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Bayes Forest: a data-intensive generator of morphological tree clones --Manuscript Draft--

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Full Title:	Bayes Forest: a data-intensive generator of morphological tree clones
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Abstract:	Background. Detailed and realistic tree form generators have numerous applications in ecology and forestry. For example, varying morphology of trees contribute differently to formation of landscapes, natural habitats of species, and eco-physiological characteristics of the biosphere. Additionally, virtual clones might be used in studies of real (e.g. genetic) clones. Findings. Here, we present an algorithm for generating morphological tree "clones" based on the detailed reconstruction of the laser scanning data, statistical measure of similarity, and a plant growth model with simple stochastic rules. The algorithm is designed to produce tree forms, i.e. morphological clones, similar as a whole (coarse-grain scale), but varying in minute details of organization (fine-grain scale). Although we opted for certain choices in our algorithm, individual parts may vary depending on the application, making it a general adaptable pipeline. Namely, we showed that specific multi-purpose procedural stochastic growth model can be algorithmically adjusted to produce the morphological clones replicated from the target experimentally measured tree. For this, we developed a statistical measure of similarity (structural distance) between any given pair of trees, which allows for the comprehensive comparing of the tree morphological features of a tree. Finally, we developed a programmable interface to manipulate data required by the algorithm. Conclusions. Our algorithm can be used in variety of applications for exploration of the morphological potential of the growth models (both theoretical and experimental), arising in all sectors of plant science research.
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Bayes Forest: a data-intensive generator of morphological tree clones

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Abstract.

Background. Detailed and realistic tree form generators have numerous applications in ecology and forestry. For example, varying morphology of trees contribute differently to formation of landscapes, natural habitats of species, and eco-physiological characteristics of the biosphere. Additionally, virtual clones might be used in studies of real (e.g. genetic) clones.

Findings. Here, we present an algorithm for generating morphological tree "clones" based on the 6 7 detailed reconstruction of the laser scanning data, statistical measure of similarity, and a plant growth model with simple stochastic rules. The algorithm is designed to produce tree forms, i.e. 8 morphological clones, similar as a whole (coarse-grain scale), but varying in minute details of 9 20 organization (fine-grain scale). Although we opted for certain choices in our algorithm, individual parts may vary depending on the application, making it a general adaptable pipeline. Namely, we 21 showed that specific multi-purpose procedural stochastic growth model can be algorithmically adjusted 2 to produce the morphological clones replicated from the target experimentally measured tree. For this, 23 we developed a statistical measure of similarity (structural distance) between any given pair of trees, 24 25 which allows for the comprehensive comparing of the tree morphologies in question by means of

empirical distributions describing geometrical and topological features of a tree. Finally, we developed a programmable interface to manipulate data required by the algorithm.

Conclusions. Our algorithm can be used in variety of applications for exploration of the morphological potential of the growth models (both theoretical and experimental), arising in all sectors of plant science research.

Keywords: quantitative structure tree model; morphological clone; stochastic data driven model; terrestrial laser scanning; large scale data; empirical distributions; distribution tomography

35 Findings

I. Background

Models for plant architecture attract significant attention due to their ability to assist the empirical studies in ecology, plant biology, forestry, and agronomy [1]. The modeling activity is especially useful in research since it arises as fruitful collaboration between specialists in different fields of studies: computer scientists, mathematicians, and biologists [2].

Modeling plant architecture is approached from many directions. Some progress has been achieved in synthesis of realistic plant forms in the field of computer graphics [3-5]. These models, although based on heuristic rules of growth, produce realistic shape outcomes in a fast and efficient manner, which is usually dictated by the application of this approach, that is natural sceneries in computer visualization. Heuristic growth rules of the procedural models for graphics applications are not firmly based on biological principles, but nevertheless elucidate some algorithmic properties of the growth process (for example, recursive [6] vs. self-organizing [3, 7] character of architecture development).

However, the most promising plant architectural models are so called functional-structural plant models (FSPM), also known as "virtual plants" [8-10], because this type of models allows for a balanced description between morphological and functional/physiological properties of a plant. Thus, it is capable of connecting the external abiotic factors (e.g. radiation, temperature and soil) and the 56 most vital functions of a plant organism (such as photosynthesis, respiration, and water and salts uptake) with its structural characteristics [1, 2].

Nevertheless, biologically relevant architectural plant models rely on data in a form of empirically fitted functions and parameters that correspond to a particular species and/or certain site conditions [11-14]. Thus, the change in these conditions requires re-calibration of the models, which is done in a manual fashion every time the model is simulated for the new conditions. Strong dependence on data, where each simulation would be calibrated automatically by data, is limited by both computation time and lack of the fast measurement and processing systems allowing for a detailed 3D morphological reconstruction of the real plant/tree.

The most recent advances in laser scanning techniques allow for fast and non-destructive measurement of trees with subsequent reconstruction of various characteristics depending on application (e.g. [15, 16]). Most of such studies dedicated to reconstruction of 3D point clouds obtained from laser scanning measurements deal with overall characteristics, such as height, width, and volume of stems/crowns, leaf index, biomass etc., resembling traditional destructive methods of measurement [15, 17]. However, the detailed precise geometrical and topological reconstruction with the preserved tree architecture as is, is rarely sought after.

We use a fast, precise, automatic, and comprehensive reconstruction algorithm initially presented in [18] and further developed and tested in [19]. The algorithm reliably reconstructs a quantitative structure model (QSM), which contains all geometrical and topological characteristics of the object tree. Input for the method is the 3D point cloud, sufficiently covering the tree, obtained from the terrestrial laser scanning measurements (TLS) and no additional allometric relations used for estimation of the branch proportions (as in [20, 21]) are needed. Compared to other similar techniques (e.g. [20-22]) this method requires few parameters and no user interaction and reconstructs the tree surface with subsequent cylinder (or any other geometrical primitive) approximation, which is usually consistent with theoretical plant growth models. The reconstruction algorithm has been validated in several studies with several different tree species and different scanner instruments [19, 23-26]. There are other published QSM reconstruction methods from TLS data that can produce similar quality QSMs, at least [23].

In this work, we utilize an inverse iterative procedure to optimize model's parameters as to match the (empirical) distribution of structural features of the simulated stochastic tree models (FSPM, graphical or other) to that of the tree reconstructed from the laser scanning data. Meanwhile, we formulate a measure of similarity of the tree structures grounded in tomographic analysis of the structural distributions (e.g. Radon transform) [27, 28]. Finally, the optimal parameter set produces morphological "clone" trees with similar overall structure, but varying minute details of organization.

95 Recently, we have reported a proof-of-concept study where we used reconstruction of a pine tree and 96 the corresponding FSPM (named LIGNUM [13, 29]) to demonstrate the practical feasibility of the 97 approach [30]. Here, however, we develop a unifying interface (in the form of a programmable 98 toolbox) for our procedure and use general-purpose fast procedural tree growth model from [3], since 99 such a simple procedural model is easier to adapt (it is simple, fast, and efficient) for technical

