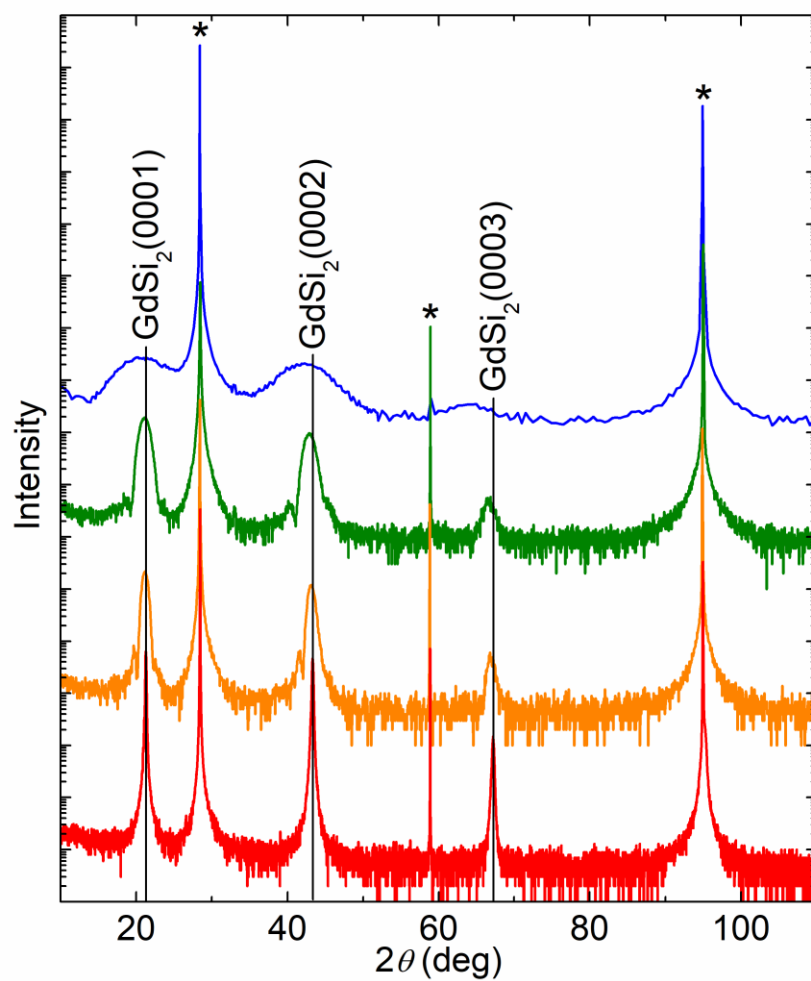
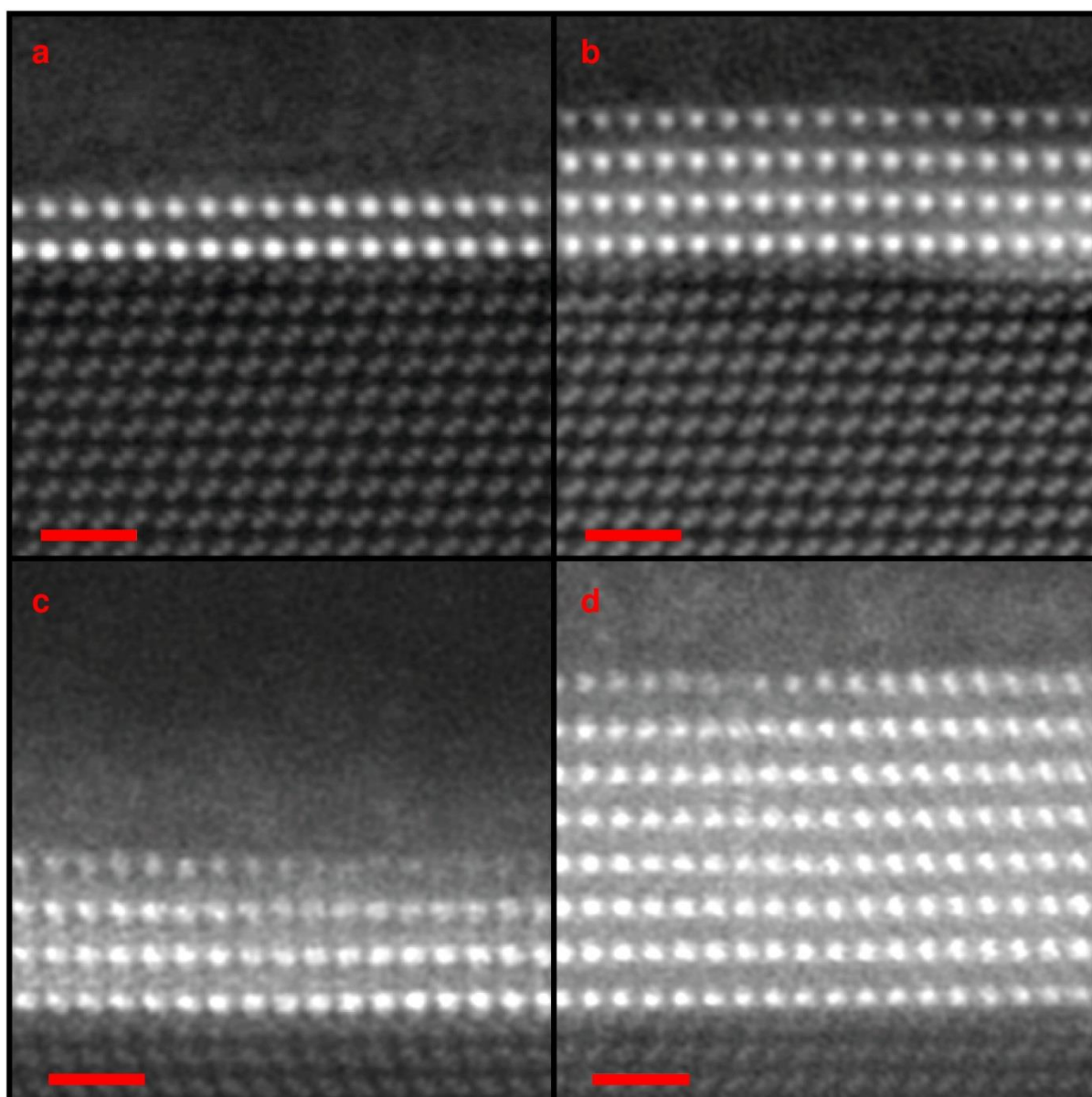


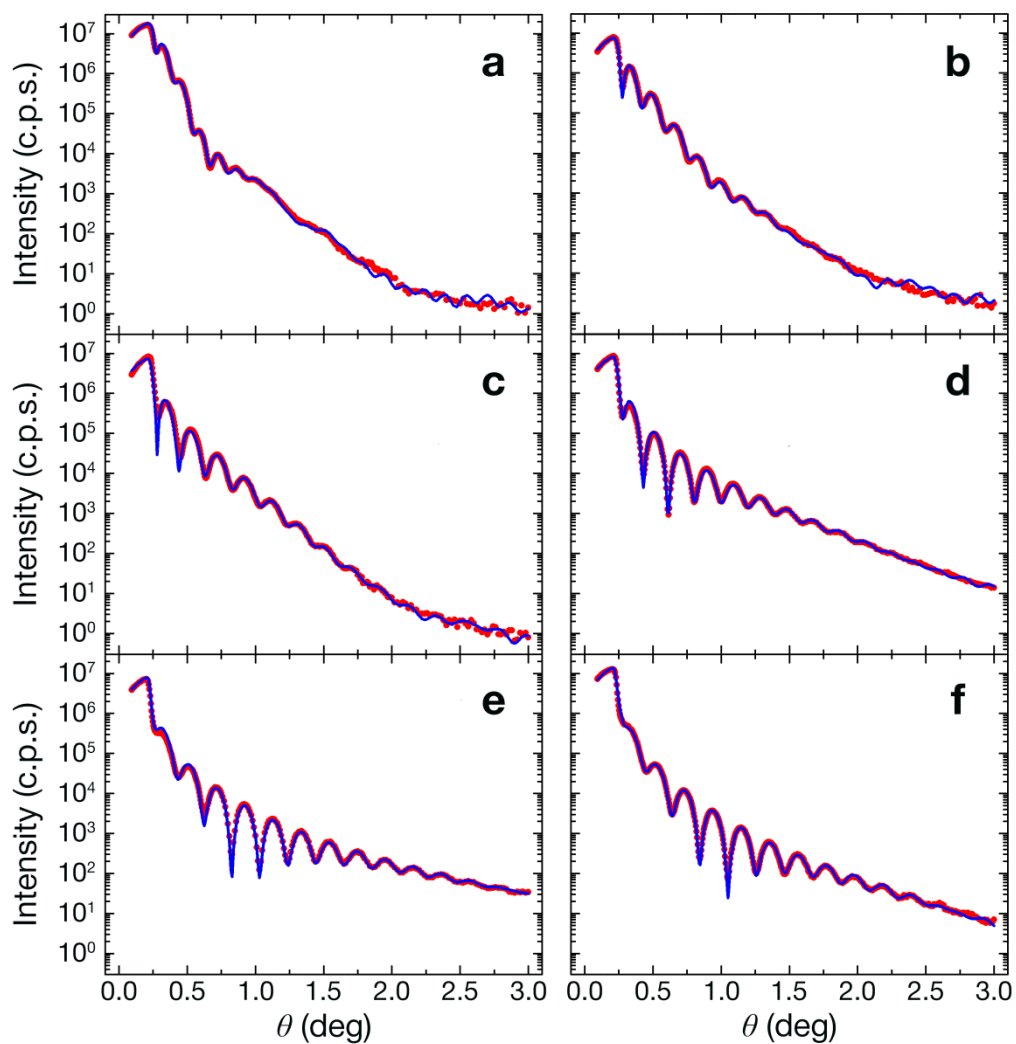
Supplementary Figure 1. RHEED images of Si(111) and GdSi₂. (a) Reconstructed Si(111) surface; (b-h) GdSi₂ with thickness 1 ML (b), 1-2 ML (c), 2 ML (d), 3 ML (e), \cong 9 ML (f), \cong 17 ML (g), \cong 160 ML (h). All images are along the $[1\bar{1}0]$ azimuth of the Si substrate.



