

# Supplementary Material

## **Additional File 1**

The following tables provide additional information on our new test sets of biological and randomly generated HP sequences and the results from our computational experiment with ACO-HPPFP-3 and PERM. For the biological sequences, we show the PDB IDs of the original protein sequences. Note that in our translation from protein sequences into HP strings, non-standard amino acid symbols, such as X and Z, were skipped; consequently, some of our HP strings differ in length from the respective PDBSELECT sequences.

ID	PDB ID	HP sequence	Length
B30-1	1HA9:A	phpphhphphpppppppphhphpphph	34
B30-2	1CE4:A	pphpppppphphhhphphhhphpph	35
B30-3	1FWO:A	pphpppphphhhpppphhphhhphpph	35
B30-4	1ZTA	hphpphpppphphpphpphphpph	35
B30-5	1G1Z:A	pphphhhpphhhhpphphhhphph	31
B30-6	1BZG	hhppphhpphpphpphphhhphpph	34
B30-7	1BH7	hphpphhhhphhphphhhhhpphph	33
B30-8	1B4G	hhpphphphpphpphpphpph	29
B30-9	1BNX:A	phhhhhpphphhhhhhhphhhhhhh	33
B30-10	1FCT	hhhhpphphhhhhhhphhhhhhh	32

Table A-1: Biological sequences of length  $\approx 30$

ID	$E_{min}$ (2D)	PERM			ACO
		$t_1$	$t_2$	$t_{exp}$	$t_{avg}$
B30-1	-12	0.43	0.56	0.49	0.71
B30-2	-12	0.15	4.09	0.29	1.08
B30-3	-14	0.15	0.02	0.04	1.19
B30-4	-10	2.5	0.3	0.54	3.64
B30-5	-13	0.10	0.17	0.12	0.22
B30-6	-13	0.84	10.40	1.55	70.94
B30-7	-16	0.02	0.02	0.02	0.19
B30-8	-8	0.09	0.003	0.006	0.17
B30-9	-18	0.002	0.008	0.003	0.06
B30-10	-16	0.003	12.50	0.006	4.08

Table A-2: Performance comparison of PERM and ACO-HPPFP-3 on biological sequences of length  $\approx 30$  in 2D

ID	$E_{min}$ (3D)	PERM			ACO
		$t_1$	$t_2$	$t_{exp}$	$t_{avg}$
B30-1	-17	1.14	1.03	1.08	1.19
B30-2	-16	1.06	1.3	1.17	2.29
B30-3	-18	1.20	1.20	1.20	2.34
B30-4	-16	3.4	1.2	1.77	20.18
B30-5	-20	2.2	3.04	2.55	65.71
B30-6	-19	1.20	1.50	1.33	23.18
B30-7	-25	1.10	2.40	1.51	62.36
B30-8	-13	1.10	1.07	1.09	1.74
B30-9	-26	1.20	1.09	1.14	1.57
B30-10	-24	1.8	3 291	3.60	163.23

Table A-3: Performance comparison of PERM and ACO-HPPFP-3 on biological sequences of length  $\approx 30$  in 3D

ID	PDB ID	HP sequence	Length
B50-1	1KBF:A	hphpppppppphhpphpppppphhhhpppppppppppppphhpp	49
B50-2	1KBH:A	phpppphhhhpphpphhpppphphpphphhhhhphhpphphhp	47
B50-3	1G9P:A	hhhhhhhhpppppppppphphpppphphhhhhhhhhhhhh	45
B50-4	1YUJ:A	hphpphphhhpppppppppphphhphhhhhpppppphphpph	50
B50-5	1GAB	phpphhpppphhhhpphphpphhpphhphpppphphpphph	53
B50-6	2BRZ	pppphhpphhpppphhpppphpppphphpphphpppphphpph	53
B50-7	1VPC	pphphphhhhhpphphhhhhphhpppphhhhpppppphhppp	45
B50-8	1VIB	hphhhhhhhpppppppphphpphphhhhhpphphppppppppp	54
B50-9	1CEU:A	hphhpppphpppphphphpphphpppphphhphhhpphphpph	51
B50-10	1CFH	hphhphpphhphpppppppppphphpphphpppppppphphpph	47