100	experimentation with the whole algorithm. Similar algorithmic pipeline was reported in [5] for
$\frac{1}{3}$ 101	procedural tree growth models in the context of graphics synthesis. However, in our approach we see
4 5102 6	the tree growth as a random process and, consequently, apply corresponding statistical methods for
8	measuring the similarity between trees. Moreover, in our algorithm the special concern is on
⁹ 104 11	biologically and physically relevant descriptions, hence, the careful choice of the reconstruction
12105 13	algorithm; possibility to use FSPM to relate physiological parameters to the morphogenetic processes
14 <mark>106</mark> 15	in trees; and no extra structures improving visual properties of trees but not supported by empirical
	observation (e.g. leaves). Finally, any other choices of parameters and feature descriptions can be used
¹⁹ 108 20 21 22109	in our approach, further facilitated with a programmable interface.
23 24110 25	II. Algorithm overview
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29112 30	Our approach is based upon five distinct parts:
³¹ 32113 33	1. Quantitative Structure Model (QSM) is a reconstruction of a tree model from 3D point clouds
34114 35	obtained from terrestrial laser scanning measurements (TLS). Here we use specific algorithm for
³⁶ 37 37 38	such reconstruction reported in [18] and [19] but others could be used as well.
39116 40	2. Stochastic Structure Model (SSM) is a tree growth model that is chosen depending on the
⁴¹ 117 42	application. There are no limitations on the class of the model, except it must produce measurable
43 44118 45	3D branching structure.
46119 47	3. Structural data set (U) is a collection of structural features (empirical distributions) to be
48 49120 50	compared between QSM and SSM. Importantly, U data sets must be determined in the same way
51 121 52	both for QSM and SSM.
53 54 55	4. Measure of structural dissimilarity, or structural distance D_S , is a measure of discrepancy between
56123 57	any two data sets in other words, $D_S(U_1, U_2)$ results in a value quantifying how much different the
58 59 60	two data sets U_1 and U_2 are.
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125 1	5. Optimization algorithm is a numerical routine capable of finding a minimum of any given function
$\frac{1}{3}$ 126	by varying its arguments. (Newton algorithm, genetic algorithm, simulated annealing etc.)
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7 ₈ 128	The connection between these components is outlined in Fig. 1 with explanation in the text below.
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12 13 130 14	Figure 1: The algorithm outline (see explanation in the text).
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	The algorithm outline (Fig. 1):
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231 34 24	Preparation stage A:
20	A1: build QSM from TLS.
29	A2: extract U_d from QSM.
³⁰ 137 ₃₁ 32	
33138 34	Main cycle B:
³⁵ 139 ₃₆	B1: simulate SSM (with fixed random generator seed for reproducibility) for the given parameters and
³⁷ 38140 39	extract U_m .
40141 41	B2 : compare U_m and U_d getting an estimation of the distance <i>D</i> between them.
⁴² ₄₃ 142 44	B3: change SSM parameters trying to decrease D, go to B1 or stop and go to B4 (changing of the
45143 46	parameters and stopping criteria depend on any particular realization of the optimization routine).
40	B4 : simulate SSM with the "best-fit" parameter values corresponding to the smallest found <i>D</i> .
49 50145 51	B5 : loose the randomness of the best-fit SSM and generate morphological clones.
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54 55147 56	At the preparation stage, the QSM is formed from the TLS point cloud (A1). The detailed description
57148 58 59	of this process is reported in [18, 19]. The resultant QSM contains all geometrical and topological
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149 features needed to form the empirical distributions U_d . The distributions can be formed for several tree ¹
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₃150 individuals if they are close by shape to ensure the sample size.

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⁷₈152 At the main cycle of the algorithm, the empirical distribution U_m is formed from the simulated SSM 9 10153 tree (B1). Next, U_m is compared against U_d using the measure of distance (B2). The optimization 11 12154 routine iteratively minimizes the distance value every time changing the parameter values of SSM 13 $^{14}_{15}$ (B3), simulating SSM, and repeating the cycle from B1. After the stopping criteria of the optimization 16 17156 routine (number of iterations, minimal allowed distance etc.) are met, the algorithm stops and produces 18 ¹⁹₂₀157 the best-fit SSM tree (B4). The best-fit SSM with different random sequences produces different 21 outcomes – morphological clones. 22158

 $^{26}_{27}$ 160 In Methods, we describe each of the main components of the algorithm in further detail.

- ³¹₃₂162 **III. Testing of the algorithm**
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³⁶₃₇164 First, we run the optimization within each of the parameter groups I - V, representing different 38 39165 processes of growth (see Methods for details), to determine the basic values of the parameters. These 40 ⁴¹/₁₆₆ basic values represent choices that generate a viable tree structure with proportions and scale 42 43 ₄₄167 approximately equal to those of the target QSM. Each optimization run takes the best parameters for 45 ⁴⁶168 the group optimized at the previous step. The target structural distributions U for these runs are 47 48 49¹⁰169 segment-related (S) features of the branches of topological order w = 0, 1, that is $S^{0,1}$ (see the details of 50 51170 the notations and description of the features in Methods). Note that this exercise serves a basic 52 ⁵³₅₄171 exploration of the model's behavior, which can be (partially) replaced, for example, by the expert 55 guesses for the parameter values or some calibration process (if the model is designed for specific 56172 57 ⁵⁸173 purposes and/or species). 59 60

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 $^{2}_{3}$ 175 Second, based on these preliminary results we determine the most influential parameters for each of 5176 the group and combine them in a single optimization set up. Several independent optimization runs ⁷177 8 were taken in order to determine the most influential parameters. For example, we found that the 10178 angular properties vary the least among these runs, whereas the apical dominance requires subtler adjustments (as can be understood from the complex structure of the target QSM). This step is required $^{14}_{15}$ 180 to reduce optimization time, and it is not needed if one possesses large computational resources. ¹⁹₂₀182 Low order topological adjustment of the shape 22183 ²⁴184 After these initial manipulations, we obtained a model with 11 parameters and good fit of the trunk (w = 0) and first order branches (Fig. 2C) with classical metrics $d_h = 0.05$, $d_g = 0.42$, $d_c = 0.57$ (see ₂₇185 ²⁹186 Methods for the definition of the classical metrics). However, the overall form of the resulting minimal ³¹₃₂187 score tree does not resemble the target QSM due to its rosette-shape (Fig. 2A, B). A closer look at the tree reveals that the higher order branches (w > 1) are mainly responsible for the formation of the ³⁶₃₇189 rosette-shape of the tree, i.e. the orders which were not subject to the optimization (Fig. 2). This 39190 example demonstrates the contribution of the higher order branches to the overall tree shape, which $^{41}_{42}191$ suggests using the scatters of these orders in further optimization steps. Moreover, the branch-related 44192 (B) features, such as the angular properties of branches of order w > 1, were not captured well (Fig. 2E), although similar order segment-related S-features show right stochastic tendencies (Fig. 2D) 49¹⁰194 generated automatically by the growth algorithm of the SSM. However, note that these features of w > 1 were not subject to optimization. This further stipulates usage of the branch-related B-scatters of ⁵³ 54<mark>196</mark> orders w > 1 (see the details of the notations and description of the features in Methods).

198 Figure 2: The rosette-shape SSM resulting from the adjustment of the low order segment-related

 $(S^{0,1})$ scatters. (A) The SSM tree; (B) the target QSM; (C) some segment related $(S^{0,1})$ scatters used in the optimization; (D) higher order (w = 2) S-scatters (not used in optimization); (E) higher order (w = 2) 2, 3) branch related B-scatters (not used in optimization). SSM/QSM scatters are shown in red/blue.

12203 Low and high order topological adjustment

The increase in number of the structural feature tables is coupled with the increase in number of 17205 ¹⁹₂₀206 distinct distance values, that is, each pair of tables (QSM vs. SSM) produces a distance score to be 21 22207 optimized. Although the optimization of the mean distance value for all tables hinders the ²⁴208 25 improvement for each table separately, the low order and high order branches need to be fitted to the 26 27209 corresponding branches of the target QSM as we have shown above (Fig. 2). To reduce the number of ²⁹210 distinct feature tables for the optimization we further utilize the merged data sets resulting in two joint ³¹₃₂211 segment- (S) and branch-related (B) tables for all topological orders (see Methods for description of the 34212 merged data sets).

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Thus, we opted for $S^{0,1}$ and $B^{2,3,4}$ merged data sets in the next run of optimization to account for the $^{41}_{42}215$ higher order branch variability (Fig. 3, $d_h = 0.08$, $d_g = 0.20$, $d_c = 0.68$). No longer we can see the $\frac{1}{44}$ rosette-shape due to the correct account of the angular properties of the higher order (w > 1) branches (Fig. 3E). The poor convergence of the branch linear dimensions (radii, lengths etc.) present in the ⁴⁸₄₉218 branch-related tables might be due to the parameter choice of the model. Namely, the small proportion 51219 of branches demonstrating right R_f values (Fig. 3E) appears to be the result of the fixed segment length we opted for as a compromise between reality and computational complexity (the QSM minimal 56221 segment length is close to zero, median is 0.06 m, whereas that of SSM is fixed to 0.2 m). Noteworthy is the similar span of the curvature data points of SSM and QSM for w = 1, 2 (Fig. 3C and D),

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although w = 2 branch curvature was not subject to the optimization. Additionally, due to the lack of the orientation landmark in the feature data sets our best-fit SSM is fitted to the target QSM with accuracy of the rotation around Z-axis (this could be adjusted, for example, by associating South direction with a coordinate axis).

