

# The Active Side of Stereopsis: Fixation Strategy and Adaptation to Natural Environments

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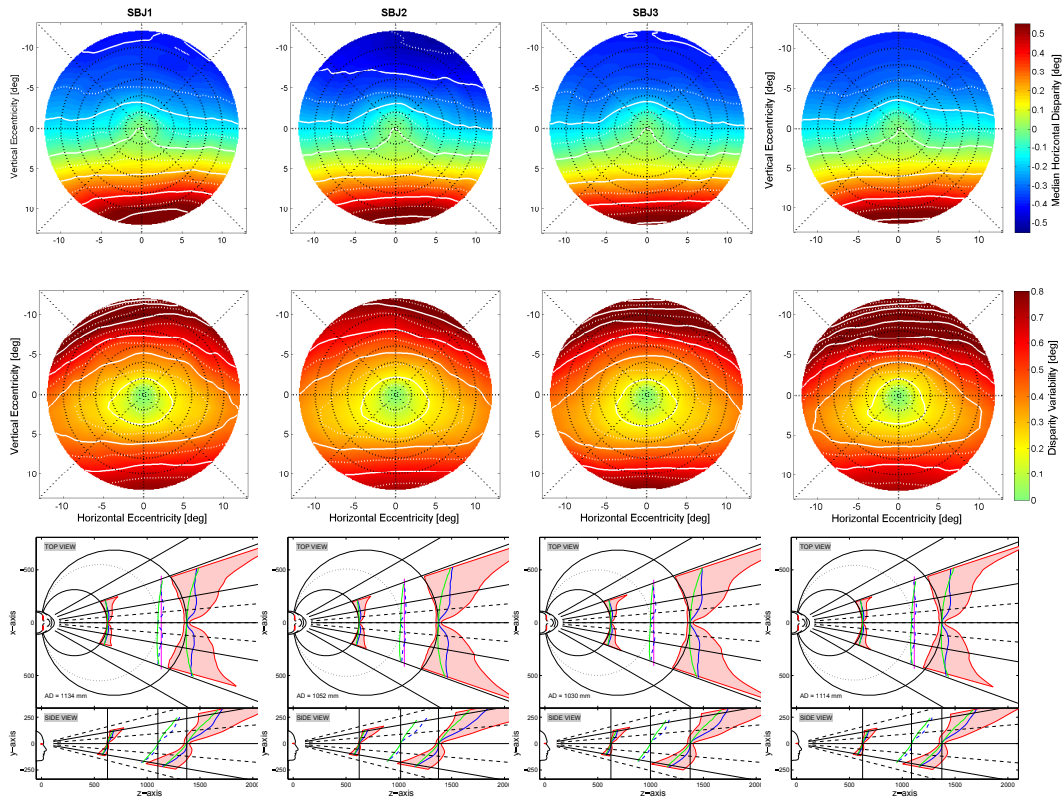
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## ABSTRACT