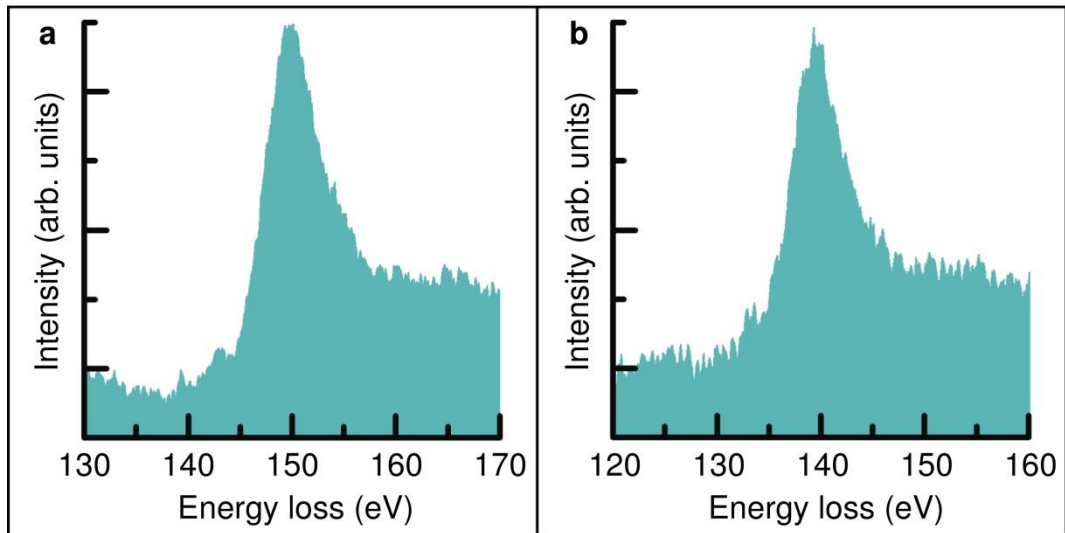
Supplementary Figure 2. X-ray diffraction study of GdSi₂ on Si(111). θ - 2θ diffraction scans for films with thickness 2 ML (blue), \cong 9 ML (green), \cong 17 ML (orange), bulk (red). Asterisk denotes peaks from the Si substrate.



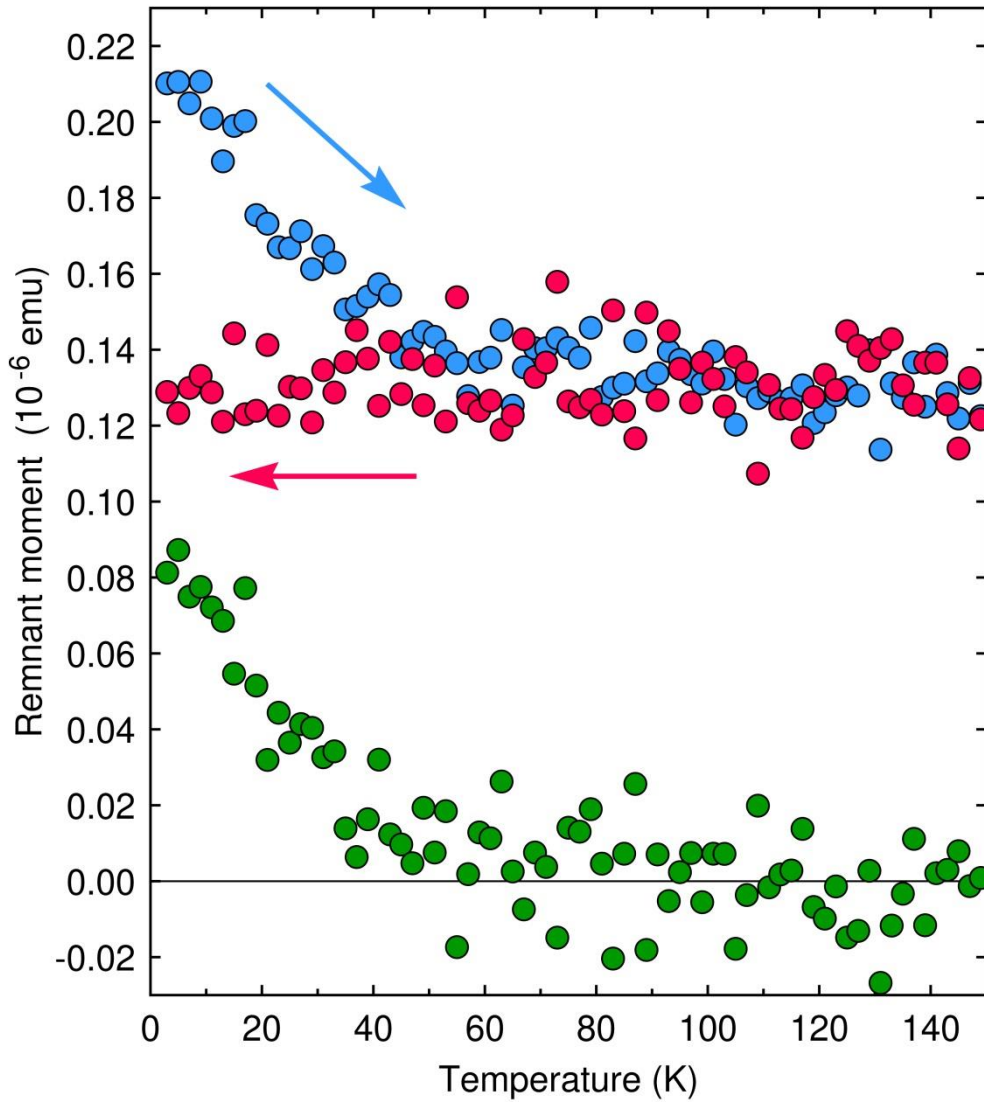
Supplementary Figure 3. Electron microscopy of ultrathin films. Cross-sectional HAADF-STEM images (viewed along the [110] zone