1 **TITLE**

2 **Machine Learning and Network Analysis of Molecular Dynamics**

3 **Trajectories Reveal Two Chains of Red/Ox-specific Residue Interactions in**

Human Protein Disulfide Isomerase

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SUPPLEMENTARY INFORMATION Supplementary Section

METHODS

Molecular Dynamic Simulations

X-ray crystal structures of ox-hPDI (PDB ID: 4EL1) and red-hPDI (PDB ID: 4EKZ) were

used as initial conformations for MD simulations¹ with CHARMM 27 force field in the

NAMD 2.10 package². Short missing regions including residues 250 to 254, 321 to 323 and

single residue 479 were recovered using Modeller $9.13³$. Missing hydrogens were added by

Reduce 3.23⁴. Each system was then solvated in a rectangular box of around 16491 TIP3P

water molecules with at least 10 Å padding around protein and neutralized by addition of 23

Sodium ions. Both systems were minimized for 20000 steps of conjugate gradient method

while harmonic restraints with a force constant of 10 kcal mol⁻¹ \AA^{-2} were applied to protein

heavy atoms. Gradual heat up from 10 to 300 K were then performed via 500 ps NPT

dynamics with a time step of 1 fs while harmonic restraints were gradually relaxed. Nosé-

Hoover Langevin piston was used to keep pressure at 1 atm and Langevin thermostat was

used to control temperature^{5,6}. Periodic boundary conditions were applied and non-bonded

interactions were truncated at 12 Å using a smooth switching started at 10 Å. Long-range

electrostatic interactions were calculated using the particle mesh Ewald (PME) method with a

grid spacing of 1 \AA^7 . After heat up and removal of restraints, the equilibration phase was

continued at 300 K up to 2 ns. In subsequent MD simulations, the time step was increased to

2 fs and all bonds with hydrogen partners were kept rigid using the SHAKE algorithm. MD

trajectories were recorded every 4 ps. To accelerate the conformational sampling, both

systems were simulated for 10 ns and recorded structures were clustered based on their

backbone RMSD via the quality threshold (QT) algorithm implemented in the VMD 1.9

package ^{8,9}. Six representative structures from most populated clusters of each of the ox-hPDI

and red-hPDI systems were then used as starting points of 55 ns NPT dynamics and all

recorded snapshots excluding those of the first 3 ns were used for subsequent analysis. This

consists of 156000 structures from a total of 600 ns NPT simulation.

Cross Correlation and Principal Component Analysis

Backbone RMSD for each domain and whole protein was calculated along each trajectory

with respect to the first production frame. Secondary structure character of all residues were

calculated over trajectories using the STRIDE program¹⁰. To identify groups of residues with

correlated motions, cross correlation matrix of atomic displacements was calculated according to equation (1):

$$
C_{ij} = \langle (\vec{r}_i - \langle \vec{r}_i \rangle)(\vec{r}_j - \langle \vec{r}_j \rangle) \rangle / \sqrt{\langle (\vec{r}_i - \langle \vec{r}_i \rangle)^2 \rangle \langle (\vec{r}_j - \langle \vec{r}_j \rangle)^2 \rangle}
$$
 (Eq. 1)

where c_{ij} is the cross correlation or normalized covariance between displacements of atoms *i*

and *j* with position vectors \vec{r}_i and \vec{r}_j , respectively ¹¹. The angular bracket $\langle \rangle$ represents time

average over collected trajectory and Cα atoms were considered as reference for position of

each residue. By this definition, c_{ij} elements, take values between -1 and 1. Extreme values -1

and 1 show average movements in opposite or the same direction, respectively, while a value

near 0 corresponds to uncorrelated displacements or movement in orthogonal directions.

Before calculation of cross correlation matrix, the overall rotation and translation of protein

were eliminated from trajectory by alignment from Ca atoms of domains b and b' to the first

frame of the first production trajectory. Though there are many arbitrary choices for such an

alignment in a multi-domain protein, our choice is the most reasonable in the case of hPDI

since the bb' pair of domains act as a base for domain motions.

To address domain motions in a more quantitative manner, some inter-domain geometric

variables were defined and calculated over trajectories. Six inter-domain distances denoted as

 $R_{ij}(i, j \in \{a, a', b, b'\})$ were defined between domain geometric centers. Two inter-domain

angles $\Theta_{abb'}$ and $\Theta_{bb'a'}$ were defined between abb' and bb'a' domain centers, respectively.