Table A-4: Biological sequences of length  $\approx 50$

ID	$E_{min}$ (2D)	$t_1$	PERM		ACO
			$t_2$	$t_{exp}$	$t_{avg}$
B50-1	-12	5.60	3.90	4.60	39.5
B50-2	-19	650.40	0.90	1.80	283.31
B50-3	-20	3.80	0.04	0.08	2.47
B50-4	-17	3.33	2.24	2.68	184.5
B50-5	-22	4.90	117.80	9.41	820.37
B50-6	-14	0.43	0.74	0.55	2.08
B50-7	-17	270.70	298.80	284.06	130.35
B50-8	-14	0.04	2.16	0.07	0.29
B50-9	-21	0.40	0.23	0.29	55.32
B50-10	-14	0.27	0.3	0.28	3.22

Table A-5: Performance comparison of PERM and ACO-HPPFP-3 on biological sequences of length  $\approx 50$  in 2D

ID	$E_{min}$ (3D)	$t_1$	PERM		ACO
			$t_2$	$t_{exp}$	$t_{avg}$
B50-1	-18	2.08	1.50	1.74	14.65
B50-2	-29	43.60	18.20	25.68	701.84
B50-3	-28	1.40	1.30	1.35	5.52
B50-4	-28	2.29	1822.2	117.90	(-27)
B50-5	-37	18.2	1235.9	164.87	(-36)
B50-6	-25	2.80	10.7	4.44	1638.29
B50-7	-26	406.90	2.70	5.36	814.11
B50-8	-25	10.05	(-24)	-	1026.12
B50-9	-36	3492.6	4.03	16.10	(-35)
B50-10	-22	2.50	1.40	1.80	200.68

Table A-6: Performance comparison of PERM and ACO-HPPFP-3 on biological sequences of length  $\approx 50$  in 3D

ID	HP sequence	Length	$H$ fraction
R30-1	pphphpphpphppppphhphpphhpph	30	0.40
R30-2	hppppphhphhhpphpphhhhhhhhpph	30	0.53
R30-3	pphpphpppphhpppphphpphphhhhh	30	0.47
R30-4	pphhhhpppphphpphphpppppphphh	30	0.40
R30-5	hhppphhphpphhphhhpphphpphphpph	30	0.50
R30-6	phhpphphppppphhhphpppppphhhh	30	0.43
R30-7	phhhphhhpppphphpphphhhpppppph	30	0.47
R30-8	pphpphhphphhhpphphhhphhhphph	30	0.50
R30-9	hhphpppphpppphphpphphpphphph	30	0.43
R30-10	hphphpphphhphpphphhhhhphhphhp	30	0.53

Table A-7: Random sequences of length 30

ID	$E_{min}$ (2D)	PERM			ACO
		$t_1$	$t_2$	$t_{exp}$	$t_{avg}$
R30-1	-90	0.4	0.001	0.002	0.27
R30-2	-13	1.60	0.011	0.022	0.58
R30-3	-10	0.14	0.001	0.002	0.17
R30-4	-9	0.04	0.07	0.05	0.26
R30-5	-13	0.01	0.038	0.02	0.44
R30-6	-11	86.3	0.33	0.65	12.85
R30-7	-8	0.007	0.03	0.01	0.10
R30-8	-12	0.033	0.017	0.045	0.38
R30-9	-9	0.002	0.11	0.004	0.14
R30-10	-12	0.007	0.001	0.002	0.34

Table A-8: Performance comparison of PERM and ACO-HPPFP-3 on random sequences of length 30 in 2D

