 | -5.659474 | -4.159471 | -3.096513 |
| 80 | 6 | 2.110703 | 4.243645 | 1.728637 |
| 81 | 1 | 3.125364 | 3.994048 | 2.049763 |
| 82 | 1 | 2.159987 | 5.103861 | 1.055568 |
| 83 | 1 | 1.539070 | 4.566354 | 2.601366 |
| 84 | 6 | -4.233437 | 2.121886 | 1.728372 |
| 85 | 1 | -3.985613 | 3.142231 | 2.032356 |
| 86 | 1 | -5.099476 | 2.157711 | 1.061928 |
| 87 | 1 | -4.546203 | 1.561930 | 2.612227 |
| 88 | 6 | -2.109494 | -4.219891 | 1.738711 |
| 89 | 1 | -3.120858 | -3.971155 | 2.070626 |
| 90 | 1 | -2.164903 | -5.080197 | 1.066230 |
| 91 | 1 | -1.528352 | -4.542075 | 2.605168 |
| 92 | 6 | 4.233456 | -2.100149 | 1.764311 |
| 93 | 1 | 3.980068 | -3.121587 | 2.059906 |
| 94 | 1 | 5.110097 | -2.133751 | 1.111762 |
| 95 | 1 | 4.532628 | -1.544473 | 2.655428 |
| 96 | 57 | -0.000071 | 0.014789 | 0.146876 |

E(RTPSSh) = -2542.844013 Hartree

Zero-point correction = 0.780582 Hartree/particle

Sum of electronic and thermal Energies = -2542.009901 Hartree

Sum of electronic and thermal Enthalpies = -2542.008957 Hartree

Sum of electronic and thermal Free Energies = -2542.155485 Hartree

Table S47. [Ce(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|---|---|
| | | X | Y | Z |
| | | | | |

| | | | | |
|----|---|-----------|-----------|-----------|
| 1 | 7 | -1.080883 | -1.864952 | 1.891583 |
| 2 | 6 | -0.104898 | -2.200902 | 2.964673 |
| 3 | 6 | 1.337429 | -2.328916 | 2.481620 |
| 4 | 7 | 1.879676 | -1.066191 | 1.894653 |
| 5 | 6 | 2.200043 | -0.094470 | 2.976700 |
| 6 | 6 | 2.331640 | 1.350432 | 2.501990 |
| 7 | 7 | 1.075563 | 1.890244 | 1.898597 |
| 8 | 6 | 0.099650 | 2.228045 | 2.970567 |
| 9 | 6 | -1.342801 | 2.352454 | 2.487065 |
| 10 | 7 | -1.879281 | 1.089685 | 1.894674 |
| 11 | 6 | -2.208247 | 0.117886 | 2.972835 |
| 12 | 6 | -2.338140 | -1.325893 | 2.494501 |
| 13 | 6 | -1.392810 | -3.047303 | 1.017645 |
| 14 | 6 | -2.187292 | -2.517325 | -0.187179 |
| 15 | 8 | -1.928254 | -1.353055 | -0.633936 |
| 16 | 6 | 3.075194 | -1.367252 | 1.035648 |
| 17 | 6 | 2.569084 | -2.134502 | -0.195883 |
| 18 | 8 | 1.410275 | -1.872178 | -0.656645 |
| 19 | 6 | 1.387171 | 3.067498 | 1.019105 |
| 20 | 6 | 2.174167 | 2.527120 | -0.187552 |
| 21 | 8 | 1.928744 | 1.353695 | -0.612324 |
| 22 | 6 | -3.063261 | 1.390943 | 1.020619 |
| 23 | 6 | -2.534467 | 2.163657 | -0.199722 |
| 24 | 8 | -1.366383 | 1.910451 | -0.635736 |
| 25 | 1 | -0.175057 | -1.417492 | 3.722275 |
| 26 | 1 | -0.377368 | -3.131893 | 3.476839 |
| 27 | 1 | 1.408204 | -3.110709 | 1.720296 |
| 28 | 1 | 1.948307 | -2.657238 | 3.332950 |
| 29 | 1 | 1.407104 | -0.167716 | 3.724029 |
| 30 | 1 | 3.124792 | -0.368160 | 3.499658 |
| 31 | 1 | 3.125765 | 1.427385 | 1.754622 |
| 32 | 1 | 2.644087 | 1.958549 | 3.361304 |
| 33 | 1 | 0.170330 | 1.446530 | 3.730266 |
| 34 | 1 | 0.370697 | 3.161041 | 3.480280 |
| 35 | 1 | -1.416056 | 3.137272 | 1.729319 |
| 36 | 1 | -1.955870 | 2.674685 | 3.339216 |
| 37 | 1 | -1.420391 | 0.189770 | 3.725788 |
| 38 | 1 | -3.136739 | 0.390972 | 3.489754 |
| 39 | 1 | -3.130678 | -1.400993 | 1.745075 |
| 40 | 1 | -2.652179 | -1.936509 | 3.351342 |
| 41 | 1 | -0.433094 | -3.378337 | 0.600357 |
| 42 | 1 | 3.415741 | -0.400758 | 0.643355 |
| 43 | 1 | 0.426268 | 3.400746 | 0.606637 |
| 44 | 1 | -3.398627 | 0.425402 | 0.621341 |
| 45 | 8 | -0.032388 | -0.327117 | -2.420345 |
| 46 | 1 | 0.613882 | -1.051284 | -2.509553 |
| 47 | 1 | -0.897283 | -0.740809 | -2.587601 |
| 48 | 7 | -3.317952 | 3.047272 | -0.779026 |
| 49 | 7 | 3.062916 | 3.306261 | -0.765312 |
| 50 | 7 | 3.357649 | -3.019298 | -0.763708 |
| 51 | 7 | -3.091926 | -3.291556 | -0.744225 |
| 52 | 1 | -4.266381 | 3.321934 | -0.461276 |
| 53 | 1 | 3.331947 | 4.258470 | -0.454645 |
| 54 | 1 | 4.297525 | -3.304950 | -0.428165 |
| 55 | 1 | -3.370783 | -4.237077 | -0.419247 |
| 56 | 6 | -3.896756 | -2.989145 | -1.921302 |
| 57 | 1 | -3.259090 | -2.817240 | -2.794650 |
| 58 | 6 | -3.020050 | 3.830136 | -1.971789 |
| 59 | 1 | -2.838062 | 3.175631 | -2.830385 |
| 60 | 6 | 3.861486 | 2.995957 | -1.944400 |
| 61 | 1 | 3.218489 | 2.803051 | -2.809280 |
| 62 | 6 | 3.076979 | -3.798037 | -1.963534 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 63 | 1 | 2.927477 | -3.141317 | -2.826881 |
| 64 | 1 | -4.498344 | -2.089073 | -1.759085 |
| 65 | 1 | -2.126153 | 4.443623 | -1.819808 |
| 66 | 1 | 4.474397 | 2.104937 | -1.774125 |
| 67 | 1 | 2.170569 | -4.397790 | -1.833274 |
| 68 | 6 | -4.271879 | 4.734954 | -2.224243 |
| 69 | 8 | -5.211073 | 4.582498 | -1.381648 |
| 70 | 8 | -4.205438 | 5.495584 | -3.212999 |
| 71 | 6 | 4.767831 | 4.246050 | -2.199888 |
| 72 | 8 | 4.603669 | 5.194753 | -1.370327 |
| 73 | 8 | 5.541117 | 4.169179 | -3.178082 |
| 74 | 6 | 4.322506 | -4.720357 | -2.184668 |
| 75 | 8 | 4.268607 | -5.482836 | -3.172320 |
| 76 | 8 | 5.243612 | -4.576424 | -1.320894 |
| 77 | 6 | -4.817972 | -4.234053 | -2.149831 |
| 78 | 8 | -4.655517 | -5.170823 | -1.306398 |
| 79 | 8 | -5.598204 | -4.164669 | -3.122585 |
| 80 | 6 | 2.064063 | 4.256092 | 1.716428 |
| 81 | 1 | 3.082626 | 4.020678 | 2.035884 |
| 82 | 1 | 2.101324 | 5.111521 | 1.036518 |
| 83 | 1 | 1.491685 | 4.578970 | 2.588619 |
| 84 | 6 | -4.247321 | 2.074283 | 1.719527 |
| 85 | 1 | -4.012686 | 3.098398 | 2.021275 |
| 86 | 1 | -5.109356 | 2.098347 | 1.047378 |
| 87 | 1 | -4.559583 | 1.514111 | 2.603445 |
| 88 | 6 | -2.060395 | -4.236672 | 1.722261 |
| 89 | 1 | -3.075808 | -4.002624 | 2.052498 |
| 90 | 1 | -2.103490 | -5.091745 | 1.042241 |
| 91 | 1 | -1.478651 | -4.559448 | 2.588097 |
| 92 | 6 | 4.249212 | -2.053720 | 1.748615 |
| 93 | 1 | 4.010417 | -3.079034 | 2.042977 |
| 94 | 1 | 5.120358 | -2.075040 | 1.088229 |
| 95 | 1 | 4.549667 | -1.497455 | 2.638951 |
| 96 | 58 | 0.000838 | 0.015141 | 0.176751 |

E(RTPSSh) = -2543.4959883 Hartree

Zero-point correction = 0.780687 Hartree/particle

Sum of electronic and thermal Energies = -2542.661835 Hartree

Sum of electronic and thermal Enthalpies = -2542.660891 Hartree

Sum of electronic and thermal Free Energies = -2542.807008 Hartree

Table S48. [Pr(DOTMA-(gly)₄(H₂O)]⁺ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.071933 | -1.870342 | 1.902771 |
| 2 | 6 | -0.092654 | -2.204791 | 2.973695 |
| 3 | 6 | 1.350998 | -2.323848 | 2.490341 |
| 4 | 7 | 1.890567 | -1.060348 | 1.900694 |
| 5 | 6 | 2.214077 | -0.085861 | 2.979413 |
| 6 | 6 | 2.335355 | 1.359952 | 2.503058 |
| 7 | 7 | 1.075975 | 1.898238 | 1.903195 |
| 8 | 6 | 0.100425 | 2.235711 | 2.976043 |
| 9 | 6 | -1.344617 | 2.351441 | 2.496288 |
| 10 | 7 | -1.881520 | 1.087111 | 1.905679 |
| 11 | 6 | -2.208416 | 0.113673 | 2.983373 |
| 12 | 6 | -2.330113 | -1.331839 | 2.506155 |
| 13 | 6 | -1.382560 | -3.047935 | 1.024777 |
| 14 | 6 | -2.168911 | -2.509045 | -0.180434 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 15 | 8 | -1.908713 | -1.341588 | -0.616611 |
| 16 | 6 | 3.076902 | -1.360677 | 1.031302 |
| 17 | 6 | 2.552837 | -2.124542 | -0.193874 |
| 18 | 8 | 1.393014 | -1.852549 | -0.644124 |
| 19 | 6 | 1.383648 | 3.070447 | 1.018060 |
| 20 | 6 | 2.157727 | 2.520343 | -0.191399 |
| 21 | 8 | 1.901280 | 1.348065 | -0.611294 |
| 22 | 6 | -3.061743 | 1.386914 | 1.028475 |
| 23 | 6 | -2.524316 | 2.150515 | -0.192683 |
| 24 | 8 | -1.357299 | 1.888439 | -0.624486 |
| 25 | 1 | -0.167038 | -1.423442 | 3.732556 |
| 26 | 1 | -0.359202 | -3.139879 | 3.481231 |
| 27 | 1 | 1.426146 | -3.107526 | 1.731589 |
| 28 | 1 | 1.962679 | -2.647986 | 3.342563 |
| 29 | 1 | 1.425910 | -0.163734 | 3.730906 |
| 30 | 1 | 3.144897 | -0.353970 | 3.494167 |
| 31 | 1 | 3.127026 | 1.439858 | 1.753474 |
| 32 | 1 | 2.649062 | 1.969349 | 3.360818 |
| 33 | 1 | 0.177556 | 1.456890 | 3.737393 |
| 34 | 1 | 0.367628 | 3.173072 | 3.479402 |
| 35 | 1 | -1.423586 | 3.136124 | 1.739120 |
| 36 | 1 | -1.955800 | 2.672231 | 3.350157 |
| 37 | 1 | -1.422078 | 0.191185 | 3.736886 |
| 38 | 1 | -3.140651 | 0.381843 | 3.495794 |
| 39 | 1 | -3.123113 | -1.410720 | 1.757793 |
| 40 | 1 | -2.642177 | -1.942112 | 3.363809 |
| 41 | 1 | -0.422255 | -3.379119 | 0.609579 |
| 42 | 1 | 3.413896 | -0.394595 | 0.635462 |
| 43 | 1 | 0.421005 | 3.404310 | 0.610863 |
| 44 | 1 | -3.398130 | 0.420841 | 0.631981 |
| 45 | 8 | -0.049982 | -0.272696 | -2.373640 |
| 46 | 1 | 0.605229 | -0.984914 | -2.487603 |
| 47 | 1 | -0.912067 | -0.702321 | -2.515445 |
| 48 | 59 | 0.001450 | 0.016342 | 0.217832 |
| 49 | 7 | -3.297856 | 3.038795 | -0.780736 |
| 50 | 7 | 3.050029 | 3.288887 | -0.780194 |
| 51 | 7 | 3.324828 | -3.020721 | -0.769204 |
| 52 | 7 | -3.071372 | -3.277153 | -0.751682 |
| 53 | 1 | -4.238610 | 3.316932 | -0.457958 |
| 54 | 1 | 3.325201 | 4.232623 | -0.463784 |
| 55 | 1 | 4.259198 | -3.307719 | -0.434048 |
| 56 | 1 | -3.348035 | -4.217644 | -0.425042 |
| 57 | 6 | -3.867310 | -2.951958 | -1.928477 |
| 58 | 1 | -3.222763 | -2.778927 | -2.796408 |
| 59 | 6 | -2.977099 | 3.811202 | -1.974104 |
| 60 | 1 | -2.800206 | 3.148885 | -2.827756 |
| 61 | 6 | 3.835449 | 2.955899 | -1.961638 |
| 62 | 1 | 3.182784 | 2.771212 | -2.821042 |
| 63 | 6 | 3.010691 | -3.796925 | -1.962063 |
| 64 | 1 | 2.858946 | -3.138275 | -2.823419 |
| 65 | 1 | -4.455215 | -2.044376 | -1.758178 |
| 66 | 1 | -2.072152 | 4.406931 | -1.816951 |
| 67 | 1 | 4.428829 | 2.052224 | -1.788852 |
| 68 | 1 | 2.093966 | -4.376709 | -1.814641 |
| 69 | 6 | -4.200240 | 4.741478 | -2.249720 |
| 70 | 8 | -5.156365 | 4.629278 | -1.421697 |
| 71 | 8 | -4.102088 | 5.489275 | -3.248438 |
| 72 | 6 | 4.769877 | 4.175660 | -2.238700 |
| 73 | 8 | 4.650321 | 5.139231 | -1.420422 |
| 74 | 8 | 5.527942 | 4.067843 | -3.228650 |
| 75 | 6 | 4.224387 | -4.747430 | -2.210879 |
| 76 | 8 | 4.128512 | -5.505576 | -3.201637 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 77 | 8 | 5.171218 | -4.637169 | -1.372077 |
| 78 | 6 | -4.808373 | -4.171714 | -2.183798 |
| 79 | 8 | -4.681431 | -5.127725 | -1.357823 |
| 80 | 8 | -5.576907 | -4.070833 | -3.165994 |
| 81 | 6 | 2.067979 | 4.261176 | 1.704232 |
| 82 | 1 | 3.090425 | 4.028355 | 2.012816 |
| 83 | 1 | 2.094959 | 5.115856 | 1.022927 |
| 84 | 1 | 1.504786 | 4.583016 | 2.582599 |
| 85 | 6 | -4.247066 | 2.075686 | 1.719634 |
| 86 | 1 | -4.014000 | 3.102107 | 2.014445 |
| 87 | 1 | -5.108727 | 2.092933 | 1.046826 |
| 88 | 1 | -4.558243 | 1.521501 | 2.607544 |
| 89 | 6 | -2.055213 | -4.239278 | 1.721169 |
| 90 | 1 | -3.073838 | -4.007956 | 2.043165 |
| 91 | 1 | -2.089559 | -5.094457 | 1.040841 |
| 92 | 1 | -1.480040 | -4.559865 | 2.592063 |
| 93 | 6 | 4.258545 | -2.047448 | 1.730687 |
| 94 | 1 | 4.024156 | -3.072983 | 2.027602 |
| 95 | 1 | 5.123495 | -2.066505 | 1.062155 |
| 96 | 1 | 4.565517 | -1.490781 | 2.618400 |

E(RTPSSh) = -2544.1537075 Hartree

Zero-point correction = 0.781716 Hartree/particle

Sum of electronic and thermal Energies = -2543.318716 Hartree

Sum of electronic and thermal Enthalpies = -2543.317772 Hartree

Sum of electronic and thermal Free Energies = -2543.462370 Hartree

Table S49. [Nd(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.057838 | -1.873705 | 1.910346 |
| 2 | 6 | -0.079345 | -2.208310 | 2.981428 |
| 3 | 6 | 1.364594 | -2.317502 | 2.497996 |
| 4 | 7 | 1.892581 | -1.049094 | 1.908921 |
| 5 | 6 | 2.214572 | -0.076204 | 2.988941 |
| 6 | 6 | 2.326660 | 1.370285 | 2.513624 |
| 7 | 7 | 1.063041 | 1.897868 | 1.913355 |
| 8 | 6 | 0.088333 | 2.234531 | 2.986771 |
| 9 | 6 | -1.357029 | 2.340641 | 2.507045 |
| 10 | 7 | -1.882393 | 1.072083 | 1.915466 |
| 11 | 6 | -2.207535 | 0.098659 | 2.993161 |
| 12 | 6 | -2.320196 | -1.346855 | 2.514903 |
| 13 | 6 | -1.359438 | -3.048023 | 1.025248 |
| 14 | 6 | -2.143887 | -2.504875 | -0.178615 |
| 15 | 8 | -1.890883 | -1.330865 | -0.602013 |
| 16 | 6 | 3.076337 | -1.339137 | 1.033123 |
| 17 | 6 | 2.549026 | -2.099870 | -0.191972 |
| 18 | 8 | 1.381842 | -1.836681 | -0.629073 |
| 19 | 6 | 1.362159 | 3.067830 | 1.022565 |
| 20 | 6 | 2.134407 | 2.514451 | -0.185985 |
| 21 | 8 | 1.886670 | 1.335670 | -0.593206 |
| 22 | 6 | -3.060602 | 1.362974 | 1.032924 |
| 23 | 6 | -2.520460 | 2.124962 | -0.187415 |
| 24 | 8 | -1.347178 | 1.871540 | -0.607657 |
| 25 | 1 | -0.158659 | -1.430185 | 3.743126 |
| 26 | 1 | -0.342236 | -3.146784 | 3.484619 |
| 27 | 1 | 1.445217 | -3.100449 | 1.739070 |
| 28 | 1 | 1.979563 | -2.637192 | 3.349528 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 29 | 1 | 1.428205 | -0.159624 | 3.741776 |
| 30 | 1 | 3.147998 | -0.340933 | 3.500770 |
| 31 | 1 | 3.118354 | 1.456175 | 1.764734 |
| 32 | 1 | 2.635101 | 1.982251 | 3.371428 |
| 33 | 1 | 0.170644 | 1.458426 | 3.750387 |
| 34 | 1 | 0.351714 | 3.174969 | 3.486383 |
| 35 | 1 | -1.441539 | 3.125339 | 1.750491 |
| 36 | 1 | -1.971490 | 2.655989 | 3.360567 |
| 37 | 1 | -1.422930 | 0.180592 | 3.748049 |
| 38 | 1 | -3.142263 | 0.362775 | 3.503159 |
| 39 | 1 | -3.113327 | -1.430569 | 1.767202 |
| 40 | 1 | -2.627083 | -1.960822 | 3.371780 |
| 41 | 1 | -0.396237 | -3.371963 | 0.611292 |
| 42 | 1 | 3.406015 | -0.369709 | 0.639582 |
| 43 | 1 | 0.396762 | 3.395439 | 0.617093 |
| 44 | 1 | -3.390342 | 0.394142 | 0.637914 |
| 45 | 8 | -0.045372 | -0.244835 | -2.339299 |
| 46 | 1 | 0.608370 | -0.958199 | -2.455045 |
| 47 | 1 | -0.908094 | -0.672775 | -2.482604 |
| 48 | 7 | -3.297125 | 3.002899 | -0.786555 |
| 49 | 7 | 3.016235 | 3.285645 | -0.786677 |
| 50 | 7 | 3.324559 | -2.983955 | -0.780702 |
| 51 | 7 | -3.037324 | -3.274544 | -0.761413 |
| 52 | 1 | -4.243535 | 3.272996 | -0.473369 |
| 53 | 1 | 3.283485 | 4.235184 | -0.480696 |
| 54 | 1 | 4.264449 | -3.264329 | -0.455136 |
| 55 | 1 | -3.307830 | -4.220290 | -0.444519 |
| 56 | 6 | -3.830963 | -2.945814 | -1.938796 |
| 57 | 1 | -3.184395 | -2.760103 | -2.802564 |
| 58 | 6 | -2.975277 | 3.771103 | -1.982341 |
| 59 | 1 | -2.783043 | 3.105304 | -2.829916 |
| 60 | 6 | 3.797692 | 2.950670 | -1.970205 |
| 61 | 1 | 3.141627 | 2.750969 | -2.823622 |
| 62 | 6 | 3.008579 | -3.755357 | -1.976197 |
| 63 | 1 | 2.845386 | -3.092708 | -2.832395 |
| 64 | 1 | -4.427290 | -2.044782 | -1.763182 |
| 65 | 1 | -2.079103 | 4.378978 | -1.821485 |
| 66 | 1 | 4.402477 | 2.055430 | -1.793184 |
| 67 | 1 | 2.098005 | -4.343996 | -1.826045 |
| 68 | 6 | -4.207246 | 4.684613 | -2.274497 |
| 69 | 8 | -5.167985 | 4.567858 | -1.452444 |
| 70 | 8 | -4.110649 | 5.425236 | -3.278671 |
| 71 | 6 | 4.716420 | 4.178471 | -2.264062 |
| 72 | 8 | 4.591721 | 5.147403 | -1.452893 |
| 73 | 8 | 5.468915 | 4.070733 | -3.258229 |
| 74 | 6 | 4.228975 | -4.693479 | -2.239332 |
| 75 | 8 | 4.132921 | -5.446490 | -3.233939 |
| 76 | 8 | 5.180704 | -4.579503 | -1.406558 |
| 77 | 6 | -4.760570 | -4.171433 | -2.208134 |
| 78 | 8 | -4.629105 | -5.132827 | -1.389118 |
| 79 | 8 | -5.525715 | -4.069150 | -3.192777 |
| 80 | 6 | 2.043899 | 4.264457 | 1.700897 |
| 81 | 1 | 3.069358 | 4.038279 | 2.004298 |
| 82 | 1 | 2.062290 | 5.117000 | 1.016633 |
| 83 | 1 | 1.483894 | 4.586017 | 2.581412 |
| 84 | 6 | -4.252105 | 2.048372 | 1.716647 |
| 85 | 1 | -4.026205 | 3.077768 | 2.006541 |
| 86 | 1 | -5.111733 | 2.056781 | 1.041069 |
| 87 | 1 | -4.562620 | 1.497047 | 2.606586 |
| 88 | 6 | -2.029098 | -4.246424 | 1.712222 |
| 89 | 1 | -3.050985 | -4.022721 | 2.029182 |
| 90 | 1 | -2.054304 | -5.098676 | 1.027826 |

| | | | | |
|----|----|-----------|-----------|----------|
| 91 | 1 | -1.457087 | -4.567401 | 2.585059 |
| 92 | 6 | 4.264967 | -2.022977 | 1.723335 |
| 93 | 1 | 4.038565 | -3.052112 | 2.013846 |
| 94 | 1 | 5.127583 | -2.031562 | 1.051578 |
| 95 | 1 | 4.571272 | -1.470371 | 2.613827 |
| 96 | 60 | 0.002159 | 0.016846 | 0.240085 |

E (RTPSSh) = -2544.7764488 Hartree

Zero-point correction = 0.781819 Hartree/particle

Sum of electronic and thermal Energies = -2543.941424 Hartree

Sum of electronic and thermal Enthalpies = -2543.940480 Hartree

Sum of electronic and thermal Free Energies = -2544.084912 Hartree

Table S50. [Sm(DOTMA-(gly)₄(H₂O)]⁺ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.030977 | -1.881051 | 1.921819 |
| 2 | 6 | -0.054085 | -2.217618 | 2.992962 |
| 3 | 6 | 1.389959 | -2.308247 | 2.509087 |
| 4 | 7 | 1.896781 | -1.030603 | 1.922224 |
| 5 | 6 | 2.216497 | -0.061711 | 3.005631 |
| 6 | 6 | 2.311705 | 1.386150 | 2.533334 |
| 7 | 7 | 1.040565 | 1.895003 | 1.932940 |
| 8 | 6 | 0.067513 | 2.229650 | 3.007834 |
| 9 | 6 | -1.378053 | 2.318417 | 2.527926 |
| 10 | 7 | -1.882236 | 1.042805 | 1.933575 |
| 11 | 6 | -2.204310 | 0.068664 | 3.010737 |
| 12 | 6 | -2.300625 | -1.376005 | 2.529013 |
| 13 | 6 | -1.317806 | -3.049325 | 1.024627 |
| 14 | 6 | -2.097779 | -2.497565 | -0.176877 |
| 15 | 8 | -1.855327 | -1.312943 | -0.577537 |
| 16 | 6 | 3.076525 | -1.302986 | 1.036549 |
| 17 | 6 | 2.543558 | -2.055551 | -0.189900 |
| 18 | 8 | 1.363965 | -1.807069 | -0.603213 |
| 19 | 6 | 1.325404 | 3.062658 | 1.034893 |
| 20 | 6 | 2.092642 | 2.505256 | -0.173795 |
| 21 | 8 | 1.859945 | 1.315932 | -0.559355 |
| 22 | 6 | -3.057965 | 1.319618 | 1.043894 |
| 23 | 6 | -2.513602 | 2.078644 | -0.175075 |
| 24 | 8 | -1.330183 | 1.839363 | -0.575274 |
| 25 | 1 | -0.141969 | -1.446889 | 3.761270 |
| 26 | 1 | -0.310428 | -3.162974 | 3.486577 |
| 27 | 1 | 1.480564 | -3.088724 | 1.748737 |
| 28 | 1 | 2.011175 | -2.620756 | 3.358710 |
| 29 | 1 | 1.434056 | -0.155789 | 3.761423 |
| 30 | 1 | 3.154917 | -0.320773 | 3.511278 |
| 31 | 1 | 3.102844 | 1.483478 | 1.785250 |
| 32 | 1 | 2.610991 | 2.002141 | 3.391415 |
| 33 | 1 | 0.158920 | 1.458576 | 3.775589 |
| 34 | 1 | 0.323983 | 3.175451 | 3.500843 |
| 35 | 1 | -1.472678 | 3.103355 | 1.772774 |
| 36 | 1 | -1.998742 | 2.623321 | 3.380688 |
| 37 | 1 | -1.423223 | 0.157589 | 3.768557 |
| 38 | 1 | -3.143569 | 0.325188 | 3.516301 |
| 39 | 1 | -3.093594 | -1.467818 | 1.782027 |
| 40 | 1 | -2.598289 | -1.997755 | 3.383506 |
| 41 | 1 | -0.349965 | -3.362252 | 0.613795 |
| 42 | 1 | 3.396073 | -0.327881 | 0.649609 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 43 | 1 | 0.355386 | 3.381778 | 0.634482 |
| 44 | 1 | -3.378139 | 0.346716 | 0.651914 |
| 45 | 8 | -0.033095 | -0.192930 | -2.276261 |
| 46 | 1 | 0.617131 | -0.909175 | -2.394634 |
| 47 | 1 | -0.897256 | -0.616047 | -2.425202 |
| 48 | 7 | -3.294596 | 2.939190 | -0.793010 |
| 49 | 7 | 2.954769 | 3.281260 | -0.795974 |
| 50 | 7 | 3.324470 | -2.917065 | -0.803714 |
| 51 | 7 | -2.976739 | -3.267674 | -0.779974 |
| 52 | 1 | -4.250903 | 3.194274 | -0.497261 |
| 53 | 1 | 3.206899 | 4.240978 | -0.508938 |
| 54 | 1 | 4.273707 | -3.186342 | -0.495502 |
| 55 | 1 | -3.237897 | -4.221999 | -0.480575 |
| 56 | 6 | -3.765912 | -2.930977 | -1.958134 |
| 57 | 1 | -3.115762 | -2.724508 | -2.814431 |
| 58 | 6 | -2.971226 | 3.698550 | -1.994022 |
| 59 | 1 | -2.748768 | 3.026183 | -2.828816 |
| 60 | 6 | 3.726296 | 2.944180 | -1.985428 |
| 61 | 1 | 3.062625 | 2.715451 | -2.825505 |
| 62 | 6 | 3.005204 | -3.677907 | -2.005127 |
| 63 | 1 | 2.822269 | -3.007151 | -2.850991 |
| 64 | 1 | -4.374908 | -2.040350 | -1.773399 |
| 65 | 1 | -2.093060 | 4.330604 | -1.827106 |
| 66 | 1 | 4.354263 | 2.066192 | -1.802911 |
| 67 | 1 | 2.105531 | -4.282155 | -1.851752 |
| 68 | 6 | -4.220012 | 4.577714 | -2.318679 |
| 69 | 8 | -5.189366 | 4.451737 | -1.508113 |
| 70 | 8 | -4.126237 | 5.304250 | -3.333315 |
| 71 | 6 | 4.612131 | 4.187688 | -2.312631 |
| 72 | 8 | 4.477187 | 5.166429 | -1.514923 |
| 73 | 8 | 5.351956 | 4.081137 | -3.316342 |
| 74 | 6 | 4.236824 | -4.593575 | -2.294585 |
| 75 | 8 | 4.140656 | -5.335489 | -3.297394 |
| 76 | 8 | 5.196405 | -4.475055 | -1.471427 |
| 77 | 6 | -4.677695 | -4.164514 | -2.252022 |
| 78 | 8 | -4.538861 | -5.136096 | -1.446269 |
| 79 | 8 | -5.437509 | -4.057776 | -3.240218 |
| 80 | 6 | 2.005142 | 4.266939 | 1.701496 |
| 81 | 1 | 3.035742 | 4.050063 | 1.993859 |
| 82 | 1 | 2.009007 | 5.117206 | 1.014180 |
| 83 | 1 | 1.452355 | 4.586881 | 2.587188 |
| 84 | 6 | -4.258239 | 2.000509 | 1.716545 |
| 85 | 1 | -4.042975 | 3.034549 | 1.997688 |
| 86 | 1 | -5.115131 | 1.994932 | 1.037476 |
| 87 | 1 | -4.567153 | 1.454387 | 2.610303 |
| 88 | 6 | -1.984371 | -4.258722 | 1.694963 |
| 89 | 1 | -3.011493 | -4.046516 | 2.002657 |
| 90 | 1 | -1.994849 | -5.105688 | 1.003652 |
| 91 | 1 | -1.418715 | -4.581351 | 2.571352 |
| 92 | 6 | 4.274998 | -1.985351 | 1.710982 |
| 93 | 1 | 4.060219 | -3.020883 | 1.987042 |
| 94 | 1 | 5.134490 | -1.975406 | 1.035263 |
| 95 | 1 | 4.579658 | -1.442791 | 2.608232 |
| 96 | 62 | 0.004513 | 0.017584 | 0.277744 |

E(RTPSSh) = -2545.9989206 Hartree

Zero-point correction = 0.781851 Hartree/particle

Sum of electronic and thermal Energies = -2545.163921 Hartree

Sum of electronic and thermal Enthalpies = -2545.162977 Hartree

Sum of electronic and thermal Free Energies = -2545.307690 Hartree

Table S51. [Eu(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.007411 | -1.895922 | 1.929433 |
| 2 | 6 | -0.029610 | -2.233553 | 2.999084 |
| 3 | 6 | 1.414539 | -2.307948 | 2.514347 |
| 4 | 7 | 1.906367 | -1.021965 | 1.933855 |
| 5 | 6 | 2.220517 | -0.057483 | 3.022379 |
| 6 | 6 | 2.302706 | 1.392879 | 2.556392 |
| 7 | 7 | 1.026297 | 1.890902 | 1.958318 |
| 8 | 6 | 0.052733 | 2.217222 | 3.035132 |
| 9 | 6 | -1.393207 | 2.292977 | 2.555322 |
| 10 | 7 | -1.882095 | 1.014240 | 1.955385 |
| 11 | 6 | -2.198580 | 0.034320 | 3.028607 |
| 12 | 6 | -2.282120 | -1.408216 | 2.539421 |
| 13 | 6 | -1.282926 | -3.059736 | 1.023342 |
| 14 | 6 | -2.059417 | -2.503656 | -0.177791 |
| 15 | 8 | -1.828358 | -1.311012 | -0.561676 |
| 16 | 6 | 3.085926 | -1.277947 | 1.043705 |
| 17 | 6 | 2.554545 | -2.020130 | -0.189231 |
| 18 | 8 | 1.367425 | -1.784250 | -0.588753 |
| 19 | 6 | 1.300054 | 3.062432 | 1.062291 |
| 20 | 6 | 2.060713 | 2.511938 | -0.153185 |
| 21 | 8 | 1.845973 | 1.315649 | -0.527626 |
| 22 | 6 | -3.058404 | 1.282988 | 1.064452 |
| 23 | 6 | -2.516117 | 2.042806 | -0.154335 |
| 24 | 8 | -1.325136 | 1.820888 | -0.541958 |
| 25 | 1 | -0.124305 | -1.469800 | 3.773511 |
| 26 | 1 | -0.278938 | -3.185011 | 3.484493 |
| 27 | 1 | 1.512628 | -3.083446 | 1.749870 |
| 28 | 1 | 2.040100 | -2.618189 | 3.361585 |
| 29 | 1 | 1.439508 | -0.162044 | 3.778352 |
| 30 | 1 | 3.161768 | -0.312077 | 3.525095 |
| 31 | 1 | 3.092567 | 1.500736 | 1.808440 |
| 32 | 1 | 2.596025 | 2.008780 | 3.416543 |
| 33 | 1 | 0.151790 | 1.447026 | 3.802865 |
| 34 | 1 | 0.301769 | 3.165349 | 3.527482 |
| 35 | 1 | -1.495825 | 3.079878 | 1.803252 |
| 36 | 1 | -2.018081 | 2.587531 | 3.408665 |
| 37 | 1 | -1.419130 | 0.126209 | 3.787788 |
| 38 | 1 | -3.140634 | 0.281864 | 3.533476 |
| 39 | 1 | -3.074230 | -1.503665 | 1.791949 |
| 40 | 1 | -2.573507 | -2.038129 | 3.390094 |
| 41 | 1 | -0.311458 | -3.364897 | 0.615682 |
| 42 | 1 | 3.399392 | -0.297151 | 0.666824 |
| 43 | 1 | 0.326064 | 3.379321 | 0.670183 |
| 44 | 1 | -3.373283 | 0.308034 | 0.673732 |
| 45 | 8 | -0.026260 | -0.159074 | -2.240518 |
| 46 | 1 | 0.626408 | -0.871873 | -2.365935 |
| 47 | 1 | -0.889184 | -0.585230 | -2.388590 |
| 48 | 7 | -3.306019 | 2.885371 | -0.785464 |
| 49 | 7 | 2.897794 | 3.300625 | -0.793233 |
| 50 | 7 | 3.344256 | -2.859035 | -0.822606 |
| 51 | 7 | -2.923275 | -3.277361 | -0.797545 |
| 52 | 1 | -4.271574 | 3.121088 | -0.503819 |
| 53 | 1 | 3.128676 | 4.270090 | -0.521237 |
| 54 | 1 | 4.301162 | -3.115576 | -0.526950 |
| 55 | 1 | -3.174257 | -4.238762 | -0.511762 |
| 56 | 6 | -3.706858 | -2.938554 | -1.978877 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 57 | 1 | -3.052483 | -2.715181 | -2.827696 |
| 58 | 6 | -2.988766 | 3.634464 | -1.994525 |
| 59 | 1 | -2.732734 | 2.955512 | -2.814121 |
| 60 | 6 | 3.648282 | 2.975678 | -1.999404 |
| 61 | 1 | 2.970446 | 2.710200 | -2.816935 |
| 62 | 6 | 3.031174 | -3.603821 | -2.035682 |
| 63 | 1 | 2.826924 | -2.921613 | -2.867349 |
| 64 | 1 | -4.329188 | -2.058065 | -1.790300 |
| 65 | 1 | -2.133703 | 4.297130 | -1.826138 |
| 66 | 1 | 4.314254 | 2.124713 | -1.823509 |
| 67 | 1 | 2.146400 | -4.230730 | -1.886802 |
| 68 | 6 | -4.259476 | 4.468416 | -2.351772 |
| 69 | 8 | -5.234063 | 4.330207 | -1.549501 |
| 70 | 8 | -4.175516 | 5.175898 | -3.380642 |
| 71 | 6 | 4.477466 | 4.246474 | -2.367557 |
| 72 | 8 | 4.333877 | 5.228046 | -1.574821 |
| 73 | 8 | 5.186800 | 4.155749 | -3.394588 |
| 74 | 6 | 4.280171 | -4.486454 | -2.352385 |
| 75 | 8 | 4.192450 | -5.209909 | -3.369314 |
| 76 | 8 | 5.243207 | -4.363332 | -1.533907 |
| 77 | 6 | -4.599516 | -4.181214 | -2.292972 |
| 78 | 8 | -4.453437 | -5.159356 | -1.496455 |
| 79 | 8 | -5.354292 | -4.073653 | -3.284871 |
| 80 | 6 | 1.980752 | 4.267146 | 1.727564 |
| 81 | 1 | 3.016085 | 4.054674 | 2.005858 |
| 82 | 1 | 1.971365 | 5.121392 | 1.045294 |
| 83 | 1 | 1.436822 | 4.578627 | 2.621752 |
| 84 | 6 | -4.263031 | 1.959043 | 1.734449 |
| 85 | 1 | -4.054842 | 2.996069 | 2.009639 |
| 86 | 1 | -5.120451 | 1.943845 | 1.056223 |
| 87 | 1 | -4.567255 | 1.415422 | 2.631382 |
| 88 | 6 | -1.946950 | -4.277208 | 1.681683 |
| 89 | 1 | -2.978386 | -4.073899 | 1.980651 |
| 90 | 1 | -1.944780 | -5.120910 | 0.986328 |
| 91 | 1 | -1.387040 | -4.599701 | 2.561802 |
| 92 | 6 | 4.289405 | -1.961200 | 1.708507 |
| 93 | 1 | 4.082517 | -3.002455 | 1.968423 |
| 94 | 1 | 5.149302 | -1.934276 | 1.033798 |
| 95 | 1 | 4.588929 | -1.429921 | 2.614217 |
| 96 | 63 | 0.009644 | 0.016577 | 0.304796 |