One torsion angle Φ_{abba} was also defined as the angle between two intersecting planes

formed by abb' and bb'a' domain centers. Beside these mechanical "ball and spring" variables, a more comprehensive assessment of domain dynamics was performed via principal component analysis (PCA) of Ca Cartesian coordinates. The standard PCA was performed by superimposition of trajectories on Ca atoms of domains b and b' and diagonalization of covariance matrix of atomic fluctuations to obtain corresponding eigenvectors and eigenvalues in descending order. MD trajectories were then transformed to the new space defined by eigenvectors. To compare oxidized and reduced systems, all trajectories were joined together for PCA. To analyze and visualize hPDI motions in reduced

dimensions, the most important collective modes of motions were selected based on their

eigenvalue magnitudes (i.e. their contribution in total variance). For visualization purposes

principal components were transformed back to Cartesian coordinates. The same procedure

was also repeated for two-domain subsets of coordinates including ab, bb' and b'a' domain

pairs to obtain basic two-domain motions that results in complicated four-domain dynamics.

The free energy landscape (FEL) spanned by the first two principal components PC1and PC2

is given by equation (2).

$\Delta G(PC_1, PC_2) = -k_B T[\ln \rho (PC_1, PC_2) - \ln \rho_{\max}]$ (Eq. 2)

where (PC1, PC2) is the probability distribution function obtained from MD data and ρ_{max} is

its maximum value which is subtracted to put zero of free energy on the most probable

conformation. The kernel density estimation with a Gaussian kernel was used for construction of probability distribution functions. Projected FELs were also obtained for PC1-PC3 and PC2-PC3 subspaces.

To check the performance of adopted multi-trajectory approach in sampling of conformational space of hPDI, the inner products between PCA eigenvectors obtained from

all data and those of different halves of the data were compared in Figure S10. Comparison of

diagonal and off diagonal elements in panel b of Figure S10 shows that the directions of

important collective motions would be the same if one considers only the half-length of all

trajectories while this is not true for full-length of all trajectories. Accordingly, starting from

multiple configurations is crucial for efficient sampling and for avoiding from trapping regions of landscape.

Statistical Machine Learning Methods

Two types of structural variables were considered to discriminate dynamical behavior of ox-

and red-hPDI: *i*) Domain level features including R_{ij} , Θ_{abb} , $\Theta_{bb'a'}$ and $\Phi_{abb'a'}$. *ii*) Residue

level features including pairwise residue-residue distances d_{ij} , defined as the Euclidean

distance between Cα atoms of residues *i* and *j* . Values of these parameters were collected

from all trajectory snapshots and labeled as "ox" or "red". To find those features that can

discriminate oxidized states from reduced ones, a binary Support Vector Machine (SVM) was

used to classify conformations as oxidized or reduced states. Those features that result in

higher classification accuracy are assumed to be more important in description of dynamical

differences between ox- and red-hPDI systems. Let *V* be any of the considered dynamical

features, with observed ranges of values $[V_{\min}^{Ox}, V_{\max}^{Ox}]$ and $[V_{\min}^{Red}, V_{\max}^{Red}]$ $\mathcal{F}^{\text{Re } d}_{\min}$, $V^{\text{Re } d}_{\max}$] in ox- and red-hPDI

systems, respectively. The question is to what extent the red/ox state of the protein can be

determined solely based on *V* values. In a special case with $|V_{\min}^{Ox}, V_{\max}^{Ox}| = |V_{\min}^{Red}, V_{\max}^{Red}|$ max $\left[V_{\text{max}}^{Ox}\right] = \left[V_{\text{min}}^{\text{Re }d}, V_{\text{max}}^{\text{Re }d}\right]$ the

state of the protein cannot be determined accurately based on the observed *V* values. On the

other hand, if $[V_{\min}^{Ox}, V_{\max}^{Ox}] \cap [V_{\min}^{Red}, V_{\max}^{Red}] = \phi$ V_{min}^{Ox} , V_{max}^{Ox} $\bigcap V_{\text{min}}^{\text{Re } d}$, $V_{\text{max}}^{\text{Re } d}$ $\big] = \phi$, there is no overlap between sampled ranges of

V values in red and ox trajectories and a given frame from an unknown trajectory can be

classified, at 100% accuracy, to either ox or red state, depending on its *V* value. For instance,

if V_{max}^{Ox} < $V_{\text{min}}^{\text{Re }d}$ then a threshold of V_{sep} in the open range $(V_{\text{max}}^{Ox}, V_{\text{min}}^{\text{Re }d})$ can be used to

discriminate the red/ox state of any hPDI structure. In other cases with limited overlap

between $[V_{\min}^{Ox}, V_{\max}^{Ox}]$ and $[V_{\min}^{Re d}, V_{\max}^{Re d}]$ $\mathcal{F}^{\text{Re } d}_{\min}$, $\mathcal{V}^{\text{Re } d}_{\max}$] ranges, we used a custom linear discriminator to find

an optimum value for V_{sep} from statistical distributions of *V* values in ox and red states which

maximizes the accuracy of ox vs. red discrimination based on the value *V* of a given

snapshot. We also used the SVM with radial-basis kernel to improve ox vs. red

discrimination accuracy over the linear models. Although this method could not provide a

single threshold V_{sen} , it significantly improved the discrimination accuracy in several cases,

particularly when the distribution of *V* was bimodal or multi-modal in some state. In all cases

the classifier was trained with 50% random selection of all available frames (in both ox and

red states) and tested with the rest of the frames. (Code available upon request)

