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Supplementary Information for

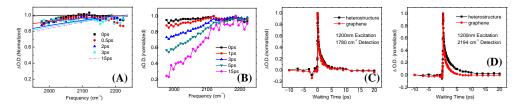
Ultrafast probes of electron-hole transitions between two atomic layers

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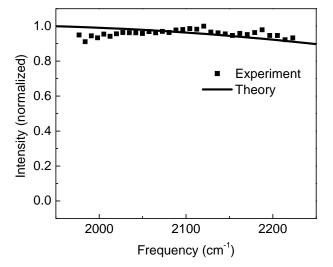


Supplementary Figure 1. Waiting time dependent IR spectra of monolayer graphene

calculations for graphene monolayer excited with 1.03 eV.

and heterostructure after excitation with 1.03 eV photons. (A) Graphene; (B) heterostructure; (C) pump/probe data detected at 1780 cm⁻¹; (C) pump/probe data detected at 2194 cm⁻¹. Dots are data, and lines are calculations. Calculation parameters: graphene Fermi level $\mu = -0.19$ eV, phonon fraction $f_{SCOPS} = 0.15$, photon flux absorbed F = 0.0069 J/m², pump/probe response time t = 170 fs, and

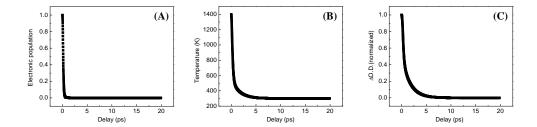
electron-phonon coupling parameter $\eta = 6.0 \frac{eV}{\text{Å}}$. These parameters are used for all



Supplementary Figure 2. Spectrum of heterostructure at t = 0 ps after excitation

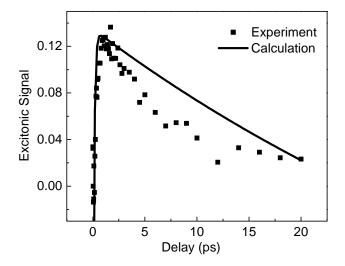
with 1.03 eV photons. Dots are data, and the line is calculation. Calculation parameters: graphene Fermi level $\mu=-0.17$ eV, phonon fraction $f_{SCOPS}=0.15$, photon flux absorbed F=0.0046 J/m², response time t=170 fs, and electron-phonon coupling parameter $\eta=6.0\frac{eV}{A}$.





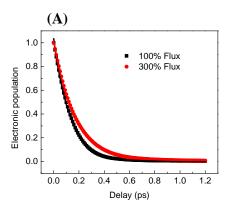
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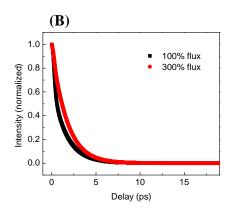
Supplementary Figure 3. (A) Calculated electronic population relaxation in 75 heterostructure after 1.03 eV excitation. (B) Calculated temperature of graphene in 76 heterostructure. (C) Calculated transient IR signal (2185 cm⁻¹) of graphene in 77 heterostructure after 1.03 eV excitation. Calculation parameters: graphene Fermi 78 level $\mu = -0.17 \, \text{eV}$, phonon fraction $f_{SCOPs} = 0.15$, photon flux absorbed 79 $F = 0.0046 J/m^2$, pump response time t = 170 fs, and electron-phonon coupling 80 parameter $\eta=6.0rac{eV}{ar{A}}$. Subtracting (C) from the experimental signal of 81 heterostructure (Supplementary Figure 3E) yields the excitonic signal (Supplementary 82 83 Figure 3F). Here the temperature increase from energy released from exciton formation is ignored. The signal reduction because of exciton formation is not 84 85 considered either. The effects of these two factors on the graphene signal are opposite. Because of this, we estimate the uncertainty of the exciton formation time introduced 86 by the approximations to be <20% (on average around 25% free carriers form 87



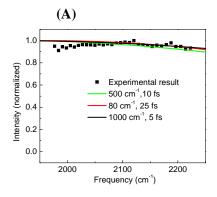
Supplementary Figure 4. Excitonic signal of heterostructure after 1.03 eV excitation.

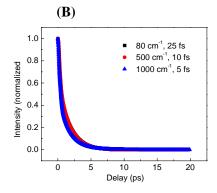
The data (dots) are obtained by directly subtracting the graphene signal from the heterostructure signal. Calculations (line) show that the excitonic formation time is 325 fs, which is essentially the same as 364 fs of Supplementary Figure 3F. Both time constants are not normalized to the absorption cross section. The line is a bioexponential with t_1 =120 fs (electronic decay time constant from graphene calculations) with factor -0.37, and t_2 =55 ps with factor 0.37. In Supplementary Figure 3F, the calculation for excitonic signal uses parameters: t_1 =120 fs (electronic decay time constant from graphene calculations) with factor -0.33, and t_2 =65 ps with factor 0.33.





Supplementary Figure 5. Calculated graphene 400nm-excitation/2185cm⁻¹-detection electronic dynamics (A) and signals (B) with two different excitation fluxes. Calculation parameters: graphene Fermi level $\mu = -0.17 \text{ eV}$, phonon fraction $f_{SCOPs} = 0.15$, photon flux absorbed $F = 0.0087 \frac{J}{m^2}$ (100% flux) and $0.0261 \frac{J}{m^2}$, pump response time t = 170 fs, and electron-phonon coupling parameter $\eta = 6.0 \frac{\text{eV}}{\text{Å}}$. The electronic decay time is 130 fs with 100% and 170 fs with 300% flux.

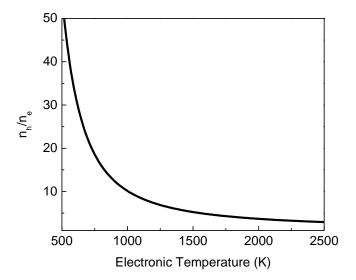




Supplementary Figure 6. Comparisons of calculations with different electronic dephasing linewidths and times of graphene. Calculation parameters: graphene Fermi level $\mu = -0.17$ eV, phonon fraction $f_{SCOPs} = 0.20$, $f_{SCOPs} = 0.15$, $f_{SCOPs} = 0.1$ for calculations with $\Gamma = 80$ cm⁻¹ and $\tau_e = 25$ fs, $\Gamma = 500$ cm⁻¹ and $\tau_e = 10$ fs, $\Gamma = 0.1$

116 1000 cm⁻¹ and $\tau_e = 5$ fs, respectively; photon flux absorbed 117 $F = 0.0087 \frac{J}{m^2}$ (100% flux), pump response time t = 170 fs, and electron-phonon 118 coupling parameter $\eta = 6.0 \frac{eV}{A}$. The parameters only slightly affect the linshape and 119 dynamics.

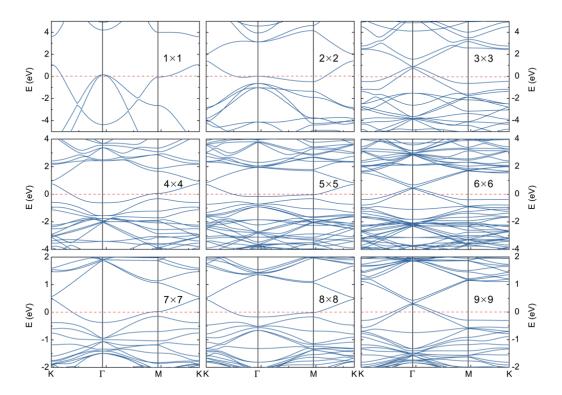
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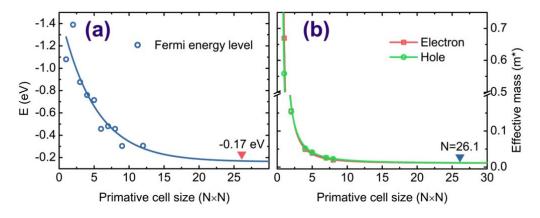
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Supplementary Figure 7. *Temperature dependent* n_h/n_e

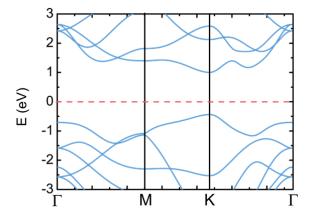
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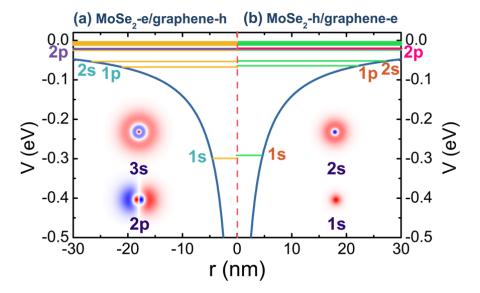
Supplementary Figure 8. Band structure. Electronic band structures of boron-doped graphene with different primitive cell.



