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Supporting Information

Identification of Pt-based Catalysts for Propane Dehydrogenation via a Probability Analysis

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S1. Computational details and the models

The adsorption energy of an adsorbate, E_{ads} , was calculated as follows:

$$E_{ads} = E_{total} - E_{adsorbate} - E_{surfact}$$

where E_{total} is the total energy of the slab with an attached adsorbate. $E_{adsorbate}$ is the total energy of a gas molecule. $E_{surface}$ is the total energy of a relaxed clean slab.

The surface *d*-band center (ε_d) and *d*-band width (W_d) were computed as the first and second moments of the projected *d*-band density of states. The *d*-band filling (N_d) was calculated by integrating the density of states to the Fermi level (E_i).¹ They were expressed as:

$$\varepsilon_{d} = \frac{\int_{-\infty}^{+\infty} \rho E dE}{\int_{-\infty}^{+\infty} \rho dE}$$
$$W_{d}^{2} = \frac{\int_{-\infty}^{+\infty} \rho E^{2} dE}{\int_{-\infty}^{+\infty} \rho dE}$$
$$N_{d} = \int_{-\infty}^{E} \rho dE$$

where ρ represents the density of states and *E* is the energy of state.



Figure S1. Top and front views of ten Ptln alloys. Pt atoms are dark blue and In atoms are light yellow.

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Surface	k-points	Slab	Surface	k-points	Slab
Pt(211)	3×2×1	3×4×4	Pt ₃ In(100)_In	3×3×1	2×2×4
Pt(100)	3×3×1	2×2×4	Pt₃In(100)_Pt	3×3×1	2×2×4
Pt(111)	3×3×1	4×4×4	Pt₃ln(111)	3×3×1	4×4×4
Pt₃In(211)_In	3×2×1	3×4×4	Pt₁ln₁(111)	3×3×1	4×4×4
Pt₃In(211)_Pt	3×2×1	3×4×4	Ptln ₂ (110)	3×3×1	6×4×4

Table S1. k-points grid and slab size of different surfaces

S2. The energy profiles in screening process and the error estimation



Scheme S1. The complete process of our probability analysis

 Table S2. Free energy barriers of different Pt-based alloys, dehydrogenation rate constants and the corresponding standard deviation calculated by BEEF-vdW

	C ₃ H ₈ * to 1-C ₃ H ₇ *			C ₃ H ₆ * desorption		C ₃ H ₆ * to 1-C ₃ H ₅ *	
Pt-based alloy	Free ener	gy barrier/eV	$C_3H_8^{-1}$ to $1-C_3H_7^{-1}$	Free energ	y barrier/eV	Free energy	gy barrier/eV
	(Standard	deviation/eV)	Rate constants/s	(Standard o	leviation/eV)	(Standard	deviation/eV)
Pt	2.08	(0.23)	1.79×10 ¹	0.71	(0.20)	0.80	(0.30)
Pt₃Sc	2.12	(0.26)	1.05×10 ¹	0.50	(0.21)	0.80	(0.33)
Pt₃Ti	2.49	(0.24)	7.67×10 ⁻²	0.14	(0.20)	0.88	(0.28)
Pt₃V	2.55	(0.23)	3.45×10 ⁻²	0.13	(0.23)	1.02	(0.34)
Pt₃Cr	2.45	(0.22)	1.31×10 ⁻¹	0.22	(0.19)	0.96	(0.28)
Pt₃Mn	2.26	(0.23)	1.63×10 ⁰	0.46	(0.20)	0.89	(0.28)
Pt₃Fe	2.14	(0.22)	8.04×10 ⁰	0.62	(0.19)	0.85	(0.27)
Pt₃Co	2.10	(0.23)	1.37×10 ¹	0.68	(0.19)	0.84	(0.28)
Pt₃Ni	2.13	(0.23)	9.18×10 ⁰	0.64	(0.20)	0.84	(0.29)
Pt₃Cu	2.22	(0.24)	2.78×10 ⁰	0.49	(0.20)	0.87	(0.27)
Pt₃Zn	2.11	(0.23)	1.20×10 ¹	0.51	(0.19)	0.86	(0.30)
Pt₃Ga	1.74	(0.31)	1.64×10 ³	0.82	(0.28)	0.74	(0.29)
Pt₃Y	2.19	(0.26))	4.14×10 ⁰	0.45	(0.23)	0.76	(0.31)
Pt₃Zr	2.41	(0.23)	2.22×10 ⁻¹	0.18	(0.21)	0.88	(0.27)
Pt₃Nb	2.85	(0.27)	6.40×10 ⁻⁴	-0.18	(0.26)	1.30	(0.27)
Pt₃Mo	2.76	(0.23)	2.12×10 ⁻³	-0.13	(0.20)	1.18	(0.27)
Pt₃Tc	2.45	(0.23)	1.31×10 ⁻¹	0.24	(0.21)	1.00	(0.27)

Pt₃Ru	2.18	(0.23)	4.72×10 ⁰	0.56	(0.20)	0.86	(0.26)
Pt₃Rh	2.07	(0.23)	2.04×10 ¹	0.72	(0.21)	0.83	(0.25)
Pt₃Pd	2.05	(0.26)	2.66×101	0.72	(0.26)	0.81	(0.26)
Pt₃Ag	2.18	(0.26)	4.72×10 ⁰	0.49	(0.23)	0.82	(0.28)
Pt₃Cd	2.19	(0.25)	4.14×10 ⁰	0.40	(0.22)	0.86	(0.28)
Pt₃In	2.15	(0.24)	7.04×10 ⁰	0.41	(0.20)	0.86	(0.25)
Pt₃Sn	2.11	(0.22)	1.20×10 ¹	0.49	(0.20)	0.86	(0.26)

All the free energies barriers were calculated according to the reaction energies under 873K. The computational details have been provided in Section S8 and the zero-point energies have been taken into consideration.