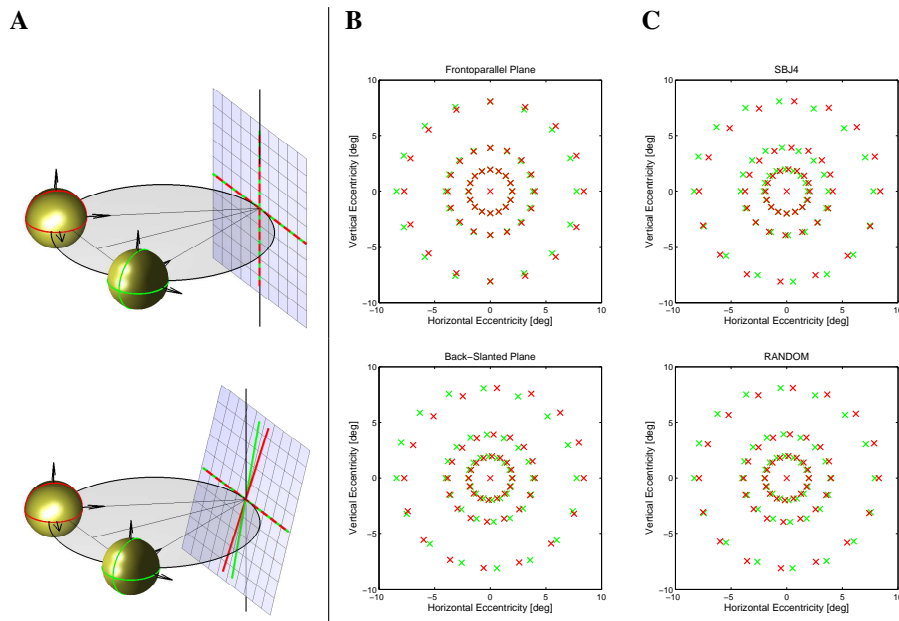
Depth perception in near viewing strongly relies on the interpretation of binocular retinal disparity to obtain stereopsis. Statistical regularities of retinal disparities have been claimed to greatly impact on the neural mechanisms that underlie binocular vision, both to facilitate perceptual decisions and to reduce computational load. In order to assess how fixation strategy can finely conditions the statistics of the disparity a novel and unconventional approach has been designed. The approach integrates accurate realistic three-dimensional models of natural scenes with binocular eye movement recording, allowing accurate ground-truth statistics of retinal disparity experienced by a subject in near viewing. Our results evidence how the organization of human binocular visual system is finely adapted to the disparity statistics that quantitatively distinguish actual fixations, revealing a novel role of the active fixation strategy over the binocular visual functionality. This suggests an ecological explanation of the intrinsic preference of the mechanism of stereopsis for a close central object surrounded by a far background, as an early binocular aspect of the figure-ground segregation process.

## Supplementary Materials

*Disparity Patterns and Empirical Horopter for the Single Subjects* - Figure S1 shows the retinotopic median horizontal disparity (top), the patterns of disparity variability (middle), and the horizontal and vertical horopter (bottom), separately for the four subjects involved in the experiment.



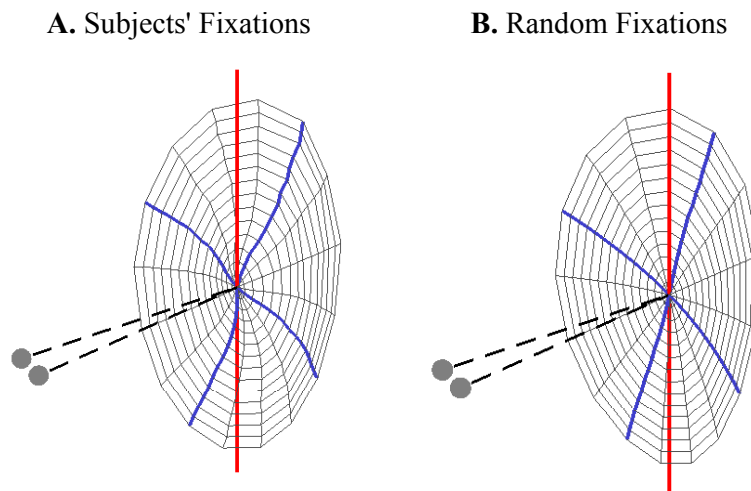
**Figure S1. Individual subjects' data.** Horizontal median disparity pattern and standard deviation (top rows), as in Fig. 3, and top and side views of the empirical horopter and Panum's fusional area (bottom row), as in Fig. 5, represented for each subject, separately.



**Figure S2. A. Geometry of viewing posture while looking a plane.** Sketches of the fixating eye system, showing the eyeballs and the horizontal and vertical meridians for the left (red) and right (green) eye, projected on the fixed plane (gray mesh). The plane is at 400 mm of distance from the observer (vergence angle  $\approx 8.5^\circ$ ), with straight-ahead binocular gaze direction, and fixation point lying on its center, with a tilt of  $0^\circ$  (top) and  $15^\circ$  (bottom). The sketch represents also the geometric horopters, as the horizontal Vieth-Müller circle (black) and vertical horopter (black vertical line). **B. Empirical Retinal Corresponding Points Generated by a Frontoparallel Plane.** Pattern of empirical corresponding points represented in the first  $10^\circ$  of visual field eccentricity, which would be generated by a frontoparallel plane (top) or by a back-slanted plane (bottom). **C. Empirical Corresponding Points Generated on Observer's Fixations.** Pattern of empirical corresponding points represented in the first  $10^\circ$  of visual field eccentricity, which would be generated by the median disparity computed on subjects' (top) or random (bottom) fixations.

