

# Supplementary Information

## **A systematic model identification method for chemical transformation pathways – the case of heroin biomarkers in wastewater**

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## Supplementary Tables

**Table S1.** Stoichiometric matrix and process rates for transformation of HER, and its human metabolites, 6MAM, MORG, MOR also including COE and NCOE, in raw wastewater (suspended biomass) adopted from Ramin et al.<sup>1</sup> Different process rates are associated with different stoichiometry indicated by numbers according to transformation pathway of chemicals,  $C_{LI}$ ,  $C_{SL}$  and  $C_{SW}$  are the concentration of drug biomarkers in the liquid phase, attached to suspended solids and attached to reactor wall. Model parameters are defined in Table S2.

Processes	$C_{LI,HER}$	$C_{LI,6MAM}$	$C_{LI,MOR}$	$C_{LI,MORG}$	$C_{LI,COE}$	$C_{LI,NCOE}$	$C_{SL,HER}$	$C_{SL,6MAM}$	$C_{SL,MOR}$	$C_{SL,MORG}$	$C_{SL,COE}$	$C_{SL,NCOE}$	$C_{SW,HER}$	$C_{SW,6MAM}$	$C_{SW,MOR}$	$C_{SW,MORG}$	$C_{SW,COE}$	$C_{SW,NCOE}$	Process rates
Abiotic transformation	-1(i)	-1(ii)	-1(iii)	-1(iv)	-1(v)	-1(vi)													(i) $k_{abio,HER}C_{LI,HER}$ (ii) $k_{abio,6MAM}C_{LI,6MAM}$ (iii) $k_{abio,MOR}C_{LI,MOR}$ (iv) $(k_{abio,MORG,1} + k_{abio,MORG,2})C_{LI,MORG}$ (v) $C_{LI,COE,1}(k_{abio,COE,1} + k_{abio,COE,2})$ (vi) $k_{abio,NCOE}C_{LI,NCOE}$
Abiotic formation		1(i)	1(ii)			1(iii)													(i) $k_{abio,HER}C_{LI,HER}(M_{6MAM}/M_{HER})$ (ii) $k_{abio,6MAM}C_{LI,6MAM}(M_{MOR}/M_{6MAM})$ + $k_{abio,COE,2}C_{LI,COE}(M_{MOR}/M_{6COE})$ (iii) $k_{abio,COE,1}C_{LI,COE}(M_{NCOE}/M_{COE})$
Biotransformation	-1(i)	-1(ii)	-1(iii)	-1(iv)	-1(v)	-1(vi)													(i) $k_{bio,HER}C_{LI,HER}X_{SS}$ (ii) $k_{bio,6MAM}C_{LI,6MAM}X_{SS}$ (iii) $k_{bio,MOR}C_{LI,MOR}X_{SS}$ (iv) $(k_{bio,MORG,1} + k_{bio,MORG,2})C_{LI,MORG}X_{SS}$ (v) $C_{LI,COE,1}(k_{bio,COE,1} + k_{bio,COE,2})X_{SS}$ (vi) $k_{abio,NCOE}C_{LI,NCOE}X_{SS}$
Biotic formation		1(i)	1(ii)			1(iii)													(i) $k_{bio,HER}C_{LI,HER}(M_{6MAM}/M_{HER})X_{SS}$ (ii) $k_{bio,6MAM}C_{LI,6MAM}(M_{MOR}/M_{6MAM})X_{SS}$ + $k_{bio,COE,2}C_{LI,COE}(M_{MOR}/M_{6COE})X_{SS}$ (iii) $k_{bio,COE,1}C_{LI,COE}(M_{NCOE}/M_{COE})X_{SS}$
De-sorption from wall	1(i)	1(ii)	1(iii)	1(iv)									-1(i)	-1(ii)	-1(iii)	-1(iv)			(i) $K_{des,w,HER}C_{SW,HER}$ (ii) $K_{des,w,6MAM}C_{SW,6MAM}$ (iii) $K_{des,w,MOR}C_{SW,MOR}$ (iv) $K_{des,w,MORG}C_{SW,MORG}$ (v) $K_{des,w,COE}C_{SW,COE}$ (vi) $K_{des,w,NCOE}C_{SW,NCOE}$
Sorption to wall	-1(i)	-1(ii)	-1(iii)	-1(iv)									1(i)	1(ii)	1(iii)	1(iv)			(i) $K_{des,w,HER}K_{d,w,HER}C_{SW,HER}\alpha_{SW}$ (ii) $K_{des,w,6MAM}K_{d,w,6MAM}C_{SW,6MAM}\alpha_{SW}$ (iii) $K_{des,w,MOR}K_{d,w,MOR}C_{SW,MOR}\alpha_{SW}$ (iv) $K_{des,w,MORG}K_{d,w,MORG}C_{SW,MORG}\alpha_{SW}$ (v) $K_{des,w,COE}K_{d,w,COE}C_{SW,COE}\alpha_{SW}$ (vi) $K_{des,w,NCOE}K_{d,w,NCOE}C_{SW,NCOE}\alpha_{SW}$
De-sorption from suspended solids	1(i)	1(ii)	1(iii)	1(iv)			-1(i)	-1(ii)	-1(iii)	-1(iv)									(i) $K_{des,HER}C_{SL,HER}$ (ii) $K_{des,6MAM}C_{SL,6MAM}$ (iii) $K_{des,MOR}C_{SL,MOR}$ (iv) $K_{des,MORG}C_{SL,MORG}$ (v) $K_{des,COE}C_{SL,COE}$ (vi) $K_{des,NCOE}C_{SL,NCOE}$
Sorption to suspended solids	-1(i)	-1(ii)	-1(iii)	-1(iv)			1(i)	1(ii)	1(iii)	1(iv)									(i) $k_{des,coc}K_{d,HER}C_{LI,HER}X_{SS}$ (ii) $k_{des,6MAM}K_{d,6MAM}C_{LI,6MAM}X_{SS}$ (iii) $k_{des,MOR}K_{d,MOR}C_{LI,MOR}X_{SS}$ (iv) $k_{des,MORG}K_{d,MORG}C_{LI,MORG}X_{SS}$ (v) $k_{des,COE}K_{d,COE}C_{LI,COE}X_{SS}$ (vi) $k_{des,NCOE}K_{d,NCOE}C_{LI,NCOE}X_{SS}$

