## **S1.** Interpolating fractional maturity ages

Resources allocated to reproduction are the product of density-dependent effects acting on fertility  $Q_R(N, x)$  and the production rate at adult size  $W_{\tau}$  (size at maturity):

$$m_{\boldsymbol{x}} = Q_{\boldsymbol{R}}(\boldsymbol{N},\boldsymbol{x})\psi(W_{\boldsymbol{\tau}},\boldsymbol{x}) \Big[ \mathbf{1}_{\boldsymbol{x} \succ \lfloor \boldsymbol{\tau} \rfloor}(\boldsymbol{x}) + \big(\boldsymbol{\tau} - \lfloor \boldsymbol{\tau} \rfloor \big) \mathbf{1}_{\boldsymbol{x} = \lfloor \boldsymbol{\tau} \rfloor}(\boldsymbol{x}) \Big] \text{ ,}$$

where  $1_{t \ge \lfloor \tau \rfloor}(t)$  is an indicator function,  $\lfloor \tau \rfloor$  is a floor function, and  $(\tau - \lfloor \tau \rfloor)$  is a fractional part of  $\tau$ .

The term in the square bracket performs a simple interpolation when au is not an integer.