

## Supplementary

Table S1: Patient summary of sex, age, BW, and BMI. For further patient characteristics see Ranjan *et al.* [25].

| Patient | Sex | Age<br>[Years] | BW<br>[kg] | BMI<br>[kg/m <sup>2</sup> ] |
|---------|-----|----------------|------------|-----------------------------|
| 1       | F   | 52             | 54         | 22.8                        |
| 2       | F   | 64             | 50         | 20.0                        |
| 3       | M   | 48             | 81         | 24.5                        |
| 4       | F   | 31             | 69         | 24.2                        |
| 5       | M   | 35             | 87         | 25.4                        |
| 6       | M   | 58             | 72         | 23.8                        |
| 7       | F   | 19             | 73         | 25.3                        |
| 8       | F   | 45             | 59         | 20.9                        |

Table S2: Prior distributions of insulin PK and glucose PD model parameters with mean, 95% CI, and references.

| Parameter  | Mean<br>(95% CI) | Distribution                                  | Reference   |
|------------|------------------|---|---|
| $t_{max}$  | 51 (32-70)       | $t_{max} \sim \mathcal{N}(51, 9.5)$           | SD changed from 19 [28] due to<br>PK reported in [34]                               |
| $Cl_{F,I}$ | 18.9 (14.0-25.5) | $\log(Cl_{F,I}) \sim \mathcal{N}(2.94, 0.15)$ | [28]  |
| $E_{max}$  | 60 (30-90)       | $E_{max} \sim \mathcal{N}(60, 15)$            | Derived from [22]   |
| $C_{E50}$  | 338 (168-508)    | $C_{E50} \sim \mathcal{N}(338, 85)$           | Derived from [22]   |
| $F_{01}$   | 15.7 (11.4-20.0) | $F_{01} \sim \mathcal{N}(15.7, 2.1)$          | Mean changed from 9.7 [29] due<br>to explicit inclusion of $G_{GNG}$ in<br>PD model |

|                    |                |   |      |
|--------------------|----------------|---|------|
| $k_{12} * 10^{-4}$ | 595 (236-1502) | $\log(k_{12}) \sim \mathcal{N}(-2.8, 0.46)$ | [29] |
| $k_{a1} * 10^{-4}$ | 34 (3.6-316)   | $\log(k_{a1}) \sim \mathcal{N}(-5.7, 1.1)$  | [29] |
| $k_{a2} * 10^{-4}$ | 555 (137-2252) | $\log(k_{a2}) \sim \mathcal{N}(-2.9, 0.70)$ | [29] |
| $k_{a3} * 10^{-4}$ | 237 (51-1098)  | $\log(k_{a3}) \sim \mathcal{N}(-3.7, 0.77)$ | [29] |
| $S_D * 10^{-4}$    | 5 (0.5-53)     | $\log(S_D) \sim \mathcal{N}(-7.6, 1.2)$     | [29] |
| $S_E * 10^{-4}$    | 412 (72-2357)  | $\log(S_E) \sim \mathcal{N}(-3.2, 0.87)$    | [29] |
| $S_T * 10^{-4}$    | 42 (10-179)    | $\log(S_T) \sim \mathcal{N}(-5.5, 0.73)$    | [29] |

Table S3: Comparison of PD model parameters estimated during leave-one-out validation and final PD model parameters for patient 1.

| Training Data | Test Data | Accept? | $C_{E50}$        | $E_{max}$           | $F_{0I}$            | $k_{I2} \times 10^{-4}$ | $k_{a1} \times 10^{-4}$ | $k_{a2} \times 10^{-4}$ | $k_{a3} \times 10^{-4}$ | $S_D \times 10^{-4}$ | $S_E \times 10^{-4}$ | $S_T \times 10^{-4}$ |
|---------------|-----------|---------|------------------|---------------------|---------------------|-------------------------|-------------------------|-------------------------|-------------------------|----------------------|----------------------|----------------------|
| BCD           | A         | N       | 329              | 70.6                | 12.0                | 288                     | 31                      | 408                     | 83                      | 7.2                  | 286                  | 31                   |
| ACD           | B         | Y       | 407              | 65.7                | 11.8                | 276                     | 39                      | 555                     | 198                     | 5.1                  | 287                  | 31                   |
| ABD           | C         | N       | 436              | 56.4                | 14.2                | 244                     | 16                      | 522                     | 215                     | 1.5                  | 155                  | 23                   |
| ABC           | D         | N       | 266              | 87.1                | 11.6                | 241                     | 42                      | 531                     | 58                      | 5.6                  | 508                  | 30                   |
| BD            | A         | Y       | 431              | 57.5                | 14.9                | 263                     | 15                      | 510                     | 192                     | 1.5                  | 136                  | 22                   |
| AD            | B         | Y       | 488              | 54.7                | 13.8                | 227                     | 16                      | 502                     | 242                     | 1.4                  | 173                  | 19                   |
| AB            | D         | N       | 394              | 66.2                | 14.3                | 236                     | 28                      | 554                     | 218                     | 1.6                  | 207                  | 24                   |
| ABD           | ABD       | 3/3     | 436<br>(355-517) | 56.4<br>(51.1-61.8) | 14.2<br>(12.9-15.5) | 244<br>(181-330)        | 16<br>(7-35)            | 522<br>(221-1233)       | 215<br>(59-778)         | 1.5<br>(0.6-3.3)     | 155<br>(83-289)      | 23<br>(16-31)        |