Supplementary Figure 9. (a) Fermi energy level of boron-doped graphene with different primitive cell. (b) The effective mass of B-doped system for electron and hole transport with different primitive cell. As the Fermi energy level is -0.17 eV, the primitive cell size is 26.1×26.1 , and the corresponding hole and electron effective

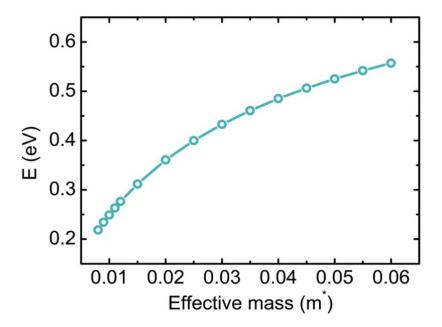


Supplementary Figure 10. The calculated Electronic band structures of monolayer MoSe₂, underestimates the band gap by around 0.5 eV.

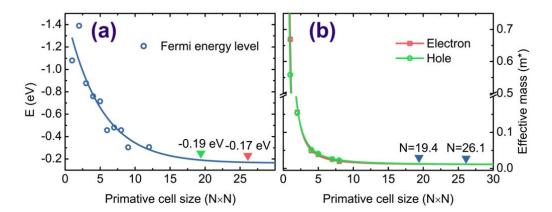


Supplementary Figure 11. Also Supplementary Figure 3D in main text. A few eigenvalues are shown on the Model Coulomb potential as a function of in-plane radius for an electron-hole pair across the graphene/MoSe₂ heterojunction van der Waals interface. (a) Hole is in graphene and electron is in the MoSe₂ monolayer. (b)

Hole is in MoSe₂ and electron is in graphene. Wave functions of several states are also shown. (red/blue: positive/negative.)

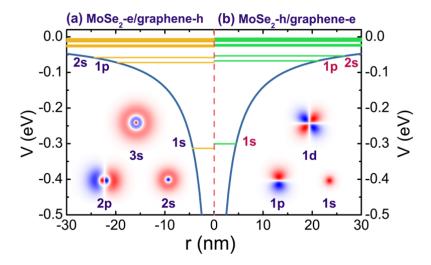


Supplementary Figure 12. The exciton transition energy (1s-2p) of graphene/MoSe₂ correlated with effective mass of the excitonic quasi particle.



Supplementary Figure 13. (a) Fermi energy level of boron-doped graphene with different primitive cell. (b) The effective mass of B-doped system for electron and hole

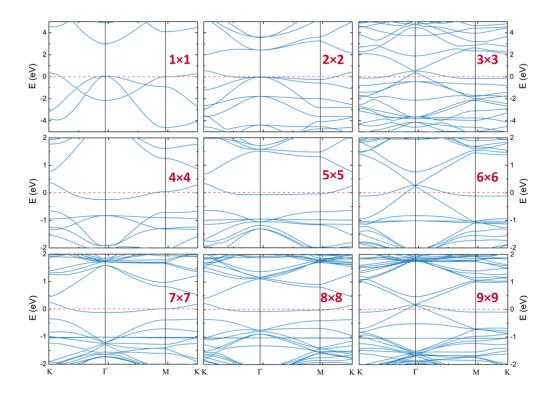
transport with different primitive cell. When the Fermi energy level is -0.19 eV, the primitive cell size is 19.4×19.4 , and the corresponding hole and electron effective mass is 0.0132 and 0.0122, respectively.



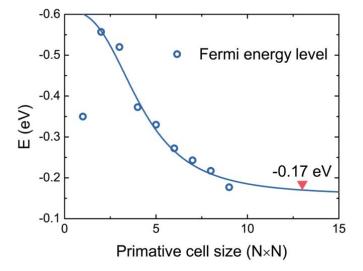
Supplementary Figure 14. A few eigenvalues are shown on the Model Coulomb potential as a function of in-plane radius for an electron-hole pair across the graphene/MoSe₂ heterojunction van der Waals interface. (a) Hole is in graphene and electron is in MoSe₂ monolayer. (b) Hole is in MoSe₂ slab and electron is in graphene. Several wave functions are also shown. (red/blue: positive/negative.) Fermi level -0.19 eV.

graphene_hole/MoSe₂_electron: $E_{ls-2p} = 0.287 \text{ eV}, \langle \rho_{CT_{1s}} \rangle = 43.1 \text{ Å}$

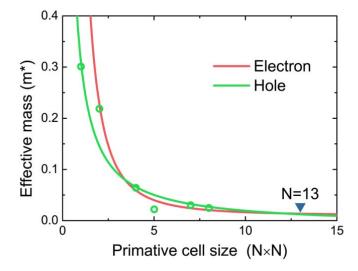
graphene_electron/MoSe₂_hole: $E_{Is-2p} = 0.276 \text{ eV}$, $\langle \rho_{CT_{1s}} \rangle = 45.1 \text{ Å}$



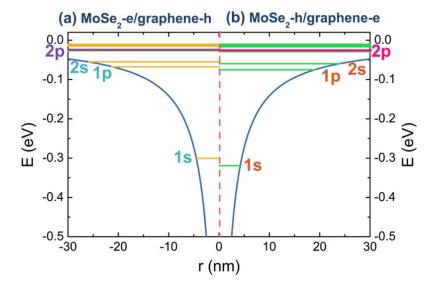
Supplementary Figure 15. Band structure. Electronic band structures of aluminum-doped graphene with different primitive cell.



Supplementary Figure 16. Fermi energy level of aluminum-doped graphene with different primitive cell.

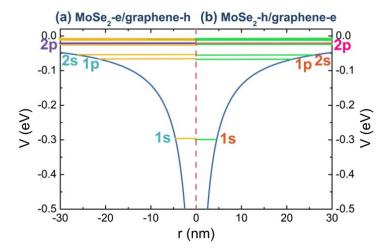


Supplementary Figure 17. The effective mass of B-doped system for electron and hole transport with different primitive cell. As the Fermi energy level is -0.17 eV, the primitive cell size is 13×13 , and the corresponding hole and electron effective mass is 0.0122 and 0.0135, respectively.

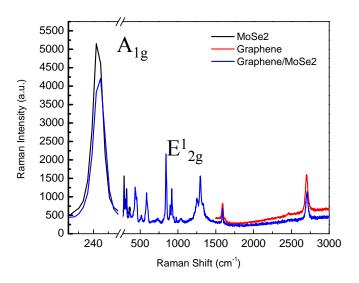


Supplementary Figure 18. A few eigenvalues are shown on the Model Coulomb

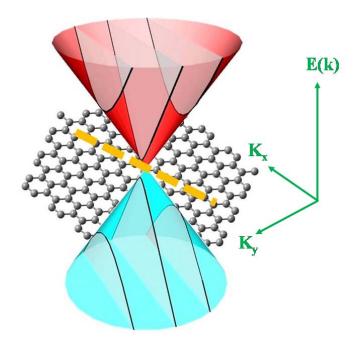
potential as a function of in-plane radius for an electron-hole pair across the graphene/MoSe₂ heterojunction van der Waals interface. (a) Hole is in graphene and electron is in the MoSe₂ monolayer. (b) Hole is in MoSe₂ and electron is in graphene. Wave functions of several states are also shown. (red/blue: positive/negative.)