Figure 3: Low and high order adjustment of the stochastic feature tables. The best-fit SSM is obtained through optimization against $S^{0,1}$ and $B^{2,3,4}$ merged feature data sets. (A) The best-fit SSM tree, (B) the target QSM tree, (C) some projection scatters from S^1 , (D) S^2 projection scatters, (E) B^2 and B^3 projection scatters.

²⁴₂₅233 **Clonal nature of the best-fit SSM**

Due to the highly discrete and stochastic nature of the tree growth, the structural distance hyperbue to the highly discrete and stochastic nature of the tree growth, the structural distance hypersurface in the space of the parameters is extremely abrupt (Fig. 4A). Hence, finding the global minima of such surface is not a trivial task (the classical smooth function optimizers are not suitable in this case, while stochastic discrete optimizers, like the genetic algorithm, seem to be more appropriate). Moreover, the hyper-surface itself is a stochastic entity changing every time the new sample of random numbers is used for a particular SSM growth realization. Therefore, any best-fit SSM is the best for a particular realization of this stochastic process: one needs to study variability of the tree shape and the chances are that other SSM growth realization can produce a lower distance value (Fig. 4B). We call these many realizations of the SSM growth *morphological tree clones*.

the distance hyper-surface projection along a dimensionless parameter λ of the SSM, controlling the apical dominance of a tree (the shown fragment of the projection with the step of 0.001 approximates

Figure 4: Stochastic structure distance profiles in the parameter space. (A) Three realizations of

30% of the allowed variability of the parameter during optimization, which was [0.35, 0.65]). (B) 248 1 ²₃249 Structural distance ($U = \{S^{0,1}, B^{2,3,4}\}$) values for 100 randomly generated SSM trees for each value of a 4 5250 discrete SSM parameter, i.e. number of growth iterations (red line connects the median points of the 6 ⁷251 8 distance distributions for each parameter value; blue line shows the same median distance profile but 9 10⁹252 for the disturbed system, see (C)). (C) Same as in (B), but $U = S^{0,1}$ (blue line is the median profile; red 11 12253 line is from (B)). The SSM is the best-fit SSM obtained in the experimentation reported in Fig. 3; the 13 $^{14}_{15}254$ black arrow indicates the parameter value of the best-fit SSM found in the experimentation.

 $^{19}_{20}256$ The structural distance profile depends not only on the parameters of the SSM, but the choice of the ²¹ 22257 structural data sets. For example, in Fig. 4B and C the median distance profile is depicted given U =23 ²⁴258 25 $\{S^{0,1}, B^{2,3,4}\}$ (red line) and $U = S^{0,1}$ (blue line). In the given parameter span the latter seems to be more 26 27**25**9 flattened and lifted compared to the former. The addition of the $B^{2,3,4}$ data set might be seen as a 28 ²⁹260 perturbation to the distance profile changing the landscape properties (like minima). In our simulations 30 ³¹₃₂261 we maintain the global parameter boundaries, which allows for the search within the full available 33 34262 space. However, we sequentially improve the model characteristics by perturbing the system, i.e. 35 ³⁶₃₇263 changing the parameters, their intervals, and the U data sets to address problematic parts of the SSM 38 39264 (like rosette-shape, Fig. 2) such that at every next optimization run the genetic algorithm is instructed 40 $^{41}_{42}265$ to search around the previous best point using the initial ranges (see Methods for details).

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46267 Given the considerations above about the nature of the structural distance hyper-surface, the further 47 $^{48}_{49}268$ study of the morphological clones is needed. Specifically, the variability and plausibility of the clonal 50 51269 shapes need to be addressed. For example, the clones must be further selected as to produce realistic 52 ⁵³₅₄270 tree shapes (especially, when the general purpose SSM is used, like in this study), however, in our 55 analysis we did not find any unrealistic tree sampled from the best-fit SSM (any specific application 56271 57 ⁵⁸272 imposes additional constraints on the parameters, which results in removal of the unrealistic shapes). 59

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Additionally, the variability of the clones can be further calibrated, for instance, by the analysis of the 273 ²₃274 natural/QSM clonal individuals.

12278 The quintessence of our work is the generation of the morphological clones. In our pipeline, this 13 $^{14}_{15}279$ occupies the last stage (see Fig. 1, B5). After the optimization is finished and the best-fit SSM is 16 found, one can further randomize the outcome of SSM by letting the random number generator 17280 18 ¹⁹₂₀281 produce different sequences every time SSM is run. As a result, the different realizations of SSM 21 22282 should constitute the morphological clone generator yielding structural copies close to QSM and to 23 ²⁴283 each other and varying in fine detail of organization of their branches. In other words, the coarse-grain 25 26 27284 structure is repeated in each clone (and possibly grasps that of the target QSM), whereas the fine-grain 28 ²⁹285 structure varies.

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34287 Figure 5: Morphological clones generated from the best-fit SSM. The best-fit SSM was found 35 ³⁶₃₇288 using the higher topological order adjustments (Fig. 3) with number of growth iterations 30 (A), 26 38 39289 (B), and 18 (C). The height, girth, crown spread, and classical metrics distributions are shown in (D) 40 ⁴¹290 for the clones in (A), (B), and (C) (the total number of generated clones for each case is n = 100, only 6 42 43 44291 are shown). The black horizontal line indicates the corresponding measure of the target QSM.

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48 49</sub>293 We demonstrate visualization of six clones for three distinct cases in Fig. 5 (clones from other best-fit 50 SSM's are provided at [31]). One can see the fine-grain variation in the structure in each panel of the 51294 52 ${}^{53}_{54}295$ figure, although the overall (coarse-grain) structure is preserved and presumably captures that of the 55 56296 (target maple QSM (Fig. 6)). The three models are: the one found during the optimization process (Fig. 57

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297 5A), the one minimizing the sample median distance profile for $D_S(U = \{S^{0,1}, B^{2,3,4}\})$ shown in Fig. 4B ¹
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⁷300 8 Out of 100 simulated clones for each case, we can see that the best-fit SSM obtained directly as the 9 10⁹301 optimization outcome (Fig. 5A) produces larger proportion of individual trees exhibiting the three 11 12302 standard allometric measures closer to those of QSM (Fig. 5D). However, we argue that such simple 13 ¹⁴₁₅303 description of a tree, as using the allometric measures, cannot be exhaustive enough to capture both the 16 overall structure and its fine details. Moreover, such static measures are absolutely useless for 17304 18 ¹⁹₂₀305 generation of morphological clones.

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The height statistics have the largest variability but by the visual inspection of the drawn clones in Fig. 5 one can see that this variability does not exert significant alterations of the Z axis span and the trees seem to have even heights. Perhaps, the way we calculate the height of a tree produces such large deviations in each particular case, which makes it a non-robust estimator (see Methods for the details of the height calculation).

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Similarly, the girth estimation, although being captured decently, produces large errors d_g , which seems to be a result of variation in its linear dimensions (Fig. 5D). The girth dimension spans a small proportion of the dimension of the whole tree: from several to tens of centimeters compared to meters of the whole tree. This makes the girth specific error look gigantic (exceeding in some cases 100%) and thus non-robust as well.

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The crown spread measure shows significant variation (Fig. 5D). We believe that this takes place due to the environment of the real tree the QSM was reconstructed from, which was not modeled appropriately in the SSM. Namely, the environmental effects (positions relative to the sun, as the tree

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grows in the Northern country, animals, winds, neighboring trees etc.) might cause systematic 322 1 ²₃323 influences exerted on the shape of the QSM tree. These influences were not accounted for in the SSM, 4 5324 which was allowed to grow in any direction, limited by the uniform light conditions, existing branches 6 ⁷325 8 of the same tree, and global boundaries of the available space. In addition to the environment 9 10³²⁶ influences, there are TLS measurement and QSM reconstruction errors, arising from the physical 11 12327 limitations of the instrumental technique and stochasticity of the QSM formation, respectively (see 13 $^{14}_{15}328$ Methods).

