# **Online Supplementary Appendix**

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**eTable 1. Potential applications of probabilistic bias analysis in pharmacoepidemiologic and comparative effectiveness research.**



examine both outcome misclassification and an unmeasured confounder in a retrospective cohort study using claims data, for example.

\*We used examples from studies in our systematic review when available. For some scenarios, we were unavailable to provide examples from included studies, and we used earlier examples from the literature or hypothetical scenarios to illustrate how probabilistic bias analysis could be implemented.







\*The formula notation is heavily adapted is from Lash, Fox, and Fink 2009.<sup>2</sup> This table provides examples of simple bias analysis formulas that can be applied to crude effect estimates using probabilistic bias analysis; it is not meant to be a comprehensive list of all plausible bias-adjustment formulas. Extensive discussions on simple bias analysis are provided elsewhere. $^{2,7,11}$ 

<sup>†</sup> All variables are assumed to be binary in the formulas provided. All formulas assume a cohort study design unless otherwise noted.

‡Notation assumes a case-control study design; the formula can be easily adapted to a cohort study design.



# **eTable 3. General description of eligible pharmacoepidemiologic in 2010-2015 and included in the systematic review, sorted by bias addressed**





\*We selected the first of two articles using probabilistic bias analysis on the same study sample [Excluded: Corrao G, Nicotra F, Parodi A, Zambon A, Soranna D, Heiman F, Merlino L, Mancia G. External adjustment for unmeasured confounders improved drugoutcome association estimates based on health care utilization data. J Clin Epidemiol 2012;65:1190-199.]





CI, confidence interval; HR, hazard ratio;  $P_1$ , prevalence of the confounder in the exposed;  $OR_{CE}$ , exposure-confounder odds ratio;  $P_0$ , prevalence of the unmeasured confounder in the unexposed; RR, relative risk; SI, simulation interval.

\*When multiple scenarios were simulated, we tried to present the least and most extreme bias simulations (defined by looking at changes in the effect estimate). In some studies, many scenarios were visually displayed but the exact values of the effect estimate and interval were not available; in this case, we have presented the corrected estimates and intervals discussed in the text.

<sup>†</sup>Simulation results were presented as single discrete scenarios, multiple discrete scenarios, or applied over a continuous interval of plausible bias parameters. See Methods for further description. ‡See eFigure1 for further description of probability distribution types.

§When conventional effect estimate was <1,estimated as [Effect estimate<sub>conventional</sub> – Effect estimate<sub>probabilistic</sub>) / Effect estimate<sub>conventional</sub>]\*100.

When conventional effect estimate was ≥1, estimated as[Effect estimate<sub>probabilistic</sub> – Effect estimate<sub>conventional</sub>) / Effect estimate<sub>conventional</sub>]\*100.

\*\*Estimated as [SI width<sub>probabilistic</sub> - CI width<sub>conventional</sub>)/ CI width<sub>conventional</sub>]. Interval width calculated as the upper interval bound – lower interval bound

††Although multiple scenarios or a range of plausible bias-adjusted estimates were generated, they were visually displayed. The estimates provided are for the example(s) discussed in the text .

‡‡Three separate unmeasured confounders were simulated using similar methods. Only one is presented for brevity (severity of hypertension).

§§Probability distribution type was provided for exposure-outcome association only. Investigators sampled the relative risk from a distribution with mean of ln(RR) and a variance of 0.04

\*\*\*This study applied a single bias scenario to two exposure-outcome associations. The least biased scenario was new use of low dose aspirin ys, no use and the most biased scenario was long-term use of dipyridamole vs. no use.



CI, confidence interval; HOR, hazard odds ratio; HR, hazard ratio; NPV, negative predictive value; PPV, positive predictive value; RR, relative risk; SI, simulation interval. \*When misclassification was simulated for multiple exposure-outcome associations, we presented the least and most extreme bias simulations (defined by looking at changes in the effect estimate). †See eFigure1 for further description of probability distribution types.