E (RTPSSh) = -2546.5959563 Hartree

Zero-point correction = 0.781668 Hartree/particle

Sum of electronic and thermal Energies = -2545.761098 Hartree

Sum of electronic and thermal Enthalpies = -2545.760154 Hartree

Sum of electronic and thermal Free Energies = -2545.905674 Hartree

Table S52. [Gd(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 1.004271 | -1.898560 | -1.936043 |
| 2 | 6 | 0.028477 | -2.236341 | -3.007393 |
| 3 | 6 | -1.416892 | -2.303715 | -2.525066 |
| 4 | 7 | -1.903672 | -1.015602 | -1.943989 |
| 5 | 6 | -2.216976 | -0.050783 | -3.032452 |
| 6 | 6 | -2.293629 | 1.399742 | -2.565699 |
| 7 | 7 | -1.015827 | 1.892029 | -1.964858 |
| 8 | 6 | -0.041163 | 2.219586 | -3.040526 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 9 | 6 | 1.405041 | 2.288364 | -2.560096 |
| 10 | 7 | 1.888231 | 1.007269 | -1.959633 |
| 11 | 6 | 2.206050 | 0.027492 | -3.032681 |
| 12 | 6 | 2.282332 | -1.415708 | -2.543757 |
| 13 | 6 | 1.274439 | -3.060102 | -1.026343 |
| 14 | 6 | 2.043079 | -2.499470 | 0.177190 |
| 15 | 8 | 1.817125 | -1.301430 | 0.547263 |
| 16 | 6 | -3.081486 | -1.268617 | -1.051655 |
| 17 | 6 | -2.545624 | -2.006156 | 0.181697 |
| 18 | 8 | -1.352581 | -1.777694 | 0.567871 |
| 19 | 6 | -1.287234 | 3.060069 | -1.064460 |
| 20 | 6 | -2.045180 | 2.502188 | 0.148902 |
| 21 | 8 | -1.836361 | 1.300476 | 0.508615 |
| 22 | 6 | 3.060631 | 1.272373 | -1.063512 |
| 23 | 6 | 2.510109 | 2.027789 | 0.153813 |
| 24 | 8 | 1.313828 | 1.809769 | 0.526486 |
| 25 | 1 | 0.127788 | -1.475071 | -3.783776 |
| 26 | 1 | 0.275484 | -3.190347 | -3.489017 |
| 27 | 1 | -1.519933 | -3.079349 | -1.761408 |
| 28 | 1 | -2.042939 | -2.610129 | -3.373295 |
| 29 | 1 | -1.437023 | -0.157815 | -3.789248 |
| 30 | 1 | -3.159913 | -0.302559 | -3.533448 |
| 31 | 1 | -3.084362 | 1.510473 | -1.819133 |
| 32 | 1 | -2.582630 | 2.017715 | -3.425795 |
| 33 | 1 | -0.142744 | 1.452428 | -3.811045 |
| 34 | 1 | -0.286995 | 3.170564 | -3.528978 |
| 35 | 1 | 1.511006 | 3.074947 | -1.808201 |
| 36 | 1 | 2.031747 | 2.579872 | -3.413116 |
| 37 | 1 | 1.429536 | 0.122663 | -3.794560 |
| 38 | 1 | 3.151092 | 0.272182 | -3.533355 |
| 39 | 1 | 3.072622 | -1.514629 | -1.794835 |
| 40 | 1 | 2.572556 | -2.046883 | -3.393846 |
| 41 | 1 | 0.300749 | -3.364694 | -0.623968 |
| 42 | 1 | -3.394799 | -0.286894 | -0.677527 |
| 43 | 1 | -0.312592 | 3.375554 | -0.673284 |
| 44 | 1 | 3.374002 | 0.296272 | -0.674877 |
| 45 | 8 | 0.024108 | -0.141880 | 2.207017 |
| 46 | 1 | -0.625595 | -0.857842 | 2.330175 |
| 47 | 1 | 0.888840 | -0.566743 | 2.349089 |
| 48 | 7 | 3.297595 | 2.862701 | 0.798083 |
| 49 | 7 | -2.874197 | 3.289373 | 0.801221 |
| 50 | 7 | -3.336883 | -2.833206 | 0.828529 |
| 51 | 7 | 2.894669 | -3.273974 | 0.812609 |
| 52 | 1 | 4.267300 | 3.094602 | 0.527749 |
| 53 | 1 | -3.099246 | 4.263344 | 0.540690 |
| 54 | 1 | -4.299107 | -3.082371 | 0.543750 |
| 55 | 1 | 3.141748 | -4.239487 | 0.537110 |
| 56 | 6 | 3.669877 | -2.931333 | 1.998432 |
| 57 | 1 | 3.009551 | -2.700028 | 2.840556 |
| 58 | 6 | 2.971772 | 3.607790 | 2.007357 |
| 59 | 1 | 2.704226 | 2.926386 | 2.821233 |
| 60 | 6 | -3.621985 | 2.956999 | 2.007061 |
| 61 | 1 | -2.942682 | 2.678470 | 2.819025 |
| 62 | 6 | -3.021304 | -3.570442 | 2.045603 |
| 63 | 1 | -2.801722 | -2.883188 | 2.869145 |
| 64 | 1 | 4.298074 | -2.055065 | 1.809893 |
| 65 | 1 | 2.121777 | 4.275554 | 1.833566 |
| 66 | 1 | -4.294657 | 2.112583 | 1.825245 |
| 67 | 1 | -2.145475 | -4.209337 | 1.894821 |
| 68 | 6 | 4.243028 | 4.433638 | 2.381288 |
| 69 | 8 | 5.225028 | 4.293917 | 1.588361 |
| 70 | 8 | 4.152226 | 5.136883 | 3.412488 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 71 | 6 | -4.440690 | 4.229710 | 2.391848 |
| 72 | 8 | -4.292581 | 5.218812 | 1.609365 |
| 73 | 8 | -5.147325 | 4.132869 | 3.420184 |
| 74 | 6 | -4.277805 | -4.435106 | 2.381857 |
| 75 | 8 | -4.190560 | -5.147580 | 3.406521 |
| 76 | 8 | -5.245390 | -4.310613 | 1.568959 |
| 77 | 6 | 4.553404 | -4.176580 | 2.327934 |
| 78 | 8 | 4.406673 | -5.160021 | 1.538069 |
| 79 | 8 | 5.300827 | -4.066305 | 3.325047 |
| 80 | 6 | -1.970043 | 4.266827 | -1.723716 |
| 81 | 1 | -3.006168 | 4.055265 | -1.999705 |
| 82 | 1 | -1.958758 | 5.118912 | -1.038788 |
| 83 | 1 | -1.428464 | 4.580909 | -2.618479 |
| 84 | 6 | 4.267763 | 1.951297 | -1.725933 |
| 85 | 1 | 4.060645 | 2.989399 | -1.997798 |
| 86 | 1 | 5.122577 | 1.933452 | -1.044494 |
| 87 | 1 | 4.575148 | 1.411025 | -2.623862 |
| 88 | 6 | 1.943454 | -4.278538 | -1.677802 |
| 89 | 1 | 2.977496 | -4.076086 | -1.968108 |
| 90 | 1 | 1.934910 | -5.121674 | -0.981820 |
| 91 | 1 | 1.390650 | -4.601174 | -2.562388 |
| 92 | 6 | -4.285500 | -1.955245 | -1.712007 |
| 93 | 1 | -4.078967 | -2.997839 | -1.966697 |
| 94 | 1 | -5.145043 | -1.924796 | -1.037018 |
| 95 | 1 | -4.585220 | -1.428308 | -2.620243 |
| 96 | 64 | -0.008244 | 0.015899 | -0.333447 |

E(RTPSSh) = -2547.1861739 Hartree

Zero-point correction = 0.781926 Hartree/particle

Sum of electronic and thermal Energies = -2546.351198 Hartree

Sum of electronic and thermal Enthalpies = -2546.350253 Hartree

Sum of electronic and thermal Free Energies = -2546.495205 Hartree

Table S53. [Tb(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.987420 | -1.901001 | -1.939571 |
| 2 | 6 | 0.012399 | -2.239763 | -3.010797 |
| 3 | 6 | -1.431718 | -2.298918 | -2.527162 |
| 4 | 7 | -1.905882 | -1.006087 | -1.947920 |
| 5 | 6 | -2.217982 | -0.044537 | -3.039015 |
| 6 | 6 | -2.287099 | 1.406032 | -2.574414 |
| 7 | 7 | -1.005318 | 1.888103 | -1.975249 |
| 8 | 6 | -0.032439 | 2.213112 | -3.052775 |
| 9 | 6 | 1.412972 | 2.274178 | -2.572015 |
| 10 | 7 | 1.883785 | 0.990112 | -1.969454 |
| 11 | 6 | 2.199574 | 0.009616 | -3.041906 |
| 12 | 6 | 2.268794 | -1.431593 | -2.549313 |
| 13 | 6 | 1.250305 | -3.061185 | -1.025547 |
| 14 | 6 | 2.019733 | -2.499264 | 0.176125 |
| 15 | 8 | 1.798851 | -1.298113 | 0.539573 |
| 16 | 6 | -3.083388 | -1.249567 | -1.052173 |
| 17 | 6 | -2.547538 | -1.984485 | 0.182073 |
| 18 | 8 | -1.352049 | -1.759405 | 0.563387 |
| 19 | 6 | -1.268785 | 3.058060 | -1.074467 |
| 20 | 6 | -2.024071 | 2.503650 | 0.141489 |
| 21 | 8 | -1.822459 | 1.299291 | 0.496992 |
| 22 | 6 | 3.057430 | 1.248755 | -1.072453 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 23 | 6 | 2.509410 | 2.005055 | 0.144723 |
| 24 | 8 | 1.310515 | 1.794087 | 0.513663 |
| 25 | 1 | 0.114861 | -1.482318 | -3.790483 |
| 26 | 1 | 0.256758 | -3.196581 | -3.488104 |
| 27 | 1 | -1.538555 | -3.072536 | -1.761958 |
| 28 | 1 | -2.062010 | -2.602225 | -3.373320 |
| 29 | 1 | -1.440191 | -0.156920 | -3.797285 |
| 30 | 1 | -3.162960 | -0.294537 | -3.537028 |
| 31 | 1 | -3.076376 | 1.521984 | -1.827083 |
| 32 | 1 | -2.572714 | 2.025949 | -3.434184 |
| 33 | 1 | -0.138419 | 1.447856 | -3.824619 |
| 34 | 1 | -0.275318 | 3.165893 | -3.539139 |
| 35 | 1 | 1.523338 | 3.060869 | -1.820825 |
| 36 | 1 | 2.043526 | 2.559887 | -3.424109 |
| 37 | 1 | 1.424779 | 0.106989 | -3.805258 |
| 38 | 1 | 3.146266 | 0.250806 | -3.541111 |
| 39 | 1 | 3.058820 | -1.532880 | -1.800407 |
| 40 | 1 | 2.554050 | -2.068449 | -3.396801 |
| 41 | 1 | 0.274858 | -3.359888 | -0.623503 |
| 42 | 1 | -3.391352 | -0.265189 | -0.681122 |
| 43 | 1 | -0.291735 | 3.370411 | -0.687273 |
| 44 | 1 | 3.366571 | 0.271177 | -0.684665 |
| 45 | 8 | 0.021147 | -0.122149 | 2.188347 |
| 46 | 1 | -0.625862 | -0.838791 | 2.320046 |
| 47 | 1 | 0.887015 | -0.540964 | 2.339572 |
| 48 | 7 | 3.299859 | 2.833597 | 0.793159 |
| 49 | 7 | -2.843572 | 3.294765 | 0.800675 |
| 50 | 7 | -3.339603 | -2.805924 | 0.834671 |
| 51 | 7 | 2.867148 | -3.274043 | 0.816433 |
| 52 | 1 | 4.272857 | 3.057877 | 0.528121 |
| 53 | 1 | -3.061268 | 4.271925 | 0.545785 |
| 54 | 1 | -4.304585 | -3.050703 | 0.555204 |
| 55 | 1 | 3.109125 | -4.242574 | 0.546836 |
| 56 | 6 | 3.641609 | -2.929801 | 2.002258 |
| 57 | 1 | 2.980653 | -2.690162 | 2.841533 |
| 58 | 6 | 2.976408 | 3.574175 | 2.005846 |
| 59 | 1 | 2.695965 | 2.890274 | 2.813197 |
| 60 | 6 | -3.582632 | 2.965744 | 2.012813 |
| 61 | 1 | -2.898141 | 2.674014 | 2.815662 |
| 62 | 6 | -3.024359 | -3.537394 | 2.055285 |
| 63 | 1 | -2.794897 | -2.846329 | 2.872869 |
| 64 | 1 | 4.275554 | -2.058382 | 1.810671 |
| 65 | 1 | 2.135584 | 4.253492 | 1.832155 |
| 66 | 1 | -4.268202 | 2.131090 | 1.833999 |
| 67 | 1 | -2.154801 | -4.184859 | 1.904806 |
| 68 | 6 | 4.255596 | 4.381813 | 2.392287 |
| 69 | 8 | 5.239333 | 4.237275 | 1.602349 |
| 70 | 8 | 4.168540 | 5.077390 | 3.428987 |
| 71 | 6 | -4.380546 | 4.246937 | 2.412785 |
| 72 | 8 | -4.230273 | 5.237101 | 1.632019 |
| 73 | 8 | -5.074910 | 4.154973 | 3.449892 |
| 74 | 6 | -4.286701 | -4.388776 | 2.403442 |
| 75 | 8 | -4.201462 | -5.093515 | 3.433583 |
| 76 | 8 | -5.256319 | -4.262756 | 1.593167 |
| 77 | 6 | 4.516471 | -4.178889 | 2.340355 |
| 78 | 8 | 4.364130 | -5.166036 | 1.556162 |
| 79 | 8 | 5.263217 | -4.067756 | 3.337852 |
| 80 | 6 | -1.950177 | 4.267169 | -1.731070 |
| 81 | 1 | -2.988659 | 4.059819 | -2.001243 |
| 82 | 1 | -1.931654 | 5.119510 | -1.046628 |
| 83 | 1 | -1.412200 | 4.578656 | -2.628911 |
| 84 | 6 | 4.268124 | 1.923519 | -1.732727 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 85 | 1 | 4.066337 | 2.963308 | -2.002042 |
| 86 | 1 | 5.122277 | 1.899794 | -1.050644 |
| 87 | 1 | 4.573716 | 1.384057 | -2.631766 |
| 88 | 6 | 1.914973 | -4.285219 | -1.671000 |
| 89 | 1 | 2.950624 | -4.088951 | -1.959736 |
| 90 | 1 | 1.900779 | -5.125459 | -0.971621 |
| 91 | 1 | 1.362687 | -4.608892 | -2.555525 |
| 92 | 6 | -4.292291 | -1.933465 | -1.706445 |
| 93 | 1 | -4.091606 | -2.978236 | -1.956799 |
| 94 | 1 | -5.149838 | -1.895629 | -1.029293 |
| 95 | 1 | -4.591918 | -1.409340 | -2.616341 |
| 96 | 65 | -0.010325 | 0.016241 | -0.336397 |

E(RTPSSh) = -2547.7756483 Hartree

Zero-point correction = 0.781873 Hartree/particle

Sum of electronic and thermal Energies = -2546.940698 Hartree

Sum of electronic and thermal Enthalpies = -2546.939754 Hartree

Sum of electronic and thermal Free Energies = -2547.084962 Hartree

Table S54. [Dy(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.963223 | -1.918700 | -1.948641 |
| 2 | 6 | -0.011133 | -2.248593 | -3.023373 |
| 3 | 6 | -1.457079 | -2.282927 | -2.543986 |
| 4 | 7 | -1.909270 | -0.980935 | -1.966850 |
| 5 | 6 | -2.205140 | -0.016081 | -3.060096 |
| 6 | 6 | -2.256673 | 1.434394 | -2.593633 |
| 7 | 7 | -0.969152 | 1.896273 | -1.990466 |
| 8 | 6 | 0.008556 | 2.212677 | -3.066366 |
| 9 | 6 | 1.453378 | 2.248699 | -2.582140 |
| 10 | 7 | 1.898963 | 0.955716 | -1.978745 |
| 11 | 6 | 2.203596 | -0.028542 | -3.051140 |
| 12 | 6 | 2.253263 | -1.469345 | -2.555519 |
| 13 | 6 | 1.206970 | -3.079286 | -1.030183 |
| 14 | 6 | 1.973370 | -2.521204 | 0.174405 |
| 15 | 8 | 1.768579 | -1.313510 | 0.525546 |
| 16 | 6 | -3.092249 | -1.205130 | -1.073586 |
| 17 | 6 | -2.567206 | -1.936073 | 0.167249 |
| 18 | 8 | -1.364548 | -1.734617 | 0.539416 |
| 19 | 6 | -1.218208 | 3.068081 | -1.088310 |
| 20 | 6 | -1.973774 | 2.518928 | 0.129404 |
| 21 | 8 | -1.798854 | 1.306000 | 0.469208 |
| 22 | 6 | 3.073420 | 1.195453 | -1.077505 |
| 23 | 6 | 2.528770 | 1.953190 | 0.139551 |
| 24 | 8 | 1.322668 | 1.761919 | 0.495269 |
| 25 | 1 | 0.105892 | -1.496411 | -3.805603 |
| 26 | 1 | 0.221442 | -3.211207 | -3.494936 |
| 27 | 1 | -1.578469 | -3.053179 | -1.777659 |
| 28 | 1 | -2.091630 | -2.575650 | -3.390485 |
| 29 | 1 | -1.426242 | -0.138549 | -3.815855 |
| 30 | 1 | -3.151646 | -0.254738 | -3.560833 |
| 31 | 1 | -3.045748 | 1.559043 | -1.847641 |
| 32 | 1 | -2.530905 | 2.061050 | -3.452040 |
| 33 | 1 | -0.108018 | 1.454058 | -3.843079 |
| 34 | 1 | -0.220134 | 3.171938 | -3.546897 |
| 35 | 1 | 1.574821 | 3.032352 | -1.829582 |
| 36 | 1 | 2.092509 | 2.523429 | -3.431274 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 37 | 1 | 1.431117 | 0.078061 | -3.815531 |
| 38 | 1 | 3.153919 | 0.200832 | -3.549114 |
| 39 | 1 | 3.039291 | -1.579015 | -1.803696 |
| 40 | 1 | 2.531594 | -2.113106 | -3.399881 |
| 41 | 1 | 0.225636 | -3.367300 | -0.634970 |
| 42 | 1 | -3.392284 | -0.215168 | -0.711480 |
| 43 | 1 | -0.237115 | 3.372855 | -0.705827 |
| 44 | 1 | 3.370146 | 0.212977 | -0.692767 |
| 45 | 8 | 0.012785 | -0.106473 | 2.157081 |
| 46 | 1 | -0.640222 | -0.817656 | 2.287971 |
| 47 | 1 | 0.874732 | -0.532149 | 2.310740 |
| 48 | 66 | -0.009020 | 0.012938 | -0.362202 |
| 49 | 7 | 3.327739 | 2.763426 | 0.800420 |
| 50 | 7 | -2.767250 | 3.322497 | 0.805137 |
| 51 | 7 | -3.375324 | -2.729287 | 0.834753 |
| 52 | 7 | 2.801609 | -3.304236 | 0.829416 |
| 53 | 1 | 4.308703 | 2.967834 | 0.548865 |
| 54 | 1 | -2.960389 | 4.308490 | 0.565043 |
| 55 | 1 | -4.349931 | -2.948209 | 0.567406 |
| 56 | 1 | 3.024239 | -4.281761 | 0.575671 |
| 57 | 6 | 3.563212 | -2.965697 | 2.025199 |
| 58 | 1 | 2.894172 | -2.691472 | 2.847147 |
| 59 | 6 | 3.007333 | 3.500939 | 2.015846 |
| 60 | 1 | 2.700851 | 2.817029 | 2.813636 |
| 61 | 6 | -3.501125 | 2.999203 | 2.021973 |
| 62 | 1 | -2.816379 | 2.675760 | 2.812302 |
| 63 | 6 | -3.074968 | -3.445573 | 2.068069 |
| 64 | 1 | -2.810276 | -2.746319 | 2.867710 |
| 65 | 1 | 4.228922 | -2.118306 | 1.833077 |
| 66 | 1 | 2.185378 | 4.202070 | 1.838416 |
| 67 | 1 | -4.214078 | 2.188331 | 1.840426 |
| 68 | 1 | -2.232694 | -4.129523 | 1.923367 |
| 69 | 6 | 4.301256 | 4.273667 | 2.424096 |
| 70 | 8 | 5.290564 | 4.110426 | 1.644774 |
| 71 | 8 | 4.219057 | 4.963110 | 3.465229 |
| 72 | 6 | -4.255113 | 4.298406 | 2.448359 |
| 73 | 8 | -4.081331 | 5.294842 | 1.680490 |
| 74 | 8 | -4.942432 | 4.212662 | 3.490637 |
| 75 | 6 | -4.365032 | -4.240664 | 2.447223 |
| 76 | 8 | -4.298010 | -4.920299 | 3.495403 |
| 77 | 8 | -5.335232 | -4.100965 | 1.639852 |
| 78 | 6 | 4.391085 | -4.236358 | 2.399219 |
| 79 | 8 | 4.224417 | -5.229137 | 1.624962 |
| 80 | 8 | 5.119356 | -4.134337 | 3.411175 |
| 81 | 6 | -1.893601 | 4.282761 | -1.741708 |
| 82 | 1 | -2.935914 | 4.084566 | -2.003681 |
| 83 | 1 | -1.862333 | 5.135856 | -1.058708 |
| 84 | 1 | -1.359386 | 4.588248 | -2.643947 |
| 85 | 6 | 4.293836 | 1.859627 | -1.730838 |
| 86 | 1 | 4.104367 | 2.902494 | -1.997093 |
| 87 | 1 | 5.145013 | 1.824377 | -1.045537 |
| 88 | 1 | 4.597226 | 1.319945 | -2.630541 |
| 89 | 6 | 1.864935 | -4.311275 | -1.667561 |
| 90 | 1 | 2.904662 | -4.125593 | -1.948493 |
| 91 | 1 | 1.837337 | -5.149589 | -0.966265 |
| 92 | 1 | 1.316375 | -4.631848 | -2.555588 |
| 93 | 6 | -4.305519 | -1.883013 | -1.726702 |
| 94 | 1 | -4.115011 | -2.932502 | -1.964813 |
| 95 | 1 | -5.165899 | -1.828852 | -1.054300 |
| 96 | 1 | -4.595201 | -1.365223 | -2.643507 |

E (RTPSSh) = -2548.3617554 Hartree

Zero-point correction = 0.781867 Hartree/particle
 Sum of electronic and thermal Energies = -2547.526848 Hartree
 Sum of electronic and thermal Enthalpies = -2547.525903 Hartree
 Sum of electronic and thermal Free Energies = -2547.670990 Hartree

Table S55. [Ho(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.982834 | -1.896760 | -1.945957 |
| 2 | 6 | 0.012559 | -2.240717 | -3.019174 |
| 3 | 6 | -1.431155 | -2.296584 | -2.536809 |
| 4 | 7 | -1.898352 | -1.001796 | -1.956728 |
| 5 | 6 | -2.215245 | -0.043441 | -3.048646 |
| 6 | 6 | -2.281281 | 1.406167 | -2.583343 |
| 7 | 7 | -0.997465 | 1.880931 | -1.982983 |
| 8 | 6 | -0.027722 | 2.210730 | -3.061343 |
| 9 | 6 | 1.416758 | 2.268607 | -2.580080 |
| 10 | 7 | 1.880032 | 0.982674 | -1.976034 |
| 11 | 6 | 2.201576 | 0.005068 | -3.048828 |
| 12 | 6 | 2.267059 | -1.435062 | -2.555116 |
| 13 | 6 | 1.242045 | -3.052010 | -1.025256 |
| 14 | 6 | 2.004615 | -2.479047 | 0.174383 |
| 15 | 8 | 1.784089 | -1.272362 | 0.520060 |
| 16 | 6 | -3.071367 | -1.243627 | -1.055438 |
| 17 | 6 | -2.524414 | -1.971957 | 0.176795 |
| 18 | 8 | -1.323174 | -1.747843 | 0.541156 |
| 19 | 6 | -1.258871 | 3.046356 | -1.076141 |
| 20 | 6 | -2.008952 | 2.480586 | 0.136804 |
| 21 | 8 | -1.808430 | 1.271006 | 0.474908 |
| 22 | 6 | 3.048501 | 1.239653 | -1.072374 |
| 23 | 6 | 2.488090 | 1.990450 | 0.141493 |
| 24 | 8 | 1.283761 | 1.779706 | 0.492607 |
| 25 | 1 | 0.116910 | -1.486329 | -3.801625 |
| 26 | 1 | 0.258676 | -3.199637 | -3.491379 |
| 27 | 1 | -1.540534 | -3.070543 | -1.772346 |
| 28 | 1 | -2.063462 | -2.596465 | -3.382593 |
| 29 | 1 | -1.440164 | -0.156693 | -3.809625 |
| 30 | 1 | -3.162317 | -0.294437 | -3.542214 |
| 31 | 1 | -3.070701 | 1.523488 | -1.836429 |
| 32 | 1 | -2.563788 | 2.029064 | -3.441894 |
| 33 | 1 | -0.134621 | 1.448217 | -3.835833 |
| 34 | 1 | -0.271695 | 3.165509 | -3.543230 |
| 35 | 1 | 1.528694 | 3.055664 | -1.829555 |
| 36 | 1 | 2.050231 | 2.550873 | -3.431068 |
| 37 | 1 | 1.430238 | 0.103111 | -3.815643 |
| 38 | 1 | 3.150822 | 0.247157 | -3.542745 |
| 39 | 1 | 3.056214 | -1.537585 | -1.805509 |
| 40 | 1 | 2.550324 | -2.075172 | -3.400734 |
| 41 | 1 | 0.265580 | -3.349650 | -0.625606 |
| 42 | 1 | -3.380046 | -0.259054 | -0.686286 |
| 43 | 1 | -0.281497 | 3.358206 | -0.690163 |
| 44 | 1 | 3.357434 | 0.261886 | -0.685687 |
| 45 | 8 | 0.020443 | -0.097553 | 2.150583 |
| 46 | 1 | -0.617726 | -0.821390 | 2.285346 |
| 47 | 1 | 0.891173 | -0.506419 | 2.300914 |
| 48 | 7 | 3.270636 | 2.814924 | 0.804193 |
| 49 | 7 | -2.823986 | 3.264446 | 0.809713 |
| 50 | 7 | -3.310210 | -2.787127 | 0.844178 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 51 | 7 | 2.846346 | -3.246895 | 0.829865 |
| 52 | 1 | 4.247711 | 3.038248 | 0.553470 |
| 53 | 1 | -3.040368 | 4.245383 | 0.568395 |
| 54 | 1 | -4.279634 | -3.030152 | 0.578337 |
| 55 | 1 | 3.087501 | -4.219551 | 0.574173 |
| 56 | 6 | 3.615599 | -2.890042 | 2.015456 |
| 57 | 1 | 2.951108 | -2.639775 | 2.848794 |
| 58 | 6 | 2.932657 | 3.551279 | 2.015564 |
| 59 | 1 | 2.640433 | 2.864729 | 2.816441 |
| 60 | 6 | -3.559621 | 2.921687 | 2.020186 |
| 61 | 1 | -2.873031 | 2.618960 | 2.817120 |
| 62 | 6 | -2.983793 | -3.511264 | 2.066284 |
| 63 | 1 | -2.741104 | -2.815468 | 2.875958 |
| 64 | 1 | 4.252197 | -2.022175 | 1.816901 |
| 65 | 1 | 2.095562 | 4.232994 | 1.833606 |
| 66 | 1 | -4.247296 | 2.090566 | 1.833325 |
| 67 | 1 | -2.119610 | -4.164540 | 1.910207 |
| 68 | 6 | 4.208483 | 4.354647 | 2.421789 |
| 69 | 8 | 5.202366 | 4.210163 | 1.644599 |
| 70 | 8 | 4.109234 | 5.046886 | 3.459601 |
| 71 | 6 | -4.353765 | 4.199433 | 2.438496 |
| 72 | 8 | -4.202807 | 5.199291 | 1.670286 |
| 73 | 8 | -5.045880 | 4.095620 | 3.475963 |
| 74 | 6 | -4.246608 | -4.353162 | 2.435749 |
| 75 | 8 | -4.153703 | -5.049211 | 3.471057 |
| 76 | 8 | -5.224274 | -4.228998 | 1.634869 |
| 77 | 6 | 4.486019 | -4.137127 | 2.372375 |
| 78 | 8 | 4.333826 | -5.133494 | 1.599855 |
| 79 | 8 | 5.228998 | -4.015608 | 3.371402 |
| 80 | 6 | -1.945138 | 4.257587 | -1.723513 |
| 81 | 1 | -2.984089 | 4.049933 | -1.991592 |
| 82 | 1 | -1.926132 | 5.105917 | -1.034113 |
| 83 | 1 | -1.410422 | 4.575165 | -2.621207 |
| 84 | 6 | 4.261484 | 1.919846 | -1.722652 |
| 85 | 1 | 4.059146 | 2.960112 | -1.989656 |
| 86 | 1 | 5.111341 | 1.895747 | -1.035230 |
| 87 | 1 | 4.573744 | 1.383965 | -2.621574 |
| 88 | 6 | 1.912251 | -4.278561 | -1.659964 |
| 89 | 1 | 2.948999 | -4.082372 | -1.944739 |
| 90 | 1 | 1.896013 | -5.114608 | -0.955617 |
| 91 | 1 | 1.364678 | -4.608276 | -2.545215 |
| 92 | 6 | -4.281574 | -1.933883 | -1.700501 |
| 93 | 1 | -4.079649 | -2.979317 | -1.947022 |
| 94 | 1 | -5.135898 | -1.895059 | -1.019346 |
| 95 | 1 | -4.586673 | -1.414460 | -2.611311 |
| 96 | 67 | -0.009968 | 0.016223 | -0.358846 |