Figure S2. BEEF-vdW prediction errors for 2000 ensemble energy barriers of first dehydrogenation step of Pt₃In and the ensemble energy variation of other catalysts are all like this.



Figure S3. The probability of Pt-based catalysts better than pure Pt under a given activity ((a) $k_{Pt3X} > k_{Pt} \times 0.1$ and (b) $k_{Pt3X} > k_{Pt} \times 0.033$) and selectivity constraint condition.

Pt-based alloy	Y _{Pt3X} -Y _{Pt} <-0.2	Y _{Pt3X} -Y _{Pt} <-0.3	Y _{Pt3X} -Y _{Pt} <-0.4	Y _{Pt3X} -Y _{Pt} <-0.2	Y _{Pt3X} -Y _{Pt} <-0.3	Y _{Pt3X} -Y _{Pt} <-0.4
	k _{Pt3X} >k _{Pt} ×0.1	k _{Pt3X} >k _{Pt} ×0.1	k _{Pt3X} >k _{Pt} ×0.1	k _{Pt3X} >k _{Pt} ×0.033	k _{Pt3X} >k _{Pt} ×0.033	$k_{Pt3X} > k_{Pt} \times 0.033$
Pt	0.00	0.00	0.00	0.00	0.00	0.00
Pt₃Sc	0.51	0.25	0.07	0.53	0.27	0.08
Pt₃Ti	0.00	0.00	0.00	0.00	0.00	0.00
Pt ₃ V	0.00	0.00	0.00	0.03	0.03	0.03
Pt₃Cr	0.00	0.00	0.00	0.00	0.00	0.00
Pt₃Mn	0.37	0.13	0.00	0.77	0.49	0.11
Pt₃Fe	0.13	0.00	0.00	0.13	0.00	0.00
Pt₃Co	0.00	0.00	0.00	0.00	0.00	0.00
Pt₃Ni	0.10	0.00	0.00	0.11	0.00	0.00
Pt₃Cu	0.59	0.18	0.00	0.84	0.43	0.07
Pt₃Zn	0.72	0.29	0.04	0.72	0.29	0.04
Pt₃Ga	0.01	0.00	0.00	0.02	0.00	0.00
Pt₃Y	0.40	0.16	0.02	0.54	0.30	0.13
Pt₃Zr	0.00	0.00	0.00	0.07	0.06	0.04
Pt₃Nb	0.00	0.00	0.00	0.00	0.00	0.00
Pt ₃ Mo	0.00	0.00	0.00	0.00	0.00	0.00
Pt₃Tc	0.00	0.00	0.00	0.06	0.06	0.06
Pt₃Ru	0.51	0.01	0.00	0.52	0.01	0.00
Pt₃Rh	0.02	0.00	0.00	0.03	0.00	0.00
Pt₃Pd	0.06	0.00	0.00	0.11	0.02	0.00
Pt₃Ag	0.39	0.09	0.00	0.59	0.29	0.07
Pt₃Cd	0.69	0.47	0.15	0.89	0.67	0.35
Pt₃In	0.92	0.69	0.34	0.93	0.69	0.35
Pt₃Sn	0.80	0.36	0.06	0.80	0.36	0.06

Table S3. The probability of being in ideal region under different given constraint conditions

 ${}^{a} Y_{Pt3X} - Y_{Pt} < -0.2$ and $k_{Pt3X} > k_{Pt} \times 0.1$ (Y: the difference of propylene desorption free energy barrier and further dehydrogenation step free energy barrier of Pt₃X, k_{Pt3X} : the rate constants of Pt₃X) mean is Pt₃X owns a better selectivity and an acceptable activity. Then, we consider Pt₃X in the acceptable region of selectivity and activity.



Figure S4. The probability that the activity and selectivity of a given catalyst better than pure Pt under a given activity and selectivity constraint condition as a function of propylene desorption free energy barrier relative to that of Pt ((a) $Y_{Pt3X}-Y_{Pt}<-0.3$ and $k_{Pt3X}>k_{Pt}\times0.1$ (b) $Y_{Pt3X}-Y_{Pt}<-0.2$ and $k_{Pt3X}>k_{Pt}\times0.033$ (c) $Y_{Pt3X}-Y_{Pt}<-0.3$ and $k_{Pt3X}>k_{Pt}\times0.033$)

S3. Experimental section

All the catalysts were prepared by incipient wetness impregnation method to obtain 0.3wt % Pt loading. $H_2PtCl_6 \cdot 6H_2O$ (Chemart (Tianjin) Chemical Technology Co., Ltd., 99.9%) and $In(NO_3)_2 \cdot xH_2O$ (J&K Scientific Ltd., 99.9%) were used as precursors and SiO₂ (Alfa Aesar (China) Chemicals Co., Ltd., amorphous fumed) was used as support. After impregnation, the catalysts were dried at 80 °C for 12 h and then calcined at 600 °C for 2h. The metal loading was based on the weight ratio between metal and SiO₂.