*Retinal Empirical Correspondence across the Field of View.* - The empirical correspondence has been commonly studied along the horizontal<sup>14,36-38,40,42</sup> and vertical<sup>13,15,34,37,40-42</sup> meridians of the field of view, as cardinal directions of human vision. The definition of the Hering-Hillebrand (horizontal) and Helmholtz shear (vertical) deviation, does not imply that retinal deviations occur along the two meridians only, but they encompass the whole field of view<sup>15,39</sup>. Thus, we extended the comparison to the whole (central) field of view, and compared our results to the disparity pattern projected by a frontoparallel and a back-slanted plane, as in<sup>15</sup> (see Fig. 2A). Both the patterns of empirical corresponding points computed by our disparity statistics for of subjects' and random fixations (see Fig. 2B, right) are more similar to a pattern produced by a back-slanted plane than that produced by a frontoparallel plane (see Fig. 2B, left). Again, the subjects' pattern presents a higher similarity with those measured in humans ( $rmse = 0.14^\circ$ ), than that obtained by random fixations ( $rmse = 0.15^\circ$ ).

*The 3D shape of the empirical horopter.* - The empirical corresponding point over the whole field of view (first 10° of eccentricity) have been exploited to compute the 3D shape of the empirical horopter (see Fig. S3, derived by the disparity statistics for subjects' fixations. The horopter has been computed as the surfaces that project with minimum retinal disparity to the pairs of empirical corresponding points<sup>35</sup>. It is evident how random fixations (B) result in a 3D shape which is smooth and continuous moving from the center to the periphery of the field of view, while the horopter derived by subjects' fixation is characterized by a close central bump surrounded by a further background.



**Figure S3. A. 3D shape of the empirical horopter for subjects' fixations.** The 3D empirical horopter, derived by the disparity statistics for subjects' fixations, computed as the surfaces that project with minimum retinal disparity to the pairs of empirical corresponding points. The optical axes (black dashed lines) originating from the eyeballs, intersect at the fixation point. The observer is fixating straight-ahead, with a vergence angle of  $7^\circ$ , *i.e.* at a distance of  $\approx 500$  mm. The empirical horopter is represented within the first  $10^\circ$  of eccentricity (gray mesh), highlighting the horizontal and vertical meridians (blue lines), and showing the geometric vertical horopter (red line). The observer is fixating straight-ahead, with a vergence angle of  $7^\circ$ , *i.e.* at a distance of  $\approx 500$  mm. **B. 3D shape of the empirical horopter for random fixations.** The 3D empirical horopter, derived by the disparity statistics for subjects' fixations, computed as in Panel A.

**A**

**B**

**Figure S4. A. Empirical horopters and Panum's areas with fixation disparity.** Representation of the horizontal (top) and vertical (bottom) horopter, with the associate Panum's area, for subjects' (A) and random (B) fixations, as in Fig. 5. The graphs display the variation of the empirical horopter and Panum's area when a fixation disparity varying from zero to 40 arcmin<sup>58</sup> is introduced.

*Fixation disparity and Panum's fusional area* - Fig. S4 shows the horizontal (top) and vertical (bottom) horopter, with the associate Panum's area (pink area), for subjects' (A) and random (B) fixations, as in Fig. 5, but simulating a fixation disparity. We assumed a positive fixation disparity, as commonly measured in normal subjects<sup>58</sup>, and we simulated the fixation disparity varying from zero to 40 arcmin. The increasing fixation disparity has the effect of shifting the empirical horopter closer to the geometric horopter. This effect is more convenient in subjects' fixations, since it reduces the global disparity experienced by the subject, while a local adaptation of the retinal correspondence accounts for a null perceived disparity at fixation.

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