**Table S2.** Fate model parameter for HER and COE drug biomarkers

Symbol	Definition	Unit	HER	MORG	COE	NCOE	6MAM	MOR
$k_{des,w}$	Desorption rate from reactor wall	$d^{-1}$	100	100	100	100	100	100
$K_{dw}$	Reactor wall–liquid partition coefficient	$L\ dm^{-2}$	0.01	0	0	0.02	0	0.03
$k_{des}$	Desorption rate from suspended solids	$d^{-1}$	100	100	100	100	100	100
$K_d$	Solid–liquid partition coefficient	$L\ gTSS^{-1}$	0	0	0	0.01	0.31	0
$k_{abio}$	Abiotic transformation rate constant	$d^{-1}$	See Table S3					
$k_{bio}$	Biotransformation rate constant	$L\ gTSS^{-1}\ d^{-1}$	See Table S3					
$M$	Biomarker molecular weight	$g\ mol^{-1}$	369.41	461.46	299.36	285.34	327.37	285.34
$X_{SS}$	Concentration of suspended solids	$gTSS\ L^{-1}$	0.318					
$\alpha_{sw}$	wet-surface-to-volume ratio of the reactor	$dm^2\ L^{-1}$	Ramin et al. <sup>1</sup>					

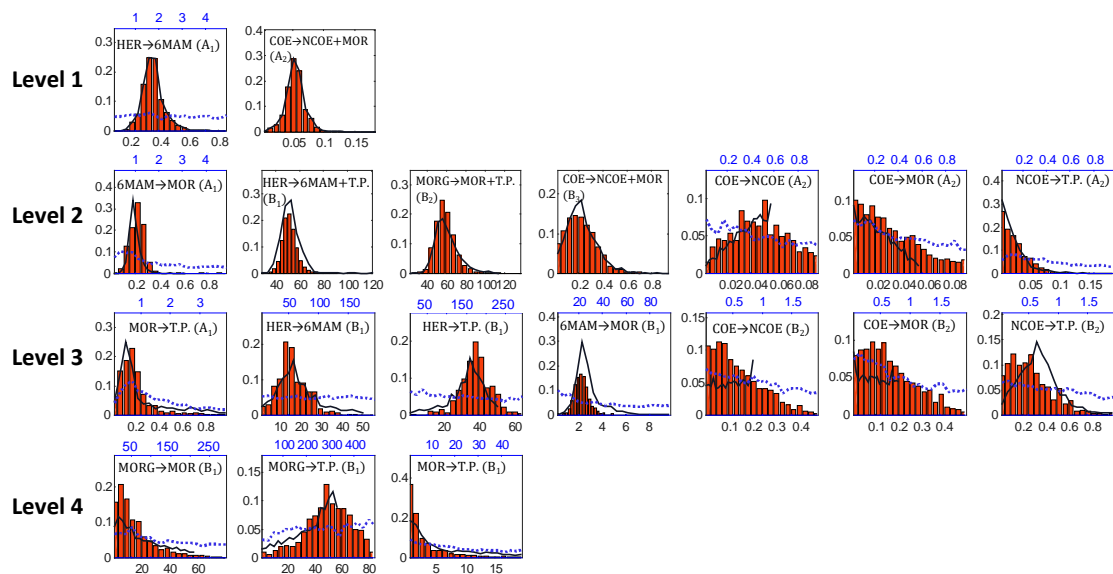
**Table S3.** Estimated parameters at each level, including, parameter type, pathway, range of parameters and type of distribution at each level for the proposed calibration *Method 1*.

	Parameter type	Model	Pathway	parameter	Min	Max	Distribution		
Level 1	Primary	abiotic (A)	HER→6MAM	$k_{abio,HER}$	0	5	uniform		
	Combinatorial	abiotic (A)	COE→COE+NCOE	$k_{abio,COE}$	0	1	uniform		
Level 2	Primary	abiotic (A)	6MAM→MOR	$k_{abio,6MAM}$	0	1	uniform		
		abiotic (A)	COE→NCOE	$k_{abio,COE,1}$	0.0014	0.0843	generalized pareto		
		abiotic (A)	COE→MOR	$k_{abio,COE,2}$	0.0064	0.0862	rician		
		abiotic (A)	NCOE→T.P.	$k_{abio,NCOE}$	0.0008	0.0843	weibull		
	Combinatorial	biotic (B)	HER→6MAM+T.P.	$k_{bio,HER}$	0	3000	uniform		
		biotic (B)	MORG→MOR+T.P.	$k_{bio,MORG}$	0	4000	uniform		
		biotic (B)	COE→COE+NCOE	$k_{bio,COE}$	0	2	uniform		
	Subsidiary	abiotic (A)	HER→6MAM	$k_{abio,HER}$	0.2261	0.5624	loglogistic		