axis of the Si substrate) of GdSi₂ films of (a) 2 ML and (b) 4-5 ML thickness and EuSi₂ films of (c) 4 ML and (d) \cong 8 ML thickness. Scale bar, 1 nm.



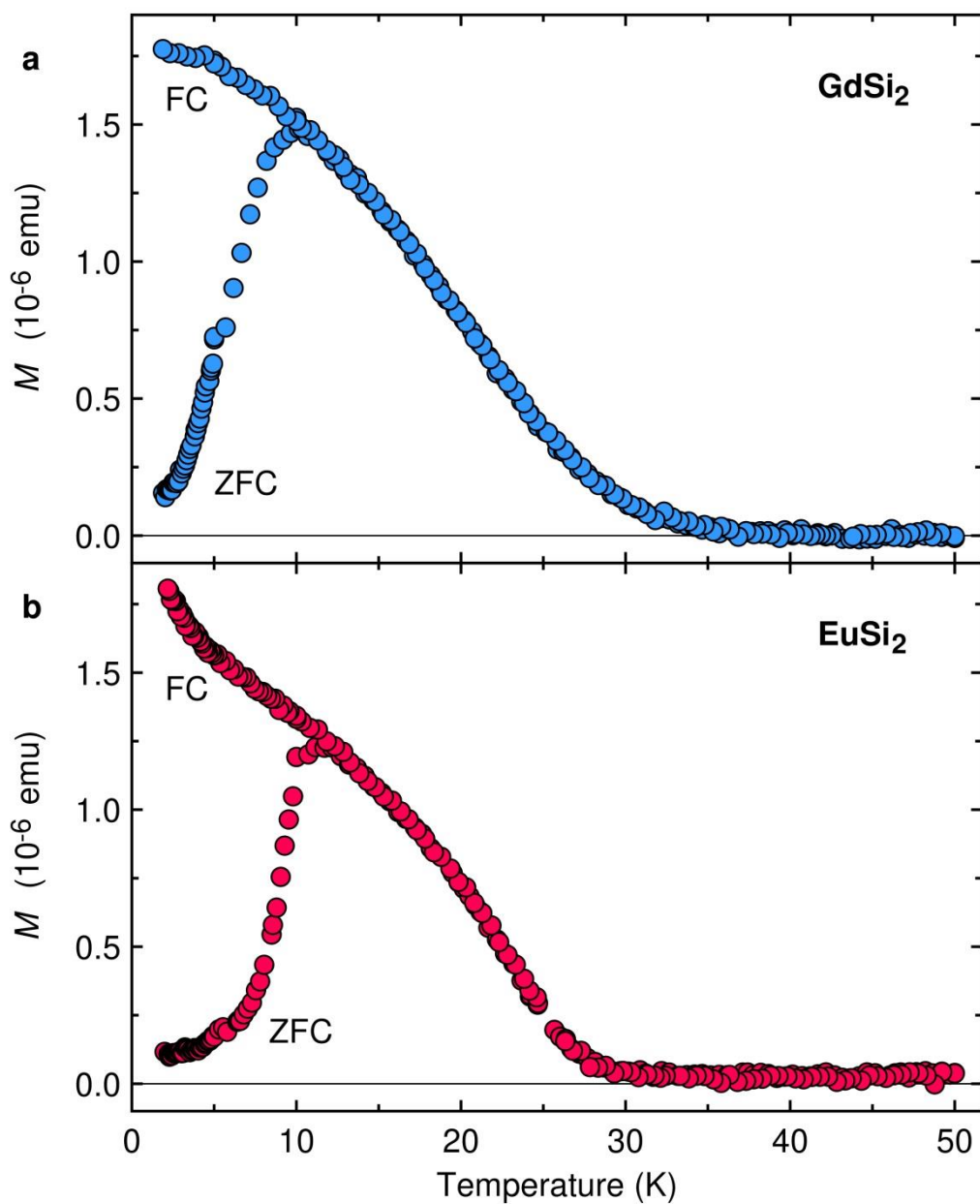
Supplementary Figure 4. X-ray reflectivity study of the films. Experimental curves (red) and theoretical fits (blue) for GdSi₂ on Si(111): **(a)** \cong 17 ML; **(b)** \cong 9 ML; **(c)** 4-5 ML; **(d)** 2 ML; **(e)** 1-2 ML; **(f)** 1 ML. The