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 $^{19}_{20}330$ Finally, the true understanding of the variability of any measures of the morphological clones comes 21 with the measurements of the real clones. Carrying out control experiments with QSM reconstructed 22331 23 ²⁴332 from the real clonal individuals (with the application dependent definition of a clone, e.g. genetic 25 26 27<mark>333</mark> clones) can only assess the variability. These real clone controlled experiments can further identify 28 ²⁹334 whether the obtained variability is large/small for the given species/clones and lead to the adjustment 30 ³¹₃₂335 of the optimization parameters.

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³⁶₃₇337 **IV. Bayes Forest toolbox**

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We have further developed a unified interface using Matlab, facilitating exploration, drawing, data optimization, and simulation of SSM and QSM as well as study of the morphological tree clones. Our interface allows for faster and easier manipulation of the required data, models, and optimization routines from the Matlab Optimization Toolbox, using only the required elements of otherwise complex Matlab configuration for the analysis.

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The Bayes Forest toolbox is freely available at [31] (the version used in this study) and at [32] (the link 57 58 346 is preferred for contributions and contains the latest version of the package). We also encourage the

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plant and computer scientists' community to expand their efforts using the toolbox with other species 347 ²₃348 and models. Such a systematic approach can further be useful in tinkering the best options for creating 4 5349 QSM, SSM, and construction of the structural data sets.

12352 13 $^{14}_{15}353$ In this work, we described an algorithmic pipeline aimed at producing stochastic structural replicas, or 16 17354 morphological "clones", of trees from a QSM tree (data from TLS reconstruction) and a 18 $^{19}_{20}355$ complimentary SSM tree (analytical/procedural growth model). The pipeline is based on an iterative 21 22356 minimization of a distance between morphological structures. The distance is based on construction of 23 ²⁴357 the structural data sets of the tree morphologies and subsequent measure of their discrepancy using the 25 26 27**35**8 ideas of distribution tomography analysis. The resulting best-fit morphological clones are statistically 28 29359 similar which is expressed in overall similarity of their form (coarse-grain), but, nevertheless, 30 ³¹₃₂360 difference in fine details of structural organization (fine-grain).

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V. Discussion

 $^{36}_{37}362$ Here, we have shown the general logic behind the pipeline and principle possibility for generation of 38 39363 the morphological clones as defined above. For this purpose we used a highly variable procedural tree 40 ⁴¹364 model [3], which is more difficult to optimize. As the pipeline consists of several elementary steps, 42 43 44365 each of which can be changed according to the application and target analysis, we have proposed an 45 46366 initial set-up and basic configuration that are capable of the task we have set. We assume larger 47 48 ^{±°}49367 possibilities of exploration of the proposed configuration, let alone changing the steps and individual 50 51368 algorithms within the pipeline, which could be fulfilled by the community of plant science researchers 52 ⁵³₅₄369 (for this reason, we also created a little toolbox in Matlab for easier representation and simulation of 55 56<mark>370</mark> the algorithm). 57 ⁵⁸371 59 60 61

372 Developing the principles of the pipeline, we were interested in biological plausibility of the results $^{1}_{3}$ 373 rather than visualization purposes. Thus, for example, we use real TLS measurements and general- $^{4}_{5}$ 374 purpose measure of the distance, while omitting visual effects (e.g. shades, leaves etc.). We believe $^{6}_{8}$ 7375 this pipeline can be useful in the rigorous analysis of the plant morphogenesis and corresponding $^{9}_{10}$ 376 applications (in contrast to some similar studies done in computer graphics field, e.g. [5]).

 $^{14}_{15}378$ Moreover, in our algorithm we employ the distance measure taking into account significant portion of 16 the data (in fact, all data points of a given topological order(s)), not merely scalar overall entities 17379 18 19 20**380** proposed by other authors (e.g. [5, 33]). This allows for a more comprehensive analysis of forms and 21 22381 their description, stemming from the statistical inference theory and in the spirit of Systems Biology 23 ²⁴382 studies. Due to this reason, we do not rely on the traditional metrics comparison in this work as we 25 26 27**38**3 found that similar values for the height, girth, and crown distances may correspond to different tree 28 ²⁹384 forms and, thus, be non-robust. 30

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34386 Use of several QSM trees can enhance the robustness of the statistical analysis presented here. In this 35 ³⁶₃₇387 case, similarly looking trees should be used and the degree of similarity might be established using our 38 39388 definition of the structural distance. For example, the trunk features are more reliably reproduced in 40 $^{41}_{42}389$ statistical sense, when several QSM's are used. In these lines, it might be stressed that other notions of 43 44390 "clone" can be used to establish relationship with morphology. Thus, the genetic clones might be 45 46391 utilized to establish to what degree the morphology of a tree is encoded into genes (nature vs. nurture 47 ⁴⁸₄₉392 problem). 50 51393 52 53 54394 Methods 55 56 57**395** 58

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⁵⁹396 **I. Quantitative Structure Model (QSM)**

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1 ²398 QSM is derived from the point cloud obtained by TLS. Essentially, QSM is a surface reconstruction of 3 4 5399 the branches of the real tree measured by TLS. The reconstruction itself is a stochastic process, giving б ⁷400 8 different architecture results for different runs. Therefore, the reconstruction introduces internal errors 9 10⁹401 in addition to the TLS measurement errors. Besides giving spatial locations of parts of the tree, QSM 11 12402 also reconstructs topological relations between the tree branches. The branches of QSM consist of 13 ¹⁴₁₅403 elementary units, i.e. circular cylinders, but other geometrical primitives can also be applicable [34]. 16 Thus, any potential structural information about the original tree can be approximated with high 17404 18 ¹⁹₂₀405 accuracy with QSM (details of the reconstruction algorithm are presented in [18, 19], for the validation 21 of the algorithm see [19, 23-25]). 22406 23 24407 25 $^{26}_{27}408$ In this work, we use the reconstructed QSM of a maple tree (Fig. 6). The tree was measured in leaf-off 28 ²⁹409 conditions and our system consisted of a phase-based terrestrial laser scanner, (Leica HDS6100 with a 30 ³¹₃₂410 650-690 nm wavelength). The distance measurement accuracy and the point separation angle of the 33 34411 scanner were about 2-3 mm and 0.036 degrees, respectively. The horizontal distance of the scanner to 35 ³⁶₃₇412 the trunk was about 7–12 m, thus the average point density on the surface of the trunk (at the level of 38 39413 the scanner) for a single scan is about 2–5 points per square centimeter. The QSM of the subject maple 40 ⁴¹₄₂414 tree consists of 19,000 cylinders approximating 3,078 branches. 43 44415 45 ⁴⁶416 Figure 6: The target QSM structure in three main 2D projections. 47 48 ⁴⁹417 50 51 52418 The subject QSM was chosen due to its non-trivial form and obvious irregularities in the tree growth. 53 54419 This is needed to determine whether the stochastic rules of SSM growth can account for this variability 55 ⁵⁶₅₇420 (which, in fact, might come from some deterministic sources, like constant wind, shading from the 58 59421 neighbors, animal influences etc., and which we do not know as we do not know the history of 60 61 62 63 17 64

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growth). Thus, our algorithm tries to compensate the unknowns of the growth with simple stochastic ²₃423 rules of SSM and optimization of the stochastic distance function. ⁷425 8 II. Stochastic Structure Model (SSM) 10⁹426 SSM is a simulated model, preferably based on analytical and/or heuristic rules for the tree growth; $^{14}_{15}428$ however, any viable algorithm for generating tree forms may be used. Importantly, the ultimate output of the SSM simulation is a table containing data sets U (see IV.3 Structural data sets), describing the $^{19}_{20}430$ tree structure. ²⁴432 Additionally, SSM may be supplied with stochastic variability in its parameter values. Through our studies we implement simple stochastic variations (in the form of normal and uniform distributions) ²⁹434 added to the parameter values of SSM. ³¹ 32</sub>435 34436 Finally, the elementary units forming the SSM branches should be similar to that of QSM for the ³⁶₃₇437 appropriate comparison or, otherwise, any differences in the form primitives must be taken into 39438 account. Usually cylinders are used in SSM studies and they were also shown, when used in QSM, to ⁴¹439 produce most reliable estimation of the real tree characteristics [34]. Examples of SSM are: LIGNUM [13] - a functional-structural plant model based on the physiological principles of growth of pine trees, but also applicable to other tree forms [35]; self-organizing tree 51443 model [3] is based on the heuristic principles of growth, the algorithm is capable of producing various ⁵³ 54</sub>444 tree shapes and is-used in computer graphics; *plastic trees* [4] are procedural growth models used in computer graphics; AMAP/GreenLab (see e.g. [36, 37]) is a modeling approach to generate FSPM ⁵⁸446 based upon empirical rules of growth with some physiological processes taken into account.