Table S4: Comparison of PD model parameters estimated during leave-one-out validation and final PD model parameters for patient 2. \*Visit A did not have MPE and MAPE values less than  $\pm 15\%$  and  $20\%$ , respectively.

| Training Data | Test Data | Accept? | $C_{E50}$        | $E_{max}$           | $F_{01}$            | $k_{I2} \times 10^{-4}$ | $k_{a1} \times 10^{-4}$ | $k_{a2} \times 10^{-4}$ | $k_{a3} \times 10^{-4}$ | $S_D \times 10^{-4}$ | $S_E \times 10^{-4}$ | $S_T \times 10^{-4}$ |
|---------------|-----------|---------|------------------|---------------------|---------------------|-------------------------|-------------------------|-------------------------|-------------------------|----------------------|----------------------|----------------------|
| BCD           | A         | N       | 452              | 68.0                | 13.2                | 246                     | 14                      | 456                     | 235                     | 1.2                  | 380                  | 16                   |
| ACD           | B         | N       | 413              | 81.6                | 13.7                | 367                     | 41                      | 517                     | 119                     | 2.9                  | 434                  | 26                   |
| ABD           | C         | Y       | 416              | 60.1                | 13.9                | 283                     | 12                      | 507                     | 277                     | 0.8                  | 201                  | 19                   |
| ABC           | D         | Y       | 426              | 68.6                | 14.4                | 317                     | 15                      | 512                     | 180                     | 0.8                  | 204                  | 21                   |
| ABCD          | ABCD      | 3/4*    | 405<br>(339-471) | 67.4<br>(59.3-75.5) | 13.8<br>(12.8-14.7) | 285<br>(223-363)        | 15<br>(7-35)            | 495<br>(236-1039)       | 231<br>(137-389)        | 1.2<br>(0.6-2.3)     | 334<br>(232-481)     | 19<br>(15-25)        |

Table S5: Comparison of PD model parameters estimated during leave-one-out validation and final PD model parameters for patient 3.

| Training Data | Test Data | Accept? | $C_{E50}$        | $E_{max}$           | $F_{01}$            | $k_{12} \cdot 10^{-4}$ | $k_{a1} \cdot 10^{-4}$ | $k_{a2} \cdot 10^{-4}$ | $k_{a3} \cdot 10^{-4}$ | $S_D \cdot 10^{-4}$ | $S_E \cdot 10^{-4}$ | $S_T \cdot 10^{-4}$ |
|---------------|-----------|---------|------------------|---------------------|---------------------|------------------------|------------------------|------------------------|------------------------|---------------------|---------------------|---------------------|
| BCD           | A         | Y       | 414              | 55.3                | 15.3                | 392                    | 13                     | 524                    | 327                    | 1.2                 | 260                 | 24                  |
| ACD           | B         | Y       | 408              | 57.8                | 15.6                | 387                    | 17                     | 538                    | 333                    | 1.3                 | 241                 | 24                  |
| ABD           | C         | N       | 406              | 55.0                | 15.8                | 370                    | 21                     | 559                    | 276                    | 1.1                 | 133                 | 22                  |
| ABC           | D         | N       | 352              | 54.8                | 14.6                | 422                    | 47                     | 585                    | 104                    | 1.7                 | 254                 | 29                  |
| ABCD          | ABCD      | 4/4     | 401<br>(327-475) | 57.4<br>(49.8-65.0) | 15.5<br>(14.2-16.8) | 397<br>(277-568)       | 18<br>(8-42)           | 548<br>(268-1121)      | 327<br>(168-638)       | 1.4<br>(0.7-2.5)    | 237<br>(183-308)    | 25<br>(17-36)       |

Table S6: Comparison of PD model parameters estimated during leave-one-out validation and final PD model parameters for patient 4.

| Training Data | Test Data | Accept? | $C_{E50}$        | $E_{max}$           | $F_{01}$            | $k_{12} \cdot 10^{-4}$ | $k_{a1} \cdot 10^{-4}$ | $k_{a2} \cdot 10^{-4}$ | $k_{a3} \cdot 10^{-4}$ | $S_D \cdot 10^{-4}$ | $S_E \cdot 10^{-4}$ | $S_T \cdot 10^{-4}$ |
|---------------|-----------|---------|------------------|---------------------|---------------------|------------------------|------------------------|------------------------|------------------------|---------------------|---------------------|---------------------|
| BCD           | A         | N       | 275              | 85.8                | 13.2                | 224                    | 20                     | 245                    | 61                     | 3.0                 | 412                 | 17                  |
| ACD           | B         | Y       | 295              | 89.6                | 12.6                | 202                    | 18                     | 398                    | 58                     | 2.5                 | 435                 | 18                  |
| ABD           | C         | N       | 397              | 57.4                | 12.2                | 250                    | 18                     | 439                    | 122                    | 1.6                 | 195                 | 22                  |
| ABC           | D         | N       | 329              | 81.9                | 13.2                | 214                    | 16                     | 510                    | 188                    | 1.6                 | 192                 | 17                  |
| ABCD          | ABCD      | 4/4     | 285<br>(226-344) | 84.4<br>(73.9-94.8) | 12.8<br>(11.3-14.4) | 213<br>(157-289)       | 18<br>(9-36)           | 437<br>(183-1044)      | 68<br>(42-113)         | 2.0<br>(1.0-3.8)    | 415<br>(347-496)    | 18<br>(13-25)       |

