## Signatures of a macroscopic switching transition for a dynamic microtubule

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## Supplementary Information

## S1. Phase diagrams



Although we have not done extensive study to draw a complete parallel between the discontinuous transition in microtubules as discussed in the manuscript, and the equilibrium liquid-gas phase transition, we indicate a few simple analogies here. Temperature, pressure and specific volume in a liquid-gas transition may be compared to the polymerisation ratio k'/k, inverse concentration 1/C and mean velocity  $\langle v \rangle$ , respectively, in the microtubule system. The 1/C versus  $\langle v \rangle$  curves (equivalent of the pressure-volume phase diagram) for various k'/k are plotted in Fig. S1(a). They are reminiscent of liquid-gas isotherms. The co-existence line of inverse concentration versus k'/k (equivalent of pressure-temperature co-existence line) is plotted in Fig. S1(b) - the lower brown curve is for critical concentrations  $C^*$  at which average velocity  $\langle v \rangle$  vanishes, while the upper blue curve corresponds to the transition concentrations  $C_2^*$  at which  $d\langle v \rangle/dC$  has maximum. Like liquid-gas system, where the first order transition pressure increases monotonically with transition temperature, here too we find similar monotonic increase of  $1/C^*$  and  $1/C_2^*$  as a function of k'/k.

## S2. Cumulants of velocity distribution for the limit k'/k = 0

As mentioned in the manuscript, we plot the scaled variance  $(T\sigma^2)$  (Figure. S2(a)) and Binder cumulant (BC) (Figure. S2(b)) of velocity distribution as a function of GTP-tubulin concentration C, for k'/k = 0. We note that the behaviour of these higher cumulants as 'system size' T becomes larger is qualitatively similar to that shown for k'/k = 0.01 in Figure. 4 in the manuscript.



(a) (b) Figure S2. (a) Scaled variance  $T\sigma^2$  (where  $\sigma^2$  is the variance of the velocity distribution) is plotted against concentration C, for values of T = 200s (brown) and T = 500s (blue). It can be observed that as 'system size' T becomes large,  $T\sigma^2$  tends to diverge. (b) Binder cumulant, BC (as defined in the manuscript) is plotted as a function of concentration C for values of T = 200s (brown) and T = 500s(blue). The sharp negative dip in BC for large T near the transition concentration is indicative of a discontinuous transition as discussed in the manuscript.