		abiotic (A)	COE→COE+NCOE	$k_{abio,COE}$	0.0216	0.0909	tlocationsscale		
	Level 3	Primary	abiotic (A)	MOR→T.P.	$k_{abio,MOR}$	0	1	uniform	
biotic (B)			HER→6MAM	$k_{bio,HER,1}$	0	290.1458	uniform		
biotic (B)			HER→T.P.	$k_{bio,HER,2}$	0	290.1458	uniform		
biotic (B)			6MAM→MOR	$k_{bio,6MAM}$	0	5	uniform		
biotic (B)			COE→NCOE	$k_{bio,COE,1}$	0	0.2081	uniform		
biotic (B)			COE→MOR	$k_{bio,COE,2}$	0	0.2081	uniform		
biotic (B)			NCOE→T.P.	$k_{bio,NCOE}$	0	1	uniform		
Subsidiary		abiotic (A)	HER→6MAM	$k_{abio,HER}$	0.2261	0.5624	loglogistic		
		abiotic (A)	6MAM→MOR	$k_{abio,6MAM}$	0.1023	0.3474	tlocationsscale		
		abiotic (A)	COE→NCOE	$k_{abio,COE,1}$	0.0014	0.0843	generalized pareto		
		abiotic (A)	COE→MOR	$k_{abio,COE,2}$	0.0064	0.0862	rician		
		abiotic (A)	NCOE→T.P.	$k_{abio,NCOE}$	0.0008	0.0843	weibull		
		Level 4	Primary	biotic (B)	MORG→MOR	$k_{bio,MORG,1}$	0	85.4330	uniform
				biotic (B)	MORG→T.P.	$k_{bio,MORG,2}$	0	85.4330	uniform
biotic (B)	MOR→T.P.			$k_{bio,MOR}$	0	20	uniform		
Subsidiary	abiotic (A)	HER→6MAM	$k_{abio,HER}$	0.2261	0.5624	loglogistic			
	abiotic (A)	6MAM→MOR	$k_{abio,6MAM}$	0.1023	0.3474	tlocationsscale			
	abiotic (A)	MOR→T.P.	$k_{abio,MOR}$	0.0269	0.7047	generalized extreme value			
	abiotic (A)	COE→NCOE	$k_{abio,COE,1}$	0.0014	0.0843	generalized pareto			
	abiotic (A)	COE→MOR	$k_{abio,COE,2}$	0.0064	0.0862	rician			
	abiotic (A)	NCOE→T.P.	$k_{abio,NCOE}$	0.0008	0.0843	weibull			
	biotic (B)	HER→6MAM	$k_{bio,HER,1}$	2.9168	33.6060	generalized extreme value			
	biotic (B)	HER→T.P.	$k_{bio,HER,2}$	18.0626	54.8897	logistic			
	biotic (B)	6MAM→MOR	$k_{bio,6MAM}$	1.1367	3.7540	logistic			
	biotic (B)	COE→NCOE	$k_{bio,COE,1}$	0.0046	0.3925	generalized pareto			
	biotic (B)	COE→MOR	$k_{bio,COE,2}$	0.0055	0.4227	generalized pareto			
biotic (B)	NCOE→T.P.	$k_{bio,NCOE}$	0.0177	0.7069	nakagami				