 H_2 - O_2 titration measurements were carried out on a Micromeritics AutoChem II 2920 apparatus with a thermal conductive detector. For every test, 100 mg sample was pre-reduced at 600 °C with a flow rate of 30 mL min⁻¹ of 10 vol% H_2 /Ar for 1h, and then cooled down to 50 °C in Ar atmosphere. Subsequently, 10 vol% O_2 /He was introduced to the sample by injection pulses till no visible change in the consumption peaks. And then, 10 vol% H_2 /Ar was admitted to the sample by injection pulses. It can be assumed that the adsorption stoichiometry factor of Pt/ H_2 was equal to 2/3. The platinum dispersion is calculated by the Eq. (1):

Dispersion (%) = $V_{H2} \times 2/3 \times MW_{Pt} / (W_{Pt} \times 224.14)$ (1) where V_{H2} is the volume of adsorbed H_2 (mL), MW_{Pt} is the atomic weight of Pt (g mol⁻¹), and W_{Pt} is the weight of Pt supported on the sample (g).

Catalytic measurements were performed on a quartz fixed-bed reactor (8 mm inside diameter) at 600 °C under atmosphere pressure. 250 mg of fresh catalyst (particle size of 20 to 40 mesh) was packed inside the quartz tube and heated to reaction temperature (10 °C/min) in a N₂ flow. Then, a mixture of 14 vol% propane and 14 vol% H₂ in N₂ was fed in a rate of 50 mL/min. The hydrogen cofeeding may reduce the coverage of coke precursors and change the reaction pathway.² The weight hourly space velocity (WHSV) of propane was 3 h⁻¹.³ Exhaust streams were analyzed with an online GC (2060) equipped with a flame ionization detector (Chromosorb 102 column) and a thermal conductivity detector (Al₂O₃ Plot column). The propane conversion and selectivity to propylene were calculated from Eq. (2) and Eq. (3) respectively:

Con (%) = ($[F_{C3H8}]_{inlet}$ - $[F_{C3H8}]_{outlet}$) / $[F_{C3H8}]_{inlet}$	(2)
Sel (%) = 100 × n _i × [F _{C3H6}] _{outlet} / [3 × ([F _{C3H8}] _{inlet} - [F _{C3H8}] _{outlet})]	(3)

where i stands for different hydrocarbon products in exhaust gases, n_i is the number of carbon atom of component i, and F_i is the corresponding molar flow rate.

	Table S4. The segregation energies of PtIn catalysts					
E _{seg} /eV		Pt₃ln(211)_ln	Pt₃In(100)_In	Pt₃In(111)	Pt₁In₁(111)	
Our mode	I	0.00	0.00	0.00	0.00	
Pt segrega	ation	4.15	4.14	4.63	14.02	
In segrega	ation	1.12	Not available ^a	2.97	Not converged	

S4. Segregation energies, global optimization and surface energies of PtIn catalysts

^a no In in second layer available.

The segregation energies are calculated by the following equation:

$E_{seg} = E_{surface alloy} - E_{bulk alloy}$

where $E_{surface alloy}$ is the energy of surface alloy which first subsurface layer Pt or In segregates to the surface and $E_{bulk alloy}$ is the energy of bulk alloy which is uniform in bulk. The more positive E_{seg} is, the less stable surface alloy is.



Figure S5. The surface energies of the two possible surfaces of (a) Pt₃In(211) and (b) Pt₃In(100).

The approach we used to calculate the surface energy is listed below.^{4, 5}

The chemical potential of the bulk alloy:

 $\mu^{alloy}_{Pt3In} = 3\mu^{alloy}_{Pt} + \mu^{alloy}_{In} = 3\mu^{bulk}_{Pt} + \mu^{bulk}_{In} - \Delta H_{Pt3In}$

where the μ_{Pt3In}^{alloy} is the chemical potential of Pt₃In alloy and represented by the chemical potentials of Pt and In in Pt₃In (μ_{Pt}^{alloy} and μ_{In}^{alloy}). They can be related to the chemical potentials of bulk Pt (μ_{Pt}^{bulk}), bulk In (μ_{In}^{bulk}) and the alloy formation enthalpy (ΔH_{Pt3In}). The μ_{Pt}^{alloy} is in the range:

 $\mu_{Pt}^{bulk} - \frac{1}{3} |\Delta H_{Pt3In}| \le \mu_{Pt}^{alloy} \le \mu_{Pt}^{bulk}$

Then, the surface energy can be expressed below:

$$\gamma = \frac{E_{slab} - \Delta N \mu_{Pt}^{bulk} - N_{In} \mu_{Pt3In} - \Delta N [\mu_{Pt}^{alloy} - \mu_{Pt}^{bulk}]}{2A}$$

where $\Delta N = N_{Pt} - 3N_{In}$, N_{Pt} and N_{Pt} stand for the number of Pt and In atoms in the slab, and A is the surface area of the slab in xy plane. $\mu = G = E + E_{ZPE}$, *E* is the energy calculated by VASP and the E_{ZPE} is the zero-point energy.

