Supplementary Information

Coarse graining bacteria colonies for modeling critical solute distributions in picoliter bioreactors for bacterial studies on single-cell level

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January 23, 2017

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Table 1: Number of mesh elements

Model	2 Cells	20 Cells	50 Cells	100 Cells	200 Cells
Model 1a	1.3619×10^6	1.3619×10^6	$1.3619 imes 10^6$	$1.3619 imes 10^6$	$1.3619 imes 10^6$
Model 1b	1.3619×10^6	1.3620×10^6	1.3612×10^6	$1.3615 imes 10^6$	1.3616×10^6
Model 2a	1.3633×10^6	1.3635×10^6	1.3630×10^6	1.3643×10^6	1.3633×10^6
Model 2b	1.3635×10^6	1.3636×10^6	1.3635×10^6	1.3650×10^6	1.3642×10^6
Model 3a	1.5721×10^6	2.9147×10^6	4.3734×10^6	$6.8687 imes 10^6$	4.7444×10^6
Model 3b	1.5817×10^{6}	1.7546×10^{6}	4.4118×10^6	3.1349×10^{6}	6.4294×10^6

Table 2: Mesh independence for geometry with 100 cells

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Model	Elements	Elements	Maximum concentration difference
	Normal mesh	Refined mesh	in xy-plane at half-chamber height
Model 1a	1.3619×10^{6}	6.050076×10^{6}	$4.9 \times 10^{-2} \mathrm{mmol/L}$
Model 1b	$1.3615 imes 10^6$	6.052157×10^{6}	$2.1 imes 10^{-3} \mathrm{mmol/L}$
Model 2a	$1.3643 imes 10^6$	6.079938×10^{6}	$3.5 imes 10^{-3}\mathrm{mmol/L}$
Model 2b	$1.3650 imes 10^6$	6.079938×10^{6}	$3.6 imes 10^{-3}\mathrm{mmol/L}$
Model 3a	$6.8687 imes 10^6$	26.281688×10^6	$2.7 imes 10^{-3} \mathrm{mmol/L}$
Model $3b$	3.1349×10^6	13.547256×10^{6}	$5.5 \times 10^{-3} \mathrm{mmol/L}$



Figure 1: Measurements of the simulated chamber geometry with supply channels.



Figure 2: Different model geometries in comparison to the respective microscope images. Model 1a is not shown.



Figure 3: Nutrient distribution within microcolonies based on simulations with different coarse graining concepts. The graphs and respective zoom-outs show the glucose concentration along the y-axis through the center of the chamber/colony in mmol/L for the colony with 20 cells (A, B) and 200 cells (C, D) and two medium glucose concentrations of 0.5 mmol/L (A,C) and 5 mmol/L (B,D).



Figure 4: Nutrient distribution within microcolonies based on simulations with different coarse graining concepts. The graphs and respective zoom-outs show the glucose concentration along the x-axis through the center of the chamber/colony in mmol/L for the colony with 20 cells (A, B) and 200 cells (C, D) and two medium glucose concentrations of 0.5 mmol/L (A,C) and 5 mmol/L (B,D).



Figure 5: The concentrations B and A - B normalized to C, the Gini coefficient and the average relative uptake rate for each model and colony size and the nutrient concentration of 0.5 mmol/L.



Figure 6: The concentrations B and A – B normalized to C, the Gini coefficient and the average relative uptake rate for each model and colony size and the nutrient concentration of 5 mmol/L.



Figure 7: The concentrations B and A - B normalized to C, the Gini coefficient and the average relative uptake rate for each model and colony size and the nutrient concentration of 50 mmol/L.