theoretical analysis relies upon a model based on lamellas with fitted parameters. This model is rather crude and the applicability of the analysis is limited.



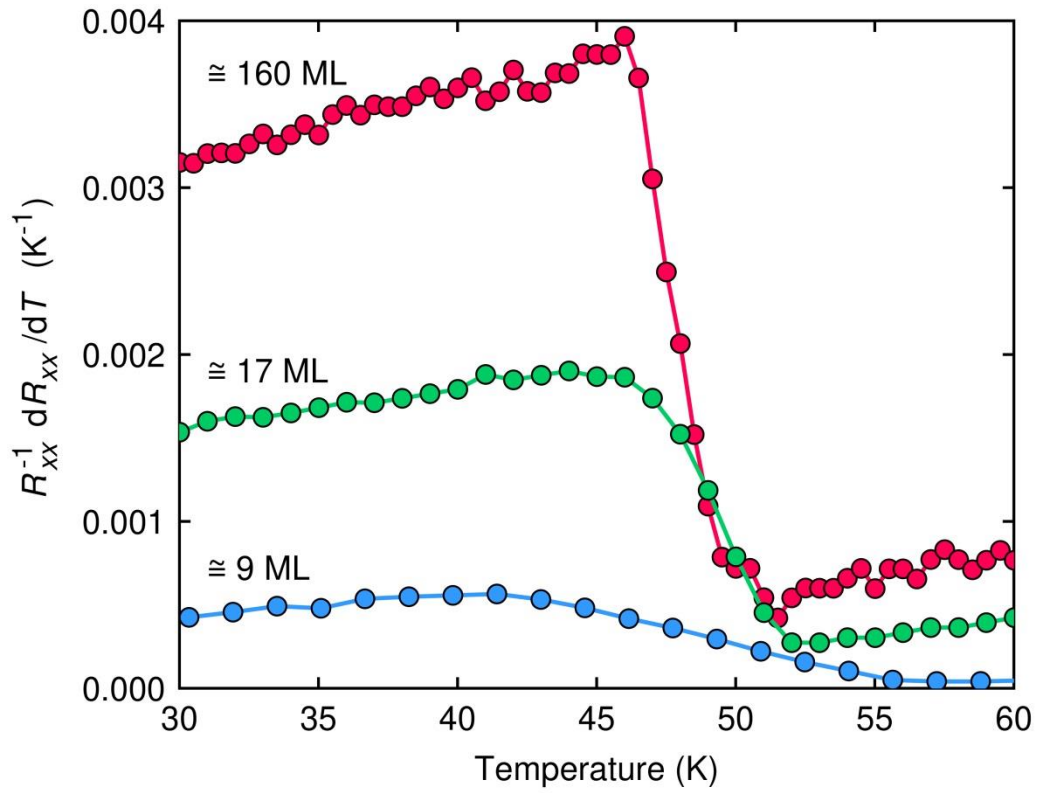
Supplementary Figure 5. Electron energy loss spectra of the films. The spectra of (a) $\cong 9$ ML of GdSi_2 and (b) $\cong 8$ ML of EuSi_2 show that the valence states of metal atoms are Gd(III) and Eu(II), respectively. Background is subtracted.