S5. Surface adsorption



Figure S6. The scheme of simulated 1.6 nm particles. Purple: step atoms represented by (211) facets, green: (100) facets, orange: (111) facets, blue: bulk atoms.

C₃H₈ & C₃H₆



Figure S7. The physisorption of propane, di- σ and π adsorption of propylene.

Table S5.	Adsorption	energies of	f propane	and propyl	lene on	different facets.
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Adsorption	Propane	Propylene	Adsorption	Propane	Propylene
energy/ev			energy/ev		
Pt(211)	-0.23	-1.37	Pt₃In(100)_In	-0.30	-0.79
Pt(100)	-0.23	-1.17	Pt₃In(100)_Pt	-0.23	-1.00
Pt(111)	-0.24	-1.10 (-1.07ª)	Pt ₃ In(111)	-0.23	-0.80 (-0.77ª)
Pt₃ln(211)_ln	-0.16	-0.87	Pt ₁ In ₁ (111)	-0.29	-0.38
Pt ₃ In(211)_Pt	-0.22	-1.31	Ptln ₂ (110)	-0.17	-0.23
ion operaty of propyl	ono oo odoorhi	na with a Ll atom	1 4112(110)	0.11	0.20

^a the adsorption energy of propylene co-adsorbing with a H atom.

Table S6. The adsorption energies of propylene on different surfaces with different adsorption modes (π adsorption energy modes

were used	l as a	reference)	
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		,	
Surface/eV	di-o mode	π mode	C ₃ H ₆ *_cross
Pt(211)	-0.13	0	0.06
Pt(100)	-0.08	0	
Pt(111)	-0.25	0	
Pt₃In(211)_In		0	0.36
Pt₃In(211)_Pt	-0.19	0	0.14
Pt₃In(100)_In		0	
Pt₃In(100)_Pt	-0.06	0	
Pt₃In(111)	-0.13	0	
Pt₁In₁(111)	0.67	0	
Ptln ₂ (110)		0	

The adsorption energies of propane on all different surfaces calculated by BEEF-vdW functional are summarized in Table S5. Common GGA functionals are suitable for computing many important quantities in chemistry and condensed matter physics, but appear

to be unable to describe van der Waals dispersion interactions.⁶ As a result, PBE and RPBE functionals offer a poor description of propane adsorption and the predicted adsorption energies are about 0.^{7, 8} BEEF-vdW includes van der Waals dispersion interactions and the calculated adsorption energies are in the range of -0.30~-0.16eV, which means the adsorption of propane is physisorption and BEEF-vdW offers a better description of van der Waals dispersion interactions than PBE and RPBE.⁶ The adsorption structure of propane on Pt(111) is illustrated in Figure S7 for an example and the others on different surfaces are all like that on Pt(111).

There are two main adsorption modes of propylene, di- σ and π adsorption, which are illustrated in Figure S7. From our calculated results, propylene prefers to bind to Pt atoms rather than In atoms. On Pt(211), Pt(100), Pt(111), Pt₃ln(211)_Pt, Pt₃ln(100)_Pt, Pt₃ln(111), di- σ mode is energetically more favorable (Table S6) due to the existence of two adjacent Pt atoms. The length of C=C bond increases from 1.34 Å in gas phase to about 1.48 Å after adsorption which is the typical length of C-C bond, indicating the rehybridization of C from sp² to sp³. On Pt₃ln(211)_In, Pt₃ln(100)_In, Pt₁ln₁(111) and Ptln₂(110), propylene prefers π mode and the length of C=C bond is about 1.40 Å, which can be attributed to the lack of two adjacent Pt atoms or the too large distance between two Pt atoms (Pt₁ln₁(111)). Therefore, one of the geometric effect of In can be attributed to the separation of adjacent Pt atoms, which leads to the transformation from di- σ adsorption mode to π adsorption mode and the decrement of propylene adsorption energy.





On all surfaces, both $C_3H_7^*$ and $C_3H_5^*$ only tend to bind with the Pt atoms. More importantly, it must be noted all the $C_3H_5^*$ prefer to only interact with the step Pt atoms on (211) facets (Figure S8), which ensures the intermediates on (211) facets discussed below all interact with the step Pt atoms.

On all surfaces, both $1-C_3H_7^*$ and $2-C_3H_7^*$ tend to adsorb to only one surface Pt atom on the top site. $C_3H_5^*$ lost three H atoms and tend to bind to three metal atoms intuitively. On Pt(211) and Pt_3ln(211)_Pt, $1-C_3H_5^*$ and $2-C_3H_5^*$ prefers binding to only two step Pt atoms (Figure S8a and g) rather than bind to two step Pt atoms and one terrace Pt atom (Figure S8b). The bond length of C=C increases from 1.34 Å to 1.41 Å, which means the breakage of C=C and the formation of three σ -like bond. On Pt_3ln(211)_In, the step sites are arrayed by Pt and In atom one by one. $1-C_3H_5^*$ and $2-C_3H_5^*$ tend to bind to only one step Pt atom in a σ -like mode (Figure S8e) rather than bind to one step and two terrace Pt atoms (Figure S8f). The bond length of C=C is still 1.34 Å just as that of propylene. This indicates that it won't break the C=C of $C_3H_5^*$ on Pt_3ln(211)_In. On Pt(100), Pt_3ln(100)_Pt and Pt_1ln_1(111) (Figure S8c, i and k), due to the lack of three adjacent Pt atoms, $1-C_3H_5^*$ and $2-C_3H_5^*$ tend to bind to two Pt atoms, just like on Pt_3ln(211)_Pt. On Pt(111) and Pt_3ln(111) (Figure S8d and j), $1-C_3H_5^*$ and $2-C_3H_5^*$ tend to bind to only one Pt atoms in σ -like mode. On Pt_3ln(100)_In and Ptln_2(110) (Figure S8h and I), $1-C_3H_5^*$ and $2-C_3H_5^*$ tend to bind to only one Pt atom, due to the lack of two adjacent Pt atoms.