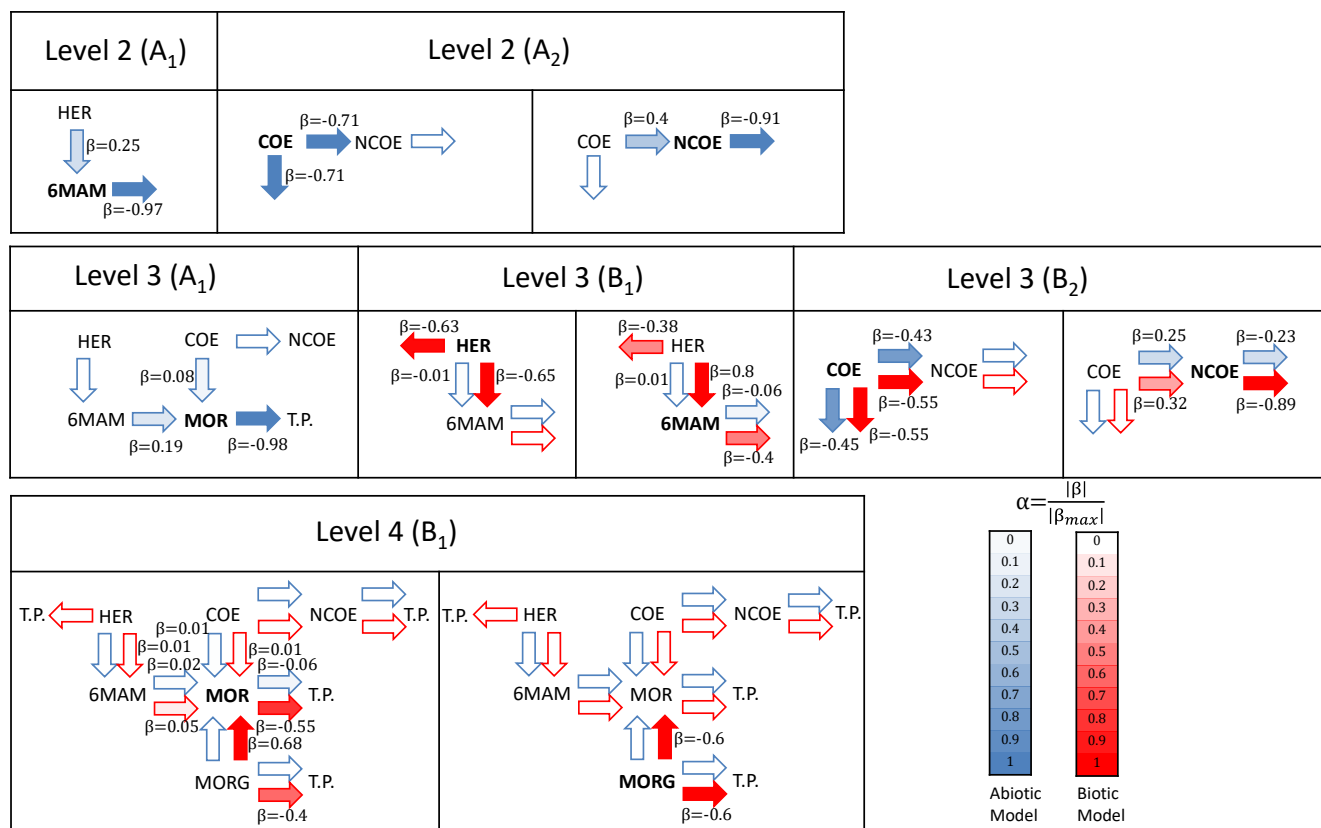
**Table S4.** Estimated parameters using 3 different calibration methods. Estimated values are reported as median with uncertainty reported as 95% credibility interval (lower bound, upper bound). Abbreviations: T.P. = transformation product(s).

