

A β 42 pentamers/hexamers are the smallest detectable oligomers in solution.

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SUPPORTING INFORMATION

Partial specific volumes of A β peptides

Table S1 lists the partial specific volumes of the amyloid beta peptides used in this study. All values for peptides had been calculated by using the software SEDNTERP¹ and for dye conjugated peptides by additionally summing up partial specific volumes of molecular fragments according to Durchschlag & Zipper².

Table S1: Partial specific volumes and molar masses of the A β -peptides used in this study.

	Molar mass (g/mol)	\bar{v} at 20°C (cm ³ /g)
A β 42	4514.10	0.7377
AF488-A β 42	5337.77	0.7127
FITC- β -Ala-A β 42	4974.57	0.7350
A β 40	4329.87	0.7341
Cys-A β 40	4433.01	0.7316
Cys-A β 40-dimer	8864.00	0.7288

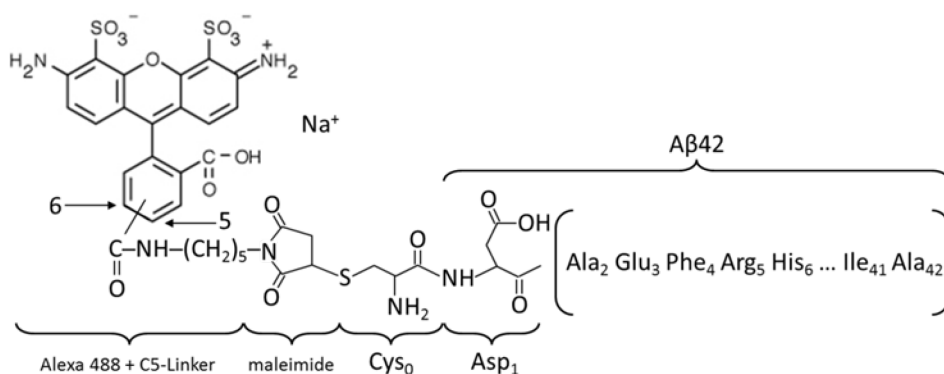


Figure S1: Structure of the N-terminally Alexa 488 labeled A β 42. The Alexa fluorophore and the N-terminal aspartate of A β 42 are separated by a C5 linker, the maleimide group, and the cysteine residue. The bond pointing into the phenyl group between C5 and C6 indicates the possibility of two isomeric forms.

Detectability of a dimer by SV analysis

The software package UltraScan II (vs 9.9; rev. 1927) (<http://www.ultrascan.uthscsa.edu>) offers a simulation tool based on finite element (ASTFEM) methods for the calculation of radial sedimentation profiles as a function of time for single or multiple components³. Beforehand, the components have to be modelled with regard to their mass, shape and partial specific volume. Afterwards, the calculated sedimentation profiles can be processed by data evaluation software like SEDFIT in order to retrieve for example a $c(s)$ distribution. A model for two ideal, non-interacting components was chosen for monomeric and dimeric cys-A β 40. To evaluate whether in SV analysis it is possible to specifically detect the dimer we simulated a particle with the double mass of A β 42 and a slightly more compact shape than the monomer with a theoretical s -value between 1.0 and 1.5 S. Assuming a composition of 50 % monomer and 50 % dimer as independent species at 20°C in sodium phosphate buffer the dimer is clearly distinguishable from the monomer by sedimentation velocity centrifugation at maximum speed (289,000g). Experimentally this could be verified by analysing a covalently linked A β 40 dimer, which was generated by introducing a disulphide bridge between a cysteine engineered at the N-terminus. Data evaluation reveals a difference in s -value of 0.25 S between the monomer and the dimer (Fig. S2).