1 $^{2}_{2}$ 448 In this work, we use self-organizing tree model (SOT) with shadow propagation algorithm [3] as SSM 3 4 5449 with the minimal changes as to calculate the morphological features and produce the resulting data sets, б ⁷450 8 for comparison with QSM (in this work we used SOT implemented in the LPFG simulator, part of the 9 10⁹451 Virtual Laboratory software suite [38], version 4.4.0-2424 for 64-bit Mac OS, see [39]). This 11 12452 procedural tree model is fast and able to generate variety of forms, hence we can use it effectively to 13 ¹⁴₁₅453 optimize the whole algorithm in respect to technical details as well as to cover various tree shapes. 16 Note that more specialized tree growth models designed for the species in question would be easier 17454 18 ¹⁹₂₀455 subjects for the morphology optimization, but, nevertheless, can be more valuable in biologically 21 motivated studies (the usual choice is FSPM's, e.g. [30]). 22**456** 23 ²⁴457 25 26 $\frac{1}{27}$ The total number of growth parameters of the model is 27: 23 are grouped, 4 are fixed for all times. 28 ²⁹459 The values of the latter are dictated both by suggestions of the authors in [3] and the compromise 30 ³¹₃₂460 between computation time and details of the morphological description. For example, the segment 33 length is 0.2 m (we found this optimal to grow a full size tree within a reasonable span of time, 34461 35 ³⁶₃₇462 although this is not the minimum length of the target QSM segments), the voxel size is 0.2 m, and the 38 39463 model tree grows within 12x12x12 m cube from the center of XY plane of the cube (Z-axis is oriented 40 ⁴¹₄₂464 upwards). 43 44465 45 46466 The grouped parameters are divided between 5 distinct groups corresponding to different related 47 48 49⁴⁶⁷ processes: 50 51468 *Group I*: the initial growth parameters, including limiting values, and pipe model related parameters. 52 ⁵³₅₄469 Group II: environmental effects such as sensing of the neighborhood shading, vertical gradient of the 55 light, tropism etc. 56470 57 ⁵⁸471 Group III: apical dominance parameters. 59 60 61 62 63 19 64 65

Group IV: shadow propagation related constants (see [3]). 472 1 ²₃473 Group V: angular/branching properties. 4 5474 б ⁷475 8 III. Structural data sets (U) 9 10⁹476 11 12477 Structural data sets for any given tree structure are empirical collections of the physical dimensions 13 $^{14}_{15}478$ and spatial orientation measures of segments and branches that are composed of segments. These data 16 sets must be similarly obtained for any pair of $\{U_m, U_d\}$ that is to be compared by means of the distance 17479 18 $^{19}_{20}480$ algorithm. 21 22481 23 ²⁴482 Quantities in the data sets may represent scalar characteristics and/or relations between several 25 26 27483 covariates (e.g. radii, lengths, angles, tapering function of a branch etc.). On the one hand, one needs to 28 29484 exhaustively describe morphology of the tree using various geometrical and topological features. On 30 ³¹₃₂485 the other hand, as the number of compared data sets $\{U_m, U_d\}$ grows the efficiency of the optimization 33 34486 routine decreases, since the number of distance measures to be minimized grows correspondingly (one 35 ³⁶₃₇487 distance value for each pair $\{U_m, U_d\}$). Thus, one needs more compact representation of the data. One 38 39488 solution is to use larger data sets with all possibly needed (for a given application) features. (Another 40 ⁴¹489 solution is to use multi-objective optimization routines finding, e.g. Pareto front, though we do not 42 43 44490 employ such an approach in this work.) Therefore, we use larger tables of all measured features; hence, 45 46<u>491</u> one table represents a data set. However, we are unable to merge segment- and branch-related features 47 48 $\frac{1}{49}$ 492 into a single table as these differ in dimension (Table 1). Thus, we usually compare the array of pairs 50 51493 $\{U_m, U_d\}$, having as a result the array of distance values, but with such larger table representation we 52 $^{53}_{\sim}$,494 have smaller size of these arrays. 55 56495 57 58 59 60 61 62 63 20 64 65

496 Branch- and segment-related data are described in Table 1 and Fig. 7. Throughout the manuscript we ²₃497 maintain the notations B^w and S^w for the branch and segment-related data sets of the (Gravelius) order 5498 w, respectively. The zero order w is assigned to the trunk (a branch connecting the tree with the 7499 8 ground). At the branching points, the lateral buds give rise to branches with order w+1, where w is the 10⁹500 order of the parent branch, while the apical buds continue the branch of the same order.

¹⁴₁₅502 **Table 1: Branch and segment features.**

Branch features, units	Description
β, degree	Inclination angle of the branch, i.e. angle with its parent branch.
α, degree	Azimuthal angle of the branch, i.e. angle around its parent branch (calculated from the fixed direction).
L _t , m	Total length of the branch (calculated as the sum of the segment length)
	constituting the branch).
R _f , m	Initial radius of the branch, i.e. radius of its first segment.
L _a , m	Length of over the parent branch from its beginning segment to the poir
	where the current (child) branch emanates.
Segment features, units	Description
R, m	Radius of the segment.
L, m	Distance from the beginning of the branch to the segment.
γ, degree	Angle between horizontal projections of the segment and its parent.
	Angle between vertical projections of the segment and its parent.

Figure 7: Visual structure of a tree and its representation using the structural data sets U. (A) A 504 ²₃505 sample tree; (B) geometrical features of the branch- (B) and segment-related (S) data sets; and (C) 4 5506 various projections of the U data sets.

7 8507 These features are not exhaustive and can be augmented at will, but we found this set sufficient for 9 10508 obtaining realistic tree shape outcomes. Representation of the data sets in the form of large branch and 11 12 segment related tables reduces the complexity of optimization process by reducing the number of 13<mark>509</mark> 14 ¹⁵510 distance values to minimize. Additionally, such representation of the data allows for the fast extraction 16 17 18</sub>511 of all required relations between covariates or scalar entities without having them as separate data sets. 19 20512

 $^{22}_{23}$ 513 In a simulated SSM structure the extraction of topological relations between branches is 24 straightforward as the user observes the whole process of growth: the lateral buds start the next order 25514 26 $^{27}_{28}515$ and apical buds continue the current order. However, this is not the case with QSM since it is a time 29 30516 snapshot of a tree form that does not retain the history of the tree growth. Thus, the reconstruction 31 32517 algorithm requires other principles for extraction of topology. Although the reconstruction algorithm 33 ³⁴₃₅518 defines a complicated procedure that outlines the topology of a tree, it could be roughly approximated 36 37519 by the following rule: at branching points the thickest branch is the continuation of the same order w, 38 ³⁹₄₀520 while thinner branches are lateral expansions of the order w + 1 [18]. For the species with weak apical 41 42521 dominance (shrubby trees) we maintain similar procedure when simulating corresponding SSM (for 43 ⁴⁴₄₅522 the species with strong apical dominance, both techniques should converge to the same result).