E(RTPSSh) = -2548.9457093 Hartree

Zero-point correction = 0.782121 Hartree/particle

Sum of electronic and thermal Energies = -2548.110619 Hartree

Sum of electronic and thermal Enthalpies = -2548.109675 Hartree

Sum of electronic and thermal Free Energies = -2548.254636 Hartree

Table S56. [Tm(DOTMA-(gly)₄(H₂O)]⁺ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.921450 | -1.915423 | -1.961735 |
| 2 | 6 | -0.055751 | -2.236628 | -3.035756 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 3 | 6 | -1.499120 | -2.246174 | -2.552251 |
| 4 | 7 | -1.919367 | -0.937130 | -1.968567 |
| 5 | 6 | -2.216536 | 0.029729 | -3.058761 |
| 6 | 6 | -2.236805 | 1.478219 | -2.588859 |
| 7 | 7 | -0.937056 | 1.906884 | -1.988752 |
| 8 | 6 | 0.037964 | 2.217055 | -3.068497 |
| 9 | 6 | 1.483118 | 2.227689 | -2.588527 |
| 10 | 7 | 1.902277 | 0.925477 | -1.987579 |
| 11 | 6 | 2.200120 | -0.056489 | -3.063456 |
| 12 | 6 | 2.220395 | -1.497437 | -2.570866 |
| 13 | 6 | 1.146615 | -3.075486 | -1.038023 |
| 14 | 6 | 1.915280 | -2.515942 | 0.162982 |
| 15 | 8 | 1.734906 | -1.297393 | 0.489722 |
| 16 | 6 | -3.094539 | -1.145727 | -1.061396 |
| 17 | 6 | -2.556417 | -1.884074 | 0.167733 |
| 18 | 8 | -1.342613 | -1.699013 | 0.512141 |
| 19 | 6 | -1.162274 | 3.074637 | -1.074776 |
| 20 | 6 | -1.917904 | 2.518129 | 0.138055 |
| 21 | 8 | -1.756620 | 1.296959 | 0.454052 |
| 22 | 6 | 3.075819 | 1.145385 | -1.080638 |
| 23 | 6 | 2.528460 | 1.899913 | 0.135782 |
| 24 | 8 | 1.313062 | 1.727485 | 0.468591 |
| 25 | 1 | 0.071428 | -1.489482 | -3.821935 |
| 26 | 1 | 0.163004 | -3.204823 | -3.502384 |
| 27 | 1 | -1.632812 | -3.017139 | -1.788586 |
| 28 | 1 | -2.143839 | -2.522501 | -3.396561 |
| 29 | 1 | -1.450549 | -0.105007 | -3.825607 |
| 30 | 1 | -3.174031 | -0.193979 | -3.545123 |
| 31 | 1 | -3.020187 | 1.616967 | -1.839278 |
| 32 | 1 | -2.500352 | 2.114697 | -3.443333 |
| 33 | 1 | -0.093346 | 1.464290 | -3.848901 |
| 34 | 1 | -0.179708 | 3.182514 | -3.541450 |
| 35 | 1 | 1.620240 | 3.008279 | -1.835434 |
| 36 | 1 | 2.126558 | 2.490820 | -3.438001 |
| 37 | 1 | 1.435121 | 0.066299 | -3.833275 |
| 38 | 1 | 3.158263 | 0.159880 | -3.551981 |
| 39 | 1 | 3.005040 | -1.624446 | -1.820270 |
| 40 | 1 | 2.482699 | -2.147883 | -3.415186 |
| 41 | 1 | 0.161340 | -3.350023 | -0.644288 |
| 42 | 1 | -3.377515 | -0.153085 | -0.694071 |
| 43 | 1 | -0.175169 | 3.361227 | -0.694907 |
| 44 | 1 | 3.360954 | 0.157583 | -0.702105 |
| 45 | 8 | 0.019206 | -0.078550 | 2.111548 |
| 46 | 1 | -0.626046 | -0.795822 | 2.246731 |
| 47 | 1 | 0.885129 | -0.496845 | 2.262322 |
| 48 | 7 | 3.330033 | 2.689096 | 0.818310 |
| 49 | 7 | -2.698535 | 3.318492 | 0.831904 |
| 50 | 7 | -3.358617 | -2.668741 | 0.851692 |
| 51 | 7 | 2.721988 | -3.303817 | 0.838315 |
| 52 | 1 | 4.316977 | 2.882395 | 0.582102 |
| 53 | 1 | -2.884853 | 4.309394 | 0.607237 |
| 54 | 1 | -4.340106 | -2.879246 | 0.602859 |
| 55 | 1 | 2.927941 | -4.289179 | 0.601466 |
| 56 | 6 | 3.487159 | -2.958136 | 2.029864 |
| 57 | 1 | 2.820717 | -2.665554 | 2.847668 |
| 58 | 6 | 3.000635 | 3.423091 | 2.033500 |
| 59 | 1 | 2.677558 | 2.737653 | 2.823387 |
| 60 | 6 | -3.435359 | 2.980366 | 2.042982 |
| 61 | 1 | -2.752305 | 2.646274 | 2.830342 |
| 62 | 6 | -3.038106 | -3.396482 | 2.073279 |
| 63 | 1 | -2.758157 | -2.704759 | 2.874348 |
| 64 | 1 | 4.162519 | -2.121161 | 1.826948 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 65 | 1 | 2.187347 | 4.132419 | 1.849163 |
| 66 | 1 | -4.148495 | 2.172511 | 1.849666 |
| 67 | 1 | -2.200126 | -4.080829 | 1.907895 |
| 68 | 6 | 4.295735 | 4.181838 | 2.463648 |
| 69 | 8 | 5.294765 | 4.013015 | 1.698109 |
| 70 | 8 | 4.204861 | 4.866998 | 3.506967 |
| 71 | 6 | -4.188350 | 4.274696 | 2.485557 |
| 72 | 8 | -4.011966 | 5.281373 | 1.731869 |
| 73 | 8 | -4.877113 | 4.175639 | 3.525767 |
| 74 | 6 | -4.323689 | -4.190923 | 2.468599 |
| 75 | 8 | -4.237986 | -4.884730 | 3.506024 |
| 76 | 8 | -5.309900 | -4.035528 | 1.683882 |
| 77 | 6 | 4.299146 | -4.233477 | 2.422574 |
| 78 | 8 | 4.116750 | -5.236893 | 1.665941 |
| 79 | 8 | 5.031541 | -4.124256 | 3.430816 |
| 80 | 6 | -1.825061 | 4.305216 | -1.710204 |
| 81 | 1 | -2.871292 | 4.124222 | -1.968802 |
| 82 | 1 | -1.778759 | 5.149341 | -1.016942 |
| 83 | 1 | -1.291557 | 4.614129 | -2.611695 |
| 84 | 6 | 4.305976 | 1.802799 | -1.722229 |
| 85 | 1 | 4.129330 | 2.850317 | -1.978569 |
| 86 | 1 | 5.153542 | 1.751169 | -1.033493 |
| 87 | 1 | 4.607085 | 1.268834 | -2.626168 |
| 88 | 6 | 1.793747 | -4.318367 | -1.665184 |
| 89 | 1 | 2.837704 | -4.147181 | -1.939165 |
| 90 | 1 | 1.750491 | -5.152873 | -0.960155 |
| 91 | 1 | 1.247633 | -4.636056 | -2.555784 |
| 92 | 6 | -4.324557 | -1.809187 | -1.697117 |
| 93 | 1 | -4.149428 | -2.860202 | -1.939984 |
| 94 | 1 | -5.173728 | -1.746815 | -1.011277 |
| 95 | 1 | -4.622308 | -1.286319 | -2.608463 |
| 96 | 69 | -0.008761 | 0.018839 | -0.389646 |

E(RTPSSh) = -2550.108215 Hartree

Zero-point correction = 0.782127 Hartree/particle

Sum of electronic and thermal Energies = -2549.273182 Hartree

Sum of electronic and thermal Enthalpies = -2549.272238 Hartree

Sum of electronic and thermal Free Energies = -2549.416688 Hartree

Table S57. [Yb(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.743136 | -1.973706 | -1.955866 |
| 2 | 6 | -0.256741 | -2.209884 | -3.029996 |
| 3 | 6 | -1.693306 | -2.098844 | -2.540867 |
| 4 | 7 | -1.990397 | -0.758514 | -1.953083 |
| 5 | 6 | -2.212566 | 0.228227 | -3.042882 |
| 6 | 6 | -2.106508 | 1.671291 | -2.570595 |
| 7 | 7 | -0.770019 | 1.976001 | -1.976899 |
| 8 | 6 | 0.218945 | 2.203040 | -3.063320 |
| 9 | 6 | 1.660384 | 2.091849 | -2.587878 |
| 10 | 7 | 1.960328 | 0.757394 | -1.987987 |
| 11 | 6 | 2.175175 | -0.243466 | -3.065060 |
| 12 | 6 | 2.073573 | -1.678548 | -2.567593 |
| 13 | 6 | 0.865148 | -3.147164 | -1.027967 |
| 14 | 6 | 1.685936 | -2.653190 | 0.167154 |
| 15 | 8 | 1.611927 | -1.421191 | 0.488699 |
| 16 | 6 | -3.173868 | -0.865461 | -1.036460 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 17 | 6 | -2.691861 | -1.658068 | 0.181820 |
| 18 | 8 | -1.463354 | -1.575258 | 0.517661 |
| 19 | 6 | -0.885125 | 3.155311 | -1.054986 |
| 20 | 6 | -1.690093 | 2.660985 | 0.153312 |
| 21 | 8 | -1.641935 | 1.426123 | 0.455595 |
| 22 | 6 | 3.148713 | 0.873744 | -1.079044 |
| 23 | 6 | 2.666650 | 1.675207 | 0.134882 |
| 24 | 8 | 1.438768 | 1.609095 | 0.462547 |
| 25 | 1 | -0.072511 | -1.470809 | -3.812947 |
| 26 | 1 | -0.117709 | -3.190279 | -3.502322 |
| 27 | 1 | -1.888003 | -2.857207 | -1.777468 |
| 28 | 1 | -2.365554 | -2.313651 | -3.381398 |
| 29 | 1 | -1.463588 | 0.034497 | -3.814245 |
| 30 | 1 | -3.187285 | 0.083437 | -3.525271 |
| 31 | 1 | -2.870759 | 1.874510 | -1.815969 |
| 32 | 1 | -2.314202 | 2.333180 | -3.420982 |
| 33 | 1 | 0.025015 | 1.460461 | -3.840925 |
| 34 | 1 | 0.077478 | 3.181464 | -3.539111 |
| 35 | 1 | 1.864092 | 2.857344 | -1.834204 |
| 36 | 1 | 2.324951 | 2.295609 | -3.437177 |
| 37 | 1 | 1.421585 | -0.062124 | -3.835244 |
| 38 | 1 | 3.147125 | -0.106455 | -3.555476 |
| 39 | 1 | 2.844722 | -1.868527 | -1.816062 |
| 40 | 1 | 2.274212 | -2.355219 | -3.407970 |
| 41 | 1 | -0.140085 | -3.329935 | -0.630453 |
| 42 | 1 | -3.363015 | 0.146787 | -0.661255 |
| 43 | 1 | 0.124689 | 3.346587 | -0.674029 |
| 44 | 1 | 3.346003 | -0.135516 | -0.700391 |
| 45 | 8 | 0.014148 | -0.061437 | 2.115863 |
| 46 | 1 | -0.681808 | -0.727866 | 2.258660 |
| 47 | 1 | 0.847292 | -0.538832 | 2.274178 |
| 48 | 7 | 3.531206 | 2.393961 | 0.815918 |
| 49 | 7 | -2.395712 | 3.523051 | 0.851213 |
| 50 | 7 | -3.549439 | -2.384074 | 0.860752 |
| 51 | 7 | 2.425900 | -3.504297 | 0.839730 |
| 52 | 1 | 4.537120 | 2.508192 | 0.589926 |
| 53 | 1 | -2.501345 | 4.532929 | 0.639769 |
| 54 | 1 | -4.551123 | -2.523495 | 0.623463 |
| 55 | 1 | 2.557735 | -4.509106 | 0.612110 |
| 56 | 6 | 3.232148 | -3.226090 | 2.022290 |
| 57 | 1 | 2.603438 | -2.883939 | 2.850765 |
| 58 | 6 | 3.270240 | 3.164598 | 2.025477 |
| 59 | 1 | 2.895144 | 2.517166 | 2.824463 |
| 60 | 6 | -3.173439 | 3.250031 | 2.053526 |
| 61 | 1 | -2.531512 | 2.863267 | 2.851393 |
| 62 | 6 | -3.284420 | -3.164442 | 2.063480 |
| 63 | 1 | -2.958646 | -2.516809 | 2.884011 |
| 64 | 1 | 3.972088 | -2.447124 | 1.813442 |
| 65 | 1 | 2.519531 | 3.939157 | 1.838306 |
| 66 | 1 | -3.949636 | 2.504443 | 1.853169 |
| 67 | 1 | -2.498067 | -3.903576 | 1.881397 |
| 68 | 6 | 4.635257 | 3.811382 | 2.434468 |
| 69 | 8 | 5.604512 | 3.531466 | 1.661707 |
| 70 | 8 | 4.615470 | 4.521696 | 3.461947 |
| 71 | 6 | -3.817545 | 4.612234 | 2.476153 |
| 72 | 8 | -3.527539 | 5.590733 | 1.718979 |
| 73 | 8 | -4.535909 | 4.581546 | 3.497803 |
| 74 | 6 | -4.633499 | -3.870728 | 2.427949 |
| 75 | 8 | -4.607658 | -4.608561 | 3.435001 |
| 76 | 8 | -5.596745 | -3.600616 | 1.644221 |
| 77 | 6 | 3.938555 | -4.573531 | 2.392306 |
| 78 | 8 | 3.650842 | -5.545806 | 1.626180 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 79 | 8 | 4.694162 | -4.537748 | 3.385833 |
| 80 | 6 | -1.432970 | 4.445367 | -1.681748 |
| 81 | 1 | -2.489758 | 4.360168 | -1.947246 |
| 82 | 1 | -1.318245 | 5.274056 | -0.977740 |
| 83 | 1 | -0.869223 | 4.718064 | -2.576804 |
| 84 | 6 | 4.432174 | 1.422332 | -1.718785 |
| 85 | 1 | 4.346064 | 2.480446 | -1.978539 |
| 86 | 1 | 5.268733 | 1.302969 | -1.024890 |
| 87 | 1 | 4.693328 | 0.862427 | -2.619755 |
| 88 | 6 | 1.396344 | -4.445276 | -1.652075 |
| 89 | 1 | 2.448801 | -4.367308 | -1.936521 |
| 90 | 1 | 1.289652 | -5.266800 | -0.938445 |
| 91 | 1 | 0.816442 | -4.723630 | -2.534780 |
| 92 | 6 | -4.462904 | -1.413661 | -1.664694 |
| 93 | 1 | -4.381346 | -2.472928 | -1.921481 |
| 94 | 1 | -5.294342 | -1.289161 | -0.965583 |
| 95 | 1 | -4.728637 | -0.856387 | -2.565744 |
| 96 | 70 | -0.010768 | 0.023529 | -0.370722 |

E(RTPSSh) = -2550.6691996 Hartree

Zero-point correction = 0.781801 Hartree/particle

Sum of electronic and thermal Energies = -2549.834625 Hartree

Sum of electronic and thermal Enthalpies = -2549.833681 Hartree

Sum of electronic and thermal Free Energies = -2549.977647 Hartree

Table S58. [Lu(DOTMA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -0.722692 | 1.977754 | -1.959643 |
| 2 | 6 | 0.278238 | 2.205533 | -3.034352 |
| 3 | 6 | 1.713074 | 2.079627 | -2.544781 |
| 4 | 7 | 1.994788 | 0.736274 | -1.956402 |
| 5 | 6 | 2.209767 | -0.252298 | -3.045790 |
| 6 | 6 | 2.087932 | -1.693336 | -2.572107 |
| 7 | 7 | 0.747865 | -1.981801 | -1.978349 |
| 8 | 6 | -0.242143 | -2.201917 | -3.065045 |
| 9 | 6 | -1.681934 | -2.075181 | -2.589544 |
| 10 | 7 | -1.966202 | -0.737002 | -1.990438 |
| 11 | 6 | -2.173681 | 0.264420 | -3.068142 |
| 12 | 6 | -2.056699 | 1.697964 | -2.570629 |
| 13 | 6 | -0.832494 | 3.151028 | -1.030332 |
| 14 | 6 | -1.654630 | 2.661260 | 0.165127 |
| 15 | 8 | -1.593228 | 1.426771 | 0.480463 |
| 16 | 6 | 3.177468 | 0.832338 | -1.037842 |
| 17 | 6 | 2.698337 | 1.627756 | 0.179332 |
| 18 | 8 | 1.467066 | 1.557591 | 0.508492 |
| 19 | 6 | 0.851080 | -3.159747 | -1.053402 |
| 20 | 6 | 1.659556 | -2.667918 | 0.153183 |
| 21 | 8 | 1.623614 | -1.430843 | 0.448347 |
| 22 | 6 | -3.153654 | -0.840849 | -1.079016 |
| 23 | 6 | -2.674608 | -1.645002 | 0.133876 |
| 24 | 8 | -1.444239 | -1.591271 | 0.454635 |
| 25 | 1 | 0.086910 | 1.469038 | -3.818010 |
| 26 | 1 | 0.148541 | 3.187868 | -3.505332 |
| 27 | 1 | 1.915013 | 2.835903 | -1.781221 |
| 28 | 1 | 2.388533 | 2.286843 | -3.384582 |
| 29 | 1 | 1.464481 | -0.051758 | -3.818949 |
| 30 | 1 | 3.187101 | -0.117381 | -3.525764 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 31 | 1 | 2.849548 | -1.903735 | -1.816829 |
| 32 | 1 | 2.288263 | -2.359000 | -3.421255 |
| 33 | 1 | -0.041007 | -1.462796 | -3.844061 |
| 34 | 1 | -0.109859 | -3.182810 | -3.538399 |
| 35 | 1 | -1.893359 | -2.837824 | -1.835153 |
| 36 | 1 | -2.349448 | -2.271980 | -3.438122 |
| 37 | 1 | -1.423413 | 0.075618 | -3.839720 |
| 38 | 1 | -3.148038 | 0.136570 | -3.556265 |
| 39 | 1 | -2.825114 | 1.895618 | -1.818298 |
| 40 | 1 | -2.250403 | 2.377483 | -3.410288 |
| 41 | 1 | 0.174930 | 3.324950 | -0.634630 |
| 42 | 1 | 3.357797 | -0.181587 | -0.663087 |
| 43 | 1 | -0.160550 | -3.340653 | -0.672430 |
| 44 | 1 | -3.340840 | 0.170542 | -0.701107 |
| 45 | 8 | -0.014895 | 0.055072 | 2.104839 |
| 46 | 1 | 0.685728 | 0.716741 | 2.246610 |
| 47 | 1 | -0.844819 | 0.539416 | 2.258946 |
| 48 | 7 | -3.543076 | -2.353405 | 0.820569 |
| 49 | 7 | 2.355706 | -3.533252 | 0.856342 |
| 50 | 7 | 3.560005 | 2.343381 | 0.863868 |
| 51 | 7 | -2.382878 | 3.517225 | 0.844014 |
| 52 | 1 | -4.551191 | -2.457488 | 0.599345 |
| 53 | 1 | 2.451568 | -4.545138 | 0.649688 |
| 54 | 1 | 4.564128 | 2.473055 | 0.631167 |
| 55 | 1 | -2.504795 | 4.524337 | 0.620708 |
| 56 | 6 | -3.188218 | 3.243355 | 2.028213 |
| 57 | 1 | -2.560371 | 2.892434 | 2.853714 |
| 58 | 6 | -3.284972 | -3.124677 | 2.030339 |
| 59 | 1 | -2.899565 | -2.479933 | 2.826580 |
| 60 | 6 | 3.135177 | -3.262602 | 2.058064 |
| 61 | 1 | 2.496570 | -2.865915 | 2.853717 |
| 62 | 6 | 3.297873 | 3.124594 | 2.066686 |
| 63 | 1 | 2.963088 | 2.478908 | 2.885165 |
| 64 | 1 | -3.936728 | 2.472645 | 1.819359 |
| 65 | 1 | -2.543496 | -3.907634 | 1.841347 |
| 66 | 1 | 3.919080 | -2.525841 | 1.855099 |
| 67 | 1 | 2.519293 | 3.871455 | 1.882827 |
| 68 | 6 | -4.655101 | -3.755948 | 2.446500 |
| 69 | 8 | -5.624509 | -3.467661 | 1.677017 |
| 70 | 8 | -4.638552 | -4.463864 | 3.475678 |
| 71 | 6 | 3.765102 | -4.629368 | 2.487354 |
| 72 | 8 | 3.466404 | -5.608136 | 1.733916 |
| 73 | 8 | 4.482326 | -4.601423 | 3.509870 |
| 74 | 6 | 4.652372 | 3.817252 | 2.437289 |
| 75 | 8 | 4.629789 | 4.553753 | 3.445365 |
| 76 | 8 | 5.615877 | 3.538943 | 1.656773 |
| 77 | 6 | -3.879488 | 4.596857 | 2.404794 |
| 78 | 8 | -3.583976 | 5.568572 | 1.640946 |
| 79 | 8 | -4.632314 | 4.565541 | 3.400544 |
| 80 | 6 | 1.387921 | -4.456507 | -1.675722 |
| 81 | 1 | 2.445631 | -4.381795 | -1.940762 |
| 82 | 1 | 1.265295 | -5.281850 | -0.969103 |
| 83 | 1 | 0.822242 | -4.726973 | -2.570256 |
| 84 | 6 | -4.443584 | -1.378895 | -1.714623 |
| 85 | 1 | -4.367715 | -2.438053 | -1.973364 |
| 86 | 1 | -5.277122 | -1.251286 | -1.018552 |
| 87 | 1 | -4.702184 | -0.817654 | -2.615513 |
| 88 | 6 | -1.354591 | 4.454390 | -1.651191 |
| 89 | 1 | -2.408548 | 4.385939 | -1.932552 |
| 90 | 1 | -1.238705 | 5.274045 | -0.936839 |
| 91 | 1 | -0.774887 | 4.728816 | -2.535281 |
| 92 | 6 | 4.472152 | 1.370983 | -1.662735 |

| | | | | |
|----|----|----------|-----------|-----------|
| 93 | 1 | 4.400089 | 2.431329 | -1.917913 |
| 94 | 1 | 5.301169 | 1.238360 | -0.962237 |
| 95 | 1 | 4.734883 | 0.812902 | -2.564192 |
| 96 | 71 | 0.010271 | -0.024211 | -0.377916 |

E(RTPSSh) = -2551.2227829 Hartree

Zero-point correction = 0.782063 Hartree/particle

Sum of electronic and thermal Energies = -2550.388021 Hartree

Sum of electronic and thermal Enthalpies = -2550.387077 Hartree

Sum of electronic and thermal Free Energies = -2550.530756 Hartree

Table S59. [La(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.557447 | 2.097087 | 1.714084 |
| 2 | 6 | 1.472982 | 1.641656 | 2.800937 |
| 3 | 6 | 2.585585 | 0.704094 | 2.337715 |
| 4 | 7 | 2.070047 | -0.555499 | 1.718586 |
| 5 | 6 | 1.623713 | -1.487480 | 2.795804 |
| 6 | 6 | 0.678853 | -2.588645 | 2.321499 |
| 7 | 7 | -0.578973 | -2.056635 | 1.714203 |
| 8 | 6 | -1.499209 | -1.602491 | 2.798708 |
| 9 | 6 | -2.610664 | -0.664496 | 2.332747 |
| 10 | 7 | -2.089768 | 0.590973 | 1.711676 |
| 11 | 6 | -1.648421 | 1.526237 | 2.787930 |
| 12 | 6 | -0.702523 | 2.627838 | 2.316343 |
| 13 | 6 | 1.188505 | 3.166099 | 0.899726 |
| 14 | 6 | 2.172016 | 2.604023 | -0.118297 |
| 15 | 8 | 1.938497 | 1.475728 | -0.652390 |
| 16 | 6 | 3.151858 | -1.164918 | 0.902877 |
| 17 | 6 | 2.617099 | -2.144335 | -0.132417 |
| 18 | 8 | 1.497122 | -1.910640 | -0.690553 |
| 19 | 6 | -1.206188 | -3.128372 | 0.898761 |
| 20 | 6 | -2.199209 | -2.571613 | -0.112593 |
| 21 | 8 | -1.971929 | -1.443566 | -0.650573 |
| 22 | 6 | -3.159887 | 1.201541 | 0.882159 |
| 23 | 6 | -2.602827 | 2.169143 | -0.153927 |
| 24 | 8 | -1.477535 | 1.926585 | -0.693419 |
| 25 | 1 | 0.863879 | 1.145224 | 3.559854 |
| 26 | 1 | 1.934559 | 2.509621 | 3.293325 |
| 27 | 1 | 3.220500 | 1.202542 | 1.604154 |
| 28 | 1 | 3.222360 | 0.474178 | 3.203337 |
| 29 | 1 | 1.137294 | -0.889552 | 3.569792 |
| 30 | 1 | 2.495307 | -1.958913 | 3.271632 |
| 31 | 1 | 1.170470 | -3.214562 | 1.575271 |
| 32 | 1 | 0.448986 | -3.237425 | 3.178247 |
| 33 | 1 | -0.892429 | -1.105989 | 3.559378 |
| 34 | 1 | -1.960525 | -2.471801 | 3.288618 |
| 35 | 1 | -3.246583 | -1.163139 | 1.600299 |
| 36 | 1 | -3.246979 | -0.431715 | 3.197995 |
| 37 | 1 | -1.165097 | 0.930577 | 3.565666 |
| 38 | 1 | -2.522720 | 1.997927 | 3.258764 |
| 39 | 1 | -1.192542 | 3.253166 | 1.568521 |
| 40 | 1 | -0.477311 | 3.277107 | 3.174174 |
| 41 | 1 | 0.396539 | 3.648031 | 0.317289 |
| 42 | 1 | 3.624850 | -0.360110 | 0.330951 |
| 43 | 1 | -0.412806 | -3.602059 | 0.311326 |
| 44 | 1 | -3.634407 | 0.396036 | 0.312613 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 45 | 8 | 0.136162 | -0.459643 | -2.608038 |
| 46 | 1 | 0.695234 | -1.254987 | -2.660444 |
| 47 | 1 | -0.676888 | -0.669165 | -3.093229 |
| 48 | 7 | -3.350605 | 3.198861 | -0.488794 |
| 49 | 7 | -3.233422 | -3.323381 | -0.425828 |
| 50 | 7 | 3.376383 | -3.169368 | -0.450813 |
| 51 | 7 | 3.206383 | 3.351962 | -0.440731 |
| 52 | 1 | -4.270260 | 3.436500 | -0.068628 |
| 53 | 1 | -3.454068 | -4.247452 | -0.005966 |
| 54 | 1 | 4.293034 | -3.398562 | -0.016805 |
| 55 | 1 | 3.432737 | 4.275672 | -0.023911 |
| 56 | 6 | 4.204120 | 3.081802 | -1.467760 |
| 57 | 1 | 3.730426 | 2.959162 | -2.447065 |
| 58 | 6 | -3.083449 | 4.179702 | -1.532877 |
| 59 | 1 | -2.970973 | 3.690426 | -2.505694 |
| 60 | 6 | -4.239318 | -3.059550 | -1.446572 |
| 61 | 1 | -4.794738 | -2.143730 | -1.220130 |
| 62 | 6 | 3.134062 | -4.160817 | -1.491244 |
| 63 | 1 | 3.039249 | -3.681297 | -2.470894 |
| 64 | 1 | -2.161034 | 4.730703 | -1.323141 |
| 65 | 1 | 4.757318 | 2.164234 | -1.242826 |
| 66 | 1 | 2.211148 | -4.715365 | -1.294269 |
| 67 | 1 | -3.773084 | -2.937788 | -2.429596 |
| 68 | 6 | 4.367899 | -5.125922 | -1.467826 |
| 69 | 8 | 5.248950 | -4.831505 | -0.601192 |
| 70 | 8 | 4.341322 | -6.061261 | -2.294528 |
| 71 | 6 | 5.171651 | 4.313242 | -1.474160 |
| 72 | 8 | 4.880179 | 5.217241 | -0.630744 |
| 73 | 8 | 6.107796 | 4.263090 | -2.299611 |
| 74 | 6 | -4.310049 | 5.153187 | -1.543830 |
| 75 | 8 | -5.208107 | 4.879230 | -0.688188 |
| 76 | 8 | -4.262253 | 6.076059 | -2.384074 |
| 77 | 6 | -5.201486 | -4.295432 | -1.442573 |
| 78 | 8 | -4.898919 | -5.195905 | -0.599237 |
| 79 | 8 | -6.144294 | -4.251628 | -2.260590 |
| 80 | 57 | -0.007600 | 0.011505 | -0.037303 |
| 81 | 1 | -1.667111 | -3.898649 | 1.531088 |
| 82 | 1 | -3.929057 | 1.680124 | 1.502610 |
| 83 | 1 | 1.659423 | 3.931186 | 1.531212 |
| 84 | 1 | 3.919458 | -1.631230 | 1.534379 |

E(RTPSSh) = -2385.5681949 Hartree

Zero-point correction = 0.667502 Hartree/particle

Sum of electronic and thermal Energies = -2384.852552 Hartree

Sum of electronic and thermal Enthalpies = -2384.851608 Hartree

Sum of electronic and thermal Free Energies = -2384.988373 Hartree

Table S60. [Ce(DOTA-(gly)4(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | 0.620739 | 2.076249 | 1.749507 |
| 2 | 6 | 1.527594 | 1.601488 | 2.835605 |
| 3 | 6 | 2.610713 | 0.630549 | 2.371346 |
| 4 | 7 | 2.055289 | -0.613175 | 1.754246 |
| 5 | 6 | 1.585754 | -1.532909 | 2.832084 |
| 6 | 6 | 0.610976 | -2.607057 | 2.356680 |
| 7 | 7 | -0.631244 | -2.038009 | 1.750189 |
| 8 | 6 | -1.541212 | -1.564125 | 2.835039 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 9 | 6 | -2.623731 | -0.593089 | 2.369114 |
| 10 | 7 | -2.064341 | 0.646923 | 1.749709 |
| 11 | 6 | -1.598390 | 1.570127 | 2.826158 |
| 12 | 6 | -0.622855 | 2.644549 | 2.352329 |
| 13 | 6 | 1.278582 | 3.121480 | 0.925303 |
| 14 | 6 | 2.230644 | 2.524087 | -0.102344 |
| 15 | 8 | 1.961122 | 1.395619 | -0.619198 |
| 16 | 6 | 3.113132 | -1.253909 | 0.931188 |
| 17 | 6 | 2.541864 | -2.199108 | -0.116139 |
| 18 | 8 | 1.422942 | -1.925730 | -0.658315 |
| 19 | 6 | -1.286107 | -3.086793 | 0.926686 |
| 20 | 6 | -2.248896 | -2.496069 | -0.094214 |
| 21 | 8 | -1.984619 | -1.369112 | -0.618367 |
| 22 | 6 | -3.112933 | 1.287748 | 0.915487 |
| 23 | 6 | -2.523951 | 2.223192 | -0.132218 |
| 24 | 8 | -1.399362 | 1.945751 | -0.656204 |
| 25 | 1 | 0.908406 | 1.126661 | 3.600097 |
| 26 | 1 | 2.015754 | 2.458829 | 3.320702 |
| 27 | 1 | 3.258129 | 1.109415 | 1.635506 |
| 28 | 1 | 3.242679 | 0.382414 | 3.235432 |
| 29 | 1 | 1.115912 | -0.922676 | 3.606770 |
| 30 | 1 | 2.444873 | -2.027976 | 3.306562 |
| 31 | 1 | 1.085265 | -3.244852 | 1.609134 |
| 32 | 1 | 0.362923 | -3.251003 | 3.211948 |
| 33 | 1 | -0.923362 | -1.088797 | 3.600242 |
| 34 | 1 | -2.028531 | -2.422550 | 3.318756 |
| 35 | 1 | -3.272533 | -1.072217 | 1.634738 |
| 36 | 1 | -3.254668 | -0.342368 | 3.233228 |
| 37 | 1 | -1.130826 | 0.962191 | 3.604092 |
| 38 | 1 | -2.459675 | 2.065601 | 3.296441 |
| 39 | 1 | -1.096111 | 3.281633 | 1.603513 |
| 40 | 1 | -0.378283 | 3.289099 | 3.208329 |
| 41 | 1 | 0.497117 | 3.628417 | 0.350152 |
| 42 | 1 | 3.616368 | -0.461322 | 0.368299 |
| 43 | 1 | -0.503487 | -3.585708 | 0.345932 |
| 44 | 1 | -3.617481 | 0.494514 | 0.354783 |
| 45 | 8 | 0.065348 | -0.395281 | -2.536165 |
| 46 | 1 | 0.631607 | -1.182648 | -2.621996 |
| 47 | 1 | -0.784694 | -0.635903 | -2.937576 |
| 48 | 7 | -3.246020 | 3.261460 | -0.495400 |
| 49 | 7 | -3.295564 | -3.218272 | -0.433325 |
| 50 | 7 | 3.269957 | -3.236934 | -0.464392 |
| 51 | 7 | 3.276053 | 3.243084 | -0.453029 |
| 52 | 1 | -4.166523 | 3.524314 | -0.092718 |
| 53 | 1 | -3.544148 | -4.142956 | -0.030971 |
| 54 | 1 | 4.186869 | -3.496951 | -0.049700 |
| 55 | 1 | 3.529653 | 4.167933 | -0.055144 |
| 56 | 6 | 4.240618 | 2.941198 | -1.502762 |
| 57 | 1 | 3.736924 | 2.803466 | -2.464817 |
| 58 | 6 | -2.953058 | 4.207490 | -1.564488 |
| 59 | 1 | -2.826900 | 3.687058 | -2.519189 |
| 60 | 6 | -4.268589 | -2.923072 | -1.477191 |
| 61 | 1 | -4.819776 | -2.005096 | -1.248818 |
| 62 | 6 | 2.991733 | -4.191545 | -1.530013 |
| 63 | 1 | 2.882383 | -3.679363 | -2.491324 |
| 64 | 1 | -2.030471 | 4.758525 | -1.355290 |
| 65 | 1 | 4.790783 | 2.022475 | -1.274701 |
| 66 | 1 | 2.065249 | -4.739290 | -1.330307 |
| 67 | 1 | -3.772358 | -2.787991 | -2.443548 |
| 68 | 6 | 4.210385 | -5.174669 | -1.564742 |
| 69 | 8 | 5.107822 | -4.931615 | -0.699076 |
| 70 | 8 | 4.157100 | -6.073324 | -2.430151 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 71 | 6 | 5.220850 | 4.160888 | -1.562268 |
| 72 | 8 | 4.973271 | 5.078597 | -0.719581 |
| 73 | 8 | 6.123806 | 4.089242 | -2.422476 |
| 74 | 6 | -4.171220 | 5.189339 | -1.627015 |
| 75 | 8 | -5.079996 | 4.957900 | -0.770062 |
| 76 | 8 | -4.107240 | 6.077506 | -2.502943 |
| 77 | 6 | -5.245163 | -4.146421 | -1.524558 |
| 78 | 8 | -4.986504 | -5.060507 | -0.681250 |
| 79 | 8 | -6.155636 | -4.080495 | -2.377043 |
| 80 | 58 | -0.004181 | 0.012694 | 0.028128 |
| 81 | 1 | -1.778942 | -3.842442 | 1.552441 |
| 82 | 1 | -3.863419 | 1.800045 | 1.531777 |
| 83 | 1 | 1.782129 | 3.871849 | 1.549118 |
| 84 | 1 | 3.862702 | -1.756488 | 1.556374 |

E(RTPSSh) = -2386.2199658 Hartree

Zero-point correction = 0.667579 Hartree/particle

Sum of electronic and thermal Energies = -2385.504316 Hartree

Sum of electronic and thermal Enthalpies = -2385.503372 Hartree

Sum of electronic and thermal Free Energies = -2385.639620 Hartree

Table S61. [Pr(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.629835 | 2.070053 | 1.761120 |
| 2 | 6 | 1.538916 | 1.599392 | 2.847257 |
| 3 | 6 | 2.616965 | 0.623450 | 2.382739 |
| 4 | 7 | 2.052927 | -0.617441 | 1.768109 |
| 5 | 6 | 1.581418 | -1.534742 | 2.847107 |
| 6 | 6 | 0.604823 | -2.606683 | 2.370752 |
| 7 | 7 | -0.634334 | -2.032568 | 1.762449 |
| 8 | 6 | -1.546488 | -1.561789 | 2.846863 |
| 9 | 6 | -2.623792 | -0.586364 | 2.379286 |
| 10 | 7 | -2.055858 | 0.650807 | 1.762199 |
| 11 | 6 | -1.588515 | 1.572196 | 2.839784 |
| 12 | 6 | -0.610625 | 2.644126 | 2.365214 |
| 13 | 6 | 1.288200 | 3.107485 | 0.927328 |
| 14 | 6 | 2.226398 | 2.499081 | -0.106533 |
| 15 | 8 | 1.947401 | 1.367094 | -0.611688 |
| 16 | 6 | 3.103483 | -1.264846 | 0.941171 |
| 17 | 6 | 2.519334 | -2.197365 | -0.109883 |
| 18 | 8 | 1.397779 | -1.912625 | -0.640680 |
| 19 | 6 | -1.289581 | -3.075405 | 0.931670 |
| 20 | 6 | -2.239431 | -2.476915 | -0.096247 |
| 21 | 8 | -1.963143 | -1.349055 | -0.614829 |
| 22 | 6 | -3.097879 | 1.297557 | 0.924341 |
| 23 | 6 | -2.497096 | 2.223342 | -0.124653 |
| 24 | 8 | -1.369356 | 1.937088 | -0.636839 |
| 25 | 1 | 0.921038 | 1.129929 | 3.616124 |
| 26 | 1 | 2.030657 | 2.458115 | 3.326049 |
| 27 | 1 | 3.264654 | 1.098468 | 1.644500 |
| 28 | 1 | 3.249985 | 0.373179 | 3.245375 |
| 29 | 1 | 1.111886 | -0.922745 | 3.620620 |
| 30 | 1 | 2.439231 | -2.031010 | 3.322569 |
| 31 | 1 | 1.078516 | -3.245970 | 1.624086 |
| 32 | 1 | 0.353082 | -3.249856 | 3.225403 |
| 33 | 1 | -0.930116 | -1.090954 | 3.616024 |
| 34 | 1 | -2.037485 | -2.421034 | 3.325190 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 35 | 1 | -3.272058 | -1.062223 | 1.642121 |
| 36 | 1 | -3.256784 | -0.333260 | 3.241114 |
| 37 | 1 | -1.121804 | 0.962785 | 3.617094 |
| 38 | 1 | -2.448844 | 2.069054 | 3.310185 |
| 39 | 1 | -1.082700 | 3.282811 | 1.617045 |
| 40 | 1 | -0.362432 | 3.287811 | 3.220676 |
| 41 | 1 | 0.505677 | 3.617795 | 0.356807 |
| 42 | 1 | 3.614932 | -0.475190 | 0.381789 |
| 43 | 1 | -0.505908 | -3.577982 | 0.355606 |
| 44 | 1 | -3.608878 | 0.507267 | 0.365483 |
| 45 | 8 | -0.017993 | -0.372852 | -2.488074 |
| 46 | 1 | 0.608338 | -1.108108 | -2.609939 |
| 47 | 1 | -0.885725 | -0.729273 | -2.741739 |
| 48 | 7 | -3.211446 | 3.262304 | -0.500478 |
| 49 | 7 | -3.285854 | -3.191471 | -0.449393 |
| 50 | 7 | 3.238190 | -3.236281 | -0.473280 |
| 51 | 7 | 3.269419 | 3.211834 | -0.475272 |
| 52 | 1 | -4.134037 | 3.531771 | -0.106676 |
| 53 | 1 | -3.544941 | -4.116459 | -0.053237 |
| 54 | 1 | 4.156212 | -3.506454 | -0.067544 |
| 55 | 1 | 3.532022 | 4.138045 | -0.085857 |
| 56 | 6 | 4.221479 | 2.899917 | -1.533568 |
| 57 | 1 | 3.707090 | 2.759292 | -2.489500 |
| 58 | 6 | -2.907189 | 4.200284 | -1.573577 |
| 59 | 1 | -2.775929 | 3.673308 | -2.523973 |
| 60 | 6 | -4.245975 | -2.887986 | -1.503010 |
| 61 | 1 | -4.795646 | -1.968553 | -1.277020 |
| 62 | 6 | 2.945866 | -4.179383 | -1.545399 |
| 63 | 1 | 2.832207 | -3.657666 | -2.501054 |
| 64 | 1 | -1.984439 | 4.749817 | -1.361193 |
| 65 | 1 | 4.770291 | 1.980246 | -1.306204 |
| 66 | 1 | 2.017554 | -4.723254 | -1.343478 |
| 67 | 1 | -3.738571 | -2.751756 | -2.463366 |
| 68 | 6 | 4.158245 | -5.169454 | -1.598045 |
| 69 | 8 | 5.062113 | -4.941406 | -0.734923 |
| 70 | 8 | 4.094792 | -6.058369 | -2.472797 |
| 71 | 6 | 5.205797 | 4.115549 | -1.609363 |
| 72 | 8 | 4.971191 | 5.037641 | -0.767654 |
| 73 | 8 | 6.098826 | 4.037100 | -2.479200 |
| 74 | 6 | -4.121849 | 5.185609 | -1.650767 |
| 75 | 8 | -5.036791 | 4.962815 | -0.798021 |
| 76 | 8 | -4.049771 | 6.067753 | -2.532099 |
| 77 | 6 | -5.226834 | -4.107428 | -1.564544 |
| 78 | 8 | -4.982086 | -5.023524 | -0.719141 |
| 79 | 8 | -6.126336 | -4.036851 | -2.428021 |
| 80 | 59 | -0.000816 | 0.014038 | 0.065037 |
| 81 | 1 | -1.792440 | -3.829101 | 1.551602 |
| 82 | 1 | -3.844666 | 1.818645 | 1.537631 |
| 83 | 1 | 1.802899 | 3.856319 | 1.543677 |
| 84 | 1 | 3.848076 | -1.778946 | 1.562846 |