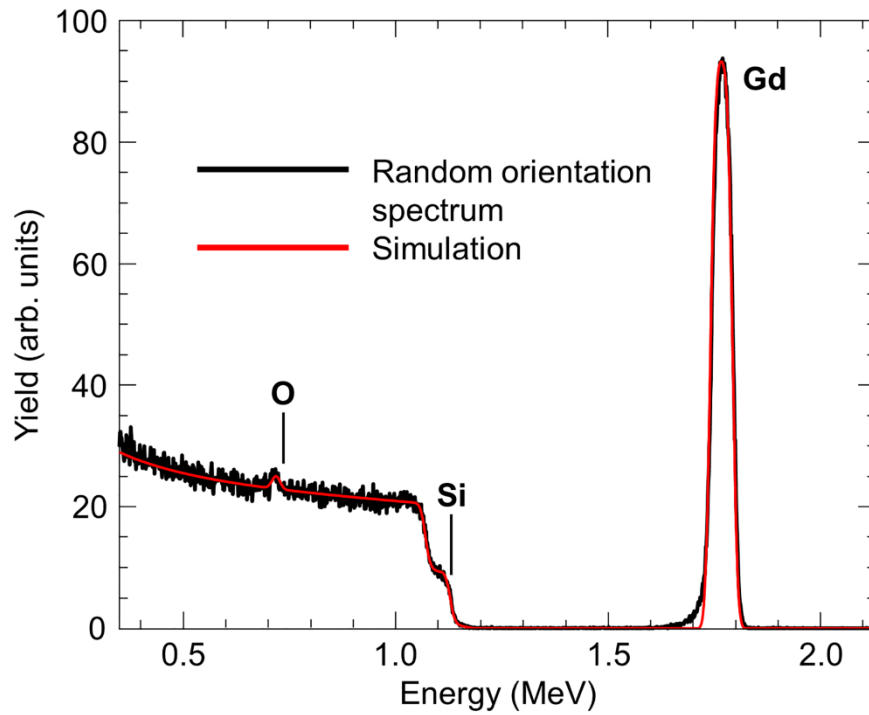
Supplementary Figure 6. Temperature dependence of the remnant moment. The moment is measured (after cooling in a magnetic field of 500 Oe) for the 17 ML sample of GdSi_2 : heating up (blue), subsequent cooling down (red), the difference between them (green). Compare with Fig. 3f of the main text.



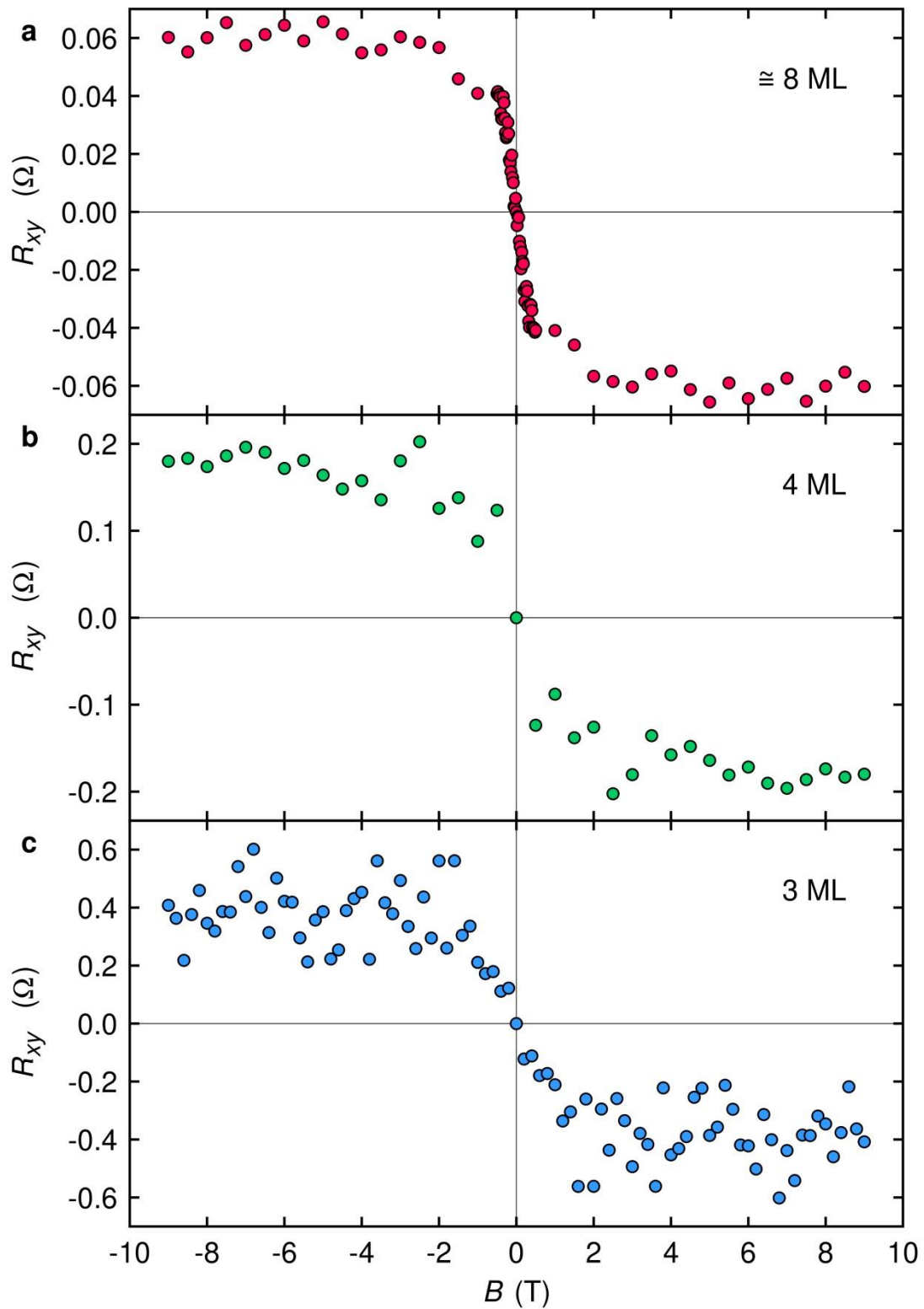