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⁴⁹524 Finally, it is possible to merge the corresponding data sets, which results at maximum in two large data 50 ⁵¹ 52⁵²⁵ sets of branch- and segment-related features, respectively. While this simplifies the search of the 53 54526 distance minimum (max two values to minimize), this technique must be used with care as in this case 55 ⁵⁶₅₇527 one heavily relies upon the growth rules of SSM. If these rules are not based on biologically motivated 58 rules, SSM can produce highly unrealistic tree forms as the "best-fit", since there is a possibility to mix 59528 60

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the features of different topological orders. For example, the branches of higher order could be much 529 1 ²₃530 thicker than those of the lower order, which is unrealistic and naturally is taken care of in the 4 5531 biologically based growth algorithms (e.g. pipe model). 6 ⁷532 8 $^{9}_{10}533$ IV. Measure of structural distance (D_{S}) 11 12534 13 $^{14}_{15}535$ The distance D_S between any two data sets, or empirical distributions (dimension or number of 16 17536 variables of which is not limited), measures the difference between the local densities of the points in 18 ¹⁹₂₀537 U-space for these data sets (i.e. large segment- (S) or branch-related (B) tables of morphological 21 features). Here, it is constructed by measuring SSM vs. QSM difference of the normalized cumulative 22538 23 $^{24}_{25}$ distributions of the point densities projected onto a number of line directions in the coordinate space of the variables in U. The directions of lines are generated with quasi-Monte Carlo method using low-28 ²⁹541 discrepancy (quasi-/sub-random) sequences, which cover the given space more evenly than uniformly 30 ³¹ 32<mark>542</mark> generated sequences. The difference between the projected cumulative distributions is further 33 34543 measured by the Kolmogorov-Smirnov statistic (any other can be used) and the resulting distance 35 ³⁶₃₇544 between the two data sets U is an average of all statistics calculated from each of the lines (see 38 39545 Fig. 8A). 40 $^{41}_{42}546$ 43 44547 In general, $U \in \mathbb{R}^N$, in our case N = 4 (segment) or N = 5 (branch) as can be seen from Table 1. The 45 ⁴⁶548 empirical probability density function p(U) can be approximated by the series of 1D density functions 47 48 ₄₉549 $p_{1D}(U,L)$, where L is a line in \mathbb{R}^N , each of these 1D functions is constructed by projecting all the data 50 51550 points of U (thus, it is not a marginal distribution) onto a line L (in total we use 1000 such line 52 ⁵³ 54<mark>551</mark> directions formed quasi-randomly). Cumulative distributions $P_{1D}(U_m, L_i)$ and $P_{1D}(U_d, L_i)$ for each line 55 direction L_i are compared, thus, for any given data set pair $\{U_m, U_d\}$ the resultant distance value is: 56552 57 58 59 60 61 62 63 23 64 65

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$$D_{S}(U_{m}, U_{d}) = \frac{1}{n} \sum_{i=1}^{n} K[P_{1D}(U_{m}, L_{i}), P_{1D}(U_{d}, L_{i})],$$

where *n* is the number of lines and operator $K[\cdot,\cdot]$ returns the Kolmogorov-Smirnov statistic for the given pair of 1D empirical cumulative distributions.

11 Figure 8: Distribution tomography of the structural data sets (A) and classical metric for the 12557 13 $^{14}_{15}558$ **crown spread (B).** (A) Data points in U (projected here for simplicity onto (u_i, u_j) plane, i.e. in 2D) are 16 used to construct the projection onto a line L. Cumulative empirical distribution is calculated along L 17559 18 $^{19}_{20}560$ (red). Only one line is shown, although typically one should use sufficiently enough number of lines ²¹ 22⁵⁶¹ (uniformly distributed over all directions) to describe the form of the distribution. (B) Top view of a 23 ²⁴562 tree: spokes (red) emanate from the ground segment (green) extending up to the most distant points 25 $^{26}_{27}563$ (blue).

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32565 **Traditional metrics** (d_x) . In order to provide a reference to traditional tree measurement systems, we 33 ³⁴₃₅566 also calculate three main tree characteristics that are used for describing a tree shape (Frank, 2010). 36 37567 Height is calculated as the highest point of a tree. Girth is calculated as the diameter of the ground 38 ³⁹₄₀568 segment (the breast-height diameter is not appropriate for the shrubby trees). Crown spread is 41 calculated as follows. First, on XY-plane (top view, Fig. 8B) the set of spokes (red lines in Fig. 8B) 42569 43 44570 emanating from the center of a tree (the ground segment, green circle) is formed (here, we opted for 45 46 47<mark>571</mark> the spokes with azimuthal separation of 10 degrees). Then the length of each spoke is calculated as a 48 49572 distance from the tree center to the most distant point of the crown in the direction of the spoke (blue 50 ⁵¹₅₂573 circles). The crown spread is twice an average of all spokes of a tree.

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 $_{57}^{56}$ 575 Finally, when comparing two tree shapes we calculate the distances as follows:

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$$d_{h} = \frac{|h_{d} - h_{m}|}{h_{d}}; d_{g} = \frac{|g_{d} - g_{m}|}{g_{d}}; d_{c} = \frac{|c_{d} - c_{m}|}{c_{d}}.$$

4577 In this, h_d , g_d , and c_d are the height, girth, and crown spread of the QSM tree, respectively, whereas h_m , ⁶578 g_m , and c_m are the corresponding entities of the best-fit SSM tree. Thus, the classical distance d_x shows 8₉579 how large is the difference between entities x in proportion of the corresponding reference/QSM tree ¹¹580 value.

16582 V. Optimization routine

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20 The measure of structural distance $D_{S}(U_{m}, U_{d})$ is minimized by adjusting the parameters v of SSM. 21584

²³₂₄585 In principle (with infinite sampling), $D_S = 0$ for two trees (or, more precisely, infinitely large groups of 24 25 $\frac{26}{26}$ 586 stochastically varying trees) that have exactly the same parameters v. These trees are not copies of each 27 ²⁸587 other, but they are structurally (statistically) similar. The choice of the U defining D_S is not unique, but 29 ³⁰₃₁588 ideally well-chosen U should satisfy the following uniqueness condition for D_S to yield an acceptable 32 ³³⁵⁸⁹ measure of distance. Let three trees be given by v_A , v_B , and v_C . Then, if $D_s(U_A, U_B) < D_s(U_A, U_C)$, one 34 ³⁵₃₆590 can update $C \leftarrow B$, find any new v_B for which the inequality holds, and repeat until $D_S(U_A, U_B) \rightarrow 0$ and 37 ³⁸591 $v_B \rightarrow v_A$. In practice, this should be true in a large enough neighborhood of v_A (any steps down the right 39 40 valley lead to its bottom); however, $D_S > 0$ due to the finite sampling and insufficient model. 42

⁴⁵₄₆594 Any algorithm from a standard optimization library (e.g. Matlab Optimization Toolbox) that finds a 47 minimum of an objective function $(D_S = F(v))$ can be used. However, to facilitate global minimum 48595 49 ⁵⁰596 search and given the nature of the problem we use the genetic algorithm (implemented in Matlab, 52 53597 version R2015b). Additionally, some parameters of SSM may take only integer values, so the genetic 54 ⁵⁵598 algorithm handles the integer parameters correctly unlike, for example, the classical steepest decent 56 57 ₅₈599 algorithm. The genetic algorithm iteratively finds a minimum of D_{s} , each iteration being called 59 60600 generation. Each generation is characterized with a number of individuals, i.e. population; one 61 62

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individual is equivalent to one set of the parameter values. The variation is controlled by the *crossover* 601 1 ²₃602 rate (rate of recombination of the population parameters) and mutation rate (rate of introduction of the 4 5603 new variability into the population). The former is fixed to 80% in the Matlab Optimization Toolbox, б ⁷604 8 whereas the latter is controlled by our configuration. The user controls ranges of the parameters. There 9 10⁶⁰⁵ are two types of ranges: global lower and upper boundaries for each of the parameter values and initial 11 12606 range, from which the algorithm tries to construct the initial population (and, perhaps, where the best 13 $^{14}_{15}607$ solution lies). The latter controls the convergence rate: if it is too broad poor convergence is attained. 16 17608 Finally, algorithm stops when there have passed a fixed number of generations without improving the 18 ¹⁹₂₀609 distance.