E(RTPSSh) = -2386.855262 Hartree

Zero-point correction = 0.668001 Hartree/particle

Sum of electronic and thermal Energies = -2386.139418 Hartree

Sum of electronic and thermal Enthalpies = -2386.138473 Hartree

Sum of electronic and thermal Free Energies = -2386.273313 Hartree

Table S62. [Nd(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

Center Atomic Coordinates (Angstroms)

| Number | Number | X | Y | Z |
|--------|--------|-----------|-----------|-----------|
| 1 | 7 | 0.636359 | 2.061983 | 1.770181 |
| 2 | 6 | 1.545300 | 1.592297 | 2.856914 |
| 3 | 6 | 2.618900 | 0.612162 | 2.391926 |
| 4 | 7 | 2.046946 | -0.625000 | 1.777473 |
| 5 | 6 | 1.575387 | -1.541768 | 2.856778 |
| 6 | 6 | 0.595346 | -2.609626 | 2.379251 |
| 7 | 7 | -0.639835 | -2.028075 | 1.770243 |
| 8 | 6 | -1.552379 | -1.558604 | 2.854862 |
| 9 | 6 | -2.625073 | -0.578944 | 2.386692 |
| 10 | 7 | -2.049344 | 0.654958 | 1.770562 |
| 11 | 6 | -1.582273 | 1.575311 | 2.849136 |
| 12 | 6 | -0.600670 | 2.643300 | 2.374265 |
| 13 | 6 | 1.298199 | 3.092814 | 0.930959 |
| 14 | 6 | 2.227037 | 2.473688 | -0.104583 |
| 15 | 8 | 1.939425 | 1.339467 | -0.600051 |
| 16 | 6 | 3.090539 | -1.276690 | 0.945374 |
| 17 | 6 | 2.494921 | -2.199200 | -0.107622 |
| 18 | 8 | 1.370593 | -1.905472 | -0.627829 |
| 19 | 6 | -1.298040 | -3.064142 | 0.933578 |
| 20 | 6 | -2.238072 | -2.454993 | -0.096526 |
| 21 | 8 | -1.952157 | -1.324965 | -0.605910 |
| 22 | 6 | -3.084803 | 1.306178 | 0.928189 |
| 23 | 6 | -2.473154 | 2.222637 | -0.122221 |
| 24 | 8 | -1.343315 | 1.927560 | -0.624747 |
| 25 | 1 | 0.927079 | 1.126449 | 3.627721 |
| 26 | 1 | 2.039984 | 2.451014 | 3.332529 |
| 27 | 1 | 3.267992 | 1.084405 | 1.653083 |
| 28 | 1 | 3.251725 | 0.358315 | 3.253601 |
| 29 | 1 | 1.108384 | -0.929270 | 3.631453 |
| 30 | 1 | 2.432697 | -2.040685 | 3.330278 |
| 31 | 1 | 1.067074 | -3.250383 | 1.632567 |
| 32 | 1 | 0.339459 | -3.252506 | 3.232825 |
| 33 | 1 | -0.936093 | -1.091580 | 3.626430 |
| 34 | 1 | -2.046604 | -2.417939 | 3.329594 |
| 35 | 1 | -3.274392 | -1.051800 | 1.648456 |
| 36 | 1 | -3.258298 | -0.322708 | 3.247364 |
| 37 | 1 | -1.118457 | 0.965001 | 3.627498 |
| 38 | 1 | -2.442232 | 2.074670 | 3.317438 |
| 39 | 1 | -1.070281 | 3.283426 | 1.625745 |
| 40 | 1 | -0.348917 | 3.286604 | 3.228883 |
| 41 | 1 | 0.517014 | 3.606912 | 0.362184 |
| 42 | 1 | 3.606716 | -0.488842 | 0.387973 |
| 43 | 1 | -0.515306 | -3.570178 | 0.359428 |
| 44 | 1 | -3.600556 | 0.517961 | 0.370968 |
| 45 | 8 | -0.030494 | -0.336361 | -2.449764 |
| 46 | 1 | 0.596791 | -1.068661 | -2.583855 |
| 47 | 1 | -0.902148 | -0.700396 | -2.679350 |
| 48 | 7 | -3.179886 | 3.262684 | -0.508872 |
| 49 | 7 | -3.285761 | -3.161443 | -0.461013 |
| 50 | 7 | 3.206057 | -3.238847 | -0.483345 |
| 51 | 7 | 3.271072 | 3.178877 | -0.484295 |
| 52 | 1 | -4.103540 | 3.539086 | -0.121955 |
| 53 | 1 | -3.552324 | -4.087599 | -0.071981 |
| 54 | 1 | 4.125793 | -3.515914 | -0.085835 |
| 55 | 1 | 3.540002 | 4.106658 | -0.102514 |
| 56 | 6 | 4.215205 | 2.857615 | -1.546970 |
| 57 | 1 | 3.694245 | 2.712692 | -2.498669 |
| 58 | 6 | -2.865687 | 4.193589 | -1.585317 |
| 59 | 1 | -2.732041 | 3.661193 | -2.532344 |
| 60 | 6 | -4.237975 | -2.847961 | -1.518967 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 61 | 1 | -4.785638 | -1.927789 | -1.291150 |
| 62 | 6 | 2.903088 | -4.173575 | -1.559893 |
| 63 | 1 | 2.784952 | -3.645079 | -2.511254 |
| 64 | 1 | -1.941759 | 4.740421 | -1.371117 |
| 65 | 1 | 4.763308 | 1.938017 | -1.317595 |
| 66 | 1 | 1.974386 | -4.715819 | -1.355424 |
| 67 | 1 | -3.724186 | -2.708551 | -2.475432 |
| 68 | 6 | 4.111928 | -5.167282 | -1.626746 |
| 69 | 8 | 5.021387 | -4.948387 | -0.767045 |
| 70 | 8 | 4.040913 | -6.049800 | -2.507330 |
| 71 | 6 | 5.202210 | 4.070329 | -1.635962 |
| 72 | 8 | 4.975855 | 4.997199 | -0.797150 |
| 73 | 8 | 6.089078 | 3.985480 | -2.511416 |
| 74 | 6 | -4.075905 | 5.183683 | -1.673334 |
| 75 | 8 | -4.995592 | 4.969121 | -0.823484 |
| 76 | 8 | -3.996545 | 6.061018 | -2.558769 |
| 77 | 6 | -5.223066 | -4.063478 | -1.592824 |
| 78 | 8 | -4.987501 | -4.984154 | -0.749693 |
| 79 | 8 | -6.116377 | -3.985980 | -2.462016 |
| 80 | 60 | 0.000210 | 0.014265 | 0.091733 |
| 81 | 1 | -1.809332 | -3.816153 | 1.548580 |
| 82 | 1 | -3.828879 | 1.835482 | 1.537664 |
| 83 | 1 | 1.820991 | 3.839571 | 1.542912 |
| 84 | 1 | 3.832571 | -1.799702 | 1.562624 |

E(RTPSSh) = -2387.4782215 Hartree

Zero-point correction = 0.668374 Hartree/particle

Sum of electronic and thermal Energies = -2386.762193 Hartree

Sum of electronic and thermal Enthalpies = -2386.761249 Hartree

Sum of electronic and thermal Free Energies = -2386.894987 Hartree

Table S63. [Sm(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.641598 | 2.048986 | 1.784322 |
| 2 | 6 | 1.552417 | 1.584347 | 2.871796 |
| 3 | 6 | 2.620941 | 0.600150 | 2.405710 |
| 4 | 7 | 2.037644 | -0.631387 | 1.791313 |
| 5 | 6 | 1.570597 | -1.549009 | 2.871735 |
| 6 | 6 | 0.587116 | -2.612222 | 2.392909 |
| 7 | 7 | -0.642879 | -2.020182 | 1.784014 |
| 8 | 6 | -1.555929 | -1.555993 | 2.870447 |
| 9 | 6 | -2.624059 | -0.572566 | 2.402074 |
| 10 | 7 | -2.038258 | 0.656538 | 1.786529 |
| 11 | 6 | -1.574384 | 1.576983 | 2.866344 |
| 12 | 6 | -0.589742 | 2.640563 | 2.389715 |
| 13 | 6 | 1.306346 | 3.070021 | 0.935389 |
| 14 | 6 | 2.220720 | 2.434470 | -0.102305 |
| 15 | 8 | 1.923899 | 1.293812 | -0.577159 |
| 16 | 6 | 3.070345 | -1.287600 | 0.949495 |
| 17 | 6 | 2.456731 | -2.194156 | -0.106111 |
| 18 | 8 | 1.326222 | -1.888545 | -0.606365 |
| 19 | 6 | -1.305080 | -3.046230 | 0.938491 |
| 20 | 6 | -2.228944 | -2.421014 | -0.095602 |
| 21 | 8 | -1.931847 | -1.284738 | -0.585290 |
| 22 | 6 | -3.064857 | 1.312511 | 0.937191 |
| 23 | 6 | -2.437488 | 2.213496 | -0.116300 |
| 24 | 8 | -1.303144 | 1.906721 | -0.601166 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 25 | 1 | 0.935558 | 1.122691 | 3.646233 |
| 26 | 1 | 2.049424 | 2.444799 | 3.341579 |
| 27 | 1 | 3.271378 | 1.069252 | 1.666017 |
| 28 | 1 | 3.253844 | 0.341187 | 3.265652 |
| 29 | 1 | 1.107166 | -0.937423 | 3.649305 |
| 30 | 1 | 2.429282 | -2.049975 | 3.340372 |
| 31 | 1 | 1.056331 | -3.254043 | 1.645499 |
| 32 | 1 | 0.326322 | -3.255429 | 3.244604 |
| 33 | 1 | -0.940299 | -1.093172 | 3.645090 |
| 34 | 1 | -2.052030 | -2.417067 | 3.339841 |
| 35 | 1 | -3.274441 | -1.042371 | 1.662716 |
| 36 | 1 | -3.257618 | -0.312149 | 3.261102 |
| 37 | 1 | -1.113238 | 0.967079 | 3.646649 |
| 38 | 1 | -2.435078 | 2.078142 | 3.331153 |
| 39 | 1 | -1.057424 | 3.282026 | 1.641077 |
| 40 | 1 | -0.332168 | 3.283847 | 3.242432 |
| 41 | 1 | 0.526125 | 3.588446 | 0.369576 |
| 42 | 1 | 3.592361 | -0.501684 | 0.395210 |
| 43 | 1 | -0.523817 | -3.558612 | 0.368331 |
| 44 | 1 | -3.587824 | 0.526658 | 0.383768 |
| 45 | 8 | -0.041686 | -0.264728 | -2.379109 |
| 46 | 1 | 0.579874 | -0.997153 | -2.536353 |
| 47 | 1 | -0.919516 | -0.624907 | -2.591833 |
| 48 | 7 | -3.134239 | 3.252670 | -0.522630 |
| 49 | 7 | -3.273879 | -3.118364 | -0.483431 |
| 50 | 7 | 3.157116 | -3.232606 | -0.503719 |
| 51 | 7 | 3.261921 | 3.131271 | -0.504197 |
| 52 | 1 | -4.060589 | 3.537658 | -0.148187 |
| 53 | 1 | -3.549613 | -4.047943 | -0.108351 |
| 54 | 1 | 4.080175 | -3.519407 | -0.120273 |
| 55 | 1 | 3.538053 | 4.062867 | -0.136613 |
| 56 | 6 | 4.194371 | 2.795139 | -1.572622 |
| 57 | 1 | 3.663818 | 2.641933 | -2.517689 |
| 58 | 6 | -2.805404 | 4.171502 | -1.605089 |
| 59 | 1 | -2.665623 | 3.629573 | -2.545790 |
| 60 | 6 | -4.212711 | -2.789739 | -1.548833 |
| 61 | 1 | -4.759325 | -1.869735 | -1.317984 |
| 62 | 6 | 2.837090 | -4.155169 | -1.585885 |
| 63 | 1 | 2.711663 | -3.617109 | -2.530896 |
| 64 | 1 | -1.881228 | 4.716680 | -1.387794 |
| 65 | 1 | 4.742320 | 1.876548 | -1.338957 |
| 66 | 1 | 1.908050 | -4.694964 | -1.376631 |
| 67 | 1 | -3.687884 | -2.643425 | -2.498232 |
| 68 | 6 | 4.040513 | -5.154119 | -1.674406 |
| 69 | 8 | 4.959570 | -4.947272 | -0.821849 |
| 70 | 8 | 3.956934 | -6.028417 | -2.561961 |
| 71 | 6 | 5.183897 | 4.004254 | -1.683722 |
| 72 | 8 | 4.967714 | 4.940350 | -0.852444 |
| 73 | 8 | 6.062468 | 3.908415 | -2.566331 |
| 74 | 6 | -4.010737 | 5.165892 | -1.713361 |
| 75 | 8 | -4.938954 | 4.962703 | -0.869952 |
| 76 | 8 | -3.920227 | 6.035034 | -2.605750 |
| 77 | 6 | -5.201735 | -4.000791 | -1.644823 |
| 78 | 8 | -4.978896 | -4.929789 | -0.807283 |
| 79 | 8 | -6.085286 | -3.912450 | -2.522793 |
| 80 | 62 | 0.001496 | 0.014439 | 0.137504 |
| 81 | 1 | -1.830123 | -3.794692 | 1.546031 |
| 82 | 1 | -3.804365 | 1.854749 | 1.540648 |
| 83 | 1 | 1.841086 | 3.814471 | 1.539570 |
| 84 | 1 | 3.809240 | -1.824161 | 1.558675 |

E(RTPSSh) = -2388.7008851 Hartree

Zero-point correction = 0.668914 Hartree/particle
 Sum of electronic and thermal Energies = -2387.984561 Hartree
 Sum of electronic and thermal Enthalpies = -2387.983617 Hartree
 Sum of electronic and thermal Free Energies = -2388.116192 Hartree

Table S64. [Eu(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.604309 | 2.055480 | 1.793150 |
| 2 | 6 | 1.523889 | 1.610713 | 2.881564 |
| 3 | 6 | 2.608894 | 0.645531 | 2.415128 |
| 4 | 7 | 2.044446 | -0.594774 | 1.801448 |
| 5 | 6 | 1.595639 | -1.520447 | 2.882629 |
| 6 | 6 | 0.631860 | -2.600529 | 2.402546 |
| 7 | 7 | -0.606835 | -2.027925 | 1.793193 |
| 8 | 6 | -1.528854 | -1.582795 | 2.879988 |
| 9 | 6 | -2.613382 | -0.618713 | 2.410385 |
| 10 | 7 | -2.046453 | 0.619354 | 1.795707 |
| 11 | 6 | -1.601127 | 1.547965 | 2.876287 |
| 12 | 6 | -0.635802 | 2.628162 | 2.398491 |
| 13 | 6 | 1.251538 | 3.084312 | 0.940310 |
| 14 | 6 | 2.168848 | 2.458583 | -0.100441 |
| 15 | 8 | 1.889599 | 1.308688 | -0.563618 |
| 16 | 6 | 3.085310 | -1.234435 | 0.957386 |
| 17 | 6 | 2.481456 | -2.143690 | -0.101070 |
| 18 | 8 | 1.341959 | -1.854471 | -0.590679 |
| 19 | 6 | -1.251112 | -3.062602 | 0.944758 |
| 20 | 6 | -2.176917 | -2.448875 | -0.093998 |
| 21 | 8 | -1.897014 | -1.303305 | -0.572675 |
| 22 | 6 | -3.081276 | 1.258688 | 0.944007 |
| 23 | 6 | -2.463396 | 2.162917 | -0.111830 |
| 24 | 8 | -1.320658 | 1.872032 | -0.586630 |
| 25 | 1 | 0.916171 | 1.139238 | 3.657335 |
| 26 | 1 | 2.005044 | 2.481403 | 3.348893 |
| 27 | 1 | 3.250253 | 1.125582 | 1.674524 |
| 28 | 1 | 3.247132 | 0.396981 | 3.274114 |
| 29 | 1 | 1.121195 | -0.917654 | 3.660449 |
| 30 | 1 | 2.463785 | -2.005425 | 3.350584 |
| 31 | 1 | 1.112770 | -3.233205 | 1.654766 |
| 32 | 1 | 0.381044 | -3.249070 | 3.253093 |
| 33 | 1 | -0.922577 | -1.109586 | 3.655756 |
| 34 | 1 | -2.009275 | -2.453659 | 3.347566 |
| 35 | 1 | -3.254011 | -1.099642 | 1.669647 |
| 36 | 1 | -3.252953 | -0.368765 | 3.267974 |
| 37 | 1 | -1.129357 | 0.946894 | 3.657106 |
| 38 | 1 | -2.471378 | 2.033307 | 3.339994 |
| 39 | 1 | -1.114766 | 3.260610 | 1.649335 |
| 40 | 1 | -0.388158 | 3.276697 | 3.250058 |
| 41 | 1 | 0.462380 | 3.592075 | 0.377532 |
| 42 | 1 | 3.597923 | -0.440409 | 0.406175 |
| 43 | 1 | -0.460741 | -3.565082 | 0.378658 |
| 44 | 1 | -3.594447 | 0.464661 | 0.393369 |
| 45 | 8 | -0.041188 | -0.240392 | -2.345816 |
| 46 | 1 | 0.598376 | -0.955682 | -2.509562 |
| 47 | 1 | -0.911472 | -0.626299 | -2.545247 |
| 48 | 7 | -3.174987 | 3.186977 | -0.530399 |
| 49 | 7 | -3.203883 | -3.163390 | -0.497525 |
| 50 | 7 | 3.197344 | -3.166252 | -0.511763 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 51 | 7 | 3.192974 | 3.171673 | -0.517063 |
| 52 | 1 | -4.108221 | 3.459209 | -0.163479 |
| 53 | 1 | -3.466608 | -4.100089 | -0.130529 |
| 54 | 1 | 4.127702 | -3.439829 | -0.136236 |
| 55 | 1 | 3.455690 | 4.110495 | -0.157983 |
| 56 | 6 | 4.123673 | 2.843901 | -1.589623 |
| 57 | 1 | 3.589599 | 2.677859 | -2.530565 |
| 58 | 6 | -2.854129 | 4.104746 | -1.616180 |
| 59 | 1 | -2.702008 | 3.560005 | -2.553361 |
| 60 | 6 | -4.139621 | -2.844570 | -1.568659 |
| 61 | 1 | -4.701559 | -1.933789 | -1.338466 |
| 62 | 6 | 2.885924 | -4.087187 | -1.597859 |
| 63 | 1 | 2.747955 | -3.545642 | -2.539150 |
| 64 | 1 | -1.939109 | 4.664486 | -1.397432 |
| 65 | 1 | 4.686796 | 1.934926 | -1.354755 |
| 66 | 1 | 1.966245 | -4.642234 | -1.387474 |
| 67 | 1 | -3.610074 | -2.686968 | -2.513672 |
| 68 | 6 | 4.103827 | -5.067297 | -1.698277 |
| 69 | 8 | 5.025377 | -4.849618 | -0.851155 |
| 70 | 8 | 4.027482 | -5.939157 | -2.588856 |
| 71 | 6 | 5.094210 | 4.067075 | -1.713528 |
| 72 | 8 | 4.867227 | 5.005799 | -0.888129 |
| 73 | 8 | 5.970418 | 3.978025 | -2.599176 |
| 74 | 6 | -4.073102 | 5.081032 | -1.735719 |
| 75 | 8 | -5.003630 | 4.867375 | -0.897474 |
| 76 | 8 | -3.989372 | 5.948073 | -2.630789 |
| 77 | 6 | -5.109533 | -4.070001 | -1.676778 |
| 78 | 8 | -4.876259 | -5.000676 | -0.843956 |
| 79 | 8 | -5.989985 | -3.989660 | -2.558564 |
| 80 | 63 | 0.000840 | 0.014857 | 0.159795 |
| 81 | 1 | -1.769854 | -3.817705 | 1.549423 |
| 82 | 1 | -3.827635 | 1.794106 | 1.545046 |
| 83 | 1 | 1.779561 | 3.836229 | 1.541062 |
| 84 | 1 | 3.830682 | -1.764636 | 1.564184 |

E(RTPSSh) = -2389.2980601 Hartree

Zero-point correction = 0.669019 Hartree/particle

Sum of electronic and thermal Energies = -2388.581684 Hartree

Sum of electronic and thermal Enthalpies = -2388.580739 Hartree

Sum of electronic and thermal Free Energies = -2388.713252 Hartree

Table S65. [Gd(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.565235 | 2.062205 | 1.800227 |
| 2 | 6 | 1.493808 | 1.637795 | 2.889083 |
| 3 | 6 | 2.595647 | 0.692523 | 2.422344 |
| 4 | 7 | 2.051251 | -0.556514 | 1.808808 |
| 5 | 6 | 1.621722 | -1.490400 | 2.890654 |
| 6 | 6 | 0.678418 | -2.587713 | 2.409842 |
| 7 | 7 | -0.569145 | -2.035723 | 1.800051 |
| 8 | 6 | -1.500016 | -1.610688 | 2.887267 |
| 9 | 6 | -2.601337 | -0.666541 | 2.417212 |
| 10 | 7 | -2.054481 | 0.580513 | 1.803052 |
| 11 | 6 | -1.628625 | 1.517096 | 2.884470 |
| 12 | 6 | -0.683581 | 2.614508 | 2.406181 |
| 13 | 6 | 1.193553 | 3.099421 | 0.943454 |
| 14 | 6 | 2.116448 | 2.484702 | -0.098649 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 15 | 8 | 1.856093 | 1.326742 | -0.552651 |
| 16 | 6 | 3.100589 | -1.178268 | 0.962093 |
| 17 | 6 | 2.507708 | -2.092717 | -0.097722 |
| 18 | 8 | 1.359915 | -1.821883 | -0.578654 |
| 19 | 6 | -1.194442 | -3.079045 | 0.948250 |
| 20 | 6 | -2.125359 | -2.477036 | -0.092433 |
| 21 | 8 | -1.864418 | -1.322991 | -0.561757 |
| 22 | 6 | -3.097710 | 1.202125 | 0.948649 |
| 23 | 6 | -2.490380 | 2.111761 | -0.108336 |
| 24 | 8 | -1.339769 | 1.838866 | -0.574652 |
| 25 | 1 | 0.895706 | 1.156277 | 3.666175 |
| 26 | 1 | 1.958551 | 2.518482 | 3.354219 |
| 27 | 1 | 3.228041 | 1.183929 | 1.681510 |
| 28 | 1 | 3.238723 | 0.454571 | 3.280644 |
| 29 | 1 | 1.136368 | -0.896762 | 3.668799 |
| 30 | 1 | 2.499393 | -1.958669 | 3.357790 |
| 31 | 1 | 1.171134 | -3.211142 | 1.662017 |
| 32 | 1 | 0.438294 | -3.241245 | 3.259568 |
| 33 | 1 | -0.903312 | -1.127326 | 3.664212 |
| 34 | 1 | -1.964076 | -2.491372 | 3.352912 |
| 35 | 1 | -3.232633 | -1.158720 | 1.675883 |
| 36 | 1 | -3.246077 | -0.427478 | 3.273954 |
| 37 | 1 | -1.146089 | 0.925017 | 3.665596 |
| 38 | 1 | -2.508435 | 1.985676 | 3.347307 |
| 39 | 1 | -1.174233 | 3.238164 | 1.657258 |
| 40 | 1 | -0.446296 | 3.267630 | 3.257094 |
| 41 | 1 | 0.395046 | 3.593903 | 0.382217 |
| 42 | 1 | 3.601192 | -0.375624 | 0.412481 |
| 43 | 1 | -0.394838 | -3.568668 | 0.384007 |
| 44 | 1 | -3.598885 | 0.399521 | 0.399572 |
| 45 | 8 | -0.037165 | -0.222221 | -2.318847 |
| 46 | 1 | 0.615808 | -0.925303 | -2.482925 |
| 47 | 1 | -0.900405 | -0.626491 | -2.513144 |
| 48 | 7 | -3.217281 | 3.120989 | -0.536482 |
| 49 | 7 | -3.135832 | -3.208138 | -0.507341 |
| 50 | 7 | 3.239476 | -3.099747 | -0.518434 |
| 51 | 7 | 3.124934 | 3.213647 | -0.525755 |
| 52 | 1 | -4.157524 | 3.378246 | -0.176735 |
| 53 | 1 | -3.382728 | -4.152378 | -0.148504 |
| 54 | 1 | 4.177147 | -3.358119 | -0.150148 |
| 55 | 1 | 3.371939 | 4.159746 | -0.174700 |
| 56 | 6 | 4.056290 | 2.895319 | -1.600624 |
| 57 | 1 | 3.520914 | 2.713790 | -2.537969 |
| 58 | 6 | -2.905549 | 4.039582 | -1.624264 |
| 59 | 1 | -2.738695 | 3.493709 | -2.558279 |
| 60 | 6 | -4.071586 | -2.899731 | -1.581572 |
| 61 | 1 | -4.651322 | -2.000871 | -1.348843 |
| 62 | 6 | 2.937949 | -4.021406 | -1.606765 |
| 63 | 1 | 2.785673 | -3.478538 | -2.545086 |
| 64 | 1 | -2.001542 | 4.615761 | -1.402516 |
| 65 | 1 | 4.636488 | 1.998015 | -1.362572 |
| 66 | 1 | 2.029223 | -4.593190 | -1.393765 |
| 67 | 1 | -3.540115 | -2.726789 | -2.522816 |
| 68 | 6 | 4.171968 | -4.979967 | -1.718159 |
| 69 | 8 | 5.095143 | -4.748869 | -0.876427 |
| 70 | 8 | 4.104563 | -5.850184 | -2.611009 |
| 71 | 6 | 5.004569 | 4.134454 | -1.737265 |
| 72 | 8 | 4.763357 | 5.075640 | -0.918799 |
| 73 | 8 | 5.879494 | 4.053524 | -2.624941 |
| 74 | 6 | -4.140016 | 4.994647 | -1.755309 |
| 75 | 8 | -5.072708 | 4.767732 | -0.923045 |
| 76 | 8 | -4.064399 | 5.860140 | -2.652586 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 77 | 6 | -5.018309 | -4.141995 | -1.702490 |
| 78 | 8 | -4.770724 | -5.074476 | -0.875892 |
| 79 | 8 | -5.896834 | -4.070963 | -2.586935 |
| 80 | 64 | 0.000273 | 0.015155 | 0.177742 |
| 81 | 1 | -1.703979 | -3.842710 | 1.549902 |
| 82 | 1 | -3.852259 | 1.728667 | 1.547224 |
| 83 | 1 | 1.712206 | 3.860353 | 1.540917 |
| 84 | 1 | 3.854082 | -1.699614 | 1.566448 |

E(RTPSSh) = -2389.8881476 Hartree

Zero-point correction = 0.669060 Hartree/particle

Sum of electronic and thermal Energies = -2389.171748 Hartree

Sum of electronic and thermal Enthalpies = -2389.170804 Hartree

Sum of electronic and thermal Free Energies = -2389.303648 Hartree

Table S66. [Tb(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -0.532165 | -2.065134 | 1.808101 |
| 2 | 6 | -1.466916 | -1.657363 | 2.898053 |
| 3 | 6 | -2.582797 | -0.729119 | 2.431570 |
| 4 | 7 | -2.054962 | 0.526274 | 1.816978 |
| 5 | 6 | -1.642130 | 1.467340 | 2.899029 |
| 6 | 6 | -0.715693 | 2.578053 | 2.417209 |
| 7 | 7 | 0.538173 | 2.041834 | 1.806758 |
| 8 | 6 | 1.475832 | 1.633708 | 2.894588 |
| 9 | 6 | 2.590904 | 0.706517 | 2.424264 |
| 10 | 7 | 2.060262 | -0.547236 | 1.809998 |
| 11 | 6 | 1.651918 | -1.490440 | 2.892350 |
| 12 | 6 | 0.723370 | -2.601434 | 2.414170 |
| 13 | 6 | -1.146109 | -3.108735 | 0.948669 |
| 14 | 6 | -2.073141 | -2.501625 | -0.093725 |
| 15 | 8 | -1.827932 | -1.336814 | -0.538363 |
| 16 | 6 | -3.110858 | 1.132653 | 0.967408 |
| 17 | 6 | -2.526110 | 2.049364 | -0.094432 |
| 18 | 8 | -1.371631 | 1.792189 | -0.567083 |
| 19 | 6 | 1.148744 | 3.091141 | 0.951772 |
| 20 | 6 | 2.082369 | 2.496369 | -0.090114 |
| 21 | 8 | 1.834943 | 1.335599 | -0.550134 |
| 22 | 6 | 3.109452 | -1.153984 | 0.952304 |
| 23 | 6 | 2.509116 | -2.067144 | -0.105106 |
| 24 | 8 | 1.351974 | -1.807945 | -0.562967 |
| 25 | 1 | -0.876070 | -1.167122 | 3.675312 |
| 26 | 1 | -1.917224 | -2.545910 | 3.362334 |
| 27 | 1 | -3.208647 | -1.230174 | 1.691652 |
| 28 | 1 | -3.228840 | -0.499237 | 3.289763 |
| 29 | 1 | -1.148277 | 0.881762 | 3.677993 |
| 30 | 1 | -2.527644 | 1.921851 | 3.364848 |
| 31 | 1 | -1.217965 | 3.194162 | 1.669665 |
| 32 | 1 | -0.483611 | 3.235518 | 3.266068 |
| 33 | 1 | 0.886945 | 1.141848 | 3.672226 |
| 34 | 1 | 1.925797 | 2.522332 | 3.358898 |
| 35 | 1 | 3.214999 | 1.208118 | 1.683154 |
| 36 | 1 | 3.239404 | 0.475969 | 3.280436 |
| 37 | 1 | 1.161481 | -0.906005 | 3.674367 |
| 38 | 1 | 2.539879 | -1.945058 | 3.353430 |
| 39 | 1 | 1.223085 | -3.218151 | 1.665491 |
| 40 | 1 | 0.494599 | -3.258054 | 3.264638 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 41 | 1 | -0.340947 | -3.593552 | 0.388662 |
| 42 | 1 | -3.602149 | 0.322757 | 0.420174 |
| 43 | 1 | 0.342329 | 3.571549 | 0.389463 |
| 44 | 1 | 3.600660 | -0.344500 | 0.404475 |
| 45 | 8 | 0.030348 | 0.200195 | -2.287880 |
| 46 | 1 | -0.624489 | 0.901214 | -2.453054 |
| 47 | 1 | 0.891735 | 0.604671 | -2.489076 |
| 48 | 7 | 3.246219 | -3.065193 | -0.541833 |
| 49 | 7 | 3.080966 | 3.237917 | -0.514944 |
| 50 | 7 | -3.269237 | 3.043726 | -0.524960 |
| 51 | 7 | -3.069523 | -3.241661 | -0.530042 |
| 52 | 1 | 4.192915 | -3.310104 | -0.190597 |
| 53 | 1 | 3.315684 | 4.188599 | -0.165067 |
| 54 | 1 | -4.213249 | 3.289813 | -0.164499 |
| 55 | 1 | -3.302940 | -4.194533 | -0.188303 |
| 56 | 6 | -4.000101 | -2.928922 | -1.607248 |
| 57 | 1 | -3.462664 | -2.729934 | -2.539831 |
| 58 | 6 | 2.939622 | -3.982711 | -1.632012 |
| 59 | 1 | 2.756259 | -3.434533 | -2.561534 |
| 60 | 6 | 4.014906 | 2.934916 | -1.592323 |
| 61 | 1 | 4.609850 | 2.047056 | -1.355766 |
| 62 | 6 | -2.974860 | 3.962906 | -1.617373 |
| 63 | 1 | -2.807286 | 3.416434 | -2.550961 |
| 64 | 1 | 2.046613 | -4.574151 | -1.405833 |
| 65 | 1 | -4.596374 | -2.043511 | -1.364356 |
| 66 | 1 | -2.077030 | 4.550775 | -1.401946 |
| 67 | 1 | 3.480533 | 2.745902 | -2.528794 |
| 68 | 6 | -4.223258 | 4.900719 | -1.743677 |
| 69 | 8 | -5.148784 | 4.659804 | -0.907322 |
| 70 | 8 | -4.163159 | 5.766512 | -2.641330 |
| 71 | 6 | -4.927120 | -4.182043 | -1.760472 |
| 72 | 8 | -4.673954 | -5.127268 | -0.950357 |
| 73 | 8 | -5.799318 | -4.106613 | -2.651335 |
| 74 | 6 | 4.187436 | -4.917890 | -1.778675 |
| 75 | 8 | 5.123817 | -4.680781 | -0.953459 |
| 76 | 8 | 4.117144 | -5.780043 | -2.679609 |
| 77 | 6 | 4.941763 | 4.190401 | -1.729368 |
| 78 | 8 | 4.684124 | 5.126434 | -0.909909 |
| 79 | 8 | 5.816693 | 4.124824 | -2.617788 |
| 80 | 65 | 0.000115 | -0.014821 | 0.196065 |
| 81 | 1 | 1.652377 | 3.860971 | 1.550491 |
| 82 | 1 | 3.870894 | -1.673927 | 1.547866 |
| 83 | 1 | -1.657861 | -3.876155 | 1.543730 |
| 84 | 1 | -3.870531 | 1.648157 | 1.568979 |