S6. Potential energy profiles of different routes

	Table 37. Potential energy promes of different routes						
Potential energy/eV	Pt(211)	Pt(100)	Pt(111)	Pt₃ln(211)_l	Pt₃ln(211)_P		
				11	<u>ا</u>		
C ₃ H ₈ (g)→1-C ₃ H ₈ *	-0.23	-0.23	-0.24	-0.16	-0.22		
C ₃ H ₈ *→1-C ₃ H ₇ * (TS)	0.69	0.76	0.95	0.81	0.91		
C ₃ H ₈ *→2-C ₃ H ₇ * (TS)	0.62	0.71	1.03	0.89	0.74		
1-C ₃ H ₇ *→C ₃ H ₆ * (TS)	0.55	0.69	0.87	0.92	0.57		
2-C ₃ H ₇ *→C ₃ H ₆ * (TS)	0.51	0.73	0.93	0.57	0.59		
C ₃ H ₆ *→1-C ₃ H ₅ * (TS)	0.54	0.74	0.96	1.19	0.63		
C ₃ H ₆ *→2-C ₃ H ₅ * (TS)	0.53	0.92	0.99	1.14	0.71		
$C_3H_6^* \rightarrow C_3H_6(g)$	-1.37	-1.17	-1.10	-0.87	-1.31		
Potential energy/eV	Pt₃ln(100)_ln	Pt₃ln(100)_Pt	Pt₃ln(111)	$Pt_1In_1(111)$	PtIn ₂ (110)		
$C_3H_8(g) \rightarrow 1-C_3H_8^*$	-0.30	-0.23	-0.23	-0.29	-0.17		
$C_3H_8^* \rightarrow 1-C_3H_7^*$ (TS)	1.15	0.81	1.00	1.93	1.75		
C ₃ H ₈ *→2-C ₃ H ₇ * (TS)	1.14	0.76	1.43		1.75		
1-C ₃ H ₇ *→C ₃ H ₆ * (TS)	1.24	0.64	0.92	1.17	1.47		
2-C ₃ H ₇ *→C ₃ H ₆ * (TS)	1.28	0.65	0.86		1.40		
C ₃ H ₆ *→1-C ₃ H ₅ * (TS)	1.25	0.71	1.02	1.42	1.44		
C ₃ H ₆ *→2-C ₃ H ₅ * (TS)	1.30	0.83	0.99		1.52		
$C_3H_6^* \rightarrow C_3H_6(g)$	-0.79	-1.00	-0.80	-0.38	-0.23		

 Table S7. Potential energy profiles of different routes



Figure S9. Potential energy diagram (a) α -type PDH reaction on Pt(211), Pt₃ln(211)_Pt and Pt₃ln(211)_ln. (b) α -type PDH reaction on Pt(111), Pt₃ln(111), Pt₁ln₁ (111) and Ptln₂(110).

From the view of potential energy (Figure S9), the energy profiles of the dominating (211) facets were compared first. The first dehydrogenation energy barrier of Pt(211) is 0.69 eV, while Pt₃ln(211)_Pt (0.91 eV) and Pt₃ln(211)_ln (0.81 eV) have a little higher activation energies. This implies the energy barrier increases with the addition of In, i.e. In decreases the activity of PDH reaction. Pt(211) and Pt₃ln(211)_Pt have a similar further dehydrogenation barrier from C₃H₆* to 1-C₃H₅* (0.54 eV and 0.63 eV) which is much lower than the desorption energy of C₃H₆* (1.37 eV and 1.31 eV), indicating Pt₃ln(211)_Pt will not improve the poor selectivity of Pt(211).⁹ However, The further dehydrogenation barrier of Pt₃ln(211)_In (1.19 eV) is much higher than the desorption energy of C₃H₆* (0.87 eV), which means Pt₃ln(211)_In will greatly improve the selectivity to propylene. Because the properties of two possible surfaces of Pt₃ln(211) may vary greatly, the surface energies of the two possible surfaces of Pt₃ln(211)_In were calculated to obtain a more thermodynamically stable surface.^{4, 5} From Figure S5a, it can be observed that Pt₃ln(211)_In has lower surface energies in the whole possible range, which means Pt₃ln(211)_In is preferred thermodynamically. This result indicates the undercoordinated sites of Pt tend be partially covered by In atoms and plays a crucial role in elucidating the improvements in propylene selectivity. The results of Pt(100), Pt₃ln(100)_Pt and Pt₃ln(100)_In are similar to (211) facets mentioned above (Table S7).