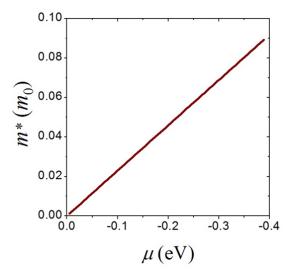
Supplementary Figure 19. A few eigenvalues are shown on the Model Coulomb potential as a function of in-plane radius for an electron-hole pair across the graphene/MoSe₂ heterojunction van der Waals interface. (a) Hole is in graphene and electron is in MoSe₂ monolayer. (b) Hole is in MoSe₂ slab and electron is in graphene. Several wave functions are also shown. (red/blue: positive/negative.) graphene_hole/MoSe₂_electron: $E_{1s-2p} = 0.273 \text{ eV}, \ \left\langle \rho_{CT_{1s}} \right\rangle = 46.4 \text{ Å}$ graphene_electron/MoSe₂_hole: $E_{1s-2p} = 0.274 \text{ eV}, \ \left\langle \rho_{CT_{1s}} \right\rangle = 45.4 \text{ Å}$



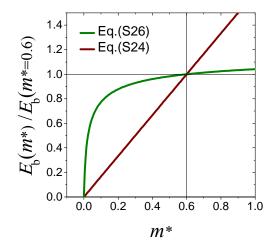
Supplementary Figure 20. Raman spectroscopy of graphene, $MoSe_2$ and graphene/ $MoSe_2$ vdW heterostructure. The frequencies of vibrational modes A_{Ig} (242 cm⁻¹) and E_{2g}^{-1} (288 cm⁻¹) of the standalone $MoSe_2$ sample and the heterostructures match previously reported data of monolayer $MoSe_2^{-26}$. The characteristic 2D (2690 cm⁻¹) and G (1580 cm⁻¹) peaks of single-layered graphene are present in both the graphene/ $MoSe_2$ heterostructures and the standalone graphene sample.



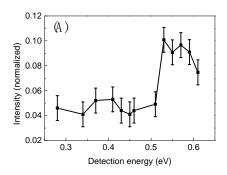
Supplementary Figure 21. Schematic illustration of the finite effective mass when **k** deviates away from the Dirac point of graphene. Some k-lines on the Dirac cones along a specified direction were shown as solid lines, which clearly have finite curvature (effective mass).

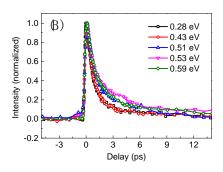


Supplementary Figure 22. The effective mass m^* (in units of m_0 , the mass of the free electron) at the level of chemical potential μ along the normal direction of Dirac cone



Supplementary Figure 23. The exciton binding energy as a function of the effective mass m^* (in units of m_0 , the mass of the free electron). The binding energy was measured with respective to that of $MoSe_2$ ($m^* = 0.6$). Supplementary Equation (26) and (28) were used in plotting the curves.

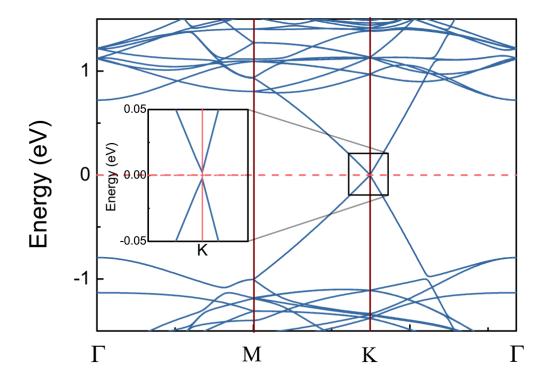




Supplementary Figure 24. (A) Detection frequency dependent (0.28-0.59 eV) photo responses of monolayer MoSe₂ at 10 ps (averaged between 8-12 ps to minimize noise) after excited with 400nm light. A resonance 1s-2p transition peak appears at 0.55 eV. The results indicate that the excitonic binding energy in monolayer MoSe₂ is about 0.6 eV. (B) Time dependent dynamics detected at different energy values. The transition between different dynamics starts at 0.51eV. The DFG midIR output from Topas OPA

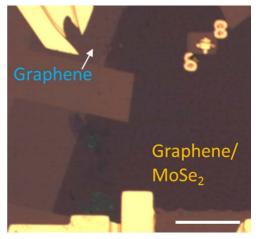
combined with HgCdTe detector was used for detection frequencies below 0.47eV. The Idler output of a Palitra OPA combined with an InSb detector was used for detection frequencies above 0.47 eV.



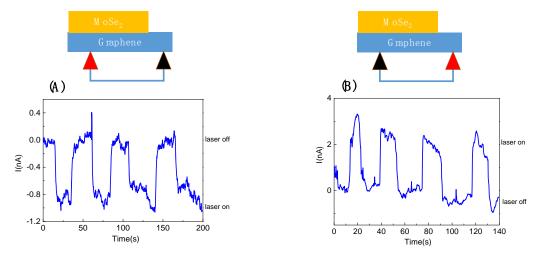


Supplementary Figure 25. *The band structure of a graphene/MoSe*₂ *heterostructure.*

The symmetry of graphene is broken, and its band structure is opened with a gap of \sim 4.4 meV (the insert). This generates a carrier mass around 0.0004 m₀. This phenomenon was also previously observed in calculations on a graphene/MoSe₂ heterostructure (JPCC, 115, 20237, 2011). However, the gap is significantly smaller than the thermal energy (26 meV) at room temperature, the effects it induced at room temperature under which our experiments were conducted are expected to be very small.



Supplementary Figure 26. MoSe₂/Graphene device used in the measurements, scale bar: 10 µm. MoSe₂/graphene vdW heterostructure device for photocurrent measurements. A monolayer of graphene (the lighter image in the center) is transferred on the top of A monolayer of MoSe₂ which is on a silicon wafer. Cr/Au (8nm/120nm) electrodes were deposited using E-beam lithography and lift-off technique. Both electrodes are on the top of graphene. One is on the top of graphene underneath which is Si (with a thin layer of SiO₂). The other electrode is on the top of graphene underneath which is MoSe₂.



Supplementary Figure 27. Photocurrent ($I_{ph}=I_{light}-I_{dark}$) of MoSe₂/Graphene vdW heterostructure under 980nm excitation. The photons only excite graphene but not MoSe₂. Top panel: measurement configurations (A) in which the external current flows from graphene on the top of MoSe₂ to graphene on the top of Si (with a thin layer of SiO₂), and (B) the external current direction is flipped. The background current is subtracted. Both results unambiguously demonstrate that the photoexcitation generates an overall electron flow from MoSe₂ to graphene inside the heterostructure. After photoexcitation, electrons move from MoSe₂ to graphene inside the heterostructure. Therefore, more electrons exist in the area of graphene directly on the top of MoSe₂ than in the area of graphene on the top of Si (with a thin layer of

 SiO_2). This results in external current flowing from graphene on the top of Si to graphene on the top of $MoSe_2$. The photocurrent measurements were conducted with a semiconductor parameter analyzer (Agilent 4155C) and a probe station. The source/drain bias $V_{sd}=0$ and the gate voltage $V_g=0$ in all tests. The two measurements were conducted under slightly different laser focus sizes.

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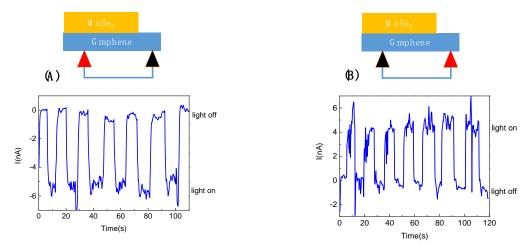
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Supplementary Figure 28. Photocurrent $(I_{ph}=I_{light}-I_{dark})$ of MoSe₂/Graphene vdW heterostructure under 405nm excitation. The photons excite both graphene and MoSe₂. Top panel: measurement configurations (A) in which the external current flows from graphene on the top of $MoSe_2$ to graphene on the top of Si (with a thin layer of SiO_2), and (B) the external current direction is flipped. The background current is subtracted. Both results unambiguously demonstrate that the photoexcitation generates an overall electron flow from MoSe₂ to graphene inside the heterostructure. After photoexcitation, electrons move from MoSe₂ to graphene inside the heterostructure. Therefore, more electrons exist in the area of graphene directly on the top of MoSe₂ than in the area of graphene on the top of Si (with a thin layer of SiO_2). This results in external current flowing from graphene on the top of Si to graphene on the top of MoSe₂. The photocurrent measurements were conducted with a semiconductor parameter analyzer (Agilent 4155C) and a probe station. The source/drain bias V_{sd} =0 and the gate voltage V_g =0 in all tests. Similar photocurrent phenomena was also observed in MoS₂/Graphene vdW heterostructures (ref: Scientific Reports 4, 3826 (2014)).