ID	$E_{min}$ (3D)	PERM			ACO
		$t_1$	$t_2$	$t_{exp}$	$t_{avg}$
R30-1	-13	0.16	0.16	0.16	0.47
R30-2	-18	0.22	0.44	0.29	3.44
R30-3	-15	1.00	1.85	1.30	17.81
R30-4	-12	0.14	0.26	0.18	0.25
R30-5	-19	0.53	0.51	0.52	28.77
R30-6	-14	0.22	0.10	0.14	1.11
R30-7	-11	0.118	0.067	0.09	0.055
R30-8	-17	0.19	0.28	0.225	0.57
R30-9	-14	0.22	0.24	0.23	1.48
R30-10	-19	2.22	0.27	0.48	16.69

Table A-9: Performance comparison of PERM and ACO-HPPFP-3 on random sequences of length 30 in 3D

ID	HP sequence	Length	$H$ fraction
R50-1	ppphrphrpppprphhhphhhpppprphrphppprphhhhhphpphh	50	0.48
R50-2	hhhhhhphpppppppphhpphhhhhhphpphhhhpppppppphhppph	50	0.52
R50-3	hhhrphrphrpppprphhhphhhhhhhhhphppprphhhphppprhpppp	50	0.54
R50-4	hhhhpprphrphrpphhpppppprphpppphhhhphhhpppprppphhh	50	0.48
R50-5	ppphpppprphrphrpphhphrphhhhhhhhhpphhpppppppppprph	50	0.46
R50-6	pphrrphrphhhpppppppprphpppppprphhhhhphrphhhhhpphhph	50	0.48
R50-7	phhpppprphrpphhpppphhhhphrphhhphrphrpphhhhphrhhhhp	50	0.56
R50-8	hpppprphrpprphrpphhhhhhpphhhhhhpppphhpprphrpppphhp	50	0.50
R50-9	pphphrphrphrpppppprphrphrphrpppppppprphhhhhhhpphh	50	0.46
R50-10	hhphrpppprphrpppppprphrpppppppphhhhhhhhhhphrph	50	0.44

Table A-10: Random sequences of length 50

ID	$E_{min}$ (2D)	PERM			ACO
		$t_1$	$t_2$	$t_{exp}$	$t_{avg}$
R50-1	-29	575.90	1.05	2.09	367.70
R50-2	-34	1.40	2.40	1.77	1 150.10
R50-3	-32	1.00	5.50	1.69	893.66
R50-4	-32	2.70	2.40	2.54	1 329.01
R50-5	-32	(-31)	5.49	-	(-31)
R50-6	-32	3.8	1.6	2.25	1 153.81
R50-7	-38	15 322.20	46.20	92.12	(-37)
R50-8	-33	1.30	0.91	1.07	837.13
R50-9	-30	9892.00	1.70	3.40	1000.49
R50-10	-27	72.80	1.80	3.51	530.84

Table A-11: Performance comparison of PERM and ACO-HPPFP-3 on random sequences of length 50 in 2D

ID	$E_{min}$ (3D)	PERM			ACO
		$t_1$	$t_2$	$t_{exp}$	$t_{avg}$
R50-1	-29	575.90	1.05	2.09	367.70
R50-2	-34	1.40	2.40	1.77	1 150.10
R50-3	-32	1.00	5.50	1.69	893.66
R50-4	-32	2.70	2.40	2.54	1 329.01
R50-5	-32	(-31)	5.49	-	(-31)
R50-6	-32	3.8	1.6	2.25	1 153.81
R50-7	-38	15 322.20	46.20	92.12	(-37)
R50-8	-33	1.30	0.91	1.07	837.13
R50-9	-30	9892.00	1.70	3.40	1000.49
R50-10	-27	72.80	1.80	3.51	530.84

Table A-12: Performance comparison of PERM and ACO-HPPFP-3 on random sequences of length 50 in 3D