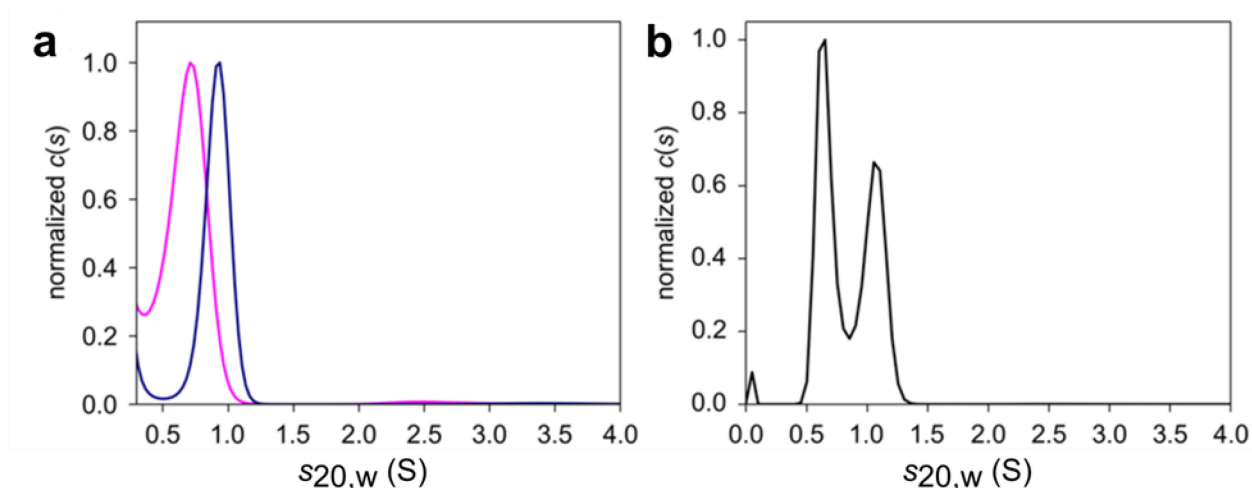


Figure S2: SV analysis of A β 40 monomer and dimer at 60,000 rpm, 15°C. **(a)** Comparison of monomeric A β 40 ($s_{20,w} = 0.65$ S), (magenta) and dimeric A β 40 (dark blue), which had been covalently linked by a disulphide bridge ($s_{20,w}=0.9$ S). **(b)** $c(s)$ distribution obtained from simulated SV data for a 1:1 mixture of monomeric A β 40 and dimeric A β 40, decorated with 0.5 % random noise, 0.02 % radial invariant, and 0.02 % time invariant noise. The frictional ratio was assumed 1.5 for the monomer and 1.4 for the dimer. The $c(s)$ distributions were normalized according to maximum peak height.

Detailed description of SV data fitting procedure

The fitting of SV data was performed with SEDFIT (14.7g; May 2015) according to the procedure reported in Wafer et al. 2016.⁴ The following steps were worked through for the SV data derived from fluorescence detection of 100 nM AF488-A β 42.

1) Generation of a normal $c(s)$

At least 100 scans, which covered the whole sedimentation process, were used. Parameters were the same for all data sets, with $s_{\min}=0$ and $s_{\max}=5$ S, resolution 251, resulting in 0.02 S effective resolution. The meniscus and bottom positions, baseline, time invariant noise and frictional ratio were allowed to float.

2) Manual Bayesian analysis, $c^{\text{MP}}(s)$

This option is found in sedfit under size-distribution options-use prior probabilities. The values for s-value and amplitude, which were entered into the table, were those obtained from initial $c(s)$. The peak width was set to 0.1 S. Whenever these starting values had been changed, the data was first re-fit to generate the normal $c(s)$.

3) Non-interacting discrete species model and F-statistics

This model allows the entries for four independent species. For our data only three species were required. Concentration of the first species (most prominent species) initialized to total optical signal and for the other species with values relative to this first species, e.g. 5 % results in 0.005. The s-value and molar mass was again taken from $c(s)$; meniscus position and time invariant noise were floated.

Then the critical value of root mean square deviation (rmsd) was determined using the F-statistics calculator in sedfit: Options – statistics - calculate variance ratio (F-statistics).

The default values for confidence level; first, second degrees of freedom were used.

In order to avoid trapping of the fit process in local minima Marquardt-Levenberg (ML) and simplex global minimization algorithm were used alternately on each data set until no further change in rmsd was observable. At this point three further MLs were added to test for stability of the solution. Individual species were defined to be statistically significant if their removal from the fit (deletion from the table of non-interacting species) resulted in an rmsd larger than the before determined critical rmsd.