E(RTPSSh) = -2390.4784054 Hartree

Zero-point correction = 0.669136 Hartree/particle

Sum of electronic and thermal Energies = -2389.761947 Hartree

Sum of electronic and thermal Enthalpies = -2389.761003 Hartree

Sum of electronic and thermal Free Energies = -2389.894084 Hartree

Table S67. [Dy(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | 0.507766 | 2.066079 | 1.815528 |
| 2 | 6 | 1.447456 | 1.671507 | 2.906039 |
| 3 | 6 | 2.573361 | 0.756094 | 2.439263 |
| 4 | 7 | 2.057368 | -0.503587 | 1.823861 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 5 | 6 | 1.657649 | -1.450087 | 2.905940 |
| 6 | 6 | 0.744118 | -2.570591 | 2.423055 |
| 7 | 7 | -0.514218 | -2.045949 | 1.812213 |
| 8 | 6 | -1.457104 | -1.651884 | 2.900593 |
| 9 | 6 | -2.582085 | -0.737263 | 2.430287 |
| 10 | 7 | -2.063286 | 0.521478 | 1.816599 |
| 11 | 6 | -1.668259 | 1.469003 | 2.900001 |
| 12 | 6 | -0.752502 | 2.590261 | 2.422021 |
| 13 | 6 | 1.110269 | 3.113818 | 0.953092 |
| 14 | 6 | 2.039632 | 2.511460 | -0.089631 |
| 15 | 8 | 1.805487 | 1.341185 | -0.525725 |
| 16 | 6 | 3.117091 | -1.098222 | 0.970985 |
| 17 | 6 | 2.536824 | -2.015928 | -0.092057 |
| 18 | 8 | 1.376648 | -1.768833 | -0.556307 |
| 19 | 6 | -1.113124 | -3.098644 | 0.953332 |
| 20 | 6 | -2.047975 | -2.507986 | -0.089375 |
| 21 | 8 | -1.810128 | -1.341746 | -0.540804 |
| 22 | 6 | -3.116328 | 1.117369 | 0.956199 |
| 23 | 6 | -2.520223 | 2.032805 | -0.101234 |
| 24 | 8 | -1.357642 | 1.783926 | -0.550921 |
| 25 | 1 | 0.862599 | 1.175126 | 3.683981 |
| 26 | 1 | 1.887033 | 2.566064 | 3.368982 |
| 27 | 1 | 3.194065 | 1.264335 | 1.699919 |
| 28 | 1 | 3.221817 | 0.531890 | 3.297089 |
| 29 | 1 | 1.157533 | -0.870919 | 3.685749 |
| 30 | 1 | 2.549105 | -1.894153 | 3.370429 |
| 31 | 1 | 1.253540 | -3.180985 | 1.675670 |
| 32 | 1 | 0.517943 | -3.231124 | 3.271075 |
| 33 | 1 | -0.874522 | -1.154465 | 3.679489 |
| 34 | 1 | -1.896503 | -2.546837 | 3.362802 |
| 35 | 1 | -3.200569 | -1.245469 | 1.688962 |
| 36 | 1 | -3.233501 | -0.513341 | 3.285951 |
| 37 | 1 | -1.171705 | 0.890176 | 3.682375 |
| 38 | 1 | -2.562239 | 1.912695 | 3.360022 |
| 39 | 1 | -1.259129 | 3.201912 | 1.673842 |
| 40 | 1 | -0.529866 | 3.249157 | 3.272290 |
| 41 | 1 | 0.299826 | 3.590726 | 0.394007 |
| 42 | 1 | 3.600883 | -0.282849 | 0.425292 |
| 43 | 1 | -0.301311 | -3.571140 | 0.392195 |
| 44 | 1 | -3.600019 | 0.302982 | 0.409046 |
| 45 | 8 | -0.026347 | -0.179761 | -2.262552 |
| 46 | 1 | 0.632938 | -0.876156 | -2.429689 |
| 47 | 1 | -0.885215 | -0.589914 | -2.463224 |
| 48 | 7 | -3.264620 | 3.021737 | -0.546065 |
| 49 | 7 | -3.037196 | -3.256533 | -0.523375 |
| 50 | 7 | 3.287665 | -3.000245 | -0.531856 |
| 51 | 7 | 3.026317 | 3.259241 | -0.534537 |
| 52 | 1 | -4.216709 | 3.256866 | -0.202742 |
| 53 | 1 | -3.263629 | -4.211932 | -0.180722 |
| 54 | 1 | 4.236826 | -3.237248 | -0.178702 |
| 55 | 1 | 3.249735 | 4.217334 | -0.200781 |
| 56 | 6 | 3.955615 | 2.949929 | -1.613882 |
| 57 | 1 | 3.416264 | 2.737494 | -2.542378 |
| 58 | 6 | -2.961248 | 3.937848 | -1.638374 |
| 59 | 1 | -2.764045 | 3.387613 | -2.563823 |
| 60 | 6 | -3.969682 | -2.956367 | -1.602858 |
| 61 | 1 | -4.574517 | -2.075961 | -1.363606 |
| 62 | 6 | 2.997244 | -3.917161 | -1.627280 |
| 63 | 1 | 2.817591 | -3.367930 | -2.556994 |
| 64 | 1 | -2.077485 | 4.541594 | -1.408400 |
| 65 | 1 | 4.563858 | 2.073703 | -1.367381 |
| 66 | 1 | 2.107820 | -4.516805 | -1.409487 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 67 | 1 | -3.433455 | -2.756619 | -2.536033 |
| 68 | 6 | 4.255882 | -4.839465 | -1.766208 |
| 69 | 8 | 5.183986 | -4.591368 | -0.934846 |
| 70 | 8 | 4.200186 | -5.701642 | -2.667577 |
| 71 | 6 | 4.866460 | 4.213130 | -1.780931 |
| 72 | 8 | 4.604900 | 5.161675 | -0.977399 |
| 73 | 8 | 5.735871 | 4.141268 | -2.674800 |
| 74 | 6 | -4.219533 | 4.856566 | -1.798943 |
| 75 | 8 | -5.159361 | 4.611102 | -0.980128 |
| 76 | 8 | -4.152974 | 5.715575 | -2.703148 |
| 77 | 6 | -4.883164 | -4.220380 | -1.751187 |
| 78 | 8 | -4.618253 | -5.159161 | -0.937210 |
| 79 | 8 | -5.755883 | -4.157890 | -2.641960 |
| 80 | 66 | -0.000018 | 0.014903 | 0.211512 |
| 81 | 1 | -1.612636 | -3.873893 | 1.548477 |
| 82 | 1 | -3.882964 | 1.632640 | 1.549129 |
| 83 | 1 | 1.617210 | 3.886533 | 1.545378 |
| 84 | 1 | 3.881896 | -1.609808 | 1.569368 |

E(RTPSSh) = -2391.0648857 Hartree

Zero-point correction = 0.669280 Hartree/particle

Sum of electronic and thermal Energies = -2390.348330 Hartree

Sum of electronic and thermal Enthalpies = -2390.347386 Hartree

Sum of electronic and thermal Free Energies = -2390.480645 Hartree

Table S68. [Ho(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.486760 | 2.065896 | 1.822604 |
| 2 | 6 | 1.430503 | 1.682961 | 2.913589 |
| 3 | 6 | 2.564852 | 0.778565 | 2.446583 |
| 4 | 7 | 2.058680 | -0.484480 | 1.830376 |
| 5 | 6 | 1.670946 | -1.435856 | 2.912263 |
| 6 | 6 | 0.768246 | -2.564347 | 2.428390 |
| 7 | 7 | -0.493584 | -2.049027 | 1.817268 |
| 8 | 6 | -1.440959 | -1.667599 | 2.906030 |
| 9 | 6 | -2.574211 | -0.763688 | 2.435760 |
| 10 | 7 | -2.065202 | 0.499108 | 1.822670 |
| 11 | 6 | -1.682400 | 1.450427 | 2.906902 |
| 12 | 6 | -0.777357 | 2.580159 | 2.429230 |
| 13 | 6 | 1.079668 | 3.116709 | 0.957261 |
| 14 | 6 | 2.010549 | 2.517679 | -0.085636 |
| 15 | 8 | 1.785854 | 1.342504 | -0.513305 |
| 16 | 6 | 3.121106 | -1.068756 | 0.973883 |
| 17 | 6 | 2.543904 | -1.986961 | -0.089966 |
| 18 | 8 | 1.378546 | -1.748627 | -0.545925 |
| 19 | 6 | -1.082491 | -3.103951 | 0.954355 |
| 20 | 6 | -2.017881 | -2.515865 | -0.088866 |
| 21 | 8 | -1.788033 | -1.344745 | -0.531898 |
| 22 | 6 | -3.120947 | 1.085498 | 0.959171 |
| 23 | 6 | -2.527661 | 2.002549 | -0.098006 |
| 24 | 8 | -1.360150 | 1.762526 | -0.539592 |
| 25 | 1 | 0.850943 | 1.181268 | 3.692107 |
| 26 | 1 | 1.860746 | 2.582596 | 3.375419 |
| 27 | 1 | 3.181173 | 1.292864 | 1.707778 |
| 28 | 1 | 3.215279 | 0.559066 | 3.304078 |
| 29 | 1 | 1.165848 | -0.862630 | 3.693265 |
| 30 | 1 | 2.567605 | -1.871090 | 3.375068 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 31 | 1 | 1.283574 | -3.169833 | 1.681072 |
| 32 | 1 | 0.546941 | -3.227505 | 3.275595 |
| 33 | 1 | -0.864089 | -1.165574 | 3.686241 |
| 34 | 1 | -1.871253 | -2.568016 | 3.366171 |
| 35 | 1 | -3.187842 | -1.277379 | 1.694175 |
| 36 | 1 | -3.228107 | -0.545403 | 3.290934 |
| 37 | 1 | -1.181021 | 0.876757 | 3.690010 |
| 38 | 1 | -2.581668 | 1.884809 | 3.365466 |
| 39 | 1 | -1.289587 | 3.187435 | 1.681313 |
| 40 | 1 | -0.559964 | 3.240993 | 3.279284 |
| 41 | 1 | 0.264785 | 3.586865 | 0.398987 |
| 42 | 1 | 3.597869 | -0.248508 | 0.429376 |
| 43 | 1 | -0.266006 | -3.569363 | 0.394156 |
| 44 | 1 | -3.597682 | 0.266782 | 0.412439 |
| 45 | 8 | -0.022329 | -0.160842 | -2.239053 |
| 46 | 1 | 0.639067 | -0.855014 | -2.407203 |
| 47 | 1 | -0.879815 | -0.573997 | -2.439604 |
| 48 | 7 | -3.277754 | 2.983443 | -0.550836 |
| 49 | 7 | -2.999038 | -3.269638 | -0.531723 |
| 50 | 7 | 3.300876 | -2.962348 | -0.538806 |
| 51 | 7 | 2.988587 | 3.271573 | -0.539106 |
| 52 | 1 | -4.234488 | 3.210536 | -0.215064 |
| 53 | 1 | -3.219140 | -4.228978 | -0.195831 |
| 54 | 1 | 4.254621 | -3.191731 | -0.192870 |
| 55 | 1 | 3.203983 | 4.234027 | -0.212719 |
| 56 | 6 | 3.916377 | 2.964029 | -1.620317 |
| 57 | 1 | 3.375258 | 2.739929 | -2.545021 |
| 58 | 6 | -2.975905 | 3.898084 | -1.644863 |
| 59 | 1 | -2.766541 | 3.346032 | -2.566533 |
| 60 | 6 | -3.929973 | -2.970406 | -1.612872 |
| 61 | 1 | -4.542268 | -2.095918 | -1.370911 |
| 62 | 6 | 3.012689 | -3.876865 | -1.636880 |
| 63 | 1 | 2.821861 | -3.325043 | -2.562821 |
| 64 | 1 | -2.099970 | 4.511762 | -1.411210 |
| 65 | 1 | 4.534324 | 2.095561 | -1.370467 |
| 66 | 1 | 2.130690 | -4.486460 | -1.416520 |
| 67 | 1 | -3.392017 | -2.761504 | -2.543041 |
| 68 | 6 | 4.279665 | -4.785788 | -1.788077 |
| 69 | 8 | 5.210581 | -4.531869 | -0.961621 |
| 70 | 8 | 4.226814 | -5.644528 | -2.692863 |
| 71 | 6 | 4.813866 | 4.235045 | -1.799838 |
| 72 | 8 | 4.545515 | 5.186729 | -1.002287 |
| 73 | 8 | 5.680803 | 4.165403 | -2.696277 |
| 74 | 6 | -4.242312 | 4.803263 | -1.818225 |
| 75 | 8 | -5.185449 | 4.551494 | -1.005157 |
| 76 | 8 | -4.178008 | 5.659269 | -2.725428 |
| 77 | 6 | -4.833240 | -4.240559 | -1.771542 |
| 78 | 8 | -4.562866 | -5.182456 | -0.962969 |
| 79 | 8 | -5.704247 | -4.179215 | -2.664032 |
| 80 | 67 | 0.000161 | 0.014988 | 0.226151 |
| 81 | 1 | -1.578689 | -3.884025 | 1.545857 |
| 82 | 1 | -3.892379 | 1.596777 | 1.549232 |
| 83 | 1 | 1.582740 | 3.893885 | 1.546895 |
| 84 | 1 | 3.890697 | -1.576970 | 1.568902 |

E(RTPSSh) = -2391.6490573 Hartree

Zero-point correction = 0.669478 Hartree/particle

Sum of electronic and thermal Energies = -2390.932377 Hartree

Sum of electronic and thermal Enthalpies = -2390.931433 Hartree

Sum of electronic and thermal Free Energies = -2391.064576 Hartree

Table S69. [Er(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.474576 | 2.064306 | 1.828349 |
| 2 | 6 | 1.420770 | 1.689301 | 2.919769 |
| 3 | 6 | 2.559605 | 0.791030 | 2.452649 |
| 4 | 7 | 2.057847 | -0.473369 | 1.836117 |
| 5 | 6 | 1.678117 | -1.427476 | 2.918158 |
| 6 | 6 | 0.781517 | -2.560233 | 2.433721 |
| 7 | 7 | -0.481691 | -2.049123 | 1.822402 |
| 8 | 6 | -1.431572 | -1.675875 | 2.911580 |
| 9 | 6 | -2.569292 | -0.778109 | 2.441214 |
| 10 | 7 | -2.064844 | 0.486346 | 1.828297 |
| 11 | 6 | -1.690024 | 1.440017 | 2.912993 |
| 12 | 6 | -0.791044 | 2.574177 | 2.435122 |
| 13 | 6 | 1.062206 | 3.115577 | 0.959853 |
| 14 | 6 | 1.992147 | 2.515859 | -0.083085 |
| 15 | 8 | 1.771938 | 1.336878 | -0.502447 |
| 16 | 6 | 3.120543 | -1.052116 | 0.976257 |
| 17 | 6 | 2.542633 | -1.968755 | -0.088132 |
| 18 | 8 | 1.373128 | -1.734798 | -0.535913 |
| 19 | 6 | -1.065245 | -3.104238 | 0.956122 |
| 20 | 6 | -1.998869 | -2.515386 | -0.087798 |
| 21 | 8 | -1.772734 | -1.340448 | -0.522799 |
| 22 | 6 | -3.121077 | 1.067432 | 0.961824 |
| 23 | 6 | -2.527140 | 1.983389 | -0.095500 |
| 24 | 8 | -1.355821 | 1.747609 | -0.529173 |
| 25 | 1 | 0.844624 | 1.185029 | 3.699184 |
| 26 | 1 | 1.845612 | 2.592245 | 3.380112 |
| 27 | 1 | 3.173589 | 1.308487 | 1.714101 |
| 28 | 1 | 3.211172 | 0.573767 | 3.309788 |
| 29 | 1 | 1.170524 | -0.857926 | 3.700255 |
| 30 | 1 | 2.578092 | -1.857540 | 3.379341 |
| 31 | 1 | 1.300019 | -3.163116 | 1.686490 |
| 32 | 1 | 0.562453 | -3.224859 | 3.280300 |
| 33 | 1 | -0.858242 | -1.171402 | 3.692852 |
| 34 | 1 | -1.856498 | -2.579677 | 3.370061 |
| 35 | 1 | -3.180297 | -1.294826 | 1.699544 |
| 36 | 1 | -3.224612 | -0.562465 | 3.295908 |
| 37 | 1 | -1.186141 | 0.869751 | 3.697004 |
| 38 | 1 | -2.592582 | 1.869082 | 3.370080 |
| 39 | 1 | -1.306343 | 3.178989 | 1.687314 |
| 40 | 1 | -0.575972 | 3.236275 | 3.284714 |
| 41 | 1 | 0.244863 | 3.582218 | 0.402314 |
| 42 | 1 | 3.593912 | -0.229277 | 0.432773 |
| 43 | 1 | -0.246224 | -3.566474 | 0.397082 |
| 44 | 1 | -3.594483 | 0.246292 | 0.415907 |
| 45 | 8 | -0.020265 | -0.144625 | -2.217689 |
| 46 | 1 | 0.640889 | -0.838827 | -2.386688 |
| 47 | 1 | -0.877875 | -0.557867 | -2.417597 |
| 48 | 7 | -3.279055 | 2.959129 | -0.556221 |
| 49 | 7 | -2.974867 | -3.270675 | -0.539072 |
| 50 | 7 | 3.301616 | -2.938494 | -0.545471 |
| 51 | 7 | 2.965075 | 3.271427 | -0.544536 |
| 52 | 1 | -4.239031 | 3.182462 | -0.227246 |
| 53 | 1 | -3.192277 | -4.232879 | -0.209527 |
| 54 | 1 | 4.258720 | -3.164276 | -0.206344 |
| 55 | 1 | 3.177033 | 4.236885 | -0.224843 |
| 56 | 6 | 3.890958 | 2.961403 | -1.626727 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 57 | 1 | 3.348007 | 2.729423 | -2.548399 |
| 58 | 6 | -2.975167 | 3.871377 | -1.651731 |
| 59 | 1 | -2.757074 | 3.317066 | -2.570000 |
| 60 | 6 | -3.903389 | -2.969078 | -1.621699 |
| 61 | 1 | -4.519422 | -2.097892 | -1.377294 |
| 62 | 6 | 3.011590 | -3.850316 | -1.645364 |
| 63 | 1 | 2.812579 | -3.296012 | -2.568089 |
| 64 | 1 | -2.103939 | 4.490531 | -1.414874 |
| 65 | 1 | 4.513352 | 2.097052 | -1.373588 |
| 66 | 1 | 2.134025 | -4.465284 | -1.422209 |
| 67 | 1 | -3.363228 | -2.753706 | -2.549110 |
| 68 | 6 | 4.282410 | -4.752020 | -1.807425 |
| 69 | 8 | 5.216973 | -4.495781 | -0.985797 |
| 70 | 8 | 4.228633 | -5.607955 | -2.714802 |
| 71 | 6 | 4.782443 | 4.235185 | -1.816666 |
| 72 | 8 | 4.512272 | 5.190631 | -1.024244 |
| 73 | 8 | 5.647080 | 4.163830 | -2.715188 |
| 74 | 6 | -4.245263 | 4.769184 | -1.836398 |
| 75 | 8 | -5.192353 | 4.515026 | -1.028689 |
| 76 | 8 | -4.179624 | 5.622592 | -2.745950 |
| 77 | 6 | -4.801655 | -4.241651 | -1.789677 |
| 78 | 8 | -4.530068 | -5.186841 | -0.985361 |
| 79 | 8 | -5.670345 | -4.178810 | -2.684294 |
| 80 | 68 | 0.000170 | 0.015217 | 0.238934 |
| 81 | 1 | -1.561423 | -3.886596 | 1.544528 |
| 82 | 1 | -3.894918 | 1.578140 | 1.549128 |
| 83 | 1 | 1.564641 | 3.895201 | 1.546692 |
| 84 | 1 | 3.892624 | -1.560077 | 1.568175 |

E(RTPSSh) = -2392.2322841 Hartree

Zero-point correction = 0.669681 Hartree/particle

Sum of electronic and thermal Energies = -2391.515490 Hartree

Sum of electronic and thermal Enthalpies = -2391.514546 Hartree

Sum of electronic and thermal Free Energies = -2391.647366 Hartree

Table S70. [Tm(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.462736 | 2.062804 | 1.833815 |
| 2 | 6 | 1.411567 | 1.695193 | 2.925467 |
| 3 | 6 | 2.554695 | 0.803116 | 2.457747 |
| 4 | 7 | 2.057592 | -0.462800 | 1.840872 |
| 5 | 6 | 1.685686 | -1.419776 | 2.923043 |
| 6 | 6 | 0.795155 | -2.556638 | 2.437821 |
| 7 | 7 | -0.469661 | -2.049960 | 1.826456 |
| 8 | 6 | -1.422312 | -1.685239 | 2.916071 |
| 9 | 6 | -2.564205 | -0.793220 | 2.445697 |
| 10 | 7 | -2.064418 | 0.473187 | 1.833312 |
| 11 | 6 | -1.697432 | 1.428955 | 2.918788 |
| 12 | 6 | -0.804615 | 2.567643 | 2.440922 |
| 13 | 6 | 1.044744 | 3.115166 | 0.962883 |
| 14 | 6 | 1.973808 | 2.515747 | -0.080665 |
| 15 | 8 | 1.758332 | 1.333448 | -0.492824 |
| 16 | 6 | 3.120822 | -1.035804 | 0.977945 |
| 17 | 6 | 2.542703 | -1.951004 | -0.087208 |
| 18 | 8 | 1.369547 | -1.721238 | -0.527706 |
| 19 | 6 | -1.047406 | -3.105246 | 0.956617 |
| 20 | 6 | -1.979965 | -2.515830 | -0.087542 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 21 | 8 | -1.758178 | -1.337198 | -0.514727 |
| 22 | 6 | -3.121268 | 1.049064 | 0.964216 |
| 23 | 6 | -2.527184 | 1.964369 | -0.093228 |
| 24 | 8 | -1.352438 | 1.733191 | -0.519927 |
| 25 | 1 | 0.838749 | 1.188298 | 3.705643 |
| 26 | 1 | 1.831161 | 2.601248 | 3.384414 |
| 27 | 1 | 3.165871 | 1.323896 | 1.719204 |
| 28 | 1 | 3.207801 | 0.588200 | 3.314262 |
| 29 | 1 | 1.175718 | -0.853797 | 3.706197 |
| 30 | 1 | 2.588954 | -1.844711 | 3.382465 |
| 31 | 1 | 1.316897 | -3.156521 | 1.690419 |
| 32 | 1 | 0.578578 | -3.223084 | 3.283567 |
| 33 | 1 | -0.852485 | -1.178994 | 3.698775 |
| 34 | 1 | -1.842129 | -2.592601 | 3.372153 |
| 35 | 1 | -3.172374 | -1.312761 | 1.703653 |
| 36 | 1 | -3.221144 | -0.580505 | 3.299839 |
| 37 | 1 | -1.191102 | 0.861703 | 3.703424 |
| 38 | 1 | -2.603255 | 1.852519 | 3.374467 |
| 39 | 1 | -1.323145 | 3.169858 | 1.693239 |
| 40 | 1 | -0.592120 | 3.231012 | 3.290118 |
| 41 | 1 | 0.224793 | 3.578616 | 0.406588 |
| 42 | 1 | 3.590868 | -0.210270 | 0.435748 |
| 43 | 1 | -0.225674 | -3.563616 | 0.398446 |
| 44 | 1 | -3.591363 | 0.225563 | 0.419050 |
| 45 | 8 | -0.017889 | -0.131025 | -2.199442 |
| 46 | 1 | 0.641170 | -0.827018 | -2.369188 |
| 47 | 1 | -0.876292 | -0.541777 | -2.400849 |
| 48 | 7 | -3.281259 | 2.934934 | -0.561178 |
| 49 | 7 | -2.950655 | -3.272953 | -0.546900 |
| 50 | 7 | 3.303793 | -2.915123 | -0.552580 |
| 51 | 7 | 2.941158 | 3.273728 | -0.549743 |
| 52 | 1 | -4.243899 | 3.154906 | -0.237796 |
| 53 | 1 | -3.165492 | -4.237657 | -0.222993 |
| 54 | 1 | 4.263526 | -3.138097 | -0.218972 |
| 55 | 1 | 3.149699 | 4.241668 | -0.235440 |
| 56 | 6 | 3.864926 | 2.962494 | -1.633412 |
| 57 | 1 | 3.320017 | 2.723736 | -2.552187 |
| 58 | 6 | -2.975717 | 3.845295 | -1.657816 |
| 59 | 1 | -2.750811 | 3.289226 | -2.573373 |
| 60 | 6 | -3.877492 | -2.968851 | -1.630291 |
| 61 | 1 | -4.496481 | -2.100477 | -1.383370 |
| 62 | 6 | 3.012073 | -3.824575 | -1.654013 |
| 63 | 1 | 2.807129 | -3.268148 | -2.574169 |
| 64 | 1 | -2.108246 | 4.468771 | -1.418517 |
| 65 | 1 | 4.491913 | 2.102091 | -1.378163 |
| 66 | 1 | 2.137699 | -4.443372 | -1.428951 |
| 67 | 1 | -3.335786 | -2.747832 | -2.555485 |
| 68 | 6 | 4.285601 | -4.721022 | -1.824456 |
| 69 | 8 | 5.223092 | -4.463143 | -1.006702 |
| 70 | 8 | 4.230886 | -5.574911 | -2.733667 |
| 71 | 6 | 4.750160 | 4.239259 | -1.832404 |
| 72 | 8 | 4.478234 | 5.197349 | -1.043783 |
| 73 | 8 | 5.612243 | 4.167401 | -2.733345 |
| 74 | 6 | -4.248731 | 4.737068 | -1.851371 |
| 75 | 8 | -5.198805 | 4.480764 | -1.047853 |
| 76 | 8 | -4.182258 | 5.588327 | -2.762873 |
| 77 | 6 | -4.771571 | -4.243309 | -1.806221 |
| 78 | 8 | -4.498201 | -5.191684 | -1.006266 |
| 79 | 8 | -5.638991 | -4.178725 | -2.701933 |
| 80 | 69 | 0.000523 | 0.015269 | 0.250596 |
| 81 | 1 | -1.543039 | -3.890406 | 1.541767 |
| 82 | 1 | -3.897500 | 1.559045 | 1.549013 |

| | | | | |
|----|---|----------|-----------|----------|
| 83 | 1 | 1.546554 | 3.896940 | 1.547412 |
| 84 | 1 | 3.895318 | -1.543495 | 1.566958 |

E(RTPSSh) = -2392.8121598 Hartree
 Zero-point correction = 0.669890 Hartree/particle
 Sum of electronic and thermal Energies = -2392.095245 Hartree
 Sum of electronic and thermal Enthalpies = -2392.094301 Hartree
 Sum of electronic and thermal Free Energies = -2392.226685 Hartree

Table S71. [Yb(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | 0.450005 | 2.061915 | 1.839164 |
| 2 | 6 | 1.401813 | 1.702374 | 2.930705 |
| 3 | 6 | 2.549706 | 0.817261 | 2.462175 |
| 4 | 7 | 2.057872 | -0.450552 | 1.845420 |
| 5 | 6 | 1.694239 | -1.410116 | 2.927856 |
| 6 | 6 | 0.810815 | -2.551914 | 2.442019 |
| 7 | 7 | -0.455933 | -2.050717 | 1.830583 |
| 8 | 6 | -1.411388 | -1.694971 | 2.920504 |
| 9 | 6 | -2.558142 | -0.809623 | 2.450141 |
| 10 | 7 | -2.063903 | 0.459097 | 1.838542 |
| 11 | 6 | -1.704813 | 1.416711 | 2.924768 |
| 12 | 6 | -0.819226 | 2.560718 | 2.446865 |
| 13 | 6 | 1.025490 | 3.115771 | 0.965812 |
| 14 | 6 | 1.953960 | 2.517317 | -0.078445 |
| 15 | 8 | 1.743831 | 1.331583 | -0.483229 |
| 16 | 6 | 3.121841 | -1.017627 | 0.979633 |
| 17 | 6 | 2.543778 | -1.932016 | -0.085827 |
| 18 | 8 | 1.366910 | -1.706925 | -0.518964 |
| 19 | 6 | -1.027176 | -3.106795 | 0.957559 |
| 20 | 6 | -1.959472 | -2.517755 | -0.086595 |
| 21 | 8 | -1.743051 | -1.335238 | -0.505897 |
| 22 | 6 | -3.122001 | 1.029549 | 0.967497 |
| 23 | 6 | -2.528474 | 1.944840 | -0.089866 |
| 24 | 8 | -1.350121 | 1.718901 | -0.509291 |
| 25 | 1 | 0.833055 | 1.192413 | 3.711855 |
| 26 | 1 | 1.815700 | 2.611740 | 3.388243 |
| 27 | 1 | 3.157497 | 1.341596 | 1.723359 |
| 28 | 1 | 3.204677 | 0.605287 | 3.317951 |
| 29 | 1 | 1.181100 | -0.848025 | 3.711746 |
| 30 | 1 | 2.600900 | -1.829070 | 3.386060 |
| 31 | 1 | 1.336221 | -3.148527 | 1.694563 |
| 32 | 1 | 0.597248 | -3.220126 | 3.287086 |
| 33 | 1 | -0.845536 | -1.186268 | 3.704504 |
| 34 | 1 | -1.825396 | -2.606009 | 3.374537 |
| 35 | 1 | -3.163087 | -1.332273 | 1.707641 |
| 36 | 1 | -3.216764 | -0.600457 | 3.303816 |
| 37 | 1 | -1.195088 | 0.852773 | 3.709608 |
| 38 | 1 | -2.613857 | 1.834005 | 3.379799 |
| 39 | 1 | -1.341547 | 3.160114 | 1.699559 |
| 40 | 1 | -0.609636 | 3.225270 | 3.295808 |
| 41 | 1 | 0.202569 | 3.575367 | 0.410802 |
| 42 | 1 | 3.588122 | -0.189440 | 0.438325 |
| 43 | 1 | -0.202520 | -3.560562 | 0.400013 |
| 44 | 1 | -3.588545 | 0.203701 | 0.422920 |
| 45 | 8 | -0.016920 | -0.118787 | -2.181834 |
| 46 | 1 | 0.642123 | -0.814751 | -2.351944 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 47 | 1 | -0.875336 | -0.530328 | -2.381749 |
| 48 | 7 | -3.285195 | 2.909748 | -0.564992 |
| 49 | 7 | -2.924174 | -3.277542 | -0.553822 |
| 50 | 7 | 3.307119 | -2.890491 | -0.558841 |
| 51 | 7 | 2.915146 | 3.278244 | -0.555234 |
| 52 | 1 | -4.250826 | 3.125395 | -0.247514 |
| 53 | 1 | -3.134827 | -4.245276 | -0.235992 |
| 54 | 1 | 4.269689 | -3.110080 | -0.230925 |
| 55 | 1 | 3.119309 | 4.249000 | -0.246684 |
| 56 | 6 | 3.836818 | 2.966843 | -1.640690 |
| 57 | 1 | 3.290022 | 2.719957 | -2.556171 |
| 58 | 6 | -2.978915 | 3.818533 | -1.662793 |
| 59 | 1 | -2.745844 | 3.260970 | -2.575378 |
| 60 | 6 | -3.849616 | -2.972603 | -1.638233 |
| 61 | 1 | -4.473851 | -2.108783 | -1.388577 |
| 62 | 6 | 3.014188 | -3.798084 | -1.661554 |
| 63 | 1 | 2.802736 | -3.239966 | -2.579211 |
| 64 | 1 | -2.116378 | 4.447774 | -1.420730 |
| 65 | 1 | 4.470012 | 2.111643 | -1.383238 |
| 66 | 1 | 2.143518 | -4.421292 | -1.434301 |
| 67 | 1 | -3.306595 | -2.744124 | -2.560841 |
| 68 | 6 | 4.290933 | -4.688399 | -1.840367 |
| 69 | 8 | 5.231342 | -4.427910 | -1.026760 |
| 70 | 8 | 4.235673 | -5.540552 | -2.751139 |
| 71 | 6 | 4.713613 | 4.247877 | -1.849532 |
| 72 | 8 | 4.439149 | 5.208162 | -1.064439 |
| 73 | 8 | 5.572470 | 4.176829 | -2.753605 |
| 74 | 6 | -4.256032 | 4.702333 | -1.865902 |
| 75 | 8 | -5.208793 | 4.443090 | -1.066489 |
| 76 | 8 | -4.189793 | 5.551033 | -2.779791 |
| 77 | 6 | -4.736394 | -4.250954 | -1.823098 |
| 78 | 8 | -4.459679 | -5.202045 | -1.027499 |
| 79 | 8 | -5.602055 | -4.186402 | -2.720479 |
| 80 | 70 | 0.000806 | 0.015604 | 0.261071 |
| 81 | 1 | -1.521184 | -3.895126 | 1.539728 |
| 82 | 1 | -3.900659 | 1.537998 | 1.550316 |
| 83 | 1 | 1.526013 | 3.900071 | 1.547972 |
| 84 | 1 | 3.899029 | -1.524281 | 1.565902 |