Dynamic Residue Interaction Network (DRIN)

The standalone version of RING 2.0 program was used for calculation of residue interaction

network (RIN). Five types of non-covalent interactions were considered including hydrogen

bond, van der Waals, salt bridge, π - π and cation- π interactions. The RING was used in a

mode that reports multiple interactions per residue pair but only one interaction per

interaction type. Accordingly, each of the 156000 structures was converted to a graph with

residues as its vertices and the pairwise interactions of the residues as its edges. There could

0

By this definition, for each type of interaction, 156000 RIN graphs were compiled to two

single DRIN graphs for each of the ox- and red-hPDI systems. The simpler choices, such as

summing $A_{ij}(t)$ for each pair of residues during the whole period of time, results in noisy and

be different edges between a pair of residues due to different types of non-covalent interactions. از یͷ برنامه ی لینوکس که خود توسعه دادیم، شبͺه ی برهم کنش اسید آمینه ها۴۴ را برای هر برداشتِ ساختاری

Let *n* be the number of residues and $A_{ij}(t)$ be the $n \times n$ adjacency matrix of a RIN graph for \sim 1 \sim 1

each type of non-covalent interaction. The $A_{ij}(t)$ elements are equal to zero or one for the $\frac{1}{\sqrt{2}}$

absence or presence of considered type of interaction between residues *i* and *j* in time *t* of • برهم کنش های π−Cation

some MD trajectory. From time series of $A_{ij}(t)$, the maximum interaction life time, Γ_{ij} , was

then extracted to build the matrix Γ which will be denoted here as the DRIN matrix for

considered type of non-covalent interaction. Here we define Γ_{ij} as the maximum length of a \mathbf{L} , and \mathbf{L} is a very set of the set of \mathbf{L}

transient on-and-off interactions often make a big total which could often dominate the effect

of persistent interactions. Accordingly, a DRIN matrix can be considered as a complete $n \times n$

weighted graph with edge weights equal to Γ_{ij} . The DRIN matrices Γ_{ij}^{Ox} and Γ_{ij}^{Red} were

calculated for each of the ox- and red-hPDI systems, respectively, and for all five types of

non-covalent interactions considered. Values of Γ_{ij} elements were averaged over six

separate trajectories of each system.

continuous period of time in which a persistent interaction type is observed in the RIN graphs به همین دلیل با تغییر روی کرد، برهم کنش هایی را جستجو کردیم که در حالت اکسید یا احیا به صورت

between the residues *i* and *j*:

$$
\Gamma_{ij} = \arg \max_{\tau} \left\{ \exists \tau_0 : \left(\prod_{t=\tau_0}^{\tau+\tau_0-1} A_{ij}(t) \right) = 1 \right\} \qquad \text{(Eq. 3)}
$$

To highlight differences between oxidized and reduced states, we computed the differential DRIN graph Δ with the same nodes and edges as DRIN graph, but adjusted weights that represent the fold change of Γ_{ij} values between ox- and red-hPDI systems. More specifically,

the elements of the differential DRIN matrix Δ were computed for each type of interaction as:

$$
\left(\Gamma_{ii}^{0x}+\varepsilon\right)
$$

In the above equation, ε is a small positive value with negligible effect on the outcome,

which is considered to prevent the division by zero. In our study, we set ϵ equal to the time

between two consecutive MD snapshots that means we have elongated the maximum

duration of each interaction by 1 more frame. This is negligible with respect to the values of

 Γ_{ii} for persistent interactions that were in the order of hundreds or thousands of frames.

We used the differential DRIN matrix in a number of ways. By considering a cutoff on the

absolute values of Δ_{ii} we could identify the pairs of residues that had a significant alternated

pattern of interactions between ox and red states. We could also consider Δ as the weights of

a graph, where positively and negatively weighted edges depict the interactions that are more

persistent in ox and red states, respectively. We visualized such a network using the

Cytoscape version 3.3.0, by assigning the colors and the thickness of the edges according to

the interaction weight in differential DRIN matrix. For visualization and analysis purposes

differential DRIN graphs obtained for different types of interactions were merged together in

a single graph with different edge styles.

