

**Table S1** Characterization of the four scenarios analyzed in this study to assess the contributions of (i) pedigree relationships among individuals in the training set ( $TS$ ) and recurrent selection candidates ( $RSC$ ) captured by SNPs, (ii) co-segregation of QTL and SNPs, and (iii) ancestral linkage disequilibrium ( $LD_A$ ) between QTL and SNPs to persistency of prediction accuracy  $r_{g,\hat{g}}$  and cumulative genetic gain  $\sum \Delta G$  in synthetics. Note that pairs of SNP markers and pairs of QTL were always allowed to be in  $LD_A$ .

Scenario	TS and RSC are	QTL and SNPs in	Relationship matrix calculated from	Type
$Re-LD_A-SNP$	Related ( $P_{TS} = P_{RSC}$ )	$LD_A$	SNPs	Realistic
$Re-LD_A-Ped$		$LD_A$	Pedigree records	Realistic
$Re-LE_A-SNP$		$LE_A$	SNPs	Artificial
$Un-LD_A-SNP$	Unrelated ( $P_{TS} \cap P_{RSC} = \emptyset$ )	$LD_A$	SNPs	Realistic