Supplementary Figure 7. Magnetic measurements of ultrathin films. Zero-field-cooled (ZFC) and field-cooled (FC) curves (50 Oe) for (a) 2 ML GdSi_2 ; (b) 1-2 ML EuSi_2 .



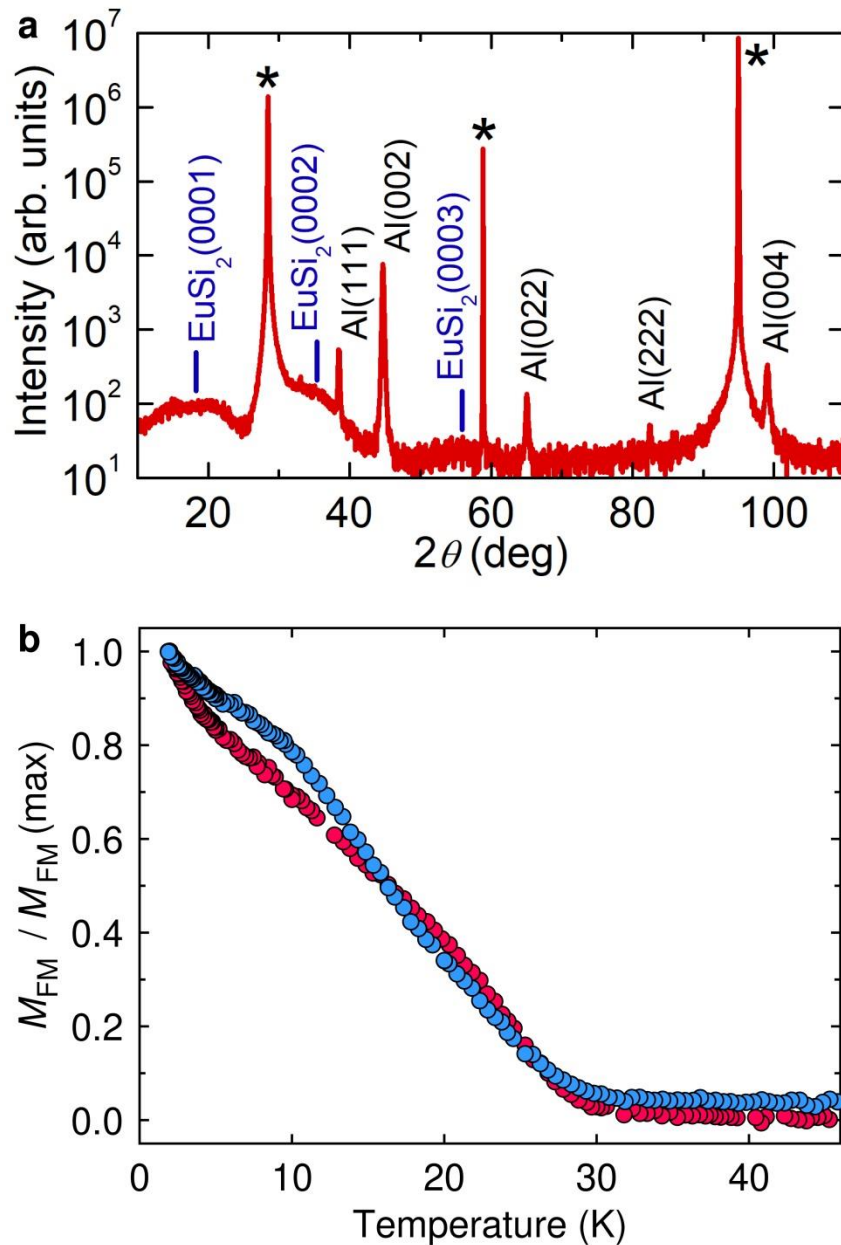
Supplementary Figure 8. Temperature dependence of resistance. Temperature coefficient of resistance for GdSi₂ films with a thickness ≈ 160 ML (red); ≈ 17 ML (green) and ≈ 9 ML (blue).