Atomic force microscopy of FITC- β -Ala-A β 42

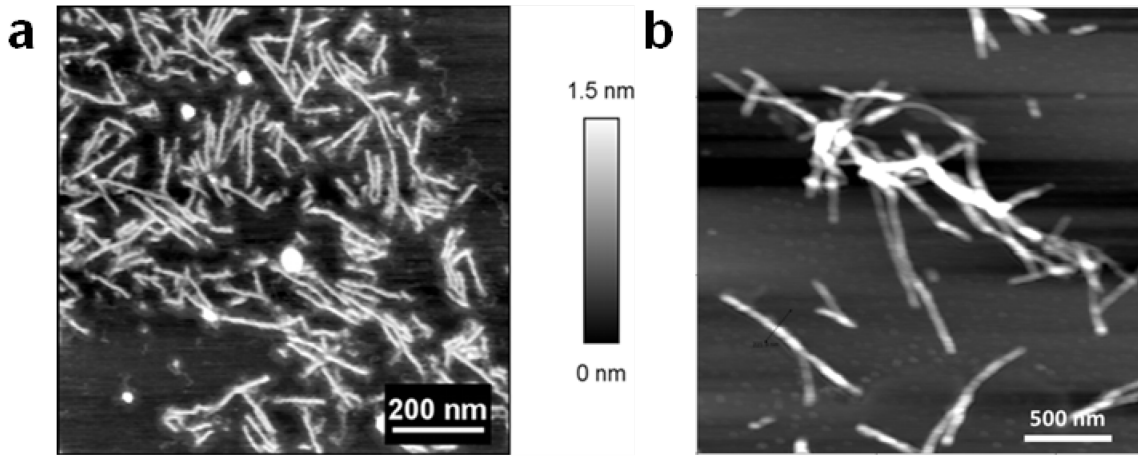


Figure S3: (a) Detection of FITC- β -Ala-A β 42 fibrils by atomic force spectroscopy. FITC- β -Ala-A β 42 (1 μ M) had been incubated for 5 days at 37 °C. Afterwards the sample had been imaged by atomic force microscopy in air on mica surface. The greyscale on the right side indicates height from black to white. (b) For comparison, A β 42 fibrils (80 μ M) after 4 days preincubation in 10 mM NaPi, pH7.4 at RT and 600 rpm. Diluted samples had been air dried on mica before analysis by tapping mode in air.

In order to demonstrate that the fluorophore labelled A β peptide was capable of fibril formation a solution of 1 μ M FITC- β -Ala-A β 42 had been incubated in phosphate buffered saline, pH 7.4 for 5 days at 37°C. Forty-microliter aliquots of the samples were transferred to freshly cleaved mica. After 30 min to 40 min incubation the mica surface was washed three times with 100 μ l deionized water (Millipore). Excess water was removed with compressed N₂. Imaging of FITC-A β 42 was performed with Nanowizard II (JPK Instruments AG) in intermittent contact in air⁵, using standard silicon cantilevers (OLYMPUS OMCL-AC160TS). In AFM fibrils with rather uniform diameter and 100 to 200 nm length were detected (Fig. S3a). For comparison amyloid fibrils formed in a sample of unlabelled A β 42 are shown in Fig. S3b.