E(RTPSSh) = -2393.3956217 Hartree

Zero-point correction = 0.670108 Hartree/particle

Sum of electronic and thermal Energies = -2392.678578 Hartree

Sum of electronic and thermal Enthalpies = -2392.677634 Hartree

Sum of electronic and thermal Free Energies = -2392.809527 Hartree

Table S72. [Lu(DOTA-(gly)₄(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | 0.425905 | 2.064065 | 1.842674 |
| 2 | 6 | 1.382555 | 1.718367 | 2.934361 |
| 3 | 6 | 2.539977 | 0.846342 | 2.465576 |
| 4 | 7 | 2.060512 | -0.426120 | 1.849041 |
| 5 | 6 | 1.710322 | -1.389867 | 2.932022 |
| 6 | 6 | 0.840412 | -2.541548 | 2.446012 |
| 7 | 7 | -0.431134 | -2.053282 | 1.834459 |
| 8 | 6 | -1.390796 | -1.711112 | 2.924876 |
| 9 | 6 | -2.547352 | -0.839098 | 2.454554 |
| 10 | 7 | -2.066013 | 0.434364 | 1.842922 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 11 | 6 | -1.719870 | 1.396228 | 2.929462 |
| 12 | 6 | -0.847863 | 2.550045 | 2.450994 |
| 13 | 6 | 0.988880 | 3.122491 | 0.966703 |
| 14 | 6 | 1.920799 | 2.530443 | -0.077837 |
| 15 | 8 | 1.722943 | 1.340405 | -0.476120 |
| 16 | 6 | 3.128673 | -0.981653 | 0.981057 |
| 17 | 6 | 2.556325 | -1.899358 | -0.084344 |
| 18 | 8 | 1.374967 | -1.685906 | -0.511340 |
| 19 | 6 | -0.990310 | -3.113997 | 0.959380 |
| 20 | 6 | -1.925463 | -2.531590 | -0.085610 |
| 21 | 8 | -1.720715 | -1.344794 | -0.498974 |
| 22 | 6 | -3.129057 | 0.992970 | 0.970350 |
| 23 | 6 | -2.542092 | 1.911888 | -0.087205 |
| 24 | 8 | -1.359395 | 1.698072 | -0.500671 |
| 25 | 1 | 0.820547 | 1.202802 | 3.716711 |
| 26 | 1 | 1.785572 | 2.633493 | 3.390081 |
| 27 | 1 | 3.141880 | 1.377246 | 1.726627 |
| 28 | 1 | 3.197629 | 0.641026 | 3.320874 |
| 29 | 1 | 1.191087 | -0.834200 | 3.716471 |
| 30 | 1 | 2.622583 | -1.797646 | 3.389176 |
| 31 | 1 | 1.372637 | -3.132303 | 1.698724 |
| 32 | 1 | 0.633673 | -3.212298 | 3.290708 |
| 33 | 1 | -0.831312 | -1.196508 | 3.709589 |
| 34 | 1 | -1.793665 | -2.627745 | 3.377646 |
| 35 | 1 | -3.146546 | -1.368433 | 1.712113 |
| 36 | 1 | -3.208418 | -0.636700 | 3.307917 |
| 37 | 1 | -1.203779 | 0.838712 | 3.714724 |
| 38 | 1 | -2.634292 | 1.802420 | 3.383747 |
| 39 | 1 | -1.377241 | 3.143702 | 1.704080 |
| 40 | 1 | -0.644597 | 3.217048 | 3.299493 |
| 41 | 1 | 0.160469 | 3.573126 | 0.412611 |
| 42 | 1 | 3.586756 | -0.148522 | 0.440431 |
| 43 | 1 | -0.160425 | -3.559656 | 0.403132 |
| 44 | 1 | -3.587459 | 0.162008 | 0.426719 |
| 45 | 8 | -0.015881 | -0.108629 | -2.167530 |
| 46 | 1 | 0.650542 | -0.797342 | -2.338231 |
| 47 | 1 | -0.870246 | -0.530047 | -2.364311 |
| 48 | 7 | -3.307462 | 2.866938 | -0.568211 |
| 49 | 7 | -2.880218 | -3.299782 | -0.559170 |
| 50 | 7 | 3.327510 | -2.848509 | -0.563167 |
| 51 | 7 | 2.871928 | 3.299819 | -0.561019 |
| 52 | 1 | -4.276794 | 3.072371 | -0.255295 |
| 53 | 1 | -3.081097 | -4.271148 | -0.245948 |
| 54 | 1 | 4.293933 | -3.058428 | -0.240162 |
| 55 | 1 | 3.066012 | 4.274132 | -0.257234 |
| 56 | 6 | 3.793930 | 2.994129 | -1.647817 |
| 57 | 1 | 3.247328 | 2.737512 | -2.560740 |
| 58 | 6 | -3.007157 | 3.775989 | -1.667445 |
| 59 | 1 | -2.764493 | 3.218449 | -2.577550 |
| 60 | 6 | -3.805646 | -3.000968 | -1.645317 |
| 61 | 1 | -4.440262 | -2.145130 | -1.394369 |
| 62 | 6 | 3.039561 | -3.756716 | -1.666698 |
| 63 | 1 | 2.818548 | -3.198873 | -2.582277 |
| 64 | 1 | -2.152618 | 4.415541 | -1.424053 |
| 65 | 1 | 4.437310 | 2.147060 | -1.388742 |
| 66 | 1 | 2.176441 | -4.389580 | -1.437339 |
| 67 | 1 | -3.262431 | -2.763056 | -2.565429 |
| 68 | 6 | 4.324989 | -4.633015 | -1.852829 |
| 69 | 8 | 5.265997 | -4.364154 | -1.042656 |
| 70 | 8 | 4.274861 | -5.483736 | -2.765202 |
| 71 | 6 | 4.655837 | 4.283949 | -1.864379 |
| 72 | 8 | 4.373040 | 5.244232 | -1.082268 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 73 | 8 | 5.512790 | 4.218654 | -2.770679 |
| 74 | 6 | -4.293308 | 4.644823 | -1.877963 |
| 75 | 8 | -5.246116 | 4.377270 | -1.081371 |
| 76 | 8 | -4.233022 | 5.491419 | -2.794207 |
| 77 | 6 | -4.677484 | -4.288493 | -1.837758 |
| 78 | 8 | -4.392546 | -5.239375 | -1.044826 |
| 79 | 8 | -5.541001 | -4.230139 | -2.737583 |
| 80 | 71 | 0.000846 | 0.016094 | 0.269455 |
| 81 | 1 | -1.478713 | -3.907315 | 1.539456 |
| 82 | 1 | -3.912811 | 1.495382 | 1.551532 |
| 83 | 1 | 1.483312 | 3.912380 | 1.546450 |
| 84 | 1 | 3.911121 | -1.482597 | 1.565199 |

E(RTPSSh) = -2393.9493149 Hartree

Zero-point correction = 0.670236 Hartree/particle

Sum of electronic and thermal Energies = -2393.232197 Hartree

Sum of electronic and thermal Enthalpies = -2393.231253 Hartree

Sum of electronic and thermal Free Energies = -2393.362962 Hartree

Table S73. [La(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.202542 | -1.752912 | 2.012427 |
| 2 | 6 | -0.274710 | -2.202297 | 3.087460 |
| 3 | 6 | 1.151324 | -2.422170 | 2.591993 |
| 4 | 7 | 1.769325 | -1.191199 | 2.014448 |
| 5 | 6 | 2.198971 | -0.269923 | 3.103447 |
| 6 | 6 | 2.426797 | 1.159493 | 2.621833 |
| 7 | 7 | 1.205245 | 1.779370 | 2.027188 |
| 8 | 6 | 0.277201 | 2.225589 | 3.102563 |
| 9 | 6 | -1.148831 | 2.444437 | 2.606894 |
| 10 | 7 | -1.763143 | 1.215830 | 2.020249 |
| 11 | 6 | -2.200383 | 0.289952 | 3.101002 |
| 12 | 6 | -2.425678 | -1.136340 | 2.609150 |
| 13 | 6 | -1.613344 | -2.907770 | 1.176996 |
| 14 | 6 | -2.347741 | -2.411375 | -0.062626 |
| 15 | 8 | -2.010605 | -1.294022 | -0.571563 |
| 16 | 6 | 2.937757 | -1.587554 | 1.191438 |
| 17 | 6 | 2.467737 | -2.298168 | -0.071734 |
| 18 | 8 | 1.354152 | -1.961598 | -0.590933 |
| 19 | 6 | 1.615253 | 2.931338 | 1.188666 |
| 20 | 6 | 2.340894 | 2.426692 | -0.054412 |
| 21 | 8 | 2.017180 | 1.298268 | -0.543097 |
| 22 | 6 | -2.920899 | 1.617044 | 1.185330 |
| 23 | 6 | -2.426879 | 2.330080 | -0.069059 |
| 24 | 8 | -1.302500 | 2.001347 | -0.564790 |
| 25 | 1 | -0.287383 | -1.446523 | 3.875685 |
| 26 | 1 | -0.636408 | -3.133531 | 3.545360 |
| 27 | 1 | 1.162633 | -3.193242 | 1.817215 |
| 28 | 1 | 1.760697 | -2.801751 | 3.423900 |
| 29 | 1 | 1.428636 | -0.286840 | 3.877314 |
| 30 | 1 | 3.121537 | -0.635000 | 3.576129 |
| 31 | 1 | 3.211884 | 1.176518 | 1.861695 |
| 32 | 1 | 2.790902 | 1.763287 | 3.464595 |
| 33 | 1 | 0.290199 | 1.468027 | 3.889292 |
| 34 | 1 | 0.637142 | 3.156375 | 3.563006 |
| 35 | 1 | -1.160831 | 3.220368 | 1.837142 |
| 36 | 1 | -1.760673 | 2.816978 | 3.440197 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 37 | 1 | -1.435143 | 0.302450 | 3.880127 |
| 38 | 1 | -3.126296 | 0.651501 | 3.569925 |
| 39 | 1 | -3.208919 | -1.148515 | 1.846867 |
| 40 | 1 | -2.791283 | -1.746766 | 3.446366 |
| 41 | 1 | -0.716390 | -3.434709 | 0.835736 |
| 42 | 1 | 3.469199 | -0.684444 | 0.875127 |
| 43 | 1 | 0.718342 | 3.461297 | 0.852234 |
| 44 | 1 | -3.453062 | 0.717017 | 0.861346 |
| 45 | 8 | -0.049268 | -0.379968 | -2.372991 |
| 46 | 1 | 0.567688 | -1.129140 | -2.460461 |
| 47 | 1 | -0.930567 | -0.755469 | -2.542653 |
| 48 | 7 | -3.208776 | 3.242980 | -0.600204 |
| 49 | 7 | 3.260449 | 3.203578 | -0.582025 |
| 50 | 7 | 3.254313 | -3.212673 | -0.590283 |
| 51 | 7 | -3.284215 | -3.180518 | -0.569308 |
| 52 | 1 | -4.121166 | 3.554406 | -0.211693 |
| 53 | 1 | 3.569911 | 4.117545 | -0.196186 |
| 54 | 1 | 4.155916 | -3.535018 | -0.183930 |
| 55 | 1 | -3.607144 | -4.083351 | -0.166332 |
| 56 | 6 | -4.064951 | -2.948004 | -1.777694 |
| 57 | 1 | -3.415154 | -2.888220 | -2.656756 |
| 58 | 6 | -2.987569 | 3.990914 | -1.831162 |
| 59 | 1 | -2.893059 | 3.314035 | -2.686249 |
| 60 | 6 | 4.025678 | 2.968583 | -1.799679 |
| 61 | 1 | 3.361595 | 2.874111 | -2.664780 |
| 62 | 6 | 3.048458 | -3.962042 | -1.823218 |
| 63 | 1 | 2.989169 | -3.287954 | -2.683830 |
| 64 | 1 | -4.624560 | -2.010209 | -1.703923 |
| 65 | 1 | -2.070042 | 4.584384 | -1.765418 |
| 66 | 1 | 4.610475 | 2.046710 | -1.718827 |
| 67 | 1 | 2.118513 | -4.537480 | -1.776807 |
| 68 | 6 | -4.233225 | 4.924958 | -2.001460 |
| 69 | 8 | -5.098187 | 4.822570 | -1.076232 |
| 70 | 8 | -4.232099 | 5.655405 | -3.014515 |
| 71 | 6 | 4.972305 | 4.205515 | -1.963825 |
| 72 | 8 | 4.860457 | 5.079230 | -1.048014 |
| 73 | 8 | 5.720609 | 4.189977 | -2.963758 |
| 74 | 6 | 4.281383 | -4.919010 | -1.958832 |
| 75 | 8 | 4.289101 | -5.657894 | -2.965336 |
| 76 | 8 | 5.127835 | -4.821962 | -1.016109 |
| 77 | 6 | -5.043878 | -4.164852 | -1.901199 |
| 78 | 8 | -4.931918 | -5.025640 | -0.973194 |
| 79 | 8 | -5.812138 | -4.148009 | -2.885426 |
| 80 | 57 | 0.004254 | 0.016772 | 0.230246 |
| 81 | 1 | -2.226097 | -3.620530 | 1.745192 |
| 82 | 1 | 3.640766 | -2.210572 | 1.760684 |
| 83 | 1 | 2.235304 | 3.642632 | 1.750992 |
| 84 | 1 | -3.628392 | 2.242254 | 1.746663 |

E(RTPSSh) = -2385.5707722 Hartree

Zero-point correction = 0.667737 Hartree/particle

Sum of electronic and thermal Energies = -2384.855077 Hartree

Sum of electronic and thermal Enthalpies = -2384.854133 Hartree

Sum of electronic and thermal Free Energies = -2384.990321 Hartree

Table S74. [Ce(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|------------------|------------------|-------------------------|---|---|
| | | X | Y | Z |
| | | | | |

| | | | | |
|----|---|-----------|-----------|-----------|
| 1 | 7 | -1.187570 | -1.759659 | 2.020346 |
| 2 | 6 | -0.260260 | -2.206846 | 3.096473 |
| 3 | 6 | 1.168148 | -2.412725 | 2.602879 |
| 4 | 7 | 1.771833 | -1.174581 | 2.025529 |
| 5 | 6 | 2.198482 | -0.253042 | 3.115144 |
| 6 | 6 | 2.412692 | 1.178219 | 2.633758 |
| 7 | 7 | 1.184489 | 1.783001 | 2.037079 |
| 8 | 6 | 0.255397 | 2.227794 | 3.111845 |
| 9 | 6 | -1.172211 | 2.432507 | 2.615755 |
| 10 | 7 | -1.771064 | 1.196729 | 2.028151 |
| 11 | 6 | -2.207081 | 0.270319 | 3.108637 |
| 12 | 6 | -2.418242 | -1.157774 | 2.616600 |
| 13 | 6 | -1.584842 | -2.911793 | 1.174826 |
| 14 | 6 | -2.318277 | -2.409189 | -0.062566 |
| 15 | 8 | -1.993194 | -1.279634 | -0.553065 |
| 16 | 6 | 2.938166 | -1.557905 | 1.193620 |
| 17 | 6 | 2.462124 | -2.268506 | -0.066988 |
| 18 | 8 | 1.336701 | -1.944689 | -0.569121 |
| 19 | 6 | 1.582570 | 2.931404 | 1.187879 |
| 20 | 6 | 2.309840 | 2.418579 | -0.050755 |
| 21 | 8 | 1.999413 | 1.278044 | -0.520156 |
| 22 | 6 | -2.925432 | 1.585119 | 1.182497 |
| 23 | 6 | -2.423240 | 2.298854 | -0.067913 |
| 24 | 8 | -1.287548 | 1.981600 | -0.545391 |
| 25 | 1 | -0.280835 | -1.454015 | 3.887453 |
| 26 | 1 | -0.616303 | -3.142622 | 3.549436 |
| 27 | 1 | 1.188026 | -3.183833 | 1.828418 |
| 28 | 1 | 1.781344 | -2.785289 | 3.435064 |
| 29 | 1 | 1.430538 | -0.277123 | 3.891315 |
| 30 | 1 | 3.125375 | -0.611966 | 3.583970 |
| 31 | 1 | 3.198655 | 1.202991 | 1.874864 |
| 32 | 1 | 2.768674 | 1.786992 | 3.476298 |
| 33 | 1 | 0.275038 | 1.473553 | 3.901731 |
| 34 | 1 | 0.609109 | 3.163332 | 3.567346 |
| 35 | 1 | -1.191640 | 3.208588 | 1.846411 |
| 36 | 1 | -1.789265 | 2.797768 | 3.448340 |
| 37 | 1 | -1.445444 | 0.289777 | 3.891247 |
| 38 | 1 | -3.137959 | 0.625792 | 3.572246 |
| 39 | 1 | -3.200853 | -1.177426 | 1.853939 |
| 40 | 1 | -2.777647 | -1.772917 | 3.452960 |
| 41 | 1 | -0.682133 | -3.427861 | 0.832332 |
| 42 | 1 | 3.458913 | -0.649322 | 0.875432 |
| 43 | 1 | 0.680566 | 3.450267 | 0.848014 |
| 44 | 1 | -3.446324 | 0.679664 | 0.855612 |
| 45 | 8 | -0.051255 | -0.336615 | -2.328280 |
| 46 | 1 | 0.567129 | -1.082929 | -2.428302 |
| 47 | 1 | -0.933155 | -0.714696 | -2.490155 |
| 48 | 7 | -3.207581 | 3.200571 | -0.613997 |
| 49 | 7 | 3.217111 | 3.198777 | -0.594049 |
| 50 | 7 | 3.253675 | -3.169637 | -0.600713 |
| 51 | 7 | -3.240813 | -3.183243 | -0.586336 |
| 52 | 1 | -4.128283 | 3.504136 | -0.238922 |
| 53 | 1 | 3.517495 | 4.121782 | -0.222585 |
| 54 | 1 | 4.165072 | -3.481727 | -0.207949 |
| 55 | 1 | -3.555453 | -4.095430 | -0.197455 |
| 56 | 6 | -4.018515 | -2.944067 | -1.795478 |
| 57 | 1 | -3.365497 | -2.866128 | -2.670731 |
| 58 | 6 | -2.976404 | 3.948630 | -1.843107 |
| 59 | 1 | -2.865186 | 3.271446 | -2.695941 |
| 60 | 6 | 3.982941 | 2.953975 | -1.809474 |
| 61 | 1 | 3.318653 | 2.840757 | -2.672167 |
| 62 | 6 | 3.042371 | -3.916154 | -1.834527 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 63 | 1 | 2.962275 | -3.239137 | -2.691123 |
| 64 | 1 | -4.589048 | -2.013681 | -1.712509 |
| 65 | 1 | -2.064761 | 4.549763 | -1.766224 |
| 66 | 1 | 4.576862 | 2.039135 | -1.716378 |
| 67 | 1 | 2.121551 | -4.505281 | -1.778786 |
| 68 | 6 | -4.227529 | 4.871969 | -2.030852 |
| 69 | 8 | -5.103886 | 4.762698 | -1.117180 |
| 70 | 8 | -4.219116 | 5.601583 | -3.044438 |
| 71 | 6 | 4.916945 | 4.197852 | -1.992446 |
| 72 | 8 | 4.795925 | 5.084163 | -1.089971 |
| 73 | 8 | 5.665622 | 4.174687 | -2.991904 |
| 74 | 6 | 4.287172 | -4.854645 | -1.990280 |
| 75 | 8 | 4.293164 | -5.588292 | -3.000530 |
| 76 | 8 | 5.143518 | -4.750128 | -1.057301 |
| 77 | 6 | -4.982874 | -4.170502 | -1.938493 |
| 78 | 8 | -4.864317 | -5.041533 | -1.020861 |
| 79 | 8 | -5.747492 | -4.150092 | -2.925376 |
| 80 | 58 | 0.003111 | 0.016163 | 0.262136 |
| 81 | 1 | -2.194158 | -3.634140 | 1.734413 |
| 82 | 1 | 3.650566 | -2.176968 | 1.755348 |
| 83 | 1 | 2.198267 | 3.652737 | 1.742004 |
| 84 | 1 | -3.643108 | 2.206068 | 1.735432 |

E(RTPSSh) = -2386.2222416 Hartree

Zero-point correction = 0.667943 Hartree/particle

Sum of electronic and thermal Energies = -2385.506442 Hartree

Sum of electronic and thermal Enthalpies = -2385.505498 Hartree

Sum of electronic and thermal Free Energies = -2385.641236 Hartree

Table S75. [Pr(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.153351 | -1.774704 | 2.030664 |
| 2 | 6 | -0.220761 | -2.209662 | 3.106945 |
| 3 | 6 | 1.210782 | -2.388991 | 2.613273 |
| 4 | 7 | 1.787932 | -1.139078 | 2.034168 |
| 5 | 6 | 2.203900 | -0.212330 | 3.123155 |
| 6 | 6 | 2.390847 | 1.222111 | 2.641006 |
| 7 | 7 | 1.150263 | 1.800371 | 2.043477 |
| 8 | 6 | 0.216991 | 2.234872 | 3.118588 |
| 9 | 6 | -1.214335 | 2.412292 | 2.623800 |
| 10 | 7 | -1.787697 | 1.163990 | 2.037157 |
| 11 | 6 | -2.211112 | 0.233379 | 3.118760 |
| 12 | 6 | -2.395775 | -1.198383 | 2.627762 |
| 13 | 6 | -1.527889 | -2.928373 | 1.177317 |
| 14 | 6 | -2.266387 | -2.427956 | -0.057589 |
| 15 | 8 | -1.964283 | -1.284707 | -0.531657 |
| 16 | 6 | 2.954372 | -1.499478 | 1.192649 |
| 17 | 6 | 2.477745 | -2.216249 | -0.063847 |
| 18 | 8 | 1.338733 | -1.914519 | -0.549634 |
| 19 | 6 | 1.525116 | 2.948540 | 1.183637 |
| 20 | 6 | 2.258860 | 2.434408 | -0.050400 |
| 21 | 8 | 1.971067 | 1.280338 | -0.501413 |
| 22 | 6 | -2.943988 | 1.528735 | 1.183933 |
| 23 | 6 | -2.443751 | 2.246988 | -0.064243 |
| 24 | 8 | -1.296447 | 1.950256 | -0.527389 |
| 25 | 1 | -0.255083 | -1.459035 | 3.899634 |
| 26 | 1 | -0.561687 | -3.152513 | 3.556799 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 27 | 1 | 1.244922 | -3.160448 | 1.839763 |
| 28 | 1 | 1.832411 | -2.748229 | 3.444988 |
| 29 | 1 | 1.439342 | -0.250277 | 3.902210 |
| 30 | 1 | 3.138688 | -0.555978 | 3.587684 |
| 31 | 1 | 3.176391 | 1.261264 | 1.882430 |
| 32 | 1 | 2.734104 | 1.839372 | 3.482550 |
| 33 | 1 | 0.251320 | 1.484163 | 3.911417 |
| 34 | 1 | 0.556129 | 3.178237 | 3.568904 |
| 35 | 1 | -1.248962 | 3.187423 | 1.854138 |
| 36 | 1 | -1.838600 | 2.765582 | 3.456092 |
| 37 | 1 | -1.451588 | 0.267505 | 3.903002 |
| 38 | 1 | -3.149065 | 0.574058 | 3.579125 |
| 39 | 1 | -3.178459 | -1.233083 | 1.865825 |
| 40 | 1 | -2.742133 | -1.820921 | 3.464080 |
| 41 | 1 | -0.615534 | -3.425915 | 0.833123 |
| 42 | 1 | 3.455168 | -0.581139 | 0.870636 |
| 43 | 1 | 0.613119 | 3.447209 | 0.840331 |
| 44 | 1 | -3.446107 | 0.613210 | 0.855885 |
| 45 | 8 | -0.048724 | -0.297575 | -2.286995 |
| 46 | 1 | 0.576768 | -1.036679 | -2.395706 |
| 47 | 1 | -0.927461 | -0.684290 | -2.446425 |
| 48 | 7 | -3.239328 | 3.130481 | -0.623363 |
| 49 | 7 | 3.147822 | 3.224806 | -0.608588 |
| 50 | 7 | 3.280203 | -3.099258 | -0.610986 |
| 51 | 7 | -3.168699 | -3.214964 | -0.596482 |
| 52 | 1 | -4.169534 | 3.418218 | -0.259374 |
| 53 | 1 | 3.430908 | 4.158935 | -0.251522 |
| 54 | 1 | 4.202165 | -3.394915 | -0.230215 |
| 55 | 1 | -3.464799 | -4.139192 | -0.221647 |
| 56 | 6 | -3.944483 | -2.977360 | -1.807234 |
| 57 | 1 | -3.288139 | -2.871952 | -2.677104 |
| 58 | 6 | -3.009109 | 3.877693 | -1.853193 |
| 59 | 1 | -2.875103 | 3.199239 | -2.701707 |
| 60 | 6 | 3.915505 | 2.977207 | -1.822314 |
| 61 | 1 | 3.251609 | 2.838783 | -2.681617 |
| 62 | 6 | 3.067619 | -3.847730 | -1.843424 |
| 63 | 1 | 2.965225 | -3.171146 | -2.697981 |
| 64 | 1 | -4.537333 | -2.061921 | -1.715134 |
| 65 | 1 | -2.110388 | 4.497016 | -1.768875 |
| 66 | 1 | 4.527234 | 2.075479 | -1.717519 |
| 67 | 1 | 2.158374 | -4.453539 | -1.777703 |
| 68 | 6 | -4.275844 | 4.775588 | -2.058824 |
| 69 | 8 | -5.159293 | 4.654441 | -1.153502 |
| 70 | 8 | -4.270901 | 5.499913 | -3.076197 |
| 71 | 6 | 4.824946 | 4.236043 | -2.025385 |
| 72 | 8 | 4.688413 | 5.133028 | -1.135733 |
| 73 | 8 | 5.572012 | 4.212675 | -3.026020 |
| 74 | 6 | 4.327378 | -4.763144 | -2.015461 |
| 75 | 8 | 4.334768 | -5.494972 | -3.026991 |
| 76 | 8 | 5.192622 | -4.644504 | -1.092410 |
| 77 | 6 | -4.878858 | -4.223978 | -1.973018 |
| 78 | 8 | -4.745670 | -5.104287 | -1.066310 |
| 79 | 8 | -5.637471 | -4.208052 | -2.964581 |
| 80 | 59 | 0.002160 | 0.017614 | 0.290184 |
| 81 | 1 | -2.126434 | -3.664850 | 1.729961 |
| 82 | 1 | 3.682607 | -2.106801 | 1.746723 |
| 83 | 1 | 2.129186 | 3.685868 | 1.729317 |
| 84 | 1 | -3.675917 | 2.138901 | 1.730041 |

E(RTPSSh) = -2386.8571702 Hartree

Zero-point correction = 0.668228 Hartree/particle

Sum of electronic and thermal Energies = -2386.141211 Hartree

Sum of electronic and thermal Enthalpies = -2386.140267 Hartree
 Sum of electronic and thermal Free Energies = -2386.275453 Hartree

Table S76. [Nd(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.138647 | -1.778470 | 2.037905 |
| 2 | 6 | -0.205658 | -2.213666 | 3.113458 |
| 3 | 6 | 1.226368 | -2.382741 | 2.618850 |
| 4 | 7 | 1.791988 | -1.127498 | 2.040033 |
| 5 | 6 | 2.207571 | -0.201703 | 3.129700 |
| 6 | 6 | 2.384524 | 1.233949 | 2.648477 |
| 7 | 7 | 1.138955 | 1.801720 | 2.051104 |
| 8 | 6 | 0.206449 | 2.235319 | 3.127039 |
| 9 | 6 | -1.226031 | 2.402938 | 2.633283 |
| 10 | 7 | -1.788847 | 1.149845 | 2.046673 |
| 11 | 6 | -2.209835 | 0.218796 | 3.128616 |
| 12 | 6 | -2.385328 | -1.213532 | 2.636924 |
| 13 | 6 | -1.505027 | -2.928527 | 1.176400 |
| 14 | 6 | -2.243555 | -2.420820 | -0.055160 |
| 15 | 8 | -1.949586 | -1.268959 | -0.513897 |
| 16 | 6 | 2.955136 | -1.478474 | 1.190353 |
| 17 | 6 | 2.471500 | -2.192741 | -0.064569 |
| 18 | 8 | 1.324128 | -1.898324 | -0.535589 |
| 19 | 6 | 1.505194 | 2.947191 | 1.184021 |
| 20 | 6 | 2.237812 | 2.426667 | -0.047778 |
| 21 | 8 | 1.958005 | 1.264839 | -0.483998 |
| 22 | 6 | -2.943764 | 1.505962 | 1.188123 |
| 23 | 6 | -2.439343 | 2.222282 | -0.059086 |
| 24 | 8 | -1.285163 | 1.932912 | -0.509914 |
| 25 | 1 | -0.244380 | -1.466256 | 3.909047 |
| 26 | 1 | -0.542391 | -3.160057 | 3.558926 |
| 27 | 1 | 1.265120 | -3.153321 | 1.844758 |
| 28 | 1 | 1.852177 | -2.737620 | 3.449228 |
| 29 | 1 | 1.445819 | -0.245147 | 3.911287 |
| 30 | 1 | 3.145806 | -0.541563 | 3.589974 |
| 31 | 1 | 3.169773 | 1.278866 | 1.890013 |
| 32 | 1 | 2.722755 | 1.854197 | 3.489763 |
| 33 | 1 | 0.246253 | 1.487005 | 3.921941 |
| 34 | 1 | 0.541872 | 3.181782 | 3.573490 |
| 35 | 1 | -1.266302 | 3.177777 | 1.863665 |
| 36 | 1 | -1.853265 | 2.751224 | 3.465371 |
| 37 | 1 | -1.451676 | 0.257383 | 3.914031 |
| 38 | 1 | -3.150340 | 0.555170 | 3.586832 |
| 39 | 1 | -3.168610 | -1.252907 | 1.875913 |
| 40 | 1 | -2.725793 | -1.840116 | 3.472559 |
| 41 | 1 | -0.589468 | -3.418408 | 0.829938 |
| 42 | 1 | 3.448809 | -0.556574 | 0.867874 |
| 43 | 1 | 0.589831 | 3.439001 | 0.840033 |
| 44 | 1 | -3.439712 | 0.587121 | 0.860307 |
| 45 | 8 | -0.048145 | -0.257888 | -2.250508 |
| 46 | 1 | 0.573780 | -0.998339 | -2.369581 |
| 47 | 1 | -0.928879 | -0.639246 | -2.412017 |
| 48 | 7 | -3.236717 | 3.096465 | -0.629898 |
| 49 | 7 | 3.117963 | 3.217699 | -0.618597 |
| 50 | 7 | 3.274991 | -3.066125 | -0.625113 |
| 51 | 7 | -3.137620 | -3.208293 | -0.606510 |
| 52 | 1 | -4.172995 | 3.377559 | -0.276330 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 53 | 1 | 3.394764 | 4.158177 | -0.273319 |
| 54 | 1 | 4.202999 | -3.356809 | -0.255012 |
| 55 | 1 | -3.427234 | -4.139531 | -0.243840 |
| 56 | 6 | -3.912464 | -2.962494 | -1.816267 |
| 57 | 1 | -3.255013 | -2.841607 | -2.683266 |
| 58 | 6 | -3.001952 | 3.838933 | -1.861766 |
| 59 | 1 | -2.852278 | 3.157059 | -2.704875 |
| 60 | 6 | 3.883429 | 2.962543 | -1.832184 |
| 61 | 1 | 3.217754 | 2.809228 | -2.687569 |
| 62 | 6 | 3.055381 | -3.811884 | -1.857981 |
| 63 | 1 | 2.941354 | -3.133268 | -2.709443 |
| 64 | 1 | -4.512934 | -2.053051 | -1.714750 |
| 65 | 1 | -2.110704 | 4.468247 | -1.772113 |
| 66 | 1 | 4.502737 | 2.066974 | -1.719433 |
| 67 | 1 | 2.150462 | -4.423382 | -1.785930 |
| 68 | 6 | -4.275922 | 4.722279 | -2.085149 |
| 69 | 8 | -5.166337 | 4.598064 | -1.187076 |
| 70 | 8 | -4.269063 | 5.439794 | -3.107298 |
| 71 | 6 | 4.782051 | 4.226284 | -2.052395 |
| 72 | 8 | 4.640675 | 5.132294 | -1.172670 |
| 73 | 8 | 5.526484 | 4.197490 | -3.054820 |
| 74 | 6 | 4.319254 | -4.718931 | -2.044408 |
| 75 | 8 | 4.321747 | -5.448141 | -3.057794 |
| 76 | 8 | 5.192440 | -4.596961 | -1.129268 |
| 77 | 6 | -4.836265 | -4.214715 | -1.998777 |
| 78 | 8 | -4.696893 | -5.104880 | -1.102641 |
| 79 | 8 | -5.593645 | -4.192981 | -2.991113 |
| 80 | 60 | 0.002926 | 0.018480 | 0.314767 |
| 81 | 1 | -2.101204 | -3.671861 | 1.722309 |
| 82 | 1 | 3.689812 | -2.084641 | 1.737069 |
| 83 | 1 | 2.107654 | 3.690441 | 1.723323 |
| 84 | 1 | -3.680680 | 2.114732 | 1.728980 |

E(RTPSSh) = -2387.4797495 Hartree

Zero-point correction = 0.668445 Hartree/particle

Sum of electronic and thermal Energies = -2386.763680 Hartree

Sum of electronic and thermal Enthalpies = -2386.762736 Hartree

Sum of electronic and thermal Free Energies = -2386.897563 Hartree

Table S77. [Sm(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.118796 | -1.785883 | 2.045588 |
| 2 | 6 | -0.187411 | -2.227856 | 3.119247 |
| 3 | 6 | 1.244732 | -2.383196 | 2.623098 |
| 4 | 7 | 1.795192 | -1.119448 | 2.048144 |
| 5 | 6 | 2.212455 | -0.199398 | 3.141589 |
| 6 | 6 | 2.377628 | 1.238482 | 2.665068 |
| 7 | 7 | 1.125773 | 1.793680 | 2.068588 |
| 8 | 6 | 0.196040 | 2.226753 | 3.146754 |
| 9 | 6 | -1.237265 | 2.383555 | 2.654264 |
| 10 | 7 | -1.785314 | 1.125472 | 2.064294 |
| 11 | 6 | -2.206502 | 0.193472 | 3.144884 |
| 12 | 6 | -2.370956 | -1.237928 | 2.649034 |
| 13 | 6 | -1.476093 | -2.926338 | 1.167991 |
| 14 | 6 | -2.212699 | -2.399504 | -0.055881 |
| 15 | 8 | -1.924970 | -1.234731 | -0.486381 |
| 16 | 6 | 2.952866 | -1.457250 | 1.186390 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 17 | 6 | 2.456589 | -2.160878 | -0.068845 |
| 18 | 8 | 1.296650 | -1.873716 | -0.514293 |
| 19 | 6 | 1.482057 | 2.935683 | 1.193043 |
| 20 | 6 | 2.209517 | 2.404964 | -0.036891 |
| 21 | 8 | 1.940339 | 1.231708 | -0.449044 |
| 22 | 6 | -2.935957 | 1.473320 | 1.197099 |
| 23 | 6 | -2.420337 | 2.186741 | -0.046421 |
| 24 | 8 | -1.254527 | 1.908084 | -0.473951 |
| 25 | 1 | -0.231269 | -1.488125 | 3.921842 |
| 26 | 1 | -0.520621 | -3.180213 | 3.554380 |
| 27 | 1 | 1.288856 | -3.150348 | 1.846002 |
| 28 | 1 | 1.876317 | -2.734832 | 3.450323 |
| 29 | 1 | 1.454816 | -0.251319 | 3.926772 |
| 30 | 1 | 3.154929 | -0.537119 | 3.594585 |
| 31 | 1 | 3.162750 | 1.292161 | 1.907197 |
| 32 | 1 | 2.708967 | 1.860941 | 3.507276 |
| 33 | 1 | 0.242202 | 1.480797 | 3.943641 |
| 34 | 1 | 0.528314 | 3.176308 | 3.588763 |
| 35 | 1 | -1.284212 | 3.159840 | 1.886594 |
| 36 | 1 | -1.869186 | 2.723086 | 3.486258 |
| 37 | 1 | -1.451249 | 0.235397 | 3.933033 |
| 38 | 1 | -3.150472 | 0.525084 | 3.599273 |
| 39 | 1 | -3.155406 | -1.281209 | 1.889555 |
| 40 | 1 | -2.703216 | -1.872237 | 3.481966 |
| 41 | 1 | -0.557445 | -3.406566 | 0.816846 |
| 42 | 1 | 3.440164 | -0.530989 | 0.867645 |
| 43 | 1 | 0.563244 | 3.421470 | 0.850439 |
| 44 | 1 | -3.425539 | 0.551851 | 0.867976 |
| 45 | 8 | -0.040255 | -0.196935 | -2.184762 |
| 46 | 1 | 0.568540 | -0.946791 | -2.312742 |
| 47 | 1 | -0.927021 | -0.560537 | -2.353641 |
| 48 | 7 | -3.216779 | 3.047826 | -0.637637 |
| 49 | 7 | 3.075247 | 3.195579 | -0.629454 |
| 50 | 7 | 3.258847 | -3.018079 | -0.654788 |
| 51 | 7 | -3.099525 | -3.179444 | -0.628395 |
| 52 | 1 | -4.163604 | 3.318270 | -0.304365 |
| 53 | 1 | 3.342644 | 4.145851 | -0.304029 |
| 54 | 1 | 4.195713 | -3.304417 | -0.303431 |
| 55 | 1 | -3.384655 | -4.120579 | -0.287849 |
| 56 | 6 | -3.873820 | -2.910978 | -1.833707 |
| 57 | 1 | -3.215838 | -2.768678 | -2.697008 |
| 58 | 6 | -2.969587 | 3.782654 | -1.871674 |
| 59 | 1 | -2.791402 | 3.095615 | -2.704940 |
| 60 | 6 | 3.832498 | 2.928661 | -1.845673 |
| 61 | 1 | 3.160871 | 2.749798 | -2.691357 |
| 62 | 6 | 3.026009 | -3.753495 | -1.891456 |
| 63 | 1 | 2.895737 | -3.067704 | -2.734809 |
| 64 | 1 | -4.478508 | -2.006665 | -1.713493 |
| 65 | 1 | -2.091037 | 4.427863 | -1.770272 |
| 66 | 1 | 4.465903 | 2.044385 | -1.722530 |
| 67 | 1 | 2.126342 | -4.371741 | -1.812391 |
| 68 | 6 | -4.253483 | 4.642170 | -2.128907 |
| 69 | 8 | -5.158964 | 4.512056 | -1.246851 |
| 70 | 8 | -4.238780 | 5.349266 | -3.158197 |
| 71 | 6 | 4.710549 | 4.200860 | -2.098018 |
| 72 | 8 | 4.564361 | 5.120889 | -1.233738 |
| 73 | 8 | 5.445760 | 4.164241 | -3.106952 |
| 74 | 6 | 4.293640 | -4.649554 | -2.104746 |
| 75 | 8 | 4.285990 | -5.370804 | -3.123684 |
| 76 | 8 | 5.180015 | -4.527571 | -1.202324 |
| 77 | 6 | -4.791297 | -4.163569 | -2.044255 |
| 78 | 8 | -4.646275 | -5.073114 | -1.168639 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 79 | 8 | -5.549514 | -4.123485 | -3.035299 |
| 80 | 62 | 0.006433 | 0.017458 | 0.356208 |
| 81 | 1 | -2.071533 | -3.679608 | 1.700753 |
| 82 | 1 | 3.693902 | -2.066977 | 1.720254 |
| 83 | 1 | 2.085725 | 3.684185 | 1.723489 |
| 84 | 1 | -3.678755 | 2.082065 | 1.729726 |