To elucidate the relationship between the ratio of In and reaction activity, the potential energies on Pt(111), Pt₃In(111), Pt₁In₁(111) and PtIn₂(110) were also compared. The first dehydrogenation barrier of Pt(111) (0.95 eV) and Pt₃In(111) (1.00 eV) are almost the same. When the PtIn ratio comes to 1:1 and 1:2, the first dehydrogenation energy barrier has an obvious increase (1.93 eV and 1.75 eV). This means the activity will suffer a great loss when the PtIn ratio is higher than 3:1, When it comes to selectivity, the desorption energy barrier of propylene is higher than propylene further dehydrogenation barrier on Pt(111), which corresponds to the selectivity problem of pure Pt catalyst that propylene tend to further dehydrogenation rather than desorption. With the addition of In, Pt₃In(111),

 $Pt_1In_1(111)$ and $PtIn_2(111)$ all have a lower propylene desorption energy barrier than that of further dehydrogenation. Although $Pt_1In_1(111)$ and $PtIn_2(110)$ have an obviously higher further dehydrogenation barrier than $Pt_3In(111)$ which means a better selectivity, their reaction activity is much lower and the improvements in selectivity are hard to compensate for the great loss of activity.



Figure S10. Potential energy diagram (a) β-type PDH reaction on Pt(211), Pt₃ln(211)_Pt and Pt₃ln(211)_In. (b) β-type PDH reaction on Pt(111), Pt₃ln(111), Pt₁ln₁(111) and Ptln₂(110).

The route of β -type PDH reaction (from $C_3H_8^*$ to $2-C_3H_7^*$ to $C_3H_6^*$ to $2-C_3H_5^*$) has the similar trends to α -type PDH reaction (Figure S10).

In summary, a Pt_3In cluster which contains $Pt_3In(211)_In$, $Pt_3In(100)_In$ and $Pt_3In(111)$ have a similar activity to a pure Pt cluster, while the clusters which own higher In ratio have a great loss in activity. Furthermore, the addition of In can improve the selectivity of pure Pt cluster. In other words, a Pt_3In cluster may finally have the largest propylene formation performance.

S7. Free energy profiles of different routes

Free energy/eV	Pt(211)	Pt(100)	Pt(111)	Pt₃ln(211)_ln	Pt₃In(211)_Pt
$C_3H_8(g) \rightarrow 1-C_3H_7^*$ (TS)	1.84	1.91	2.08	2.05	2.08
$C_3H_8(g) \rightarrow 2 - C_3H_7^*$ (TS)	1.78	1.85	2.16	2.12	1.91
$1-C_3H_7^* \rightarrow C_3H_6^*$ (TS)	0.30	0.42	0.63	0.67	0.33
$2-C_3H_7^* \rightarrow C_3H_6^*$ (TS)	0.29	0.47	0.68	0.33	0.37
$C_{3}H_{6}^{*} \rightarrow 1 - C_{3}H_{5}^{*}$ (TS)	0.41	0.60	0.80	1.02	0.50
$C_{3}H_{6}^{*} \rightarrow 2 - C_{3}H_{5}^{*}$ (TS)	0.40	0.76	0.84	0.96	0.57
$C_3H_6^* \rightarrow C_3H_6(g)$	-0.15	-0.35	-0.43	-0.66	-0.21
Free energy/eV	Pt₃ln(100)_ln	Pt₃In(100)_Pt	Pt₃In(111)	Pt₁In₁(111)	Ptln ₂ (110)
$C_3H_8(g) \rightarrow 1-C_3H_7^*$ (TS)	2.27	1.95	2.15	3.04	2.96
C ₃ H ₈ (g)→2-C ₃ H ₇ * (TS)	2.24	1.89	2.57		2.96
1-C ₃ H ₇ *→C ₃ H ₆ * (TS)	0.99	0.36	0.61	0.85	1.14
2-C ₃ H ₇ *→C ₃ H ₆ * (TS)	1.03	0.38	0.58		1.14
C ₃ H ₆ *→1-C ₃ H ₅ * (TS)	1.07	0.57	0.86	1.27	1.29
C ₃ H ₆ *→2-C ₃ H ₅ * (TS)	1.12	0.67	0.83		1.36
$C_3H_6^* \rightarrow C_3H_6(q)$	-0.75	-0.51	-0.73	-1.13	-1.27

Table S8. Free energy profiles of different routes



Figure S11. Gibbs free energy diagram (a) β -type PDH reaction on Pt(211), Pt₃ln(211)_Pt and Pt₃ln(211)_ln. (b) β -type PDH reaction on Pt(111), Pt₃ln(111), and Ptln₂(110)

Due to the deficient performance of harmonic approximation for estimating the entropy of adsorbed species, the entropies were calculated based on the empirical equation suggested by Campbell et al. $^{10, 11}$:

$$S_{ad}(I) = S_{gas}(I) - 3.3R$$

where S_{ad} and S_{gas} are the entropies of adsorbate and gas molecules and *R* is the ideal gas constant. For a surface reaction, the entropy change was ignored. It must be pointed out the analysis proposed by Campbell et al. only corresponds to terrace sites and should be carefully applied to defect sites.¹⁰

The adsorption mode of propane was not taken into consideration in free energy analysis. The adsorption mode of propane is physisorption on the surface which makes it hard to identify the entropy of propane.