²⁴611 Thus, the objective function takes the input parameters v, simulates SSM with v, calculates and returns 25 26 $_{27}612$ structural data sets U_m . Subsequently, the objective function calculates $D_S(U_m, U_d)$ and returns it to the 28 ²⁹613 optimization routing. The SSM, being a stochastic model, *must* have a fixed random generator seed 30 ³¹ 32⁶¹⁴ during optimization, i.e. the same input parameter set must produce the same structural output. This is 33 34615 needed for convergence of the optimization. After obtaining the final best-fit form of SSM, one can 35 ³⁶₃₇616 further explore the variability coming from different random number sequences used in the SSM 38 39617 simulations (in addition to Matlab, we used GNU Octave version 4.2.0 for clone generation, see [40]). 40 $^{41}_{42}618$ Thus, such random best-fit SSM is capable of producing the clonal morphologies (the same overall 43 44<mark>619</mark> structure with varying details of organization), which is the main goal of our algorithm. 45 46620 47 48

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Availability of supporting source code and requirements

51 52622 Project name: Bayes Forest

⁵⁴₅₅ Project home page: http://math.tut.fi/inversegroup/app/bayesforest/v1/

⁵⁶ 57624 Operating system: Platform independent

⁵⁹625 Programming language: Matlab

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Other requirements: VLAB software suite, version >= 4.4.0-2424
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 <sup>2</sup><sub>3</sub>627 License: MIT
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        Data availability
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         All data needed to reproduce the results of this study, some additional materials, and Bayes Forest
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         Toolbox are available at [31]. The most recent version of the Toolbox is also available at [32] (this
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<sup>15</sup><sub>16</sub>632
        interface is preferred for the contributors and also contains the most recent version of the software).
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<sup>20</sup>634 List of Abbreviations
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        FSPM – functional-structural plant model.
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<sup>25</sup>636 QSM – quantitative structure model.
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<sup>27</sup><sub>28</sub>637
         SSM – stochastic structure model.
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30638 SOT – self-organizing tree model.
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^{32}_{33}639 TLS – terrestrial laser scanning.
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<sup>37</sup>641
         Ethics approval and consent to participate
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40^{\circ}642 Not applicable
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<sup>44</sup><sub>45</sub>644 Consent for publication
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52647 Competing interests
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         The authors declare that they have no competing interests
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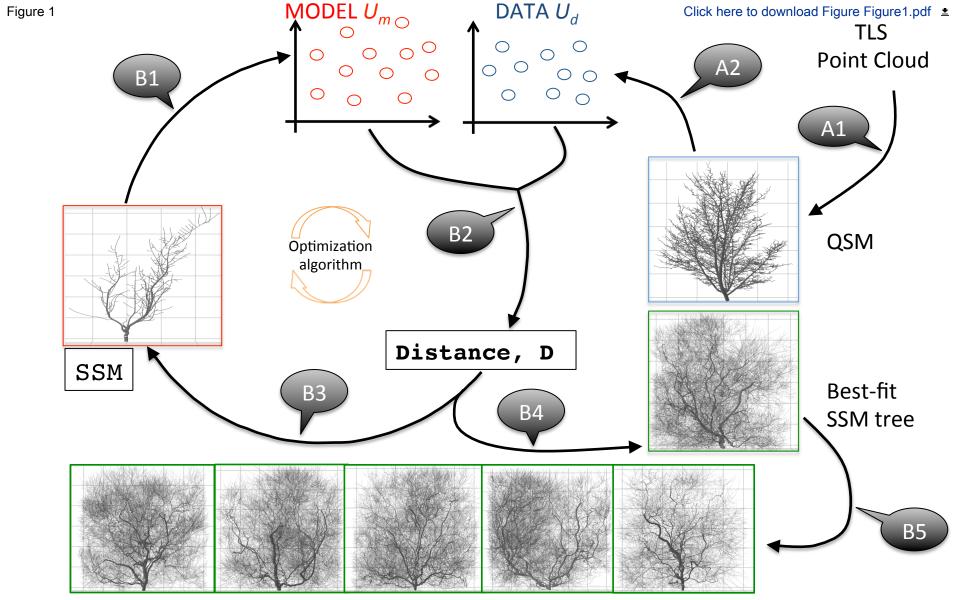
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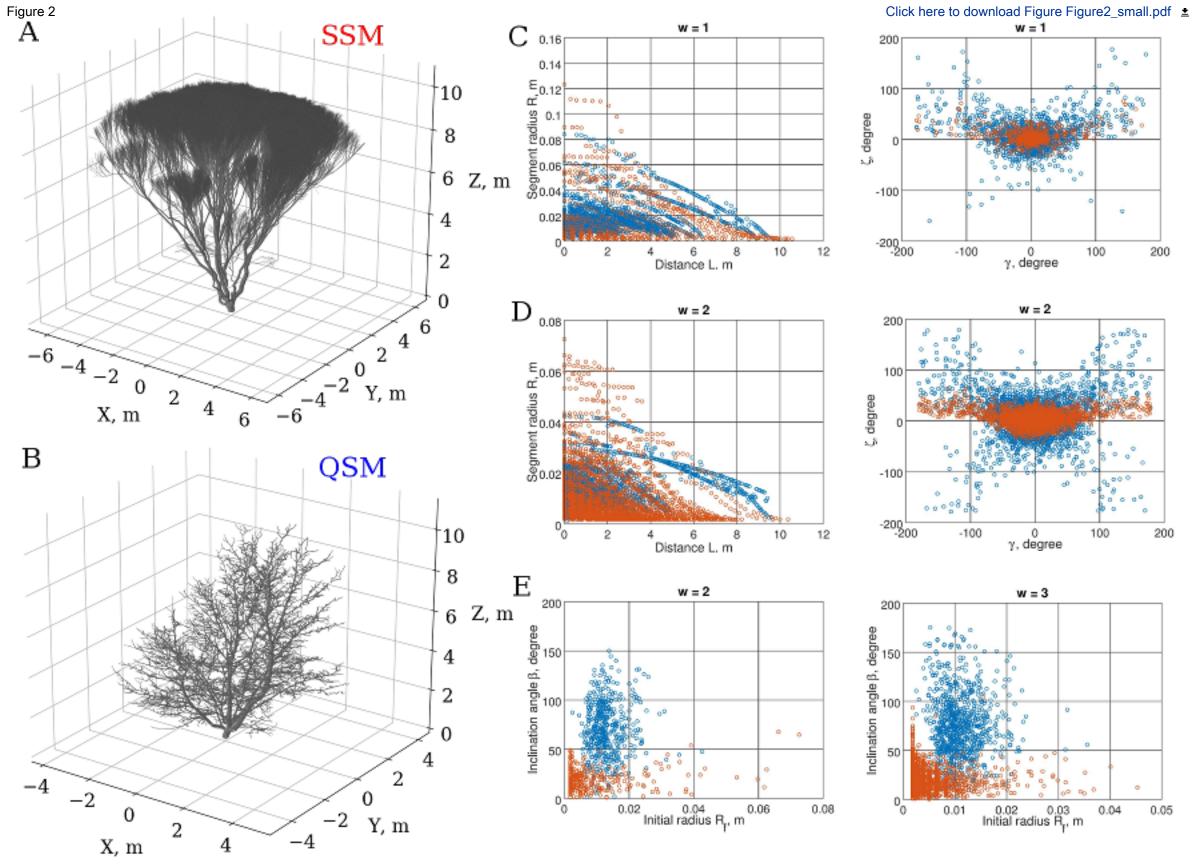
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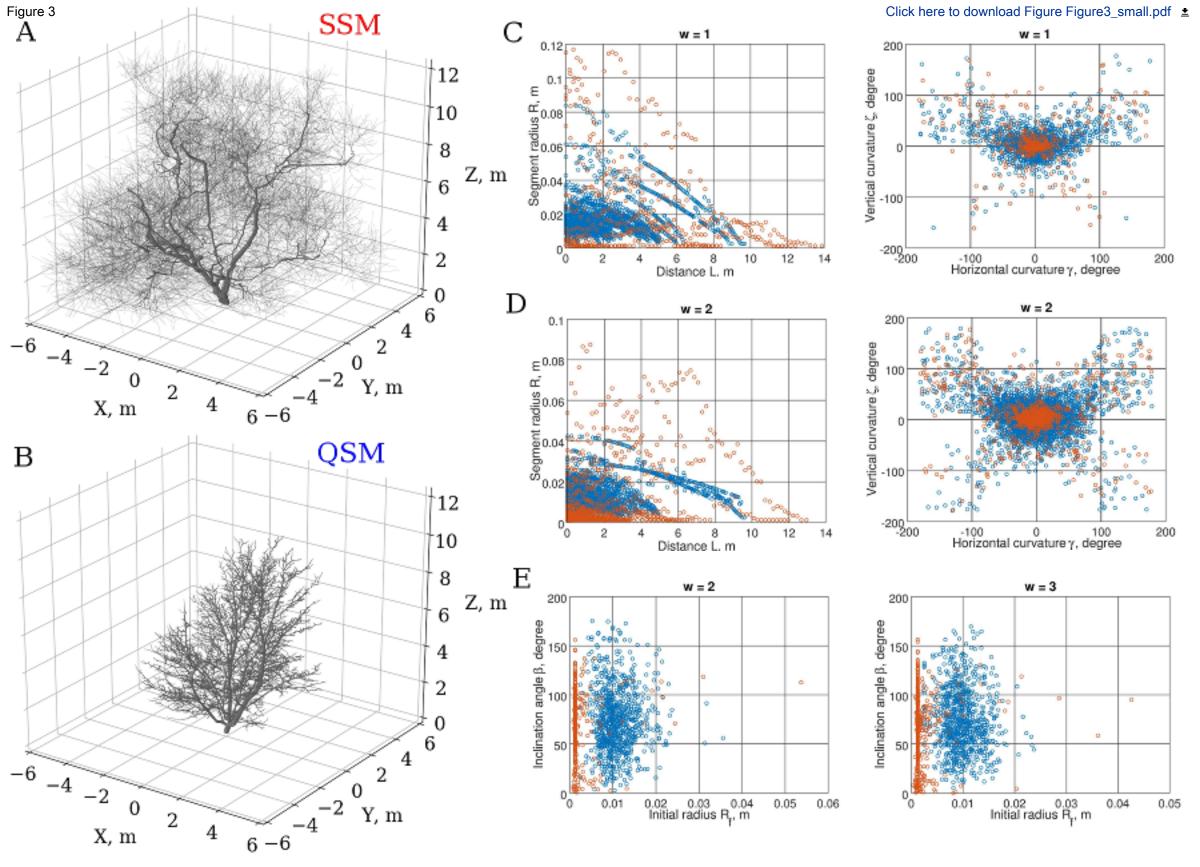
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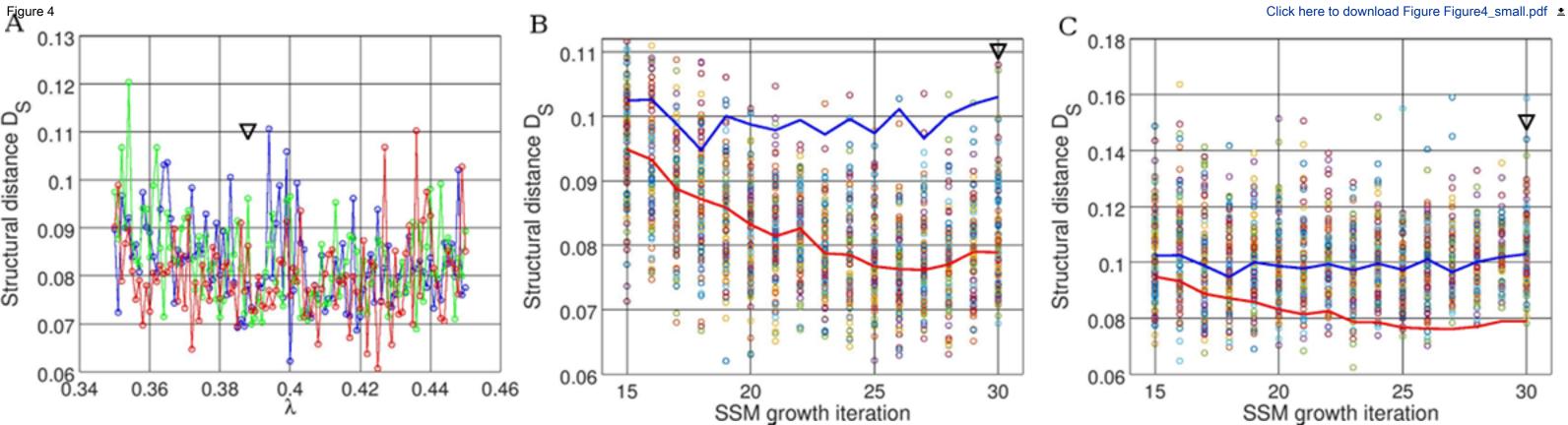
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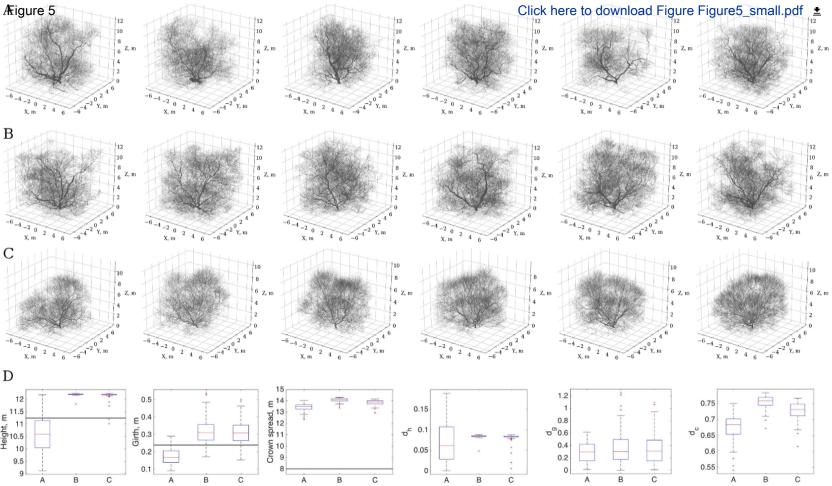