(1)

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Supplementary Note 1: Optical conductivity of graphene

291 The tight-binding Hamiltonian for the cone-like band structure of graphene is written as

$$H = \begin{bmatrix} 0 & \hbar v_{\mathrm{F}} (k_{x} + ik_{y}) \\ \hbar v_{\mathrm{F}} (k_{x} - ik_{y}) & 0 \end{bmatrix},$$

where v_F is the Fermi velocity, and k_x and k_y are 2D components of the electronic 294 295 wave vector **k**. With the Hamiltonian, the optical conductivity $[\sigma(\omega)]$ is written as the 296 sum of the interband conductivity $[\sigma_{inter}(\omega)]$ and the intraband conductivity $[\sigma_{inter}(\omega)]$ given below^{1, 2, 3, 4}: 297

$$\sigma(\omega) = \sigma_{\text{inter}}(\omega) + \sigma_{\text{intra}}(\omega)$$

$$\sigma_{\text{inter}}(\omega) = i \frac{e^{2} \hbar \omega}{\pi \hbar} \int_{0}^{+\infty} d\varepsilon \frac{1}{(2\varepsilon)^{2} - (\hbar \omega + i\Gamma)^{2}} [f_{\text{FD}}(\varepsilon - \mu) - f_{\text{FD}}(-\varepsilon - \mu)], \qquad (2)$$

$$\sigma_{\text{intra}}(\omega) = i \frac{e^{2} / \pi \hbar}{\hbar \omega + i \hbar / \tau_{e}} \int_{0}^{+\infty} d\varepsilon [f_{\text{FD}}(\varepsilon - \mu) + 1 - f_{\text{FD}}(-\varepsilon - \mu)]$$

299 where $f_{\rm FD}$ is the Fermi-Dirac distribution function, μ is the chemical potential (Fermi energy), and e is the elementary charge. Γ is the broadening of the interband 300 transitions, and τ_e is the relaxation time due to intraband carrier scattering. In 301 literature $^{5,\,6},~\Gamma$ lies between 0.01 and 0.06 eV while τ_e is in the range of 5 \sim 40 fs. 302 303 Here, considering that electronic motions typically occur within a few fs rather tens of fs, we use the fast values $\Gamma = 0.062 \text{ eV} (500 \text{ cm}^{-1})$ and $\tau_e = 10 \text{ fs throughout the study}$. 304 305 Nonetheless, effects of these two parameters are also tested and listed in Supplementary Figure 6. It turns out that the results are not very sensitive to the 306 307 parameter selections.

Applying the Fresnel equations, the change of optical transmission due to the

309 existence of graphene is given as

310
$$\frac{\Delta T_{\rm s}}{T_0} \approx -\frac{2}{\cos\theta + n_{\rm sub}\cos\theta''} \sqrt{\frac{\mu_0}{\varepsilon_0}} \operatorname{Re}[\sigma(\omega)]$$
 (3)

for s-polarized light. θ is the incident angle, and θ'' is the incident angle in the substrate. n_{sub} is the refractive index of the substrate. ε_0 and μ_0 are vacuum permittivity and permeability, respectively. For p-polarized light, the change of optical transmission is

315
$$\frac{\Delta T_{\rm p}}{T_0} \approx -\frac{2\cos\theta\cos\theta''}{n_{\rm sub}\cos\theta + \cos\theta''} \sqrt{\frac{\mu_0}{\varepsilon_0}} \operatorname{Re}[\sigma(\omega)]. \tag{4}$$

In our experiments, $\theta = 0^{\circ}$, so we have

317
$$\frac{\Delta T}{T_0} \approx -\frac{2}{1 + n_{\text{sub}}} \sqrt{\frac{\mu_0}{\varepsilon_0}} \operatorname{Re}[\sigma(\omega)], \qquad (5)$$

where $n_{\text{sub}} = 1.39$ for the used substrate (CaF₂).

Supplementary Note 2: Heat transfer between electrons and phonons in

graphene

Strongly coupled optical phonons (COPs) are in-plane optical phonons for which intra- and inter-valley carrier scattering can simultaneously conserve energy and momentum⁷. The considered SCOPs include phonons near the Γ -point with energy \sim 200 meV (for intra-valley carrier scattering) and those near the K-point with energy \sim 150 meV (for inter-valley carrier scattering). The interaction between phonons and electrons/holes in graphene is described by a deformation potential theory,^{8,9} and the transition matrix element is determined to be

$$M_{\mathbf{k}',\mathbf{k}}^{(\text{TO\&LO})} \approx 3\eta \sqrt{\frac{\hbar}{4M_C \omega_{\text{phonon}}}},$$
 (6)

where η is the electron-phonon coupling parameter, and $M_{\rm C}$ is the mass of a carbon atom. The energy dispersion of the transverse optical (TO) and longitudinal optical (LO) phonon modes is ignored, and Supplementary Equation (6) accounts for the total contribution from TO and LO at Γ - or K-points. Both emission and absorption of the phonons are considered under the second quantization. The probability of scattering from \mathbf{k} to \mathbf{k}' by the SCOPs is

$$W_{\mathbf{k}',\mathbf{k}}^{(\text{TO\&LO})} = \frac{2\pi}{\hbar} \left| M_{\mathbf{k}',\mathbf{k}}^{(\text{TO\&LO})} \right|^{2} \left[N_{\mathbf{q}} \delta \left(\varepsilon_{\mathbf{k}} - \varepsilon_{\mathbf{k}'} + \hbar \omega_{\text{phonon}} \right) + \left(N_{\mathbf{q}} + 1 \right) \delta \left(\varepsilon_{\mathbf{k}} - \varepsilon_{\mathbf{k}'} - \hbar \omega_{\text{phonon}} \right) \right]$$

$$= \frac{9\pi \eta^{2}}{2M_{C} \omega_{\text{phonon}}} \left[N_{\mathbf{q}} \delta \left(\varepsilon_{\mathbf{k}} - \varepsilon_{\mathbf{k}'} + \hbar \omega_{\text{phonon}} \right) + \left(N_{\mathbf{q}} + 1 \right) \delta \left(\varepsilon_{\mathbf{k}} - \varepsilon_{\mathbf{k}'} - \hbar \omega_{\text{phonon}} \right) \right]$$

$$337 (7)$$

where $N_{\bf q}$ is the phonon occupation number described by the Bose-Einstein distribution. The first and second terms in the square brackets correspond to the phonon emission and absorption processes, respectively. Integrating ${\bf k'}$ gives the scattering rate of ${\bf k}$ as

$$R_{\mathbf{k}\to^*} = \int W_{\mathbf{k}',\mathbf{k}}^{(\text{TO\&LO})} \frac{A}{(2\pi)^2} d^2 \mathbf{k'}$$

$$= \frac{9\eta^2}{2\hbar^2 \rho v_F^2 \omega_{\text{phonon}}} \left[\left(\varepsilon_{\mathbf{k}} + \hbar \omega_{\text{phonon}} \right) N_{\mathbf{q}} + \left(\varepsilon_{\mathbf{k}} - \hbar \omega_{\text{phonon}} \right) \left(N_{\mathbf{q}} + 1 \right) \right]^{\prime}$$
(8)

where ρ is the 2D mass density of graphene. Therefore, the rate of phonon emission