Dynamic light scattering in parallel to SANS measurements

Samples used for SANS were in parallel subjected to dynamic light scattering measurements. Experiments were performed with a Zetasizer Nano ZS (Malvern Instruments, Worcestershire, UK). The instrument uses a He-Ne laser with $\lambda = 632.8$ nm and vertical polarization in backscattering geometry at 173° . The sample cell is a UV-Cuvette micro (BRAND, Wertheim, Germany) with 70 μ l sample volume. To cover also larger aggregates the measurements duration was set to 1h to get reliable data at long times. The auto correlation function was analyzed by non-negative least square (NNLS) algorithm⁶ followed by protein analysis (L-curve)⁷ as implemented in the instrument software. Figure S4a shows the correlation functions with the resulting distribution of relaxation times after 0.5 h incubation at 7°C for the three different A β 42 concentrations also studied by SANS. Surprisingly, we observe for the lowest A β 42 concentration the slowest relaxation indicating the largest aggregates. This effect might be caused by a faster aggregation at higher A β 42 concentrations leading to aggregates that are large enough to sediment before the DLS measurement. The relaxation time distributions from L-curve analysis show three populations. For the higher concentrations we observe 3 populations analogously in size: low molecular weight oligomers (LMW) with $R_H \approx 4$ nm, middle molecular weight oligomers (MMW) with $R_H \approx 11$ nm and high molecular weight oligomers (HMW) with $R_H \approx 70$ nm. For the lowest concentration we observe two populations of much larger size ($R_H > 100$ nm) and one population around the average size of the populations observed at higher concentration. In case of the lowest concentration the correlation function is dominated by the contribution of the larger aggregates. The L-Curve analysis, in the same way as the well-known CONTIN analysis⁸, tries to minimize the number of populations resulting in only one population describing the smaller aggregates as one population of minor contribution to the overall signal.

We observe the remaining populations, which contribute stronger to the signal allowing the L-curve analysis to resolve details of the contributing populations.

Monomers as observed in SEC measurements have a hydrodynamic radius of about 1 nm⁹. Monomers cannot be separated from the contribution of LMW because of the small scattering contribution even if their concentration might be large as the scattered intensity is proportional to R^6 . On the other side for a separation of species in DLS hydrodynamic radii need to be separated by a factor of 5, which is not given for monomers and LMW oligomers. The HMW oligomers contribute a factor 4 more to the scattered intensity than the LMW oligomers despite their extreme low concentration (<1% volume fraction) because of their huge size. Increasing the concentration to 1 mg/ml the MMW species grows to 33% (intensity fraction), which was also observed in prior research³. With more than 80% v/v the LMW oligomers are the main component of the oligomers (Fig. S4b).

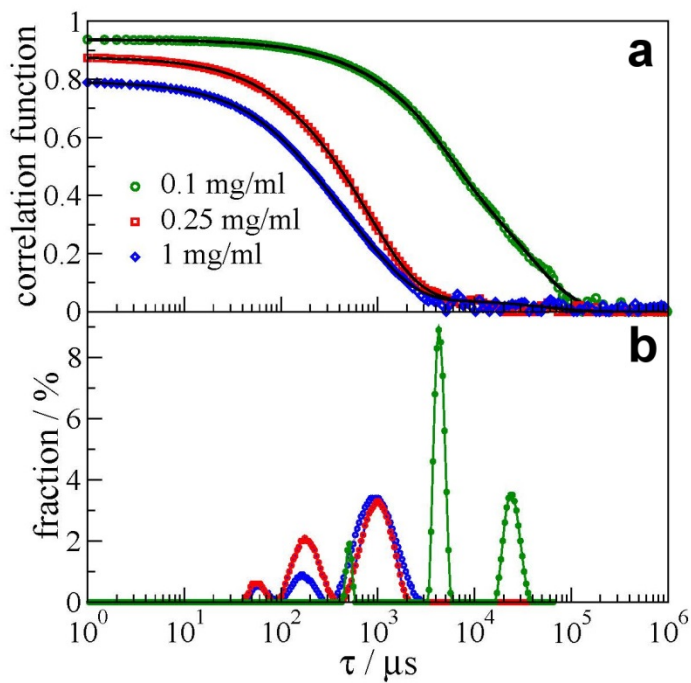


Figure S4: DLS experiments of A β 1-42 after 0.5 h incubation at 7°C. **(a)** Correlation functions with the result of the L-Curve analysis as black line over the data. **(b)** Intensity weighted relaxation time distribution with colours as in a). X-scales of a) and b) are the same.