	Pathway	Abiotic model parameters, $k_{abio}$ (d <sup>-1</sup> )			Biotic model parameters, $k_{bio}$ (L gTSS d <sup>-1</sup> )		
		method 1	method 2	method 3	method 1	method 2	method 3
Heroin (HER)	HER→	0.351	2.429	0.351	15.057	99.735	16.997
	6MAM	(0.226,0.562)	(0.117, 4.889)	(0.226, 0.562)	(2.917, 33.606)	(4.337, 194.178)	(2.661, 44.769)
	HER→T.P.	0	0	0	38.045 (18.063, 54.890)	135.546 (6.626, 293.389)	34.600 (6.829, 48.937)
6-monoacetylmorphine (6-MAM)	6MAM→	0.218	1.489	0.184	2.201	37.440	2.473
	MOR	(0.102, 0.347)	(0.104, 4.761)	(0.110, 0.308)	(1.137, 3.754)	(1.322, 97.069)	(1.219, 6.779)
Morphine-3-β-D-glucuronide (MORG)	MORG→	0	0	0	11.488	115.930	15.668
	MOR				(0.722, 55.372)	(4.551, 289.899)	(0.801, 53.730)
	MORG→T.P.	0	0	0	50.672 (11.328, 78.832)	273.698 (18.489, 487.744)	42.533 (4.471, 57.399)
Morphine (MOR)	MOR→T.P.	0.170 (0.027, 0.705)	1.191 (0.149, 3.750)	0.164 (0.035, 0.874)	1.458 (0.077, 14.718)	18.057 (0.729, 48.463)	3.442 (0.205, 18.486)
Codeine (COE)	COE→NCOE	0.044 (0.006, 0.086)	0.406 (0.020, 0.962)	0.036 (0.006, 0.053)	0.114 (0.005, 0.393)	0.835 (0.037, 1.935)	0.110 (0.004, 0.204)
	COE→MOR	0.026 (0.001, 0.084)	0.408 (0.019, 0.959)	0.018 (0.001, 0.048)	0.146 (0.005, 0.423)	0.726 (0.029, 1.934)	0.098 (0.004, 0.204)
Norcodeine (NCOE)	NCOE→T.P.	0.021 (0.001, 0.084)	0.365 (0.022, 0.958)	0.017 (0.001, 0.092)	0.246 (0.018, 0.707)	0.850 (0.043, 1.932)	0.332 (0.056, 0.772)