344 per unit area is

$$\frac{dN_{\text{emission}}}{dt} = \int \frac{9\eta^{2}}{2\hbar^{2}\rho v_{F}^{2}\omega_{\text{phonon}}} \left(\varepsilon_{\mathbf{k}} - \hbar\omega_{\text{phonon}}\right) \left(N_{\mathbf{q}} + 1\right) f_{\text{FD}}\left(\varepsilon_{\mathbf{k}}\right) \left(1 - f_{\text{FD}}\left(\varepsilon_{\mathbf{k}} - \hbar\omega_{\text{phonon}}\right)\right) \frac{1}{\left(2\pi\right)^{2}} d^{2}\mathbf{k}$$

$$= \frac{9\eta^{2}}{4\pi(\hbar v_{F})^{4}\rho\omega_{\text{phonon}}} \left(N_{\mathbf{q}} + 1\right) \int \varepsilon_{\mathbf{k}} \left(\varepsilon_{\mathbf{k}} - \hbar\omega_{\text{phonon}}\right) f_{\text{FD}}\left(\varepsilon_{\mathbf{k}}\right) \left(1 - f_{\text{FD}}\left(\varepsilon_{\mathbf{k}} - \hbar\omega_{\text{phonon}}\right)\right) d\varepsilon_{\mathbf{k}}$$

and the rate of phonon absorption is

$$\frac{dN_{\rm adsorption}}{dt} = \frac{9\eta^2}{4\pi(\hbar v_{\rm F})^4 \rho \omega_{\rm phonon}} N_{\rm q} \int \varepsilon_{\bf k} (\varepsilon_{\bf k} + \hbar \omega_{\rm phonon}) f_{\rm FD}(\varepsilon_{\bf k}) (1 - f_{\rm FD}(\varepsilon_{\bf k} + \hbar \omega_{\rm phonon})) d\varepsilon_{\bf k} ,$$

which are used to simulate the heat transfer between electrons/holes and SCOPs.

The heat capacity of the SCOPs is described by the Einstein model, and the fraction of Brillouin zone filled by the SCOPs, f_{SCOPs} , is assumed to be temperature independent for simplicity⁴. The energy stored in the SCOP subsystem relaxes at a rate of $1/\tau_{\text{ph}}$ to lower energy phonons^{4, 10}. The value of f_{SCOPs} and τ_{ph} are determined by fitting the experimental probe signal profiles.

Supplementary Note 3: Fermi level of graphene in heterostructure

Graphene used in our experiments are p-doped with Fermi level -0.19 eV determined by fitting the transient spectra and dynamics in Supplementary Figure 1 and Supplementary Figure 3E. MoSe₂ is n-doped. When the two monolayers were placed together to form a heterostructure, some electrons transfer from MoSe₂ to graphene¹¹, raising the graphene Fermi level to -0.17 eV. The Fermi level of graphene in heterostructure is obtained by fitting the transient IR spectrum of heterostructure at time 0 with 1.03 eV excitation (Supplementary Figure 2). The carrier density of graphene is

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$$n = \int \frac{1}{(2\pi)^2} f(\varepsilon - \mu) d^2 \mathbf{k} = \int \frac{k}{2\pi} f(\varepsilon - \mu) dk = \int_0^{+\infty} \frac{\varepsilon}{2\pi (\hbar v_F)^2} f(\varepsilon - \mu) d\varepsilon, \quad (11)$$

When $|\mu| >> k_B T$, Supplementary Equation 11 can be simplified into (degenerate spin and KK'):

$$n \approx \frac{\mu^2}{\pi (\hbar v_{\rm F})^2} \,. \tag{12}$$

According to Supplementary Equation 11&12, the Fermi level increase indicates that about $5 \times 10^{11} \frac{e}{cm^2}$ have transferred from MoSe₂ to graphene after they form a heterostructure.

Supplementary Note 4: Calculated IR response of graphene with Fermi level

-0.17 eV

In the heterostructure excited with 1.03 eV photons, the initial response is only from graphene. Because of fast interlayer charge transfers, some excited carriers move to MoSe₂ very rapidly (< 50 fs) and effectively reduce the electronic temperature in the graphene layer. In our calculations, we consider this problem equivalent to the reduction of excitation flux because the charge transfer and electronic thermalization are extremely fast (< 50 fs), much faster than the exciton formation and electron/phonon couplings. Under ideal fast equilibrium, at most 50% of the excitation energy is transferred to MoSe₂ by the transferred carriers. However, in our experiments, this is obviously not likely because very few electrons can reach CBM of MoSe₂. Therefore, we set the upper limit of flux reduction as 1/3. Calculation results for the exciton formation time with no flux reduction to 1/3 reduction are all within experimental uncertainty.

Supplementary Note 5: Excitonic signal from direct experimental data subtraction

The excitonic signal presented in Supplementary Figure 3F is obtained by considering pump flux and Fermi level changes. Since these two parameters don't change significantly, we also directly subtract the signal of monolayer graphene from that of heterostructure (both presented in Supplementary Figure 3E) to obtain the excitonic signal. Kinetic analyses on the result by this method are plotted in Supplementary Figure 4. The results from this method and that from the more accurate method in Supplementary Figure 3F turn out to be essentially the same.

Supplementary Note 6: Larger flux results in slower graphene signal decay

MoSe₂ absorbs 14% and graphene absorbs 4.14% of 3.1 eV photons. Under ideal fast equilibrium, ~9% of excitation photons would be in either layer of the heterostructure. However, because the graphene Fermi level is between MoSe₂ VBM and CBM, more carriers are expected to flow into graphene. From photoluminescence, we can see that around 15% of free carriers that are originally excited in MoSe₂ remain in MoSe₂. Estimated from the results with 1.03 eV photons, about 33% free carriers form interlayer excitons. These two portions together account for 6% of the 18.14% total absorption. Therefore, the excitation flux the graphene layer gains from interlayer charge transfers must not exceed 12.5% (300% of 4.14%) besides direct absorption. The charge transfers results in higher electronic temperature and slower dynamics in graphene.

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Supplementary Note 7: MoSe₂ bandgap

According to STM measurements¹², the bandgap of MoSe₂ monolayer samples 413 on different substrates varies. On graphite, it is 1.94 eV, whereas on bilayer graphene 414 415 it is 2.18 eV. The PL peak central frequency also varies from 1.67 eV to 1.63 eV at 416 77K. The determined binding energy is 0.55 eV, slightly higher than the theoretical value 0.47 eV¹³. The PL central frequency of our sample at room temperature is 1.56 417 eV (on graphene). 1.56 + 0.47 = 2.03 eV. Considering all results from literature and 418 our own experiments, we adopt around 2.0 eV as the bandgap of MoSe₂ in the 419 420 heterostructures measured in our experiments.

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- Supplementary Note 8: Ratio of electron/hole transferred from graphene to
- 423 $MoSe_2$
- The population of electrons in graphene that have higher energy than the CBM
- value of MoSe₂ and thus are capable of interlayer transferring is calculated as

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$$n_e(T; E_{\text{CBM}}) = \int_{E_{\text{CBM}}}^{+\infty} \frac{\varepsilon}{2\pi (\hbar v_{\text{E}})^2} f(\varepsilon - \mu) d\varepsilon$$
 (13)

Similarly, the population of holes being capable of interlayer transferring is

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$$n_h(T; E_{\text{VBM}}) = \int_{-\infty}^{E_{\text{VBM}}} \frac{\varepsilon}{2\pi(\hbar v_{\text{E}})^2} f(-\varepsilon + \mu) d\varepsilon$$
. (14)

- By subtracting the populations before pumping ($T_0=300$ K), the ratio of n_b/n_e
- determined is plotted in Supplementary Figure 7. With 100% flux of 1200nm
- excitation, the electronic temperature reaches 1583K. At this temperature, n_h/n_e is 4.9.

With 2/3 flux, the electronic temperature reaches 1399 K and n_h/n_e is 5.8. Because charge transfers result in a lower temperature, the exact n_b/n_e should lie between these two values. Interlayer charge transfers and electronic thermalization in graphene are extremely fast (<50 fs) 4, 14, 15. Thus, they can be treated as semi-instantaneous, compared to the electron/hole recombination (100~200 fs) in graphene and the formation of interlayer excitons (~500 fs). Therefore, the transfer of photo-excited charge carriers between two layers forms a quasi-equilibrium in which the electron/hole population ratio in MoSe₂ is approximately equal to that in graphene. Once the charge carriers form interlayer excitons, the interlayer quasi-equilibrium is perturbed and more carriers are transferred to MoSe₂ as the charge carriers in graphene are continuously adjusting their population distributions. This process makes sure that even though the hole population in graphene below the VBM of MoSe₂ is only a small portion of the total number photo-generated, the total number of transferred holes is still substantial. The process results in that the majority of interlayer excitons have their holes in the MoSe₂ layer and electrons in graphene. The estimated exciton density is about $0.45 \times 10^{12} \text{ cm}^{-2}$ and $0.58 \times 10^{12} \text{ cm}^{-2}$ under the excitation photon energy 1.03 eV and 3.1 eV, respectively. Another possible mechanism can also lead to that electrons stay in graphene and holes prefer MoSe₂. According to literature¹¹, charged impurities in MoSe₂ and graphene can produce an effective electric field that is from graphene to MoSe₂. Such an electric field can provide driving force for holes to move to MoSe₂ and for electrons to go to graphene.