 $*$ When conventional effect estimate was <1,estimated as [Effect estimate<sub>conventional</sub> – Effect estimate<sub>probabilistic</sub>) / Effect estimate<sub>conventional</sub>]\*100.

When conventional effect estimate was ≥1, estimated as[Effect estimate<sub>probabilistic</sub> – Effect estimate<sub>conventional</sub>) / Effect estimate<sub>conventional</sub>]\*100.

 ${}^{\$}$ Estimated as [SI width<sub>probabilistic</sub> - CI width<sub>conventional</sub>)/ CI width<sub>conventional</sub>]. Interval width calculated as the upper interval bound – lower interval bound

\*\*Sensitivity and specificity point estimates for calculating negative predictive value were provided (Sensitivity=95%, Specificity=90%)

††Investigators reported that they "used plausible estimates" of sensitivity and specificity based on positive predictive values from internal validation study

#Investigators did not report any quantitative results from bias analysis; they only discussed findings qualitatively. Scenario 1 compares any use of propionates vs. never users. Scenario 2 compares any aspirin use vs. never users.

**eFigure 1. Common probability distributions assigned to bias parameters – simulating sensitivity as an example.**

### $10$  $10$ £.  $Percent$ Percent  $\overline{4}$  $\overline{\phantom{a}}$  $\overline{2}$ 0  $0.2$  $0.2$  $1.0$  $0.4$  $0.6\,$  $0.8$  $1.0$  $0.0$  $0.4$  $0.6$ Sensitivity **C. Triangular distribution D. Truncated normal distribution**  $10$  $10$ s 8 ĥ Percent Percent  $\overline{1}$  $\overline{2}$

Sensitivity Sensitivity Sensitivity Sensitivity Sensitivity Sensitivity Sensitivity Sensitivity Sensitivity Sensitivity

 $1.0$ 

 $0.8$ 

 $\mathfrak o$ 

 $0.0$ 

 $0.2$ 

 $0.4$ 

 $06$ 

٥s

 $1.0$ 

**E. Beta distribution**

 $0.4$ 

 $0.6$ 

 $0.2$ 

 $\overline{0}$ 

 $0.0$ 



# **A. Uniform distribution B. Trapezoidal distribution**

**eFigure 1** shows five commonly simulated probability distributions assigned to bias parameters (simulating plausible distributions for sensitivity as an example). Panel A simulates a uniform probability for sensitivity with a minimum=0.70 and a maximum=0.90. Uniform probability distributions assume that all values between the minimum and maximum are equally plausible. Panel B shows a trapezoidal probability distribution with minimum=0.70, mode<sub>1</sub>=0.75, mode<sub>2</sub>=0.85, and maximum=0.90. Trapezoidal distributions assume that values between mode<sub>1</sub> and mode<sub>2</sub> are equally plausible but assume linear decreases in the probability density between the modes and the tails of the distribution (the minimum and maximum). Panel C shows a triangular distribution with minimum=0.70, mode=0.80, maximum=0.90. Triangular distributions assume a linear decrease from the mode to the distribution tails. Panel D shows a truncated normal distribution with mean=0.8 and standard deviation=0.1; the distribution has been truncated at 1.0 because a sensitivity > 1.0 is impossible. Panel E shows a beta distribution with mean=0.8 and a standard deviation=0.1 simulated with two shape parameters (here: alpha=12; beta=3). Beta distributions are bound between 0 and 1.

Different distribution types (including shape and type of probability distribution assigned) make different assumptions about bias parameters. For example, the uniform and triangular distributions (panels A and C) assume the same range of plausible bias parameters (min=0.70, max=0.90), but the triangular distribution assumes that 0.80 is the most likely value whereas the uniform distribution assumes that all values between the minimum and maximum are equally plausible. Alternatively – when comparing the uniform and beta distribution (panels A and E) – the beta distribution assumes a wider range of plausible values than the uniform distribution (uniform: min=0.70, max=0.90; beta: min=0.26, max=1.0), but values at the tails of the distribution are less likely than the mean/mode of 0.80. Further description of simulating bias parameter distributions is provided elsewhere.<sup>2</sup>