E (RTPSSh) = -2388.7016232 Hartree

Zero-point correction = 0.668791 Hartree/particle

Sum of electronic and thermal Energies = -2387.985379 Hartree

Sum of electronic and thermal Enthalpies = -2387.984435 Hartree

Sum of electronic and thermal Free Energies = -2388.118854 Hartree

Table S78. [Eu(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.112840 | -1.790117 | 2.048511 |
| 2 | 6 | -0.183723 | -2.238775 | 3.121101 |
| 3 | 6 | 1.248337 | -2.390316 | 2.624778 |
| 4 | 7 | 1.794889 | -1.123132 | 2.053805 |
| 5 | 6 | 2.214882 | -0.208254 | 3.150281 |
| 6 | 6 | 2.377872 | 1.230896 | 2.677849 |
| 7 | 7 | 1.124382 | 1.783798 | 2.082622 |
| 8 | 6 | 0.196749 | 2.216988 | 3.162330 |
| 9 | 6 | -1.236503 | 2.372834 | 2.670462 |
| 10 | 7 | -1.780317 | 1.114832 | 2.076514 |
| 11 | 6 | -2.204309 | 0.181415 | 3.154506 |
| 12 | 6 | -2.366627 | -1.248259 | 2.654031 |
| 13 | 6 | -1.467880 | -2.923986 | 1.161697 |
| 14 | 6 | -2.200976 | -2.385068 | -0.058700 |
| 15 | 8 | -1.913485 | -1.214409 | -0.473839 |
| 16 | 6 | 2.949324 | -1.456232 | 1.186269 |
| 17 | 6 | 2.445688 | -2.150961 | -0.070714 |
| 18 | 8 | 1.279717 | -1.865931 | -0.502164 |
| 19 | 6 | 1.478493 | 2.924638 | 1.204873 |
| 20 | 6 | 2.200449 | 2.389588 | -0.026239 |
| 21 | 8 | 1.935774 | 1.211148 | -0.426675 |
| 22 | 6 | -2.927565 | 1.463069 | 1.205246 |
| 23 | 6 | -2.404212 | 2.174844 | -0.035731 |
| 24 | 8 | -1.232410 | 1.900946 | -0.450024 |
| 25 | 1 | -0.228562 | -1.503560 | 3.927841 |
| 26 | 1 | -0.517722 | -3.193642 | 3.550006 |
| 27 | 1 | 1.293558 | -3.154784 | 1.845168 |
| 28 | 1 | 1.881291 | -2.743049 | 3.450420 |
| 29 | 1 | 1.458882 | -0.263346 | 3.936888 |
| 30 | 1 | 3.158450 | -0.547740 | 3.599597 |
| 31 | 1 | 3.162957 | 1.287911 | 1.920261 |
| 32 | 1 | 2.707385 | 1.852458 | 3.521362 |
| 33 | 1 | 0.243923 | 1.470661 | 3.958856 |
| 34 | 1 | 0.529644 | 3.166474 | 3.603922 |
| 35 | 1 | -1.284760 | 3.151340 | 1.905191 |
| 36 | 1 | -1.869915 | 2.708006 | 3.503023 |
| 37 | 1 | -1.450641 | 0.221631 | 3.944308 |
| 38 | 1 | -3.149326 | 0.512150 | 3.607262 |
| 39 | 1 | -3.151189 | -1.290207 | 1.894639 |
| 40 | 1 | -2.697057 | -1.886775 | 3.484402 |
| 41 | 1 | -0.548580 | -3.401416 | 0.808772 |
| 42 | 1 | 3.436384 | -0.528655 | 0.871451 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 43 | 1 | 0.559160 | 3.411044 | 0.864910 |
| 44 | 1 | -3.416789 | 0.542117 | 0.874544 |
| 45 | 8 | -0.034303 | -0.167278 | -2.153862 |
| 46 | 1 | 0.568926 | -0.920821 | -2.286549 |
| 47 | 1 | -0.923780 | -0.523948 | -2.323561 |
| 48 | 7 | -3.199023 | 3.029353 | -0.638314 |
| 49 | 7 | 3.056782 | 3.180717 | -0.631346 |
| 50 | 7 | 3.246772 | -2.998504 | -0.671811 |
| 51 | 7 | -3.084777 | -3.159155 | -0.643295 |
| 52 | 1 | -4.151795 | 3.293689 | -0.317134 |
| 53 | 1 | 3.318250 | 4.136358 | -0.316784 |
| 54 | 1 | 4.188343 | -3.282960 | -0.331236 |
| 55 | 1 | -3.369942 | -4.104613 | -0.314403 |
| 56 | 6 | -3.857544 | -2.877797 | -1.846690 |
| 57 | 1 | -3.198661 | -2.726276 | -2.707721 |
| 58 | 6 | -2.944622 | 3.759245 | -1.873882 |
| 59 | 1 | -2.749264 | 3.069087 | -2.700667 |
| 60 | 6 | 3.804809 | 2.910723 | -1.852646 |
| 61 | 1 | 3.126843 | 2.715255 | -2.689506 |
| 62 | 6 | 3.007575 | -3.724841 | -1.912670 |
| 63 | 1 | 2.867430 | -3.032932 | -2.749428 |
| 64 | 1 | -4.462715 | -1.975063 | -1.717538 |
| 65 | 1 | -2.074211 | 4.414377 | -1.766001 |
| 66 | 1 | 4.450347 | 2.035553 | -1.727319 |
| 67 | 1 | 2.111800 | -4.348434 | -1.831676 |
| 68 | 6 | -4.234305 | 4.603670 | -2.151599 |
| 69 | 8 | -5.148359 | 4.470106 | -1.278941 |
| 70 | 8 | -4.215180 | 5.303848 | -3.185511 |
| 71 | 6 | 4.664726 | 4.190949 | -2.126359 |
| 72 | 8 | 4.517779 | 5.116664 | -1.268295 |
| 73 | 8 | 5.388369 | 4.154204 | -3.143579 |
| 74 | 6 | 4.278329 | -4.612312 | -2.143419 |
| 75 | 8 | 4.266423 | -5.325306 | -3.168045 |
| 76 | 8 | 5.171290 | -4.492403 | -1.247211 |
| 77 | 6 | -4.774165 | -4.128644 | -2.071618 |
| 78 | 8 | -4.628489 | -5.047798 | -1.206161 |
| 79 | 8 | -5.532104 | -4.078172 | -3.062330 |
| 80 | 63 | 0.009383 | 0.016121 | 0.378065 |
| 81 | 1 | -2.065355 | -3.680994 | 1.686745 |
| 82 | 1 | 3.691401 | -2.070734 | 1.713122 |
| 83 | 1 | 2.085616 | 3.672788 | 1.731808 |
| 84 | 1 | -3.671523 | 2.073471 | 1.734296 |

E(RTPSSh) = -2389.2984991 Hartree

Zero-point correction = 0.668880 Hartree/particle

Sum of electronic and thermal Energies = -2388.582213 Hartree

Sum of electronic and thermal Enthalpies = -2388.581269 Hartree

Sum of electronic and thermal Free Energies = -2388.715821 Hartree

Table S79. [Gd(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | -1.109892 | -1.796873 | 2.049431 |
| 2 | 6 | -0.184094 | -2.251781 | 3.122055 |
| 3 | 6 | 1.248537 | -2.399823 | 2.627353 |
| 4 | 7 | 1.792556 | -1.129376 | 2.061359 |
| 5 | 6 | 2.213620 | -0.219675 | 3.161512 |
| 6 | 6 | 2.375200 | 1.220846 | 2.693653 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 7 | 7 | 1.120895 | 1.772178 | 2.098696 |
| 8 | 6 | 0.193808 | 2.204262 | 3.179138 |
| 9 | 6 | -1.238799 | 2.359850 | 2.686252 |
| 10 | 7 | -1.778199 | 1.102571 | 2.086853 |
| 11 | 6 | -2.206234 | 0.167013 | 3.161155 |
| 12 | 6 | -2.365961 | -1.260722 | 2.655269 |
| 13 | 6 | -1.461774 | -2.924636 | 1.153802 |
| 14 | 6 | -2.189846 | -2.374826 | -0.064448 |
| 15 | 8 | -1.902277 | -1.198933 | -0.465072 |
| 16 | 6 | 2.945332 | -1.457945 | 1.190245 |
| 17 | 6 | 2.437085 | -2.143005 | -0.069959 |
| 18 | 8 | 1.266081 | -1.860491 | -0.489709 |
| 19 | 6 | 1.474036 | 2.913014 | 1.220758 |
| 20 | 6 | 2.191172 | 2.375836 | -0.012097 |
| 21 | 8 | 1.931494 | 1.193165 | -0.403435 |
| 22 | 6 | -2.921242 | 1.452158 | 1.210789 |
| 23 | 6 | -2.389253 | 2.163572 | -0.026521 |
| 24 | 8 | -1.211938 | 1.893932 | -0.427982 |
| 25 | 1 | -0.230799 | -1.520847 | 3.932622 |
| 26 | 1 | -0.519319 | -3.208979 | 3.544694 |
| 27 | 1 | 1.295674 | -3.161415 | 1.845101 |
| 28 | 1 | 1.881551 | -2.754044 | 3.452246 |
| 29 | 1 | 1.458135 | -0.278032 | 3.948423 |
| 30 | 1 | 3.157631 | -0.560918 | 3.608492 |
| 31 | 1 | 3.160854 | 1.281181 | 1.936972 |
| 32 | 1 | 2.702382 | 1.841105 | 3.538965 |
| 33 | 1 | 0.240862 | 1.456678 | 3.974518 |
| 34 | 1 | 0.526732 | 3.153172 | 3.621850 |
| 35 | 1 | -1.287272 | 3.141093 | 1.923845 |
| 36 | 1 | -1.874507 | 2.690282 | 3.518888 |
| 37 | 1 | -1.455105 | 0.205066 | 3.953516 |
| 38 | 1 | -3.152821 | 0.496638 | 3.611343 |
| 39 | 1 | -3.149409 | -1.300825 | 1.894666 |
| 40 | 1 | -2.696070 | -1.903514 | 3.482391 |
| 41 | 1 | -0.541469 | -3.399719 | 0.800642 |
| 42 | 1 | 3.433296 | -0.529155 | 0.880818 |
| 43 | 1 | 0.554672 | 3.401027 | 0.883530 |
| 44 | 1 | -3.409893 | 0.532052 | 0.877233 |
| 45 | 8 | -0.026740 | -0.143906 | -2.126135 |
| 46 | 1 | 0.572098 | -0.900301 | -2.262506 |
| 47 | 1 | -0.918277 | -0.495338 | -2.296360 |
| 48 | 7 | -3.181289 | 3.013338 | -0.639187 |
| 49 | 7 | 3.038065 | 3.168706 | -0.627902 |
| 50 | 7 | 3.238594 | -2.979652 | -0.685356 |
| 51 | 7 | -3.069743 | -3.143701 | -0.661357 |
| 52 | 1 | -4.139362 | 3.272519 | -0.329659 |
| 53 | 1 | 3.292108 | 4.129531 | -0.323088 |
| 54 | 1 | 4.184980 | -3.260507 | -0.354981 |
| 55 | 1 | -3.355084 | -4.093062 | -0.343530 |
| 56 | 6 | -3.839214 | -2.850979 | -1.864204 |
| 57 | 1 | -3.178169 | -2.691214 | -2.722084 |
| 58 | 6 | -2.918120 | 3.740388 | -1.874655 |
| 59 | 1 | -2.707830 | 3.048552 | -2.696343 |
| 60 | 6 | 3.775370 | 2.898587 | -1.855740 |
| 61 | 1 | 3.090404 | 2.684728 | -2.682260 |
| 62 | 6 | 2.996539 | -3.693873 | -1.932731 |
| 63 | 1 | 2.844325 | -2.993846 | -2.760594 |
| 64 | 1 | -4.445225 | -1.949858 | -1.728108 |
| 65 | 1 | -2.054201 | 4.402794 | -1.759308 |
| 66 | 1 | 4.436053 | 2.034783 | -1.730207 |
| 67 | 1 | 2.107085 | -4.326535 | -1.852480 |
| 68 | 6 | -4.211073 | 4.573556 | -2.170674 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 69 | 8 | -5.134085 | 4.436157 | -1.308095 |
| 70 | 8 | -4.185402 | 5.269826 | -3.207063 |
| 71 | 6 | 4.612092 | 4.189225 | -2.151733 |
| 72 | 8 | 4.464736 | 5.118849 | -1.297987 |
| 73 | 8 | 5.320571 | 4.155548 | -3.179645 |
| 74 | 6 | 4.273713 | -4.566996 | -2.182857 |
| 75 | 8 | 4.261635 | -5.266948 | -3.216377 |
| 76 | 8 | 5.171334 | -4.450168 | -1.290918 |
| 77 | 6 | -4.754411 | -4.100343 | -2.103453 |
| 78 | 8 | -4.609527 | -5.027820 | -1.246763 |
| 79 | 8 | -5.510322 | -4.040861 | -3.095148 |
| 80 | 64 | 0.011763 | 0.013071 | 0.398213 |
| 81 | 1 | -2.062028 | -3.684802 | 1.670985 |
| 82 | 1 | 3.687091 | -2.077671 | 1.711390 |
| 83 | 1 | 2.084497 | 3.659708 | 1.745874 |
| 84 | 1 | -3.666713 | 2.063747 | 1.736282 |

E(RTPSSh) = -2389.8883268 Hartree

Zero-point correction = 0.668996 Hartree/particle

Sum of electronic and thermal Energies = -2389.171989 Hartree

Sum of electronic and thermal Enthalpies = -2389.171045 Hartree

Sum of electronic and thermal Free Energies = -2389.305377 Hartree

Table S80. [Tb(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.106082 | -1.797955 | 2.051189 |
| 2 | 6 | -0.182641 | -2.254266 | 3.124950 |
| 3 | 6 | 1.250566 | -2.397648 | 2.631740 |
| 4 | 7 | 1.789202 | -1.124738 | 2.066133 |
| 5 | 6 | 2.209944 | -0.216191 | 3.167114 |
| 6 | 6 | 2.367241 | 1.224529 | 2.699508 |
| 7 | 7 | 1.111153 | 1.769949 | 2.102659 |
| 8 | 6 | 0.184213 | 2.203294 | 3.182474 |
| 9 | 6 | -1.248031 | 2.354137 | 2.688237 |
| 10 | 7 | -1.780804 | 1.094361 | 2.088096 |
| 11 | 6 | -2.210672 | 0.159904 | 3.162347 |
| 12 | 6 | -2.365175 | -1.267905 | 2.656152 |
| 13 | 6 | -1.453756 | -2.923260 | 1.150996 |
| 14 | 6 | -2.178283 | -2.367393 | -0.066132 |
| 15 | 8 | -1.890845 | -1.188149 | -0.457223 |
| 16 | 6 | 2.940862 | -1.449908 | 1.192493 |
| 17 | 6 | 2.428494 | -2.131343 | -0.067596 |
| 18 | 8 | 1.253860 | -1.850741 | -0.479040 |
| 19 | 6 | 1.462011 | 2.908506 | 1.220874 |
| 20 | 6 | 2.178918 | 2.365070 | -0.008952 |
| 21 | 8 | 1.921104 | 1.178954 | -0.391069 |
| 22 | 6 | -2.921097 | 1.440570 | 1.207227 |
| 23 | 6 | -2.382262 | 2.149892 | -0.027817 |
| 24 | 8 | -1.201748 | 1.880504 | -0.420093 |
| 25 | 1 | -0.232336 | -1.525381 | 3.937247 |
| 26 | 1 | -0.517184 | -3.213122 | 3.544300 |
| 27 | 1 | 1.300856 | -3.159029 | 1.849492 |
| 28 | 1 | 1.884893 | -2.749373 | 3.456632 |
| 29 | 1 | 1.455407 | -0.276996 | 3.954810 |
| 30 | 1 | 3.155180 | -0.556029 | 3.612501 |
| 31 | 1 | 3.153759 | 1.287439 | 1.943957 |
| 32 | 1 | 2.690660 | 1.846845 | 3.544678 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 33 | 1 | 0.232762 | 1.457638 | 3.979632 |
| 34 | 1 | 0.515538 | 3.153886 | 3.622680 |
| 35 | 1 | -1.298238 | 3.135226 | 1.925790 |
| 36 | 1 | -1.886621 | 2.681963 | 3.519625 |
| 37 | 1 | -1.462081 | 0.200202 | 3.957059 |
| 38 | 1 | -3.159339 | 0.488222 | 3.609033 |
| 39 | 1 | -3.147840 | -1.310393 | 1.894880 |
| 40 | 1 | -2.693375 | -1.912894 | 3.482253 |
| 41 | 1 | -0.532293 | -3.396540 | 0.798825 |
| 42 | 1 | 3.428106 | -0.520388 | 0.884562 |
| 43 | 1 | 0.542176 | 3.394407 | 0.882299 |
| 44 | 1 | -3.407675 | 0.519667 | 0.873264 |
| 45 | 8 | -0.020497 | -0.124972 | -2.099761 |
| 46 | 1 | 0.570337 | -0.887314 | -2.237488 |
| 47 | 1 | -0.914726 | -0.465235 | -2.277375 |
| 48 | 7 | -3.169517 | 2.999047 | -0.647296 |
| 49 | 7 | 3.025114 | 3.153929 | -0.630690 |
| 50 | 7 | 3.228040 | -2.963785 | -0.690870 |
| 51 | 7 | -3.056021 | -3.132343 | -0.670958 |
| 52 | 1 | -4.129983 | 3.258326 | -0.345540 |
| 53 | 1 | 3.278008 | 4.117357 | -0.333419 |
| 54 | 1 | 4.177525 | -3.242890 | -0.367815 |
| 55 | 1 | -3.341793 | -4.084084 | -0.360644 |
| 56 | 6 | -3.822681 | -2.831235 | -1.873513 |
| 57 | 1 | -3.159661 | -2.665814 | -2.728797 |
| 58 | 6 | -2.896360 | 3.725070 | -1.881163 |
| 59 | 1 | -2.680265 | 3.032512 | -2.700726 |
| 60 | 6 | 3.762744 | 2.874661 | -1.856252 |
| 61 | 1 | 3.077982 | 2.653962 | -2.681119 |
| 62 | 6 | 2.980302 | -3.673863 | -1.939489 |
| 63 | 1 | 2.820338 | -2.971152 | -2.763619 |
| 64 | 1 | -4.428646 | -1.930825 | -1.732647 |
| 65 | 1 | -2.032704 | 4.386703 | -1.759596 |
| 66 | 1 | 4.423675 | 2.012067 | -1.723867 |
| 67 | 1 | 2.093506 | -4.309818 | -1.855971 |
| 68 | 6 | -4.186231 | 4.559116 | -2.187785 |
| 69 | 8 | -5.116615 | 4.421908 | -1.333121 |
| 70 | 8 | -4.151469 | 5.255688 | -3.223729 |
| 71 | 6 | 4.599034 | 4.163202 | -2.162265 |
| 72 | 8 | 4.450482 | 5.099847 | -1.316429 |
| 73 | 8 | 5.308280 | 4.121482 | -3.189382 |
| 74 | 6 | 4.258905 | -4.541481 | -2.201330 |
| 75 | 8 | 4.242267 | -5.238227 | -3.236927 |
| 76 | 8 | 5.162247 | -4.424039 | -1.315230 |
| 77 | 6 | -4.737508 | -4.078818 | -2.123320 |
| 78 | 8 | -4.593594 | -5.012629 | -1.273340 |
| 79 | 8 | -5.492074 | -4.012217 | -3.115577 |
| 80 | 65 | 0.010808 | 0.012014 | 0.411526 |
| 81 | 1 | -2.055625 | -3.685403 | 1.663310 |
| 82 | 1 | 3.683505 | -2.071450 | 1.710172 |
| 83 | 1 | 2.072570 | 3.657376 | 1.742696 |
| 84 | 1 | -3.668915 | 2.053051 | 1.728275 |

E(RTPSSh) = -2390.4781089 Hartree

Zero-point correction = 0.669161 Hartree/particle

Sum of electronic and thermal Energies = -2389.761678 Hartree

Sum of electronic and thermal Enthalpies = -2389.760733 Hartree

Sum of electronic and thermal Free Energies = -2389.894718 Hartree

Table S81. [Dy(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|------------------|------------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.110806 | -1.793172 | 2.053889 |
| 2 | 6 | -0.191656 | -2.255525 | 3.128503 |
| 3 | 6 | 1.241312 | -2.401958 | 2.636563 |
| 4 | 7 | 1.781367 | -1.129504 | 2.071379 |
| 5 | 6 | 2.207190 | -0.224401 | 3.172986 |
| 6 | 6 | 2.367656 | 1.215793 | 2.705802 |
| 7 | 7 | 1.112388 | 1.762156 | 2.108001 |
| 8 | 6 | 0.188122 | 2.200957 | 3.187689 |
| 9 | 6 | -1.243245 | 2.355028 | 2.692895 |
| 10 | 7 | -1.776592 | 1.096030 | 2.091669 |
| 11 | 6 | -2.212855 | 0.164236 | 3.165385 |
| 12 | 6 | -2.369969 | -1.262627 | 2.658245 |
| 13 | 6 | -1.459850 | -2.914151 | 1.149046 |
| 14 | 6 | -2.178150 | -2.349056 | -0.067141 |
| 15 | 8 | -1.886842 | -1.167149 | -0.447701 |
| 16 | 6 | 2.929574 | -1.457139 | 1.194384 |
| 17 | 6 | 2.408749 | -2.132448 | -0.065261 |
| 18 | 8 | 1.230924 | -1.849524 | -0.466410 |
| 19 | 6 | 1.466179 | 2.896945 | 1.222594 |
| 20 | 6 | 2.178767 | 2.344560 | -0.005478 |
| 21 | 8 | 1.917781 | 1.156036 | -0.377969 |
| 22 | 6 | -2.912443 | 1.445211 | 1.206383 |
| 23 | 6 | -2.363549 | 2.149681 | -0.026653 |
| 24 | 8 | -1.180495 | 1.876319 | -0.408557 |
| 25 | 1 | -0.240148 | -1.528212 | 3.942327 |
| 26 | 1 | -0.530463 | -3.214176 | 3.544846 |
| 27 | 1 | 1.290634 | -3.163398 | 1.854341 |
| 28 | 1 | 1.874981 | -2.754479 | 3.461560 |
| 29 | 1 | 1.453615 | -0.283592 | 3.961771 |
| 30 | 1 | 3.152065 | -0.567924 | 3.616260 |
| 31 | 1 | 3.154877 | 1.277297 | 1.950900 |
| 32 | 1 | 2.691077 | 1.838093 | 3.550920 |
| 33 | 1 | 0.234369 | 1.456441 | 3.986085 |
| 34 | 1 | 0.523040 | 3.151212 | 3.625837 |
| 35 | 1 | -1.291474 | 3.136694 | 1.930935 |
| 36 | 1 | -1.882313 | 2.683082 | 3.523763 |
| 37 | 1 | -1.466182 | 0.202215 | 3.962061 |
| 38 | 1 | -3.161658 | 0.496021 | 3.609159 |
| 39 | 1 | -3.152135 | -1.302991 | 1.896366 |
| 40 | 1 | -2.699595 | -1.908190 | 3.483268 |
| 41 | 1 | -0.539340 | -3.389627 | 0.797636 |
| 42 | 1 | 3.420285 | -0.529211 | 0.887502 |
| 43 | 1 | 0.547961 | 3.385411 | 0.883643 |
| 44 | 1 | -3.401669 | 0.526000 | 0.871950 |
| 45 | 8 | -0.017692 | -0.108990 | -2.077183 |
| 46 | 1 | 0.564409 | -0.877690 | -2.216621 |
| 47 | 1 | -0.915664 | -0.439087 | -2.255096 |
| 48 | 7 | -3.143223 | 2.999434 | -0.654658 |
| 49 | 7 | 3.025302 | 3.126781 | -0.634913 |
| 50 | 7 | 3.202887 | -2.962543 | -0.698231 |
| 51 | 7 | -3.054920 | -3.107482 | -0.681226 |
| 52 | 1 | -4.105483 | 3.261877 | -0.361539 |
| 53 | 1 | 3.280897 | 4.091805 | -0.345268 |
| 54 | 1 | 4.154755 | -3.243321 | -0.383551 |
| 55 | 1 | -3.344403 | -4.060636 | -0.378413 |
| 56 | 6 | -3.817686 | -2.796029 | -1.883670 |
| 57 | 1 | -3.152224 | -2.628203 | -2.736600 |
| 58 | 6 | -2.857707 | 3.721975 | -1.887795 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 59 | 1 | -2.637332 | 3.026951 | -2.704124 |
| 60 | 6 | 3.759985 | 2.836730 | -1.859761 |
| 61 | 1 | 3.073144 | 2.611692 | -2.681704 |
| 62 | 6 | 2.945651 | -3.667705 | -1.947763 |
| 63 | 1 | 2.780570 | -2.961848 | -2.768217 |
| 64 | 1 | -4.420516 | -1.894194 | -1.738700 |
| 65 | 1 | -1.992849 | 4.380959 | -1.760628 |
| 66 | 1 | 4.419063 | 1.973525 | -1.722268 |
| 67 | 1 | 2.059005 | -4.303316 | -1.860373 |
| 68 | 6 | -4.142274 | 4.559573 | -2.206735 |
| 69 | 8 | -5.080593 | 4.426015 | -1.360234 |
| 70 | 8 | -4.096182 | 5.254801 | -3.243148 |
| 71 | 6 | 4.598796 | 4.120953 | -2.176845 |
| 72 | 8 | 4.453359 | 5.064448 | -1.338136 |
| 73 | 8 | 5.306605 | 4.069613 | -3.204522 |
| 74 | 6 | 4.221899 | -4.535119 | -2.221960 |
| 75 | 8 | 4.197001 | -5.228863 | -3.259370 |
| 76 | 8 | 5.132065 | -4.420308 | -1.342532 |
| 77 | 6 | -4.736494 | -4.038852 | -2.143016 |
| 78 | 8 | -4.596863 | -4.978630 | -1.298910 |
| 79 | 8 | -5.489258 | -3.963349 | -3.135957 |
| 80 | 66 | 0.010484 | 0.011491 | 0.425251 |
| 81 | 1 | -2.066781 | -3.675537 | 1.656415 |
| 82 | 1 | 3.670433 | -2.084061 | 1.708092 |
| 83 | 1 | 2.081089 | 3.644636 | 1.740925 |
| 84 | 1 | -3.659286 | 2.062360 | 1.723252 |

E(RTPSSh) = -2391.0642526 Hartree

Zero-point correction = 0.669323 Hartree/particle

Sum of electronic and thermal Energies = -2390.347727 Hartree

Sum of electronic and thermal Enthalpies = -2390.346783 Hartree

Sum of electronic and thermal Free Energies = -2390.480435 Hartree

Table S82. [Ho(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.109895 | -1.790774 | 2.057366 |
| 2 | 6 | -0.193486 | -2.256302 | 3.132723 |
| 3 | 6 | 1.239455 | -2.402260 | 2.641634 |
| 4 | 7 | 1.777462 | -1.129092 | 2.076173 |
| 5 | 6 | 2.206427 | -0.225928 | 3.177918 |
| 6 | 6 | 2.366129 | 1.213999 | 2.710643 |
| 7 | 7 | 1.109951 | 1.758178 | 2.112685 |
| 8 | 6 | 0.187661 | 2.199669 | 3.192761 |
| 9 | 6 | -1.243426 | 2.353374 | 2.698039 |
| 10 | 7 | -1.774489 | 1.093852 | 2.095908 |
| 11 | 6 | -2.214269 | 0.163533 | 3.169218 |
| 12 | 6 | -2.370378 | -1.262806 | 2.661198 |
| 13 | 6 | -1.457622 | -2.908739 | 1.148561 |
| 14 | 6 | -2.171216 | -2.337047 | -0.066914 |
| 15 | 8 | -1.879916 | -1.151741 | -0.437234 |
| 16 | 6 | 2.922778 | -1.456543 | 1.195594 |
| 17 | 6 | 2.394843 | -2.127599 | -0.063048 |
| 18 | 8 | 1.213541 | -1.844596 | -0.454311 |
| 19 | 6 | 1.463352 | 2.890435 | 1.223998 |
| 20 | 6 | 2.172080 | 2.331515 | -0.003039 |
| 21 | 8 | 1.910868 | 1.140098 | -0.366091 |
| 22 | 6 | -2.907251 | 1.443204 | 1.206920 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 23 | 6 | -2.350893 | 2.143914 | -0.024522 |
| 24 | 8 | -1.164970 | 1.869464 | -0.396816 |
| 25 | 1 | -0.242430 | -1.530363 | 3.947779 |
| 26 | 1 | -0.533876 | -3.215457 | 3.546564 |
| 27 | 1 | 1.289542 | -3.163950 | 1.859734 |
| 28 | 1 | 1.873648 | -2.753619 | 3.466662 |
| 29 | 1 | 1.454373 | -0.285292 | 3.968176 |
| 30 | 1 | 3.152049 | -0.570500 | 3.618719 |
| 31 | 1 | 3.153314 | 1.275830 | 1.955758 |
| 32 | 1 | 2.688669 | 1.837286 | 3.555310 |
| 33 | 1 | 0.233915 | 1.456189 | 3.992148 |
| 34 | 1 | 0.523832 | 3.150330 | 3.629003 |
| 35 | 1 | -1.291989 | 3.135496 | 1.936592 |
| 36 | 1 | -1.883424 | 2.680050 | 3.528672 |
| 37 | 1 | -1.469420 | 0.201249 | 3.967650 |
| 38 | 1 | -3.163960 | 0.496228 | 3.610346 |
| 39 | 1 | -3.151976 | -1.303090 | 1.898753 |
| 40 | 1 | -2.699713 | -1.909737 | 3.485206 |
| 41 | 1 | -0.536971 | -3.384376 | 0.798046 |
| 42 | 1 | 3.414413 | -0.529056 | 0.889187 |
| 43 | 1 | 0.545398 | 3.379486 | 0.885506 |
| 44 | 1 | -3.397222 | 0.524517 | 0.872449 |
| 45 | 8 | -0.015624 | -0.094624 | -2.056095 |
| 46 | 1 | 0.559527 | -0.868188 | -2.197292 |
| 47 | 1 | -0.916437 | -0.416955 | -2.233822 |
| 48 | 7 | -3.125426 | 2.992142 | -0.660721 |
| 49 | 7 | 3.016173 | 3.109612 | -0.640643 |
| 50 | 7 | 3.184817 | -2.954651 | -0.704915 |
| 51 | 7 | -3.044231 | -3.091956 | -0.690366 |
| 52 | 1 | -4.089708 | 3.255639 | -0.375501 |
| 53 | 1 | 3.272145 | 4.076668 | -0.358367 |
| 54 | 1 | 4.139320 | -3.235447 | -0.398303 |
| 55 | 1 | -3.334301 | -4.047311 | -0.394942 |
| 56 | 6 | -3.803129 | -2.773070 | -1.893351 |
| 57 | 1 | -3.134995 | -2.600536 | -2.743267 |
| 58 | 6 | -2.830097 | 3.711320 | -1.893536 |
| 59 | 1 | -2.604246 | 3.013964 | -2.706358 |
| 60 | 6 | 3.747281 | 2.811307 | -1.865664 |
| 61 | 1 | 3.058012 | 2.580161 | -2.683836 |
| 62 | 6 | 2.918855 | -3.656306 | -1.954633 |
| 63 | 1 | 2.747686 | -2.948190 | -2.771902 |
| 64 | 1 | -4.406231 | -1.872002 | -1.744933 |
| 65 | 1 | -1.965623 | 4.369845 | -1.761567 |
| 66 | 1 | 4.407225 | 1.949426 | -1.724098 |
| 67 | 1 | 2.033158 | -4.292569 | -1.862708 |
| 68 | 6 | -4.111471 | 4.549164 | -2.224405 |
| 69 | 8 | -5.056490 | 4.418151 | -1.385044 |
| 70 | 8 | -4.056592 | 5.241951 | -3.262042 |
| 71 | 6 | 4.584463 | 4.093645 | -2.194473 |
| 72 | 8 | 4.441213 | 5.042938 | -1.361997 |
| 73 | 8 | 5.288913 | 4.035318 | -3.224096 |
| 74 | 6 | 4.193621 | -4.522176 | -2.240663 |
| 75 | 8 | 4.161150 | -5.213528 | -3.279439 |
| 76 | 8 | 5.110393 | -4.408599 | -1.367998 |
| 77 | 6 | -4.721206 | -4.014340 | -2.163002 |
| 78 | 8 | -4.583627 | -4.959344 | -1.324434 |
| 79 | 8 | -5.471219 | -3.932697 | -3.157503 |
| 80 | 67 | 0.010399 | 0.011564 | 0.438265 |
| 81 | 1 | -2.067678 | -3.670561 | 1.651453 |
| 82 | 1 | 3.663641 | -2.086679 | 1.705312 |
| 83 | 1 | 2.081176 | 3.638143 | 1.738773 |
| 84 | 1 | -3.654219 | 2.063340 | 1.719975 |

E(RTPSSh) = -2391.6480766 Hartree
 Zero-point correction = 0.669492 Hartree/particle
 Sum of electronic and thermal Energies = -2390.931451 Hartree
 Sum of electronic and thermal Enthalpies = -2390.930507 Hartree
 Sum of electronic and thermal Free Energies = -2391.063757 Hartree