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atomic fluctuations in molecular dynamics and normal mode simulations. *Proteins* **11,**

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Figure S1 backbone RMSD values with respect to the initial structure for single domains and whole protein in oxidized (**a** and **b**, respectively) and reduced (**c** and **d**, respectively) hPDI conformations.

Figure S2 The cumulative contribution of principal components in total variance.

SUPPLEMENTARY FIGURES

Figure S4 hPDI domain motion modes (PC5 & PC6).Total coverage of variances are represented as % for each PC.

Figure S5 Two domain principal motions of hPDI. Total coverage of variances are represented as % for each PC.

Figure S3 Distance between the catalytic Cysteines of the a and a' domains.

Figure S6 Representative conformations of FEL in oxidized hPDI.

Figure S7 Representative conformations of FEL in reduced hPDI.

Figure S8 Oscillation frequency of D secondary structure in **(a)** oxidized and **(b)** reduced conformations of hPDI. B: Isolated bridge; C: Coli; G: 3-10 helix; H: Alpha helix; I: Pi helix; E: Extended conformation; CT: Coil and turn.

Figure S9 Schematic view of domain- and residue- level structural features.

(a) (b)

Figure S10 The overlap between whole data and its different halves **(a);** The overlap between eigenvectors of all twelve trajectories versus to the first half of all trajectories (panel left **b**) and also versus to the half of all trajectories (panel right **b**) by evaluation of their scalar product; Values are represented between the range of 0 to 1 with lower and higher overlaps, respectively. (**c**) The cumulative contribution of principal components in total variance in all twelve trajectories, the first half of all trajectories and also the half of all trajectories.

SUPPLEMENTARY TABLES

Table S2 Overview of the experimentally point mutations in hPDI compared to the DRIN results (highlighted in red columns).

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Table S2 Overview of the experimentally point mutations in hPDI compared to the DRIN results (highlighted in red columns).

 C30 6592 31 43.8 51.7 33.3 60.1 34 86 126.9 5.5 8.8 63.4 -52.5 -44.5 18.8 **231 8816 33.1 43.2 45.2 56.7 56.7 82.8 42.9 56.7 82.8 56.7 83 52.9 52.9 52.9 52.9 52.9 534.2 54.2 54.2 54.2 54.** C32 29128 32.3 42.1 42.7 32 55.1 32.5 81.8 117.3 9.7 -19.3 112.1 25.7 -67 0.9 $\sqrt{33}$ $\sqrt{34421}$ $\sqrt{32.1}$ $\sqrt{44.5}$ $\sqrt{38.6}$ $\sqrt{32.3}$ $\sqrt{54.7}$ $\sqrt{34.87.2}$ $\sqrt{32.9}$ $\sqrt{34.9}$ $\sqrt{38}$ $\sqrt{35.4}$ $\sqrt{36.4}$ $\sqrt{36.4}$ $\sqrt{32.7}$ $\sqrt{35.4}$ $\sqrt{36.4}$ $\sqrt{32.7}$ $\sqrt{35.4}$ $\sqrt{35.4}$ $\$ $\sqrt{3}^{34}$ 154370 33.2 463.6 58.6 332.4 66 \$4.1 36 \$5.6 $\sqrt{3}^{2.4}$ 150.8 652 150.40.8 6527.8 30.0^{14.8} 100.30.3 151.039.9 70.0^{-71.9} 0.0^{-4.1} C35 28171 32.8 54.7 73.3 32.1 55.7 31.3 114.8 123.1 84 -255.2 -139.8 6.9 109.9 3.5 **Table S1**³⁶Structural features of representative conformers from FEL. R: imter domain distance; θ: ⁹ angle; Φ: Dihedral torsion. **The angles of representative conformation** and angles from the distance of an angle ├──C31 8816 33.1 43.2 45.2 56.7 56.7 33 82.8 121 -1.9 52.9 89.3 -34.2 -28.8 75.4 H C32 129128 32.3 42.1 42.7 55.1 55.1 32.5 81.8 117.3 9.7 -19.3 112.1 25.7 9.7 9.9 H C33 | 24421 | 32.1 | 44.5 | 48.6 | 32.3 | 54.7 | 32.9 | 87.2 | 113.9 | 105.4 | 60.4 | 98.4 | −32.7 | 13.8 H C34 14370 33.2 43.6 58.6 83.2 83.2 83.2 140.8 27.8 44.8 9 39.9 -71.9 4.1 C35 28171 32.8 54.7 73.3 32.1 55.7 31.3 114.8 123.1 84 -255.2 -139.8 6.9 109.9 3.5 C36 15299 33.2 46.6 66.3 32.3 66.5 36.5 90.7 150.5 6.5 39.9 -109.8 -154.9 -78.3 8.9