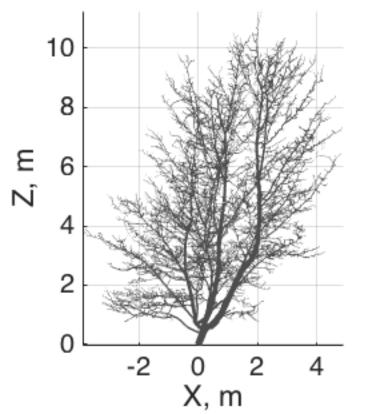


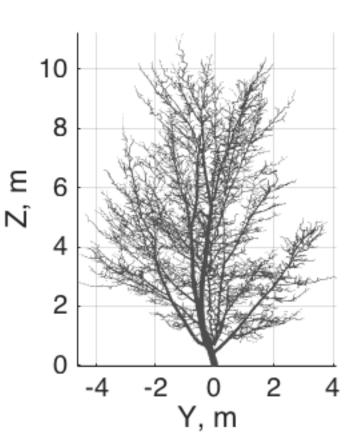


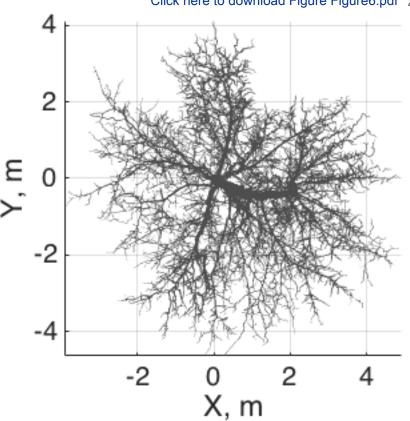
SSM growth iteration











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