The RE cells were also modeled as a single compartment neuron:

$$\frac{dV_D}{dt} = -I^{K-leak} - I^{leak} - I^{Na} - I^K - I^{LCa} - I^h - I^{syn}.$$
(C.4)

The conductances for leak currents were I^{leak}: 0.05 mS/cm² and I^{K-leak}: 0.016 mS/cm². The maximal conductances for other currents were fast Na⁺ (I^{Na}) current: 100 mS/cm²; fast K⁺ (I^K) current: 10 mS/cm²; and low-threshold Ca²⁺(I^{LCa}) current: 2.2 mS/cm².

C.2 Synaptic Currents. GABA-A, NMDA and AMPA synaptic currents were described by first-order activation schemes (Timofeev, Grenier, Bazhenov, Sejnowski, & Steriade, 2000). The equations for all synaptic currents used in this model are given in our previous publications (Bazhenov et al., 2002; Chen et al., 2012). We mention only the relevant equations:

$$I_{syn}^{AMPA} = g_{syn}[O](V - E_{AMPA}),$$

$$I_{syn}^{NMDA} = g_{syn}[O](V - E_{NMDA}),$$

$$I_{syn}^{GABA} = g_{syn}[O](V - E_{GABA}).$$
(C.5)



Appendix D: Supplementary Figures

Figure 17: Passive neuron model with 5 ms fixed synaptic delay. Results from correlation-based methods. (A) Ground-truth connection matrix. Neurons 1–50 are visible neurons. Neurons 51–60 are invisible neurons. (B) Estimation from the correlation method. (C) Estimation from the precision matrix. (D) Sparse + latent regularized precision matrix.



Figure 18: Differential covariance analysis of the passive neuron model with 5 ms fixed synaptic delay. The color in panels B, C, and D indicates the direction of the connections. For element A_{ij} , a warm color indicates *i* is the sink and *j* is the source: $i \leftarrow j$. A cool color indicates *j* is the sink and *i* is the source: $i \rightarrow j$. (A) Ground-truth connection matrix. (B) Estimation from the differential covariance method. (C) Estimation from the sparse + latent regularized partial differential covariance method.



Figure 19: Passive neuron model with 0–10 ms uniformly distributed synaptic delay. Results from correlation-based methods. (A) Ground-truth connection matrix. Neurons 1–50 are visible neurons. Neurons 51–60 are invisible neurons. (B) Estimation from the correlation method. (C) Estimation from the precision matrix. (D) Sparse + latent regularized precision matrix.



Figure 20: Differential covariance analysis of the passive neuron model with 0–10 ms uniformly distributed synaptic delay. The color in panels B, C, and D indicates the direction of the connections. For element A_{ij} , a warm color indicates *i* is the sink and *j* is the source: $i \leftarrow j$. A cool color indicates *j* is the sink and *i* is the source: $i \leftarrow j$. A cool color indicates *j* is the sink and *i* is the source: $i \leftarrow j$. A cool color indicates *j* is the sink and *i* is the source: $i \rightarrow j$. (A) Ground-truth connection matrix. (B) Estimation from the differential covariance method. (C) Estimation from the partial differential covariance method.

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References

- Banerjee, O., Ghaoui, L. E., d'Aspremont, A., & Natsoulis, G. (2006). Convex optimization techniques for fitting sparse gaussian graphical models. In *Proceedings* of the 23rd International Conference on Machine Learning (pp. 89–96). New York: ACM.
- Battistin, C., Hertz, J., Tyrcha, J., & Roudi, Y. (2015). Belief propagation and replicas for inference and learning in a kinetic Ising model with hidden spins. *Journal of Statistical Mechanics: Theory and Experiment*, 2015(5), P05021.