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Supplementary Note 9: Kinetic analysis

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To analyze the electron/hole gas transformation dynamics, we create a kinetic model. In the model, interlayer charge transfers and electronic thermalization in graphene are assumed to be semi-instantaneous. Free carriers (y) in graphene decay with a total rate constant k_3 . The interlayer exciton (x) formation rate constant is k_1 and the exciton decay rate constant is k_2 . The model can be expressed as

$$\begin{array}{ccc}
 & y \xrightarrow{k_3} & & \\
 & y \xrightarrow{k_1} & x \xrightarrow{k_2} & & \\
\end{array} (15)$$

The solution of the kinetic model is

$$\frac{dx}{dt} = k_1[y] - k_2[x]$$

$$\frac{dy}{dt} = -k_3[y] , \qquad (16)$$

$$x(t) = \frac{k_1}{k_3 - k_2} (1 - e^{-(k_3 - k_2)t}) e^{-k_2 t}$$

- where k_3 is obtained from the electronic decay of graphene. k_1 and k_2 are obtained from fitting the experimental excitonic signal.
- 465 In Supplementary Figure 3F, $1/k_1 = 364 fs$, $1/k_2 = 65 ps$, $1/k_2 = 120 fs$.
- 466 In Supplementary Figure 4F, $1/k_1 = 379 fs$, $1/k_2 = 55 ps$, $1/k_2 = 170 fs$.
 - The binding energy of MoSe₂ intralayer exciton is >0.4 eV, which exceeds the photon energy of our IR probe. In addition, the optical response of free carriers in MoSe₂ is only 1/6 of the free carries in graphene. Therefore, in the kinetic model the contribution from free carriers in MoSe₂ is ignored. The response ratio 1/6 is calculated based on experimental results: with the same 3.1 eV excitation, 14% photons are absorbed by MoSe₂, producing a signal size of -0.006, whereas 4.14%

- 473 photons are absorbed by graphene producing a signal size of -0.011.
- 474 $0.011/0.006*14\%/4.14\% \sim 6$.

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476 Supplementary Note 10: Exciton and free carrier optical responses

The free carrier optical conductivity from the Drude model¹⁶ is

$$\sigma_{free} = \frac{ne^2\tau}{\mu(\omega^2\tau^2 + 1)} = \frac{n\hbar e^2\Gamma_D}{\mu[(\hbar\omega)^2 + \Gamma_D^2]},$$
(17)

- where n is the carrier population, μ is the reduced mass and $\Gamma_{\scriptscriptstyle D}$ is the scattering
- 480 (dephasing) line width. The 1s-2p transition optical conductivity¹⁷ is

$$\sigma_{1s-2p} = \frac{n_X \hbar e^2 \Gamma_{1s-2p} \cdot (\hbar \omega)^2 f_{1s-2p}}{\mu \left[((\hbar \omega)^2 - E_{res}^2)^2 + (\hbar \omega \Gamma_{1s-2p})^2 \right]},$$
(18)

- 482 where E_{res} is the resonant energy. The optical conductivity ratio between the 1s-2p
- 483 transition and free carrier is therefore:

$$\frac{\sigma_{\text{ls-2p}}}{\sigma_{\text{e-h}}} \approx \frac{2n_X f_{\text{ls-2p}}}{\Gamma_{\text{ls-2p}}} / \frac{n_{\text{e-h}} \Gamma_D}{(\hbar \omega)^2} \approx \frac{2f_{\text{ls-2p}}(\hbar \omega)^2}{\Gamma_D \Gamma_{\text{ls-2p}}},$$
(19)

485 where f_{1s-2p} is the oscillator strength that can be calculated in the following ¹⁸:

$$f_{1s-n} = \frac{2\mu a^2}{\hbar^2} (E_n - E_0) \frac{\left(n + \frac{1}{2}\right)^5 n^{2s-3}}{(n+1)^{2s+5}}$$

$$= \frac{2\mu a^2}{\hbar^2} \cdot \frac{e^2 \lambda}{8\pi \varepsilon_0 \varepsilon_A} \left[\frac{1}{(1/2)^2} - \frac{1}{(n+1/2)^2} \right] \frac{\left(n + \frac{1}{2}\right)^5 n^{2s-3}}{(n+1)^{2s+5}}$$

$$= \frac{\mu e^2 \lambda a}{4\pi \varepsilon_0 \varepsilon_A \hbar^2} \left[\frac{1}{(1/2)^2} - \frac{1}{(n+1/2)^2} \right] \frac{\left(n + \frac{1}{2}\right)^5 n^{2s-3}}{(n+1)^{2s+5}}$$

$$= \frac{\mu e^2 \lambda}{4\pi \varepsilon_0 \varepsilon_A \hbar^2} \cdot \frac{4\pi \hbar^2 \varepsilon_0 \varepsilon_r}{e^2 \mu \lambda} \left[\frac{1}{(1/2)^2} - \frac{1}{(n+1/2)^2} \right] \frac{\left(n + \frac{1}{2}\right)^5 n^{2s-3}}{(n+1)^{2s+5}}$$

$$= \left[\frac{1}{(1/2)^2} - \frac{1}{(n+1/2)^2} \right] \frac{\left(n + \frac{1}{2}\right)^5 n^{2s-3}}{(n+1)^{2s+5}}$$

$$= \left[\frac{1}{(1/2)^2} - \frac{1}{(n+1/2)^2} \right] \frac{\left(n + \frac{1}{2}\right)^5 n^{2s-3}}{(n+1)^{2s+5}}$$

$$= \left[\frac{1}{(1/2)^2} - \frac{1}{(n+1/2)^2} \right] \frac{\left(n + \frac{1}{2}\right)^5 n^{2s-3}}{(n+1)^{2s+5}}$$

$$= \frac{1}{(1/2)^2} - \frac{1}{(n+1/2)^2} \frac{1}{(n$$

Based on Supplementary Equation 18, $f_{1s-2p} = 0.21$, slightly different from the

value 0.32 derived from a non-hydrogen model¹⁷. Γ_{1s-2p} is experimentally determined

to be 280 cm⁻¹. Using the ratio $\Gamma_D / \Gamma_{1s-2p} = 6$ adopted in literature¹⁸, $\frac{\sigma_{1s-2p}}{\sigma_{nb}}$ is 489 calculated to be 3.6. However, $\frac{\sigma_{\text{ls-2p}}}{\sigma_{\text{\tiny e.h}}}$ calculated here is for exciton and free carrier in 490 the same material. In our experiments, the interlayer exciton is within two very 491 different materials of which the free carrier response ratio is $1/6 = MoSe_2/graphene$. It 492 is reasonable to expect that σ_{1s-2p} of the MoSe₂/graphene interlayer exciton is 1~3.5 493 494 times (it doesn't go to 6 because the 1s-2p transition is a bound-bound transition and graphene cannot affect it in a way like free carriers) of $\sigma_{\text{1s-2p}}$ of MoSe₂, giving 495 $\frac{\sigma_{\text{1s-2p-interlayer}}}{\sigma_{\text{1s-2p-interlayer}}} = 0.6 \sim 2.1$. Normalized with the ratio, the excitonic formation time 496 497 constants obtained from fitting the experimental results in Supplementary Figure 3F&4F are 218 fs~764 fs (Supplementary Figure 3F) and 227 fs~796 fs 498 (Supplementary Figure 4F), respectively. 499

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Supplementary Note 11: Exciton 1s-2p transition energy calculations

Methods:

First-principle calculations in this work are conducted using DFT methods implemented in the Vienna *ab initio* simulation package (VASP)¹⁹. The projector-augmented-wave (PAW) pseudopotentials and the generalized gradient approximation of Perdew, Burke, and Ernzerhof (PBE) for exchange-correlation functional are adopted in our simulations²⁰. In order to study the influence of Fermi level on the electronic properties for hole-doped graphene system, we conducted the first-principle investigation on the electronic band structures of graphene sheets

(N×N×1 primitive unit cell) doped by the Boron atoms (which can effectively modulate the position of Fermi level but minimally alter other physical properties of graphene). For Brillouin zone (BZ) integrations, a Monkhorst-Pack k-point mesh scheme with $7 \times 7 \times 1$ are adopted²¹. Meanwhile, for graphene and monolayer MoSe₂ system, we use a 9×9×1 k-meshes for Brillouin zone sampling in the Monkhorst-Pack scheme. In order to simulate the graphene/MoSe₂ 2D heterostructures, we imposes a commensurability condition between them, where a 4×4 supercell of the graphene is used to match a 3×3 supercell of the MoSe₂ monolayer. The lateral lattice parameter for the triangular lattice of graphene/MoSe₂ nanocomposite is set to be $a(graphene/MoSe_2) = (4*a(graphene)+3*a(MoSe_2)) =$ 9.912 Å, in which a(graphene) = 2.468 Å and a(MoSe₂)=3.317 Å are optimized for isolated graphene and monolayer MoSe₂, respectively. Since there is only a very small lattice mismatch of ~0.4% between the graphene and the MoSe₂ monolayers, the approximation used here is reasonable. Boron-doped graphene/MoSe₂ nanocomposite in which one random carbon atom is replaced with a boron atom is also used to study the influence of doping on the thickness of graphene/MoSe₂ heterojunction (along z direction). Since the heterostructure contains one graphene and one MoSe₂ monolayer, van der Waals (vdW) interactions are taken into account by using the semi-empirical DFT-D3 method²². For the pristine as well as the boron-doped graphene/MoSe₂ heterojunction, a 5×5×1 Monkhorst-Pack k-point mesh is used. A cutoff of 500 eV is used for the plane-wave expansion of the wave function to converge the relevant quantities. The structure relaxations are carried out until all the atomic forces on each

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ion are less than 0.01~eV/Å, enforcing a total energy convergence of $1\times10^{-7}~\text{eV}$. To avoid spurious interactions with replicas, a vacuum slab larger than 15 Å is added in the z direction for all system.

Results:

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monolayer MoSe2, respectively.

As demonstrated in Supplementary Figure 8, the Fermi energy levels are adjusted, by boron doping, to the valence bands and the whole doping system acts as a p-dopant. Supplementary Figure 9(a) shows the Fermi energy levels of the doped graphene with different N×N primitive cells. With the decrease of dopant concentration, the Fermi energy level gradually decreases to the experimental value. As the Fermi energy level of boron-doped graphene reaches the experimental value (-0.17eV), the primitive cell size is 26.1×26.1, and the calculated effective mass of B-doped system for electron and hole is 0.0116 and 0.0121, respectively. (Supplementary Figure 9(a)) The optimized thickness between the two layers (C atom - Mo atom) of Boron-doped graphene/MoSe2 heterojunction is 5.178Å, which is very close to the value of undoped heterojunction (5.183Å), thereby low concentration of boron doping does not alter the thickness between the two layers significantly. Furthermore, the in-plane dielectric constant of B-doped graphene is almost equal to the value of pristine graphene when the primitive cell size is larger than 8×8. We set the dielectric constant of graphene/MoSe2 heterojunction as $\bar{\epsilon} = 4.969$, which is the average value of the calculated in-plane dielectric constant $\varepsilon xx = 3.651$ and 6.287 for graphene and

To obtain the potential experienced by an electron at (ρ, z) due to the presence of

a hole at (0, z0), we use a field method described by Smythe23 and extended by Sritharan13:

$$V(\rho) =$$

$$558 \quad \frac{(K_2 - K_1)/(K_2 + K_1)}{\sqrt{(z + z_0 - 2a + 2nc)^2 + \rho^2}} + \frac{(K_2 - K_3)/(K_2 + K_3)}{\sqrt{(2b - z - z_0 + 2nc)^2 + \rho^2}} \right\},\tag{21}$$

- where $\beta_P = (\bar{\varepsilon} + 1)^2$ and $\beta_N = (\bar{\varepsilon} 1)^2$, K1=K3=1 since the graphene/MoSe2
- 560 heterojunction is approximated as a single dielectric slab sandwiched between
- vacuum. When the electron and hole are at different layers, they are assumed to be at
- the center of the graphene and MoSe2 monolayer along the z direction with a fixed
- distance of 5.183Å which is the thickness of heterojunction. The exciton is then
- simplified as a two dimensional quasi-particle 24.
- When the hole is in graphene and the electron is in the MoSe2 layer, the effective mass of exciton can be obtained from $\frac{1}{\mu} = \frac{1}{m_h^*} + \frac{1}{m_e^*}$, where the effective mass of monolayer MoSe2 conduction band $m_e^* = 0.502m_0$ (Supplementary Figure 10) and the effective mass of B-doped graphene valence band $m_h^* = 0.0121m_0$, m_0 is the
- free electron mass. Based on the finite element method, we then solved the
- Schrödinger equation on a 2×103 Å circle plane, with the effective mass of the
- excitonic quasi particle and aforementioned Coulomb potential. The eigenvalues and
- selected eigenfunctions calculated are presented in Supplementary Figure 11a. The
- exciton transition energy between 1s and 2p is E1s-2p= 0.274 eV, and the means
- radius of wave functions for 1s CT is $\langle \rho_{CT_{1s}} \rangle = 45.3$ Å. The 1s-1p transition energy is
- also larger than 0.20 eV. Both 1s-1p and 1s-2p transition energy values are close to the

experimental value 0.27 eV.

When electron is in graphene and hole is in MoSe2, the hole and electron effective masses should be the effective masses of the monolayer MoSe2 valence band $(0.583 \, m_0)$ and B-doped graphene conduction band $(0.0116 \, m_0)$, respectively. The eigenvalues and selected eigenfunctions are presented in Supplementary Figure 11b. The exciton transition energy between 1s and 2p is E1s-2p= 0.267 eV, and the means radius of wave functions for 1s CT is $\langle \rho_{CT_{1s}} \rangle = 46.6 \, \text{Å}$. There is a 0.007eV difference between the binding energies in two conditions. In our experiments, the difference is too small to distinguish.

Note that the energies are calculated for the Fermi level of -0.17 eV, for Fermi level of -0.19 eV, the calculated values are provided at the end of this summery.

In principle, the exciton 1s-2p transition energy can be estimated by performing the quasiparticle GW and Bethe-Salpeter equation (BSE) calculations. To model the experimental condition herein for the boron doped graphene/MoSe2 heterojunction, however, the system constructed should contain more than 1200 atoms (the supercell of graphene should larger than 26×26). On the other hand, to achieve well-converged quasiparticle energies, especially when there is transition metal element (Mo) in the system, a dense enough (21×21×1) k-gird, a large energy cutoff (~40Ry) and a large number (>10000) of unoccupied states is needed12, 25. The calculation cost is therefore far beyond computing resource we can afford.

Supplementary Note 12: Al-doped Graphene

To explore the possible effect of dopant rather than Fermi level on the binding energy, we also compute the interlayer exciton binding energy with Al-doped graphene.

As demonstrated in *Supplementary Figure 15*, the Fermi energy levels are adjusted, by aluminum doping, to the valence bands and the whole doping system also acts as a p-dopant. *Supplementary Figure 15* shows the Fermi energy levels of the doped graphene with different N×N primitive cells. With the decrease of dopant concentration, the Fermi energy level gradually decreases to the experimental value. As the Fermi energy level of aluminum-doped graphene reaches the experimental value (-0.17eV), the primitive cell size is 13×13 (Supplementary Figure 16), and the calculated effective mass of Al-doped system for electron and hole is 0.0122 and 0.0135, respectively. (Supplementary Figure 17)

When the hole is in graphene and the electron is in the MoSe₂ layer, the effective mass of exciton can be obtained from $1/(\mu) = 1/(m_h^*) + 1/(m_e^*)$, where the effective mass of monolayer MoSe₂ conduction band $m_e^* = 0.502m_0$ (Supplementary Figure 18) and the effective mass of Al-doped graphene valence band $m_h^* = 0.0122m_0$. m_0 is the free electron mass. Based on the finite element method, we then solved the Schrödinger equation on a 2×10^3 Å circle plane, with the effective mass of the excitonic quasi particle and aforementioned Coulomb potential. The eigenvalues and selected eigenfunctions calculated are presented in Supplementary Figure 18A. The exciton transition energy between 1s and 2p is $E_{Is-2p}=0.275$ eV, and the means radius of wave functions for 1s CT is $\langle \rho_{CT_{1S}} \rangle = 45.7 \text{Å}$.