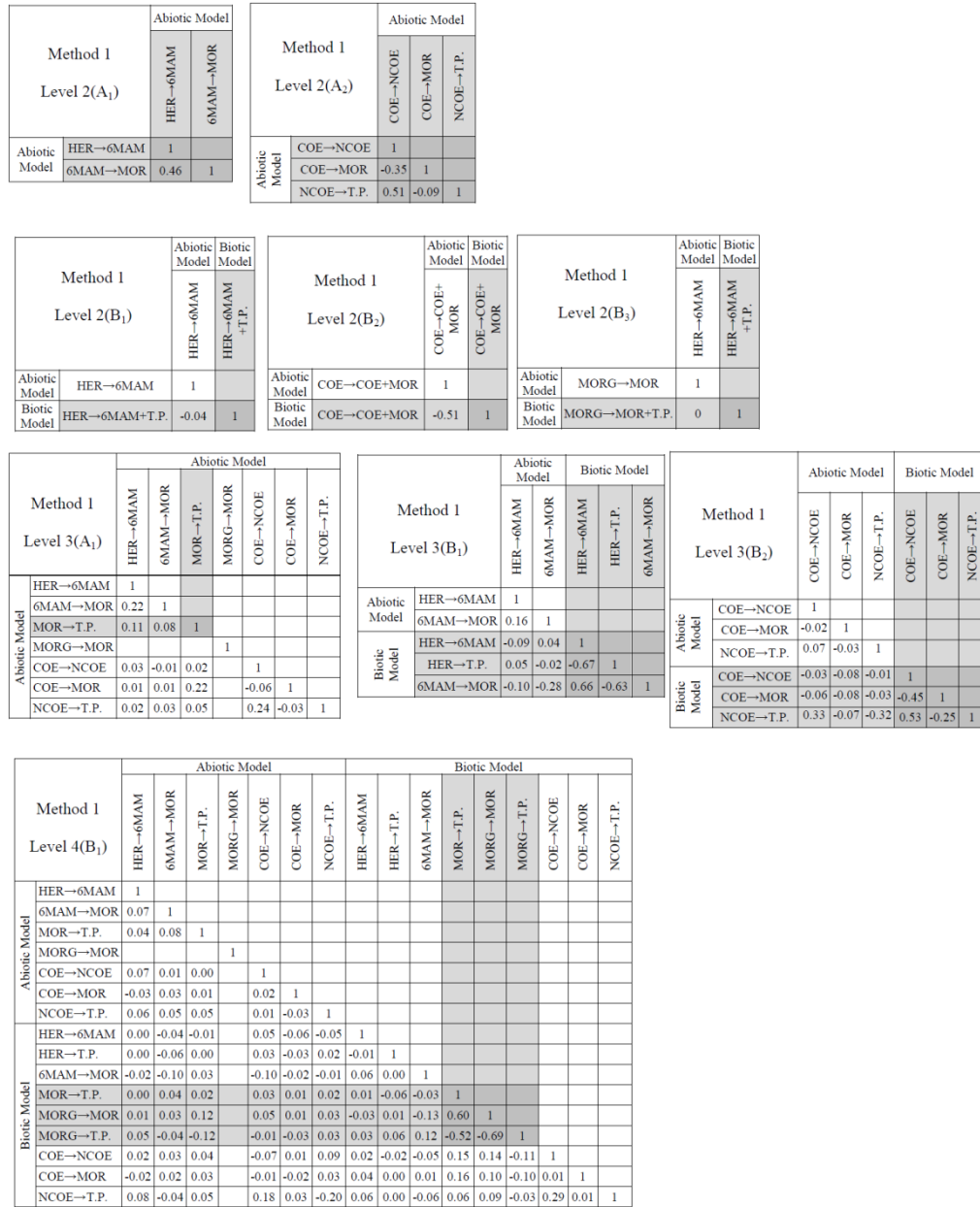
## Supplementary Figures



**Figure S1.** Posterior distribution of estimated parameters (histograms) for proposed methodology-*Method 1* (in red), *Method 2* (dotted blue line, upper X axis) and method 3 (full black line) at 4 different levels. Abbreviations: T.P. = unknown Transformation Product; A= Abiotic model, B= Biotic model.



