

Table S1: The Median (IQR) of the estimated τ^2 when no effect modification was present.

τ^2	Prevalence	Number of studies	$\tau_{two-stage}^2$	$\tau_{one-stage}^2$
0.5	30%	15	0.06 (0.26)	0.21 (0.35)
1.0	30%	15	0.47 (0.65)	0.84 (0.83)
1.5	30%	15	0.96 (1.08)	2.00 (1.67)
0.5	70%	15	0.01 (0.20)	0.18 (0.35)
1.0	70%	15	0.41 (0.67)	0.84 (0.79)
1.5	70%	15	0.89 (1.01)	1.92 (1.67)
0.5	30%	30	0.07 (0.20)	0.20 (0.26)
1.0	30%	30	0.51 (0.48)	0.86 (0.57)
1.5	30%	30	1.03 (0.73)	2.08 (1.15)
0.5	70%	30	0.04 (0.15)	0.20 (0.26)
1.0	70%	30	0.46 (0.48)	0.89 (0.63)
1.5	70%	30	0.98 (0.71)	2.13 (1.17)

Table S2: Sensitivity of heterogeneity measures^[1] to accounting for effect modification when prevalence of the outcome was 70%. Median (IQR) was presented.

τ^2	Number of studies	Strength of effect modification ^[2]	Two-stage approach		One-stage approach	
			$\frac{I^2_{mod}}{I^2_{crude}}$	$\frac{R^2_{mod}}{R^2_{crude}}$	$\frac{I^2_{mod}}{I^2_{crude}}$	$\frac{R^2_{mod}}{R^2_{crude}}$
0.5	15	Weak	1.00 (0.01)	1.00 (0.01)	0.84 (0.39)	0.83 (0.17)
1.0	15	Weak	0.85 (1.00)	0.94 (0.34)	0.90 (0.18)	0.81 (0.17)
1.5	15	Weak	0.54 (1.00)	0.71 (0.50)	0.90 (0.18)	0.79 (0.16)
0.5	15	Moderate	1.00 (0.01)	1.00 (0.01)	0.31 (0.47)	0.87 (0.19)
1.0	15	Moderate	1.00 (0.66)	1.00 (0.23)	0.41 (0.38)	0.90 (0.23)
1.5	15	Moderate	0.91 (0.96)	0.97 (0.32)	0.44 (0.37)	0.97 (0.31)
0.5	15	Strong	1.00 (0.01)	1.00 (0.01)	0.01 (0.01)	0.89 (0.19)
1.0	15	Strong	1.00 (0.01)	1.00 (0.01)	0.01 (0.15)	0.95 (0.30)
1.5	15	Strong	1.00 (0.12)	1.00 (0.10)	0.06 (0.21)	1.05 (0.49)
0.5	30	Weak	1.00 (0.01)	1.00 (0.01)	0.86 (0.32)	0.84 (0.12)
1.0	30	Weak	0.34 (1.00)	0.78 (0.39)	0.90 (0.12)	0.80 (0.10)
1.5	30	Weak	0.24 (0.71)	0.62 (0.33)	0.89 (0.12)	0.78 (0.11)
0.5	30	Moderate	1.00 (0.01)	1.00 (0.01)	0.28 (0.31)	0.87 (0.16)
1.0	30	Moderate	1.00 (1.00)	1.00 (0.24)	0.40 (0.25)	0.92 (0.19)
1.5	30	Moderate	0.69 (1.00)	0.85 (0.35)	0.43 (0.28)	1.00 (0.22)
0.5	30	Strong	1.00 (0.01)	1.00 (0.01)	0.01 (0.05)	0.88 (0.16)
1.0	30	Strong	1.00 (0.05)	1.00 (0.02)	0.05 (0.13)	0.96 (0.19)
1.5	30	Strong	1.00 (0.35)	1.00 (0.20)	0.06 (0.11)	1.09 (0.32)

^[1]We present the ratios of the measure estimated from a model that ignored the effect modifier to one that included the effect modifier and an interaction term between it and treatment status.

^[2]Effect modification was classified as weak when $\beta_w = 1$, $\beta_{xw} = 1$, as moderate when $\beta_w = 1$, $\beta_{xw} = 3$, and as strong when $\beta_w = 2$, $\beta_{xw} = 5$.

Table S3: Sensitivity of heterogeneity measures^[3] ($\frac{\tau_{mod}^2}{\tau_{crude}^2}$) to accounting for effect modification. Median (IQR) was presented.

τ^2	Number of studies	Strength of confounding ^[4]	Two-stage approach		One-stage approach	
			$\frac{\tau_{mod}^2}{\tau_{crude}^2}$ (pre = 30%)	$\frac{\tau_{mod}^2}{\tau_{crude}^2}$ (pre = 70%)	$\frac{\tau_{mod}^2}{\tau_{crude}^2}$ (pre = 30%)	$\frac{\tau_{mod}^2}{\tau_{crude}^2}$ (pre = 70%)
0.5	15	Weak	0.21 (1.00)	1.00 (0.01)	1.35 (1.55)	1.21 (1.12)
1.0	15	Weak	0.01 (0.85)	1.00 (1.00)	1.44 (0.36)	1.30 (0.59)
1.5	15	Weak	0.06 (0.78)	0.64 (1.00)	1.41 (0.38)	1.32 (0.36)
0.5	15	Moderate	0.03 (1.00)	1.00 (0.01)	0.93 (2.58)	1.19 (2.38)
1.0	15	Moderate	0.11 (1.00)	1.00 (0.57)	2.16 (2.43)	1.60 (1.39)
1.5	15	Moderate	0.49 (1.05)	1.00 (0.94)	2.47 (1.61)	1.79 (1.02)
0.5	15	Strong	0.01 (1.00)	1.00 (0.01)	1.28 (2.67)	1.35 (2.40)
1.0	15	Strong	0.56 (1.00)	1.00 (0.01)	2.89 (4.30)	1.95 (2.43)
1.5	15	Strong	0.74 (1.48)	1.00 (0.29)	3.87 (4.23)	2.09 (1.75)
0.5	30	Weak	0.01 (1.00)	1.00 (0.01)	1.38 (1.02)	1.28 (0.93)
1.0	30	Weak	0.01 (1.00)	0.43 (1.00)	1.42 (0.39)	1.31 (0.37)
1.5	30	Weak	0.19 (0.62)	0.28 (0.94)	1.41 (0.25)	1.33 (0.26)
0.5	30	Moderate	0.01 (1.00)	1.00 (0.01)	1.12 (1.69)	1.32 (1.62)
1.0	30	Moderate	0.01 (0.98)	1.00 (1.00)	2.16 (1.50)	1.70 (0.87)
1.5	30	Moderate	0.26 (1.00)	0.98 (1.07)	2.47 (1.09)	1.86 (0.66)
0.5	30	Strong	0.01 (1.00)	1.00 (0.01)	1.50 (2.21)	1.39 (2.19)
1.0	30	Strong	0.01 (1.00)	1.00 (0.01)	2.94 (2.66)	1.83 (1.23)
1.5	30	Strong	0.59 (1.41)	1.00 (0.76)	3.58 (2.33)	2.13 (1.03)

^[3]We present the ratios of the measure estimated from a model that ignored the effect modifier to one that included the effect modifier and an interaction term between it and treatment status.

^[4]Effect modification was classified as weak when $\beta_w = 1$, $\beta_{xw} = 1$, as moderate when $\beta_w = 1$, $\beta_{xw} = 3$, and as strong when $\beta_w = 2$, $\beta_{xw} = 5$.