When electron is in graphene and hole is in MoSe₂, the hole and electron effective masses should be the effective masses of the monolayer MoSe₂ valence band 0.583 m_0 and Al-doped graphene conduction band 0.0135 m_0 , respectively. The eigenvalues and selected eigenfunctions are presented in Supplementary Figure 18b. The exciton transition energy between 1s and 2p is E_{Is-2p} = 0.292 eV, and the means radius of wave functions for 1s CT is $\langle \rho_{CT_{1s}} \rangle$ = 42.3Å.

Supplementary Note 13: Both electron and hole effective masses of graphene are

$0.012m_{0}$

Using 0.012m₀ reported for a CVD-grown graphene (JAP, 113, 043708, 2013), we also calculate the interlayer binding energy.

In summary, the binding energy is only slightly affected by the nature of dopant. In three different calculations, the binding energy is between 0.265~0.292 eV. All are very close to the experimental value.

Supplementary Note 14: Origin of carrier reduced mass in graphene and large

636 interlayer binding energy

It is well known that the effective mass of the pristine graphene is zero, i.e., the effect mass of the state at $\mathbf{k} = 0$ (Dirac point, at which the Fermi level lie in the pristine graphene) is zero. However, when the \mathbf{k} point deviates from the Dirac point, e.g., the Fermi level shifts due to the effect of doping, the effective mass is no longer zero. We can approximately evaluate this effect based on a tight-binding (TB) model.

Under a TB approach, the energy dispersion of graphene near the Fermi points is expressed as Dirac cones:

$$E(\mathbf{k}) = \frac{3}{2} t_0 a_0 |\mathbf{k}|, \tag{22}$$

where $a_0 = 2.42$ Å is the equilibrium C-C bond length, and $t_0 \approx 2.7$ eV is the hopping energy between the nearest C atoms. The effective mass at **k** is defined as

$$m^*(\mathbf{k}) = \frac{\hbar^2}{\frac{\partial^2 E(\mathbf{k})}{\partial \mathbf{k}^2}}.$$
 (23)

When $\mathbf{k} \neq 0$, the energy dispersion along the normal direction has a finite curvature (effective mass) as shown as the solid lines in Supplementary Figure 21. Based on Supplementary Equation (22) and (23), the effective mass of electrons at the Fermi level (chemical potential μ) along the normal direction is given as

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$$m^* \Big|_{E(\mathbf{k})=\mu} = \frac{4\hbar^2}{9t_0^2 a_0^2} |\mu|. \tag{24}$$

The dependence of the effective mass on the chemical potential is plotted in Supplementary Figure 22. It can be seen that $m^* = 0$ for pristine graphene ($\mu = 0$), but it linearly increases with increasing $|\mu|$. For $\mu = -0.17$ eV, $m^* \approx 0.039m_0$. If we roughly regard the effective mass along the radical direction as unchanged (equal to 0 as that in pristine graphene), a direct average on both the normal and radical directions give $m^* \approx 0.02m_0$ under $\mu = -0.17$ eV. This estimated value is actually very close to $m^* \approx 0.0116m_0$ from the ab initio calculations assuming B-doped.

In 3D systems, the electric potential of a point charge under the screening of a dielectric surrounding with a relative dielectric constant ε is described by a screened Coulomb potential (in atomic units)

$$V_{3D}(\mathbf{r}) = \frac{1}{\varepsilon r}$$
 (25)

- by solving the Poisson's equation, which gives the exciton binding energy of the
- 665 hydrogen-like model:

$$E_{\rm b,3D}(\mathbf{r}) = \frac{m^*}{2\varepsilon^2},\tag{26}$$

- where m^* is the reduced effective mass. Supplementary Equation (26) suggests that E_b
- 668 is proportional to m^* .
- However, for a 2D dielectric sheet embedded into vacuum such as single-layer
- 670 MoSe₂ or other 2D systems considered in experiments, the 2D screened potential is
- not given as a screened Coulomb potential:

$$V_{\rm 2D}(\mathbf{r}) \neq \frac{1}{\varepsilon r},\tag{27}$$

- but is given as a complicated function in terms of the Struve function and the second
- kind Bessel function [refer to: P. Cudazzo, I. V. Tokatly, and A. Rubio, *Phys. Rev. B* 84,
- 675 085406 (2011)], which was also listed as Supplementary Equation (19). As a result,
- the binding energy of 2D exciton is not described by Supplementary Equation (26),
- but is given as [refer to: T. Olsen, S. Latini, F. Rasmussen, and K. S. Thygesen, *Phys.*
- 678 Rev. Lett. **116**, 056401 (2016)]

$$E_{\rm b,2D} = \frac{8m^*}{\left(1 + \sqrt{1 + \frac{32\pi\alpha m^*}{3}}\right)^2},\tag{28}$$

- where α is the 2D polarizability calculated as $\alpha = L \frac{\varepsilon 1}{4\pi}$ where ε is the dielectric
- constant of bulks and L is the thickness of the 2D sheet. A remarkable property in
- Supplementary Equation (28) is that E_b is no longer linearly proportional to m^* . When

 αm^* is large enough, we have $E_{\rm b,2D} \approx \frac{3}{4\pi\alpha}$ which is independent on m^* . Supplementary Equation 26 is applicable to both undoped and doped 2D systems. An exciton is formed between an electron and a hole no matter whether the system is doped or undoped, and the influence of doping just lies in its screening effect. As the Fermi energy level of boron-doped graphene reaches the experimental value (-0.17) eV), the primitive cell size is 26.1 (refer to page 17 of SI), and the doping ratio is actually small (less than 0.2%). Our ab initio calculation shows that the in-plane dielectric constant of B-doped graphene is almost equal to the value of pristine graphene when the primitive cell size is larger than 8 (refer to page 19 of SI). Therefore, the screening effect in doped graphene is very weak. Take the graphene-MoSe₂ as an example, $\bar{\varepsilon} \approx 4.97$ and L ≈ 10.4 Å, so we have α = 6.17 (in atomic units). E_b is plotted in Supplementary Figure 23 as a function of m^* based on Supplementary Equation (28), measured with respective to that of $m^* = 0.6$ (the value for MoSe₂). The result of Supplementary Equation (26) is also plotted to provide a comparison. It can be seen that the dependence of $E_{\rm b}$ on m^* is highly nonlinear for the 2D result in Supplementary Equation (28). For $m^* = 0.01m_0$, the 3D result in Supplementary Equation (26) gives $E_b(m^* = 0.01)/E_b(m^* = 0.6) = 1/60$, i.e., the binding energy for $m^* = 0.01$ of graphene-MoSe₂ is 60 times smaller compared to that of MoSe₂ as indicated by the reviewer, but the 2D result in Supplementary Equation (28) gives $E_b(m^*=0.01)/E_b(m^*=0.6) \approx 1/3.1$. In other words, with the 2D equation, the binding energy for $m^* = 0.01$ of graphene-MoSe₂ is merely 3.1 times smaller compared to that of MoSe₂. Taking the 0.4-0.6 eV binding energy for the latter,

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one may expect a binding enery of 0.13-0.19 eV for the graphene-MoSe₂ exciton, which is close to the results from our measurements. In our work, we used a more sophisticated theory that has been tested with other 2D systems (JACS 2015, 137, 8313-8320; Nat. Commun. 2016, 7, 12512) to calculate the binding energy and it turns out to be very close to the experimental value. The dependence of calculated 1s-2p transition energy on reduced mass is plotted in Supplementary Figure 12.

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