**Figure S2.** Global sensitivity analysis using standardized regression coefficient (SRC<sup>2</sup>) to assess the importance of abiotic and biotic model parameters uncertainty propagation according to *Method 1*. Regression coefficient,  $\beta$ , is used to rank the importance of *subsidiary* parameters on estimation of *primary* parameters at each calibration level. At each level, the sensitivity is explored for one model output, i.e., concentration of a chemical shown in bold. Sensitivity of parameters was used as an indication of error propagation (i.e., higher absolute  $\beta$  value implies more influential propagation indicated using increasing color intensity in each arrow). Direction of blue (abiotic processes) and red (biotic processes) arrows follows the transformation pathways similar to Fig. 1.  $\alpha$  is the absolute ratio of  $\beta$  values to a maximum  $\beta$  value ( $\beta_{max}$ ) at each level for each chemical, representing color intensities.  $\beta$  values equal to zero are not shown.



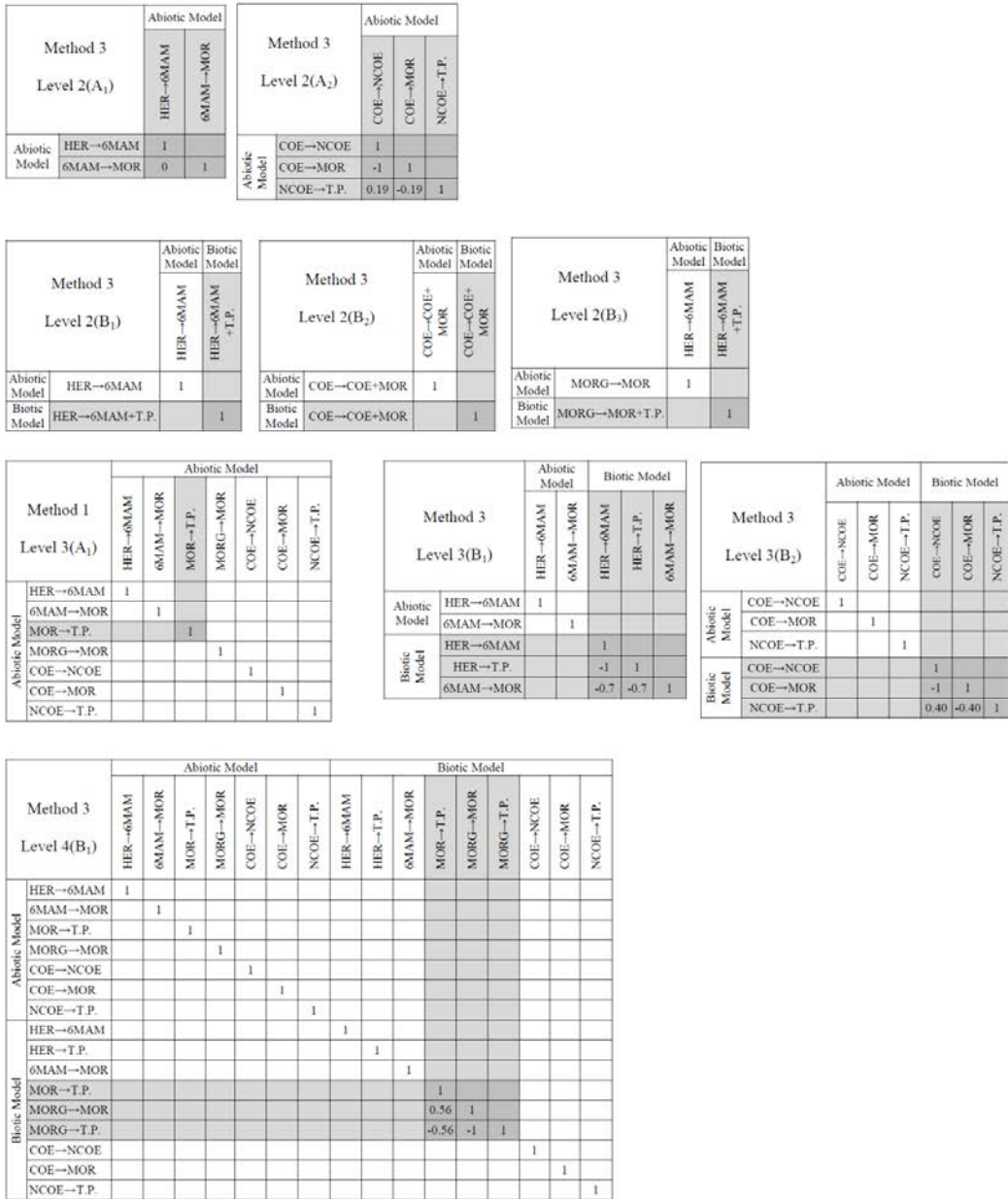
**Figure S3.** Co-linearity matrix between model parameters at each level for *Method 1*. Parameters in the shadings are the ones calibrated at each level.