S8. A mean field microkinetic analysis

A mean field microkinetic analysis was performed by our own microkinetic simulation program.¹² The model was developed based on the DFT-obtained thermodynamic and kinetic data from all elementary steps and the experimental reaction conditions (T = 873K, feed composition: $C_3H_8 = 20\%$, $H_2 = 25\%$). The rate constants were calculated based on the transition state theory (TST):

$$k = \frac{k_B T}{h} e^{-\frac{\Delta G^{\neq}}{k_B T}}$$

where k is the rate constant of an elementary reaction step, ΔG^{\sharp} is the Gibbs activation energy, k_B is the Boltzmann constant and T is the reaction temperature.

In the microkinetic modeling, the steady state is calculated by a time integration method until a steady surface coverage and product pressure are reached.¹² The rate at time t of each individual step is calculated, according to the partial pressure and surface coverage of each species at that time. The new partial pressure or surface coverage for species c at time $t+\Delta t$ is calculated following the formula below:

$$\theta_c(t + \Delta t) = \theta_c(t) + \Delta \theta_c = \theta_c(t) + \int_t^{t} \int_t^{\Delta t} \frac{d\theta_c}{dt} = \theta_c(t) + r_c \Delta t$$

where t is time, Δt is time step which is used in the integration, $\theta_c(t)$ is the coverage of species c at time t and r_c is the total reaction rate of species c.

The rate-controlling steps was identified via calculating the "Degree of Rate Control" introduced by Campbell et al.¹³⁻¹⁵:

$$X_{RC,i} = \frac{k_i}{r} \left(\frac{\partial r}{\partial k_i}\right)_{k_j \neq i, K_i} = \left(\frac{\partial In(r)}{\partial In(k_i)}\right)_{k_j \neq i, K_i}$$

where r is the reaction rate and k is the rate constants. The degree of rate control is calculated in our kinetic model by increasing both the forward and reverse rate constants by 1% for the elementary reactions, which won't change the equilibrium.

Adsorbates on an ordered surface attempt to minimize their free energy when moving on the surface, which is difficult to treat exactly.¹⁶ Thus, basic assumptions of our kinetic model were introduced:

1. Surface is homogeneous (For PtIn alloys, only the Pt active sites were taken into consideration)

- 2. All Pt sites are equivalent
- Each site can hold at most one adsorbate 3

dt

There are no interactions between adsorbates 4.

In this microkinetic modeling, three types of free molecules, seven surface species and eight elementary steps were included. The temperature was set as 873K and pressure was set to $P_{C3HB(g)} = 0.2$ and $P_{H2(g)} = 0.25$. The rate equations of all surface species are as follows:

$$r_{C3H8(g)} = \frac{d\theta_{C3H8(g)}}{dt} = -r1 - r2$$

$$r_{C3H6(g)} = \frac{d\theta_{C3H6(g)}}{dt} = +r7$$

$$r_{H2(g)} = \frac{d\theta_{H2(g)}}{dt} = +r8$$

$$r_{1-C3H7*} = \frac{d\theta_{1-C3H7*}}{dt} = -r3 + r1$$
(1)
(2)
(3)

$$r_{2-C3H7*} = \frac{d\theta_{2-C3H7*}}{dt} = -r4 + r2$$
(5)

$$r_{C3H6*} = \frac{d\theta_{C3H6*}}{dt} = -r5 - r6 - r7 + r3 + r4$$

$$r_{1-C3H5*} = \frac{d\theta_{1-C3H5*}}{dt} = +r5$$
(7)

(6)

$$r_{2-C3H5*} = \frac{d\theta_{2-C3H5*}}{dt} = +r6$$
(8)
$$r_{H*} = \frac{d\theta_{H*}}{dt} = -r8 - r8 + r1 + r2 + r3 + r4 + r5 + r6$$
(9)

The coke formation was not explicitly included in our micro-kinetic modeling. The simplification of our reaction network in the micro-kinetic modeling is mainly due to the following reasons: (1) the coke formation mechanism is very complex, which is also not the main focus of our study. (2) the formation of $C_3H_5^*$ is just used as a model precursor for coke formation, which seems to be widely accepted by previous studies C-C bond breaking needs deeply dehydrogenated precursor, i.e. propyne (CH₃CCH^{*}), which means the 1-C₃H₅^{*} (CH₃CHCH^{*}) can be viewed as the origin of deeply dehydrogenated species and coke precursors.^{4, 8}