Calculation of hydrodynamic radii for different oligomers based on determined sedimentation coefficients

For comparability, hydrodynamic radii for three different oligomers, the tetramer, pentamer and hexamer have been calculated assuming a hydration of 0.398 g H₂O/g protein. Equation (S1) is obtained from the Svedberg equation by insertion of the expression for the frictional coefficient $f = 6\pi\eta R_H$ according to Stokes' law.

$$R_H = m(1 - \bar{v}\rho)/6\pi\eta s \quad (\text{S1})$$

with $m = (nM_p + \delta nM_p)/N_A$ and $\bar{v} = (M_p\bar{v}_p + \delta M_p\bar{v}_h)/(M_p + \delta M_p)$

- R_H hydrodynamic radius
- m mass of hydrated oligomer build from n monomers
- ρ water density at 20°C: 0.99823g/cm³
- η water viscosity at 20°C: 0.01002 Poise
- s sedimentation coefficient in water at 20 °C
- M_p molar mass of protein
- δ estimated fraction of bound hydration water, here $\delta = 0.398$ g H₂O/g protein¹⁰⁻¹²
- N_A Avogadro constant
- \bar{v}_p partial specific volume of protein (index p)
- \bar{v}_h partial specific volume of hydration shell (index h)

The density of hydration shell water is assumed to be 10 % higher than bulk water density¹³.

Table S2: Calculated hydrodynamic radii for the different oligomeric states based on experimentally determined sedimentation coefficient.

Given:	A β 42	MW (g/mol)	R_H (nm)
$s_{20,w} = 2.56$ S	tetramer	1.8056E+04	1.85
	pentamer	2.2571E+04	2.31
	hexamer	2.7085E+04	2.77
	AF488-A β 42	MW (g/mol)	R_H (nm)
$s_{20,w} = 2.32$ S	tetramer	2.1351E+04	2.63
	pentamer	2.6689E+04	3.28
	hexamer	3.2027E+04	3.94

Determination of molar mass M based on scaling law:

N_A is the Avogadro constant $6.022 \cdot 10^{23} \text{ mol}^{-1}$, ρ the density of water at 20 °C (0.998 g/cm³), η the viscosity of water at 20 °C (0.010019 Poise), \bar{v} the partial specific volume (0.7377 cm³/g) of A β 42.

$$\left(\frac{M}{N_A}\right)^{2/3} = \frac{s \cdot f / f_0}{1 - \bar{v}\rho} 6\pi\eta \left(\frac{3\bar{v}}{4\pi}\right)^{1/3}$$

For a particle with sedimentation coefficient $s_{20,w}=2.56$ S and frictional ratio $f/f_0=1.2$ the molar mass calculated with the above equation is 26,100 g/mol. This is in agreement with the pentamer/hexamer of A β 42.

Sedimentation velocity analysis in the presence of 150 mM sodium chloride

In order to investigate that the different ionic strength conditions lead to comparable A β 42 size distributions in SV analysis we analysed 1 μ M FITC- β -Ala-A β 42 in phosphate buffer with 150 mM NaCl (Fig. S5). The truncated peak at 0.3 S is caused by free fluorophore. The oligomer fraction is slightly higher than at lower salt conditions. Nevertheless the oligomer

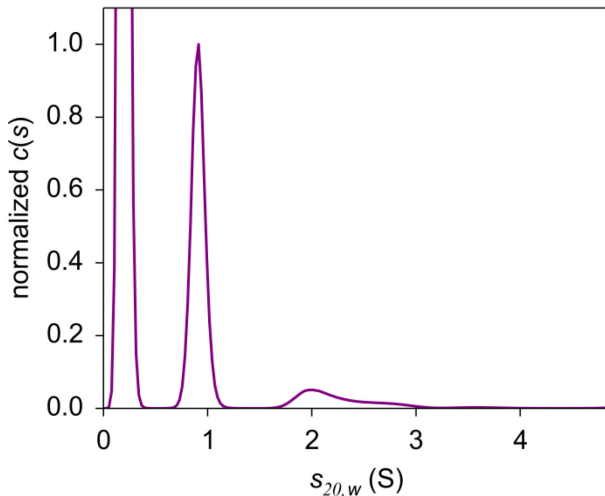


Figure S5: SV analysis of 1 μM FITC- $\beta\text{-A}\beta\text{42}$ in phosphate buffer with 150 mM NaCl, pH 7.4; at 20°C and 60,000 rpm. Normalization with regard to peak height of monomeric FITC- $\beta\text{-A}\beta\text{42}$.

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