Method 2 Abiotic Model		Abiotic Model						
		HER→6MAM	6MAM→MOR	MOR→T.P.	MORG→MOR	COE→NCOE	COE→MOR	NCOE→T.P.
Abiotic Model	HER→6MAM	1						
	6MAM→MOR	0.00	1					
	MOR→T.P.	0.04	0.22	1				
	MORG→MOR				1			
	COE→NCOE	0.01	0.05	0.07		1		
	COE→MOR	-0.02	0.10	0.17		0.11	1	
	NCOE→T.P.	0.01	0.12	0.15		0.25	0.04	1

Method 2 Biotic Model		Abiotic Model							Biotic Model								
		HER→6MAM	6MAM→MOR	MOR→T.P.	MORG→MOR	COE→NCOE	COE→MOR	NCOE→T.P.	HER→6MAM	HER→T.P.	6MAM→MOR	MOR→T.P.	MORG→MOR	MORG→T.P.	COE→NCOE	COE→MOR	NCOE→T.P.
Abiotic Model	HER→6MAM	1															
	6MAM→MOR	-0.02	1														
	MOR→T.P.	0.01	0.04	1													
	MORG→MOR				1												
	COE→NCOE	0.04	0.05	0.01		1											
	COE→MOR	-0.02	0.01	0.00		0.10	1										
	NCOE→T.P.	0.03	0.01	-0.03		0.22	0.03	1									
Biotic Model	HER→6MAM	0.04	-0.01	-0.01		0.00	0.01	-0.01	1								
	HER→T.P.	0.01	-0.03	-0.02		-0.01	0.05	-0.03	0.00	1							
	6MAM→MOR	-0.01	0.06	0.03		0.03	0.02	0.02	-0.03	0.00	1						
	MOR→T.P.	0.04	0.04	0.05		0.04	0.07	0.00	0.03	0.02	0.19	1					
	MORG→MOR	0.00	0.01	0.03		0.02	0.05	0.02	0.00	0.02	-0.02	0.14	1				
	MORG→T.P.	-0.04	0.01	-0.06		0.01	-0.03	0.00	-0.03	-0.04	0.03	-0.16	0.11	1			
	COE→NCOE	0.03	0.00	0.00		-0.06	0.05	0.18	-0.03	-0.01	0.08	0.10	0.04	-0.10	1		
COE→MOR	0.00	0.03	-0.01		0.07	0.04	-0.05	-0.01	0.04	0.07	0.09	0.00	-0.02	-0.01	1		
NCOE→T.P.	0.05	0.04	0.07		0.18	0.01	-0.19	0.00	0.03	0.04	0.05	0.05	-0.06	0.05	0.06	1	

**Figure S4.** Co-linearity matrix between for abiotic and biotic model parameters for *Method 2*. Parameters in the shadings are the ones calibrated at each level.



**Figure S5.** Co-linearity matrix between for abiotic and biotic model parameters for *Method*. Parameters in the shadings are the ones calibrated at each level.

# References

1. Ramin, P., Brock, A. L., Polesel, F., Causanilles, A., Emke, E., de Voogt, P. & Plósz, B. G. Transformation and sorption of illicit drug biomarkers in sewer systems: understanding the role of suspended solids in raw wastewater. *Environ. Sci. Technol.* 2016, **50** (24), 13397–13408.
2. Sin, G., Gernaey, K. V., Neumann, M. B., van Loosdrecht, M. C. M. & Gujer, W. Global sensitivity analysis in wastewater treatment plant model applications: Prioritizing sources of uncertainty. *Water Res.* **45**, 639–651 (2011).