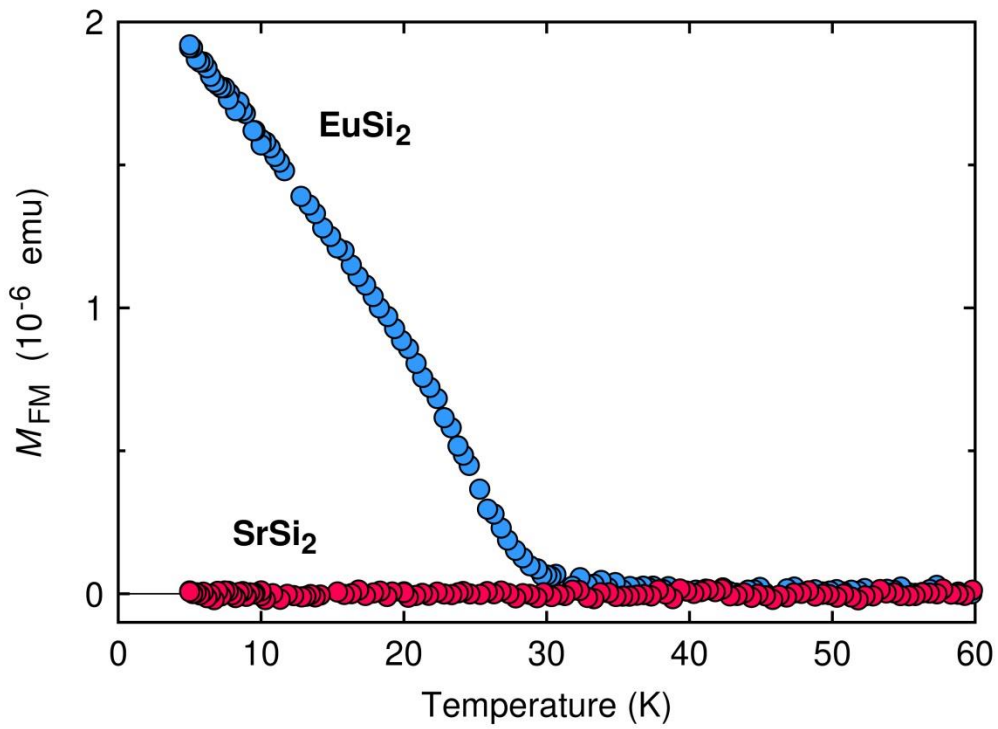
Supplementary Figure 9. Rutherford backscattering spectrum. The spectrum in random orientation (black) and its simulation (red) for bulk GdSi_2 on $\text{Si}(111)$ reveal the $\text{GdSi}_{1.84}$ stoichiometry.



Supplementary Figure 10. Anomalous Hall effect. Hall resistance at 2 K demonstrates anomalous Hall effect in EuSi_2 on $\text{Si}(111)$: **(a)** ≈ 8 ML (red); **(b)** 4 ML (green) and **(c)** 3 ML (blue). Note different scale of the effect for different film thickness.



Supplementary Figure 11. Study of the film of 3 ML of EuSi_2 on $\text{Si}(111)$ capped with 20 nm of Al. (a) θ - 2θ X-ray diffraction scan showing peaks from EuSi_2 (the peaks are rather broad due to a very small thickness of the film), polycrystalline Al and the Si substrate (denoted by asterisk). (b) Comparison of 3 ML EuSi_2 films with different capping: temperature dependence of magnetic moment in a magnetic field of 100 Oe: $\text{SiO}_x/\text{EuSi}_2/\text{Si}(111)$ (red) and $\text{Al}/\text{EuSi}_2/\text{Si}(111)$ (blue). The effective Curie temperatures are quite close; the difference in the form of the curves probably comes from a slight variation of growth parameters and resulting film thicknesses in two separate syntheses.



Supplementary Figure 12. Comparison of magnetism in silicene-based silicides.

Temperature dependence of magnetic moment in a magnetic field of 100 Oe: non-magnetic SrSi_2 (red) and ferromagnetic EuSi_2 (blue) of equivalent thickness ($\approx 2 \text{ nm}$).