List of reactions Reaction rate $\begin{array}{l} r_{1} = k_{1} P_{C3H8(g)} \theta_{v} - k_{-1} \theta_{1-C3H7} * \theta_{H} * \\ r_{2} = k_{2} P_{C3H8(g)} \theta_{v} - k_{-2} \theta_{2-C3H7} * \theta_{H} * \end{array}$ R1 $C_3H_8(g) + * \rightleftharpoons 1 - C_3H_7 * + H *$ $C_3H_8(g) + * \rightleftharpoons 2 - C_3H_7 * + H *$ R2 $1 - \tilde{C}_3 H_7 * + * \rightleftharpoons C_3 \tilde{H}_6 * + H *$ $r_3 = k_3 \theta_{1-C3H7*} \theta_v - k_{-3} \theta_{C3H6*} \theta_{H*}$ R3 $2 - C_3 H_7 * + * \rightleftharpoons C_3 H_6 * + H *$ $r_4 = k_4 \theta_{2-C3H7*} \theta_v - k_{-4} \theta_{C3H6*} \theta_{H*}$ R4 $r_{5} = k_{5}\theta_{C3H6*}\theta_{v} - k_{-5}\theta_{1-C3H5*}\theta_{H*}$ R5 $_6^* + * \rightleftharpoons 1 - C_3 H_5 * + H *$ $r_{6} = k_{6}\theta_{C3H6*}\theta_{v} - k_{-6}\theta_{2-C3H5*}\theta_{H*}$ R6 $C_3H_6 * + * \rightleftharpoons 2 - C_3H_5 * + H *$ $C_3H_6* \rightleftharpoons C_3H_6(g) + *$ $r_7 = k_7 \theta_{C3H6*} - k_{-7} P_{C3H6} \theta_{\nu}$ R7 $H * + H * \rightleftharpoons H_2(g) + 2 *$ R8 $r_8 = k_8 \theta_{H^*}^2 - k_{-8} P_{H2} \theta_v^2$

Table S9. List of PDH rate (molC₃H₆ molsite⁻¹ s⁻¹) of elementary steps

Table S10	. Coverage	of reaction	intermediate
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Surface	1-C ₃ H ₇ *	2-C ₃ H ₇ *	C ₃ H ₆ *	$1-C_{3}H_{5}^{*}$	2-C ₃ H ₅ *	H*	*
Pt(211)	2.57 × 10 ⁻¹⁰	5.00 × 10 ⁻¹⁰	1.49 × 10 ⁻¹¹	7.93 × 10 ⁻⁰⁹	1.35 × 10 ⁻⁰⁸	2.98 × 10 ⁻⁰²	0.970
Pt(100)	5.00 × 10 ⁻¹⁰	2.16 × 10 ⁻⁰⁹	6.00 × 10 ⁻¹²	1.26 × 10 ⁻⁰⁹	2.79 × 10 ⁻⁰⁹	1.05 × 10 ⁻⁰²	0.990
Pt(111)	8.51 × 10 ⁻¹⁰	5.71 × 10 ⁻¹⁰	2.61 × 10 ⁻¹³	3.67 × 10 ⁻¹¹	9.30 × 10 ⁻¹¹	1.36 × 10 ⁻⁰²	0.986
Pt₃ln(211)_ln	2.03 × 10 ⁻⁰⁹	9.27 × 10 ⁻¹²	3.89 × 10 ⁻¹³	5.10 × 10 ⁻¹⁴	2.52 × 10 ⁻¹³	3.41 × 10 ⁻⁰³	0.996
Pt₃ln(100)_ln	4.81 × 10 ⁻⁰⁹	8.12 × 10 ⁻⁰⁹	1.82 × 10 ⁻¹⁴	3.56 × 10 ⁻¹⁵	3.12 × 10 ⁻¹⁵	1.28 × 10 ⁻⁰²	0.987
Pt₃ln(111)	2.56 × 10 ⁻¹⁰	6.50 × 10 ⁻¹³	7.64 × 10 ⁻¹⁴	1.37 × 10 ⁻¹²	4.53 × 10 ⁻¹²	1.28 × 10 ⁻⁰²	0.987
$Pt_1In_1(111)$	4.55 × 10 ⁻¹⁴		5.64 × 10 ⁻¹⁹	1.05 × 10 ⁻¹⁸		1.29 × 10 ⁻⁰⁵	1.000

The rate-controlling steps was identified via calculating the "Degree of Rate Control" introduced by Campbell et al.¹³⁻¹⁵:

$$X_{RC,i} = \frac{k_i}{r} (\frac{\partial r}{\partial k_i})_{k_j \neq i, K_i} = (\frac{\partial In(r)}{\partial In(k_i)})_{k_j \neq i, K_i}$$

where *r* is the reaction rate and *k* is the rate constants. The degree of rate control is calculated in our kinetic model by increasing both the forward and reverse rate constants by 1% for the elementary reactions, which won't change the equilibrium.



Figure S12 The relationship between the reaction energy from $C_3H_6^*$ to our model coke precursor $(1-C_3H_5^*)$ and the coverage of coke precursor on Pt(211).

For the coverage of our model coke precursor $(1-C_3H_5^*$ that has a thermodynamic equilibrium with $C_3H_6^*$ at steady state), it changed with the adsorption energy of $1-C_3H_5^*$.

S9. Correlation between ε_d^W and propylene π adsorption energy



Figure S13. Correlation between ε_d^W and propylene π adsorption energy

A slight modification has been identified to improve the *d*-band center descriptor. Vojvodic et al. introduced an alternative descriptor $\varepsilon_d^W = \varepsilon_d + W_d/2$. This model explicitly explains how the bond strength depends on the anti-bonding state formed between adsorbate and metal through the upper-edge position of the *d*-states. This descriptor not only takes the average energy of *d*-band into consideration but also utilizes the information in the *d*-band width. The introduction of a width dependence ensures correlations with the upper band-edge position and hence the bond strength¹⁷. ε_d^W was found to be a better descriptor than *d*-band center.

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