Table S83. [Er(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.103969 | -1.789551 | 2.062889 |
| 2 | 6 | -0.188452 | -2.254840 | 3.138842 |
| 3 | 6 | 1.244598 | -2.396983 | 2.647968 |
| 4 | 7 | 1.777153 | -1.122132 | 2.081292 |
| 5 | 6 | 2.207126 | -0.219110 | 3.182484 |
| 6 | 6 | 2.362231 | 1.220683 | 2.714248 |
| 7 | 7 | 1.103626 | 1.759052 | 2.116116 |
| 8 | 6 | 0.182395 | 2.201387 | 3.196512 |
| 9 | 6 | -1.248962 | 2.350714 | 2.702179 |
| 10 | 7 | -1.774909 | 1.088902 | 2.100442 |
| 11 | 6 | -2.215077 | 0.159647 | 3.174234 |
| 12 | 6 | -2.366775 | -1.266928 | 2.666404 |
| 13 | 6 | -1.448008 | -2.906313 | 1.151495 |
| 14 | 6 | -2.157876 | -2.331282 | -0.064249 |
| 15 | 8 | -1.870066 | -1.142154 | -0.425364 |
| 16 | 6 | 2.920195 | -1.447123 | 1.197096 |
| 17 | 6 | 2.386645 | -2.116108 | -0.059983 |
| 18 | 8 | 1.201356 | -1.836045 | -0.441687 |
| 19 | 6 | 1.453549 | 2.889234 | 1.223535 |
| 20 | 6 | 2.159239 | 2.325087 | -0.002580 |
| 21 | 8 | 1.900550 | 1.130122 | -0.355741 |
| 22 | 6 | -2.906109 | 1.434943 | 1.208388 |
| 23 | 6 | -2.345223 | 2.132220 | -0.022595 |
| 24 | 8 | -1.156012 | 1.859791 | -0.385925 |
| 25 | 1 | -0.239340 | -1.529675 | 3.954490 |
| 26 | 1 | -0.527613 | -3.214999 | 3.551291 |
| 27 | 1 | 1.296952 | -3.159214 | 1.866766 |
| 28 | 1 | 1.880597 | -2.745204 | 3.472884 |
| 29 | 1 | 1.456811 | -0.280100 | 3.974304 |
| 30 | 1 | 3.154396 | -0.561977 | 3.621000 |
| 31 | 1 | 3.149013 | 1.284397 | 1.959124 |
| 32 | 1 | 2.682542 | 1.846308 | 3.557984 |
| 33 | 1 | 0.230845 | 1.459519 | 3.997291 |
| 34 | 1 | 0.517401 | 3.153556 | 3.630274 |
| 35 | 1 | -1.300001 | 3.132476 | 1.940540 |
| 36 | 1 | -1.890414 | 2.675244 | 3.532478 |
| 37 | 1 | -1.471608 | 0.199624 | 3.973873 |
| 38 | 1 | -3.166196 | 0.491028 | 3.613196 |
| 39 | 1 | -3.147984 | -1.309625 | 1.903707 |
| 40 | 1 | -2.693893 | -1.915496 | 3.489963 |
| 41 | 1 | -0.526263 | -3.380882 | 0.802720 |
| 42 | 1 | 3.410555 | -0.519111 | 0.890551 |
| 43 | 1 | 0.534586 | 3.376696 | 0.885821 |
| 44 | 1 | -3.395067 | 0.515365 | 0.875190 |
| 45 | 8 | -0.014466 | -0.081962 | -2.036319 |
| 46 | 1 | 0.556257 | -0.858474 | -2.178968 |
| 47 | 1 | -0.917110 | -0.399536 | -2.213175 |
| 48 | 7 | -3.117824 | 2.975657 | -0.667280 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 49 | 7 | 2.998622 | 3.100955 | -0.648883 |
| 50 | 7 | 3.174318 | -2.938803 | -0.710016 |
| 51 | 7 | -3.024125 | -3.086007 | -0.697061 |
| 52 | 1 | -4.084551 | 3.237664 | -0.389153 |
| 53 | 1 | 3.252837 | 4.070619 | -0.374163 |
| 54 | 1 | 4.132041 | -3.217173 | -0.411292 |
| 55 | 1 | -3.311485 | -4.044414 | -0.408833 |
| 56 | 6 | -3.778318 | -2.763508 | -1.902092 |
| 57 | 1 | -3.106692 | -2.584049 | -2.747834 |
| 58 | 6 | -2.816419 | 3.690978 | -1.900899 |
| 59 | 1 | -2.584043 | 2.991094 | -2.709690 |
| 60 | 6 | 3.726603 | 2.795998 | -1.874152 |
| 61 | 1 | 3.035311 | 2.557383 | -2.688434 |
| 62 | 6 | 2.901256 | -3.638344 | -1.959424 |
| 63 | 1 | 2.722241 | -2.928872 | -2.773836 |
| 64 | 1 | -4.385668 | -1.865612 | -1.751902 |
| 65 | 1 | -1.954214 | 4.351864 | -1.766008 |
| 66 | 1 | 4.389241 | 1.936842 | -1.728691 |
| 67 | 1 | 2.018076 | -4.277342 | -1.862549 |
| 68 | 6 | -4.097537 | 4.524717 | -2.242920 |
| 69 | 8 | -5.047644 | 4.394442 | -1.409238 |
| 70 | 8 | -4.037531 | 5.213772 | -3.282767 |
| 71 | 6 | 4.559372 | 4.078157 | -2.214685 |
| 72 | 8 | 4.416354 | 5.032890 | -1.388445 |
| 73 | 8 | 5.260555 | 4.014345 | -3.246223 |
| 74 | 6 | 4.176466 | -4.499737 | -2.256851 |
| 75 | 8 | 4.138078 | -5.189222 | -3.296655 |
| 76 | 8 | 5.099536 | -4.384866 | -1.391039 |
| 77 | 6 | -4.690123 | -4.006972 | -2.182930 |
| 78 | 8 | -4.553057 | -4.955751 | -1.348572 |
| 79 | 8 | -5.435199 | -3.923094 | -3.180926 |
| 80 | 68 | 0.010093 | 0.012507 | 0.450496 |
| 81 | 1 | -2.059709 | -3.669117 | 1.650864 |
| 82 | 1 | 3.662660 | -2.078340 | 1.703083 |
| 83 | 1 | 2.072762 | 3.638574 | 1.734203 |
| 84 | 1 | -3.654230 | 2.056705 | 1.717744 |

E(RTPSSh) = -2392.2309506 Hartree

Zero-point correction = 0.669633 Hartree/particle

Sum of electronic and thermal Energies = -2391.514239 Hartree

Sum of electronic and thermal Enthalpies = -2391.513295 Hartree

Sum of electronic and thermal Free Energies = -2391.646308 Hartree

Table S84. [Tm(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | -1.094948 | -1.790110 | 2.069052 |
| 2 | 6 | -0.179157 | -2.252268 | 3.145838 |
| 3 | 6 | 1.254368 | -2.387702 | 2.655258 |
| 4 | 7 | 1.778894 | -1.110419 | 2.086756 |
| 5 | 6 | 2.207304 | -0.205857 | 3.187018 |
| 6 | 6 | 2.354733 | 1.233952 | 2.717183 |
| 7 | 7 | 1.092691 | 1.763799 | 2.118739 |
| 8 | 6 | 0.171369 | 2.205055 | 3.199261 |
| 9 | 6 | -1.260601 | 2.346582 | 2.705219 |
| 10 | 7 | -1.778673 | 1.081189 | 2.104289 |
| 11 | 6 | -2.217065 | 0.152297 | 3.178860 |
| 12 | 6 | -2.361143 | -1.275122 | 2.671881 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 13 | 6 | -1.432837 | -2.907176 | 1.155971 |
| 14 | 6 | -2.140141 | -2.331519 | -0.060669 |
| 15 | 8 | -1.858980 | -1.138341 | -0.413696 |
| 16 | 6 | 2.920858 | -1.430888 | 1.199701 |
| 17 | 6 | 2.384181 | -2.09588 | -0.055926 |
| 18 | 8 | 1.194702 | -1.825643 | -0.429235 |
| 19 | 6 | 1.436863 | 2.892533 | 1.222172 |
| 20 | 6 | 2.141090 | 2.324673 | -0.002806 |
| 21 | 8 | 1.887803 | 1.125757 | -0.346299 |
| 22 | 6 | -2.909104 | 1.421110 | 1.209075 |
| 23 | 6 | -2.345543 | 2.115719 | -0.021891 |
| 24 | 8 | -1.152708 | 1.848008 | -0.376833 |
| 25 | 1 | -0.233673 | -1.527568 | 3.961715 |
| 26 | 1 | -0.514754 | -3.213995 | 3.557485 |
| 27 | 1 | 1.310740 | -3.150830 | 1.875220 |
| 28 | 1 | 1.892783 | -2.730931 | 3.480347 |
| 29 | 1 | 1.458673 | -0.269828 | 3.980257 |
| 30 | 1 | 3.156892 | -0.544498 | 3.623722 |
| 31 | 1 | 3.141012 | 1.300934 | 1.961825 |
| 32 | 1 | 2.671507 | 1.862808 | 3.559794 |
| 33 | 1 | 0.223711 | 1.465168 | 4.001676 |
| 34 | 1 | 0.502866 | 3.159628 | 3.630332 |
| 35 | 1 | -1.315902 | 3.127654 | 1.943171 |
| 36 | 1 | -1.904162 | 2.667791 | 3.535119 |
| 37 | 1 | -1.475186 | 0.196589 | 3.979808 |
| 38 | 1 | -3.170416 | 0.480278 | 3.615455 |
| 39 | 1 | -3.141893 | -1.322399 | 1.908987 |
| 40 | 1 | -2.684650 | -1.925493 | 3.495399 |
| 41 | 1 | -0.508976 | -3.379106 | 0.809474 |
| 42 | 1 | 3.408133 | -0.501427 | 0.892904 |
| 43 | 1 | 0.515969 | 3.376514 | 0.885010 |
| 44 | 1 | -3.395193 | 0.499489 | 0.877598 |
| 45 | 8 | -0.013352 | -0.073194 | -2.020128 |
| 46 | 1 | 0.553208 | -0.852688 | -2.162842 |
| 47 | 1 | -0.917350 | -0.386716 | -2.196964 |
| 48 | 7 | -3.118089 | 2.952881 | -0.674639 |
| 49 | 7 | 2.974562 | 3.099952 | -0.657304 |
| 50 | 7 | 3.171895 | -2.916504 | -0.713024 |
| 51 | 7 | -2.997899 | -3.088527 | -0.702140 |
| 52 | 1 | -4.087512 | 3.211647 | -0.403105 |
| 53 | 1 | 3.225208 | 4.072524 | -0.389888 |
| 54 | 1 | 4.133090 | -3.190253 | -0.421324 |
| 55 | 1 | -3.279930 | -4.050503 | -0.420707 |
| 56 | 6 | -3.747509 | -2.764857 | -1.909769 |
| 57 | 1 | -3.072374 | -2.575593 | -2.750563 |
| 58 | 6 | -2.812330 | 3.664986 | -1.909086 |
| 59 | 1 | -2.572358 | 2.963098 | -2.713888 |
| 60 | 6 | 3.700618 | 2.789512 | -1.882379 |
| 61 | 1 | 3.008187 | 2.542195 | -2.693052 |
| 62 | 6 | 2.893997 | -3.614948 | -1.962020 |
| 63 | 1 | 2.705660 | -2.904773 | -2.773708 |
| 64 | 1 | -4.362550 | -1.872468 | -1.758038 |
| 65 | 1 | -1.953595 | 4.329826 | -1.771487 |
| 66 | 1 | 4.367294 | 1.934221 | -1.732601 |
| 67 | 1 | 2.014911 | -4.258828 | -1.860382 |
| 68 | 6 | -4.094709 | 4.492360 | -2.261640 |
| 69 | 8 | -5.049112 | 4.361458 | -1.433006 |
| 70 | 8 | -4.031259 | 5.177809 | -3.303672 |
| 71 | 6 | 4.527081 | 4.072710 | -2.234138 |
| 72 | 8 | 4.382291 | 5.032597 | -1.414236 |
| 73 | 8 | 5.225506 | 4.004617 | -3.267289 |
| 74 | 6 | 4.171698 | -4.468861 | -2.270073 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 75 | 8 | 4.129533 | -5.156774 | -3.310774 |
| 76 | 8 | 5.100358 | -4.350273 | -1.410775 |
| 77 | 6 | -4.648200 | -4.013556 | -2.203017 |
| 78 | 8 | -4.508423 | -4.966180 | -1.373535 |
| 79 | 8 | -5.388144 | -3.929453 | -3.204798 |
| 80 | 69 | 0.009325 | 0.013462 | 0.461491 |
| 81 | 1 | -2.044542 | -3.671871 | 1.652422 |
| 82 | 1 | 3.666087 | -2.061228 | 1.702654 |
| 83 | 1 | 2.055674 | 3.644936 | 1.728753 |
| 84 | 1 | -3.659696 | 2.043044 | 1.714530 |

E(RTPSSh) = -2392.8104773 Hartree

Zero-point correction = 0.669742 Hartree/particle

Sum of electronic and thermal Energies = -2392.093690 Hartree

Sum of electronic and thermal Enthalpies = -2392.092746 Hartree

Sum of electronic and thermal Free Energies = -2392.225725 Hartree

Table S85. [Yb(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.083885 | -1.789656 | 2.078282 |
| 2 | 6 | -0.167210 | -2.245994 | 3.156426 |
| 3 | 6 | 1.266837 | -2.373360 | 2.666182 |
| 4 | 7 | 1.781403 | -1.093724 | 2.094220 |
| 5 | 6 | 2.207029 | -0.185553 | 3.192233 |
| 6 | 6 | 2.345028 | 1.253705 | 2.718825 |
| 7 | 7 | 1.078952 | 1.772537 | 2.119406 |
| 8 | 6 | 0.156886 | 2.212720 | 3.199406 |
| 9 | 6 | -1.275742 | 2.344085 | 2.705395 |
| 10 | 7 | -1.784412 | 1.073714 | 2.107224 |
| 11 | 6 | -2.219334 | 0.145940 | 3.183840 |
| 12 | 6 | -2.354043 | -1.283039 | 2.679518 |
| 13 | 6 | -1.414265 | -2.908574 | 1.165117 |
| 14 | 6 | -2.119206 | -2.334787 | -0.053531 |
| 15 | 8 | -1.847075 | -1.137208 | -0.398856 |
| 16 | 6 | 2.922444 | -1.409223 | 1.204451 |
| 17 | 6 | 2.383044 | -2.079720 | -0.048811 |
| 18 | 8 | 1.188891 | -1.813668 | -0.413377 |
| 19 | 6 | 1.415859 | 2.899177 | 1.217577 |
| 20 | 6 | 2.119618 | 2.326917 | -0.005349 |
| 21 | 8 | 1.872793 | 1.123500 | -0.337681 |
| 22 | 6 | -2.914841 | 1.404823 | 1.208966 |
| 23 | 6 | -2.350045 | 2.096173 | -0.022950 |
| 24 | 8 | -1.153363 | 1.834303 | -0.369359 |
| 25 | 1 | -0.226277 | -1.520635 | 3.971409 |
| 26 | 1 | -0.497885 | -3.209090 | 3.568799 |
| 27 | 1 | 1.328117 | -3.138162 | 1.888168 |
| 28 | 1 | 1.908283 | -2.709816 | 3.491677 |
| 29 | 1 | 1.459987 | -0.252290 | 3.986784 |
| 30 | 1 | 3.159219 | -0.518162 | 3.627849 |
| 31 | 1 | 3.130673 | 1.323829 | 1.963102 |
| 32 | 1 | 2.657520 | 1.887359 | 3.559390 |
| 33 | 1 | 0.213981 | 1.475751 | 4.004217 |
| 34 | 1 | 0.483646 | 3.170520 | 3.626852 |
| 35 | 1 | -1.336068 | 3.123130 | 1.941658 |
| 36 | 1 | -1.921850 | 2.662602 | 3.534310 |
| 37 | 1 | -1.478746 | 0.196564 | 3.985643 |
| 38 | 1 | -3.175109 | 0.469763 | 3.618179 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 39 | 1 | -3.133987 | -1.336657 | 1.916228 |
| 40 | 1 | -2.673481 | -1.934599 | 3.503661 |
| 41 | 1 | -0.487764 | -3.377427 | 0.821815 |
| 42 | 1 | 3.405201 | -0.478010 | 0.896144 |
| 43 | 1 | 0.492299 | 3.377633 | 0.880127 |
| 44 | 1 | -3.396611 | 0.480026 | 0.880345 |
| 45 | 8 | -0.013273 | -0.067125 | -2.003621 |
| 46 | 1 | 0.549535 | -0.849611 | -2.144856 |
| 47 | 1 | -0.918514 | -0.376642 | -2.180796 |
| 48 | 7 | -3.124220 | 2.924455 | -0.684820 |
| 49 | 7 | 2.946209 | 3.101688 | -0.668921 |
| 50 | 7 | 3.171536 | -2.890117 | -0.712727 |
| 51 | 7 | -2.965252 | -3.096708 | -0.704479 |
| 52 | 1 | -4.096634 | 3.178965 | -0.419654 |
| 53 | 1 | 3.192722 | 4.077577 | -0.409566 |
| 54 | 1 | 4.137054 | -3.157142 | -0.428780 |
| 55 | 1 | -3.239144 | -4.063114 | -0.430096 |
| 56 | 6 | -3.708338 | -2.775416 | -1.916817 |
| 57 | 1 | -3.028331 | -2.573744 | -2.750770 |
| 58 | 6 | -2.816470 | 3.632330 | -1.921231 |
| 59 | 1 | -2.568973 | 2.927946 | -2.721562 |
| 60 | 6 | 3.671621 | 2.785428 | -1.892918 |
| 61 | 1 | 2.978960 | 2.529565 | -2.700734 |
| 62 | 6 | 2.890064 | -3.587876 | -1.961342 |
| 63 | 1 | 2.689757 | -2.877346 | -2.769847 |
| 64 | 1 | -4.335420 | -1.891328 | -1.765794 |
| 65 | 1 | -1.962108 | 4.302594 | -1.782864 |
| 66 | 1 | 4.342080 | 1.934012 | -1.738151 |
| 67 | 1 | 2.017250 | -4.239434 | -1.854731 |
| 68 | 6 | -4.101855 | 4.450769 | -2.283720 |
| 69 | 8 | -5.059517 | 4.317989 | -1.459108 |
| 70 | 8 | -4.037321 | 5.131812 | -3.328528 |
| 71 | 6 | 4.492070 | 4.069606 | -2.255184 |
| 72 | 8 | 4.344194 | 5.034768 | -1.442032 |
| 73 | 8 | 5.189417 | 3.996993 | -3.288726 |
| 74 | 6 | 4.172586 | -4.430324 | -2.281020 |
| 75 | 8 | 4.128681 | -5.115560 | -3.323363 |
| 76 | 8 | 5.106406 | -4.306321 | -1.428074 |
| 77 | 6 | -4.591469 | -4.033165 | -2.224589 |
| 78 | 8 | -4.448375 | -4.988112 | -1.398352 |
| 79 | 8 | -5.322820 | -3.952698 | -3.232924 |
| 80 | 70 | 0.007533 | 0.015465 | 0.472145 |
| 81 | 1 | -2.025450 | -3.675053 | 1.659526 |
| 82 | 1 | 3.671361 | -2.037241 | 1.704828 |
| 83 | 1 | 2.033110 | 3.656202 | 1.719151 |
| 84 | 1 | -3.668708 | 2.026374 | 1.710023 |

E(RTPSSh) = -2393.393626 Hartree

Zero-point correction = 0.669830 Hartree/particle

Sum of electronic and thermal Energies = -2392.676781 Hartree

Sum of electronic and thermal Enthalpies = -2392.675837 Hartree

Sum of electronic and thermal Free Energies = -2392.808797 Hartree

Table S86. [Lu(DOTA-(gly)₄(H₂O)]⁻ [TSAP, Δ(δδδδ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|----------|
| | | X | Y | Z |
| 1 | 7 | -1.067987 | -1.793740 | 2.084429 |
| 2 | 6 | -0.149079 | -2.243147 | 3.163420 |

| | | | | |
|----|---|-----------|-----------|-----------|
| 3 | 6 | 1.285747 | -2.358996 | 2.673532 |
| 4 | 7 | 1.787871 | -1.075417 | 2.099368 |
| 5 | 6 | 2.208673 | -0.163817 | 3.196217 |
| 6 | 6 | 2.334064 | 1.275703 | 2.721004 |
| 7 | 7 | 1.062828 | 1.781357 | 2.121122 |
| 8 | 6 | 0.139124 | 2.217315 | 3.201277 |
| 9 | 6 | -1.294598 | 2.335861 | 2.708070 |
| 10 | 7 | -1.791120 | 1.060193 | 2.110885 |
| 11 | 6 | -2.220455 | 0.131230 | 3.188523 |
| 12 | 6 | -2.342981 | -1.298962 | 2.685292 |
| 13 | 6 | -1.388433 | -2.914355 | 1.170211 |
| 14 | 6 | -2.093159 | -2.343220 | -0.049561 |
| 15 | 8 | -1.832293 | -1.140903 | -0.387812 |
| 16 | 6 | 2.928732 | -1.382612 | 1.206842 |
| 17 | 6 | 2.388604 | -2.055243 | -0.044745 |
| 18 | 8 | 1.189220 | -1.800468 | -0.400704 |
| 19 | 6 | 1.389668 | 2.907428 | 1.215164 |
| 20 | 6 | 2.094244 | 2.334213 | -0.006680 |
| 21 | 8 | 1.858454 | 1.125714 | -0.328859 |
| 22 | 6 | -2.922256 | 1.380848 | 1.210073 |
| 23 | 6 | -2.358153 | 2.072349 | -0.021818 |
| 24 | 8 | -1.156784 | 1.820921 | -0.359983 |
| 25 | 1 | -0.214312 | -1.517914 | 3.978021 |
| 26 | 1 | -0.472751 | -3.208621 | 3.575684 |
| 27 | 1 | 1.353864 | -3.124641 | 1.896936 |
| 28 | 1 | 1.930603 | -2.687914 | 3.499352 |
| 29 | 1 | 1.463354 | -0.235986 | 3.991911 |
| 30 | 1 | 3.164127 | -0.488834 | 3.630322 |
| 31 | 1 | 3.118954 | 1.351869 | 1.965102 |
| 32 | 1 | 2.640584 | 1.913762 | 3.560382 |
| 33 | 1 | 0.202953 | 1.482580 | 4.007618 |
| 34 | 1 | 0.459096 | 3.178601 | 3.625932 |
| 35 | 1 | -1.362330 | 3.113969 | 1.944024 |
| 36 | 1 | -1.943541 | 2.648628 | 3.536900 |
| 37 | 1 | -1.481113 | 0.188865 | 3.990995 |
| 38 | 1 | -3.179202 | 0.448395 | 3.621134 |
| 39 | 1 | -3.122370 | -1.359900 | 1.921999 |
| 40 | 1 | -2.656356 | -1.953257 | 3.509545 |
| 41 | 1 | -0.458217 | -3.377269 | 0.829112 |
| 42 | 1 | 3.405007 | -0.448351 | 0.897902 |
| 43 | 1 | 0.462275 | 3.378518 | 0.878101 |
| 44 | 1 | -3.397287 | 0.452092 | 0.883032 |
| 45 | 8 | -0.012671 | -0.060316 | -1.989801 |
| 46 | 1 | 0.553447 | -0.840385 | -2.130720 |
| 47 | 1 | -0.916926 | -0.374533 | -2.163642 |
| 48 | 7 | -3.136862 | 2.889919 | -0.691425 |
| 49 | 7 | 2.910346 | 3.112472 | -0.678827 |
| 50 | 7 | 3.180652 | -2.856128 | -0.715723 |
| 51 | 7 | -2.927215 | -3.111225 | -0.708526 |
| 52 | 1 | -4.113110 | 3.135717 | -0.431935 |
| 53 | 1 | 3.147688 | 4.092577 | -0.426692 |
| 54 | 1 | 4.150482 | -3.114322 | -0.438241 |
| 55 | 1 | -3.191203 | -4.082106 | -0.440114 |
| 56 | 6 | -3.666865 | -2.793662 | -1.923972 |
| 57 | 1 | -2.984438 | -2.579300 | -2.752753 |
| 58 | 6 | -2.830697 | 3.596082 | -1.929232 |
| 59 | 1 | -2.572759 | 2.891151 | -2.725773 |
| 60 | 6 | 3.635127 | 2.795992 | -1.903167 |
| 61 | 1 | 2.942652 | 2.528058 | -2.707209 |
| 62 | 6 | 2.898450 | -3.554146 | -1.964028 |
| 63 | 1 | 2.686819 | -2.843967 | -2.769977 |
| 64 | 1 | -4.306476 | -1.918641 | -1.772772 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 65 | 1 | -1.983834 | 4.275558 | -1.789869 |
| 66 | 1 | 4.314944 | 1.952619 | -1.745318 |
| 67 | 1 | 2.032563 | -4.214238 | -1.853699 |
| 68 | 6 | -4.122836 | 4.399956 | -2.300451 |
| 69 | 8 | -5.082614 | 4.260830 | -1.479352 |
| 70 | 8 | -4.060757 | 5.077442 | -3.347697 |
| 71 | 6 | 4.441112 | 4.086403 | -2.275881 |
| 72 | 8 | 4.285808 | 5.054976 | -1.468200 |
| 73 | 8 | 5.136053 | 4.014590 | -3.311082 |
| 74 | 6 | 4.187178 | -4.383576 | -2.292895 |
| 75 | 8 | 4.143583 | -5.067360 | -3.336183 |
| 76 | 8 | 5.124791 | -4.252108 | -1.445265 |
| 77 | 6 | -4.531573 | -4.061333 | -2.243311 |
| 78 | 8 | -4.381690 | -5.018113 | -1.420441 |
| 79 | 8 | -5.257237 | -3.985444 | -3.256073 |
| 80 | 71 | 0.007043 | 0.016729 | 0.481936 |
| 81 | 1 | -1.996696 | -3.684779 | 1.662128 |
| 82 | 1 | 3.682688 | -2.006948 | 1.704267 |
| 83 | 1 | 2.003535 | 3.670053 | 1.712406 |
| 84 | 1 | -3.681081 | 1.999187 | 1.707624 |

E(RTPSSh) = -2393.9470345 Hartree

Zero-point correction = 0.669892 Hartree/particle

Sum of electronic and thermal Energies = -2393.230156 Hartree

Sum of electronic and thermal Enthalpies = -2393.229212 Hartree

Sum of electronic and thermal Free Energies = -2393.362131 Hartree

Table S87. [Gd(DOTA)(H₂O)]⁻ [SAP, Δ(λλλλ)], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.026330 | -1.769162 | 1.187635 |
| 2 | 6 | 0.056250 | -2.581535 | 1.806477 |
| 3 | 6 | 1.243719 | -1.728570 | 2.240553 |
| 4 | 7 | 1.864260 | -0.976961 | 1.119874 |
| 5 | 6 | 2.704379 | 0.123900 | 1.665822 |
| 6 | 6 | 1.870627 | 1.325230 | 2.101333 |
| 7 | 7 | 1.064280 | 1.910242 | 0.999650 |
| 8 | 6 | -0.002327 | 2.777378 | 1.568951 |
| 9 | 6 | -1.180564 | 1.967246 | 2.102761 |
| 10 | 7 | -1.825852 | 1.117414 | 1.068737 |
| 11 | 6 | -2.652467 | 0.071008 | 1.728353 |
| 12 | 6 | -1.807235 | -1.086739 | 2.251649 |
| 13 | 6 | -1.908110 | -2.647558 | 0.377537 |
| 14 | 6 | -2.707827 | -1.922430 | -0.719401 |
| 15 | 8 | -2.133600 | -0.869067 | -1.221976 |
| 16 | 8 | -3.782403 | -2.409035 | -1.086221 |
| 17 | 6 | 2.696566 | -1.878571 | 0.282762 |
| 18 | 6 | 1.921341 | -2.690721 | -0.770707 |
| 19 | 8 | 2.418335 | -3.744602 | -1.180576 |
| 20 | 8 | 0.815921 | -2.151553 | -1.192590 |
| 21 | 6 | 1.926612 | 2.696631 | 0.080150 |
| 22 | 6 | 2.683166 | 1.847463 | -0.961146 |
| 23 | 8 | 3.754191 | 2.281523 | -1.404434 |
| 24 | 8 | 2.088796 | 0.756891 | -1.328889 |
| 25 | 6 | -2.671427 | 1.944146 | 0.169313 |
| 26 | 6 | -1.890440 | 2.662638 | -0.948611 |
| 27 | 8 | -2.348645 | 3.721060 | -1.397664 |
| 28 | 8 | -0.828255 | 2.049977 | -1.366347 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 29 | 1 | -1.260522 | -3.350794 | -0.155545 |
| 30 | 1 | -2.593294 | -3.223465 | 1.014261 |
| 31 | 1 | 3.296304 | -2.559461 | 0.902014 |
| 32 | 1 | 3.379776 | -1.245845 | -0.291671 |
| 33 | 1 | 2.638405 | 3.322061 | 0.635878 |
| 34 | 1 | 1.267536 | 3.351687 | -0.497629 |
| 35 | 1 | -3.360514 | 1.264760 | -0.341459 |
| 36 | 1 | -3.262633 | 2.675479 | 0.736935 |
| 37 | 1 | 0.379198 | -3.319627 | 1.070558 |
| 38 | 1 | -0.319904 | -3.136596 | 2.679304 |
| 39 | 1 | 1.990195 | -2.378648 | 2.723283 |
| 40 | 1 | 0.925124 | -1.006137 | 2.997044 |
| 41 | 1 | 3.297594 | -0.224743 | 2.524853 |
| 42 | 1 | 3.409816 | 0.423613 | 0.889319 |
| 43 | 1 | 2.541952 | 2.087049 | 2.527776 |
| 44 | 1 | 1.185837 | 1.030683 | 2.901512 |
| 45 | 1 | 0.393524 | 3.403610 | 2.382944 |
| 46 | 1 | -0.341250 | 3.451478 | 0.780752 |
| 47 | 1 | -0.845121 | 1.315824 | 2.914437 |
| 48 | 1 | -1.917487 | 2.658648 | 2.540494 |
| 49 | 1 | -3.373234 | -0.296174 | 0.995858 |
| 50 | 1 | -3.228915 | 0.494577 | 2.564789 |
| 51 | 1 | -1.103964 | -0.721471 | 3.005248 |
| 52 | 1 | -2.466811 | -1.806614 | 2.761124 |
| 53 | 64 | 0.002269 | 0.009593 | -0.547794 |
| 54 | 1 | -1.176955 | -0.820271 | -2.853689 |
| 55 | 8 | -0.242384 | -0.611968 | -3.071175 |
| 56 | 1 | 0.236391 | -1.437215 | -2.836619 |

E(RTPSSh) = -1557.8519089 Hartree

Zero-point correction = 0.449472 Hartree/particle

Sum of electronic and thermal Energies = -1557.373114 Hartree

Sum of electronic and thermal Enthalpies = -1557.372169 Hartree

Sum of electronic and thermal Free Energies = -1557.459884 Hartree

Table S88. [Gd(DOTA)(H₂O)]⁻ [TSAP, $\Lambda(\lambda\lambda\lambda\lambda)$], TPSSh/LCRECP/6-31G(d,p), aqueous solution (0 Imaginary Frequencies)

| Center Number | Atomic Number | Coordinates (Angstroms) | | |
|---------------|---------------|-------------------------|-----------|-----------|
| | | X | Y | Z |
| 1 | 7 | -1.173496 | -1.691745 | 1.253317 |
| 2 | 6 | -1.986231 | -0.999227 | 2.282347 |
| 3 | 6 | -2.725706 | 0.205261 | 1.711720 |
| 4 | 7 | -1.806076 | 1.203393 | 1.104498 |
| 5 | 6 | -1.194786 | 2.048947 | 2.157233 |
| 6 | 6 | 0.048498 | 2.774014 | 1.655489 |
| 7 | 7 | 1.089136 | 1.839993 | 1.149318 |
| 8 | 6 | 1.847117 | 1.250175 | 2.278213 |
| 9 | 6 | 2.614155 | 0.002018 | 1.857706 |
| 10 | 7 | 1.726035 | -1.053283 | 1.302807 |
| 11 | 6 | 1.050392 | -1.787829 | 2.399123 |
| 12 | 6 | -0.160890 | -2.566778 | 1.900202 |
| 13 | 6 | -2.022691 | -2.525586 | 0.371256 |
| 14 | 6 | -1.277493 | -2.974658 | -0.899744 |
| 15 | 8 | -0.211041 | -2.285095 | -1.192152 |
| 16 | 6 | -2.569512 | 2.015532 | 0.127704 |
| 17 | 6 | -2.931621 | 1.195310 | -1.128840 |
| 18 | 8 | -2.198400 | 0.143971 | -1.333166 |
| 19 | 6 | 1.982021 | 2.584816 | 0.230445 |
| 20 | 6 | 1.274726 | 2.921117 | -1.098552 |

| | | | | |
|----|----|-----------|-----------|-----------|
| 21 | 8 | 0.256132 | 2.170827 | -1.388405 |
| 22 | 6 | 2.544117 | -1.969595 | 0.475423 |
| 23 | 6 | 2.985336 | -1.318740 | -0.847758 |
| 24 | 8 | 2.276232 | -0.292172 | -1.224038 |
| 25 | 1 | -1.313979 | -0.679910 | 3.084018 |
| 26 | 1 | -2.713313 | -1.688890 | 2.737967 |
| 27 | 1 | -3.414685 | -0.122727 | 0.930300 |
| 28 | 1 | -3.332877 | 0.669976 | 2.503113 |
| 29 | 1 | -0.936705 | 1.402037 | 3.000847 |
| 30 | 1 | -1.916846 | 2.788018 | 2.536990 |
| 31 | 1 | -0.221603 | 3.438716 | 0.831842 |
| 32 | 1 | 0.454072 | 3.405369 | 2.460383 |
| 33 | 1 | 1.135132 | 1.003354 | 3.071206 |
| 34 | 1 | 2.550859 | 1.981823 | 2.703899 |
| 35 | 1 | 3.338393 | 0.260066 | 1.081726 |
| 36 | 1 | 3.184457 | -0.383781 | 2.716196 |
| 37 | 1 | 0.742103 | -1.058890 | 3.154022 |
| 38 | 1 | 1.747523 | -2.479767 | 2.896168 |
| 39 | 1 | 0.155045 | -3.303714 | 1.158384 |
| 40 | 1 | -0.608268 | -3.123069 | 2.737844 |
| 41 | 1 | -2.413619 | -3.405683 | 0.901608 |
| 42 | 1 | -2.872317 | -1.925621 | 0.034225 |
| 43 | 1 | -3.481814 | 2.434415 | 0.575573 |
| 44 | 1 | -1.939274 | 2.844634 | -0.206708 |
| 45 | 1 | 2.360950 | 3.506215 | 0.694762 |
| 46 | 1 | 2.837669 | 1.950452 | -0.018088 |
| 47 | 1 | 3.425683 | -2.331108 | 1.023617 |
| 48 | 1 | 1.933850 | -2.835825 | 0.204207 |
| 49 | 8 | 0.367032 | -0.486098 | -3.045638 |
| 50 | 1 | 0.131239 | -1.409371 | -2.802585 |
| 51 | 1 | 1.322926 | -0.430163 | -2.824388 |
| 52 | 64 | -0.004957 | 0.009227 | -0.482257 |
| 53 | 8 | -1.743366 | -3.908090 | -1.558656 |
| 54 | 8 | 3.926239 | -1.819853 | -1.469661 |
| 55 | 8 | 1.733431 | 3.836284 | -1.791503 |
| 56 | 8 | -3.850154 | 1.600945 | -1.849785 |

E(RTPSSh) = -1557.8543614 Hartree

Zero-point correction = 0.449268 Hartree/particle

Sum of electronic and thermal Energies = -1557.375798 Hartree

Sum of electronic and thermal Enthalpies = -1557.374854 Hartree

Sum of electronic and thermal Free Energies = -1557.462228 Hartree

References

- (i) Cosentino, U.; Villa, A.; Pitea, D.; Moro, G.; Barone, V.; Maiocchi, A. *J. Am. Chem. Soc.* **2002**, 124, 4901-4909.

- (ii) Aime, S.; Botta, M.; Garda, Z.; Kucera, B. E.; Tircso, G.; Young, V. G.; Woods, M. *Inorg. Chem.* **2011**, *50*, 7955-7965.
- (iii) Thompson, A. L.; Parker, D.; Fulton, D. A.; Howard, J. A. K.; Pandya, S. U.; Puschmann, H.; Senanayake, K.; Stenson, P. A.; Badari, A.; Botta, M.; Avedano, S.; Aime, S. *Dalton Trans.* **2006**, 5605-5616.
- (iv) Esteban-Gomez, D.; de Blas, A.; Rodríguez-Blas, T.; Helm, L.; Platas-Iglesias, C. *ChemPhysChem* **2012**, *13*, 3640-3650.
- (v) a) Dunand, F. A.; Aime, S.; Merbach, A. E. *J. Am. Chem. Soc.* **2000**, *122*, 1506-1512; b) Aime, S.; Barge, A.; Botta, M.; De Sousa, A. S.; Parker, D. *Angew. Chem. Int. Ed.* **1998**, *37*, 2673-2675.
- (vi) Woods, M.; Kovacs, Z.; Zhang, S.; Sherry, A. D. *Angew. Chem. Int. Ed.* **2003**, *42*, 5889-5892.
- (vii) Seitz, M.; Oliver, A. G.; Raymond, K. N. *J. Am. Chem. Soc.* **2007**, *46*, 351-353.