Table S7: Comparison of PD model parameters estimated during leave-one-out validation and final PD model parameters for patient 5.

| Training Data | Test Data | Accept? | $C_{E50}$        | $E_{max}$           | $F_{0I}$            | $k_{I2} \cdot 10^{-4}$ | $k_{aI} \cdot 10^{-4}$ | $k_{a2} \cdot 10^{-4}$ | $k_{a3} \cdot 10^{-4}$ | $S_D \cdot 10^{-4}$ | $S_E \cdot 10^{-4}$ | $S_T \cdot 10^{-4}$ |
|---------------|-----------|---------|------------------|---------------------|---------------------|------------------------|------------------------|------------------------|------------------------|---------------------|---------------------|---------------------|
| BCD           | A         | Y       | 232              | 78.8                | 13.2                | 316                    | 31                     | 558                    | 351                    | 1.3                 | 436                 | 42                  |
| ACD           | B         | N       | 245              | 77.7                | 13.8                | 311                    | 54                     | 522                    | 253                    | 3.5                 | 239                 | 36                  |
| ABD           | C         | N       | 261              | 70.9                | 11.3                | 385                    | 31                     | 562                    | 305                    | 0.7                 | 526                 | 62                  |
| ABC           | D         | N       | 339              | 65.4                | 12.0                | 281                    | 15                     | 517                    | 235                    | 1.1                 | 229                 | 31                  |
| BC            | A         | Y       | 339              | 66.0                | 12.1                | 276                    | 15                     | 512                    | 237                    | 1.1                 | 222                 | 30                  |
| AC            | B         | Y       | 373              | 66.8                | 13.4                | 339                    | 14                     | 491                    | 171                    | 1.3                 | 161                 | 26                  |
| AB            | C         | Y       | 267              | 70.3                | 9.5                 | 201                    | 14                     | 365                    | 276                    | 2.3                 | 547                 | 28                  |
| ABC           | ABC       | 3/3     | 339<br>(251-427) | 65.4<br>(53.8-77.1) | 12.0<br>(10.6-13.5) | 281<br>(194-406)       | 15<br>(7-32)           | 517<br>(223-1201)      | 235<br>(95-586)        | 1.1<br>(0.4-2.6)    | 229<br>(127-415)    | 31<br>(20-47)       |

Table S8: Comparison of PD model parameters estimated during leave-one-out validation and final PD model parameters for patient 6.

| Training Data | Test Data | Accept? | $C_{E50}$        | $E_{max}$           | $F_{01}$            | $k_{12} \times 10^{-4}$ | $k_{a1} \times 10^{-4}$ | $k_{a2} \times 10^{-4}$ | $k_{a3} \times 10^{-4}$ | $S_D \times 10^{-4}$ | $S_E \times 10^{-4}$ | $S_T \times 10^{-4}$ |
|---------------|-----------|---------|------------------|---------------------|---------------------|-------------------------|-------------------------|-------------------------|-------------------------|----------------------|----------------------|----------------------|
| BCD           | A         | N       | 404              | 66.0                | 15.2                | 201                     | 34                      | 463                     | 170                     | 2.6                  | 254                  | 19                   |
| ACD           | B         | Y       | 387              | 67.0                | 11.8                | 179                     | 31                      | 404                     | 180                     | 3.7                  | 328                  | 24                   |
| ABD           | C         | N       | 424              | 60.1                | 13.1                | 238                     | 10                      | 353                     | 74                      | 2.6                  | 404                  | 21                   |
| ABC           | D         | Y       | 351              | 57.1                | 11.4                | 165                     | 44                      | 475                     | 156                     | 2.8                  | 384                  | 22                   |
| BD            | A         | Y       | 472              | 60.2                | 14.1                | 315                     | 14                      | 212                     | 75                      | 3.7                  | 279                  | 22                   |
| AD            | B         | N       | 439              | 50.8                | 13.5                | 221                     | 10                      | 431                     | 132                     | 1.3                  | 194                  | 20                   |
| AB            | D         | Y       | 328              | 63.4                | 12.9                | 195                     | 10                      | 441                     | 120                     | 2.6                  | 461                  | 19                   |
| ABD           | ABD       | 3/3     | 424<br>(333-515) | 60.1<br>(46.3-74.0) | 13.1<br>(11.7-14.5) | 238<br>(172-330)        | 10<br>(4-22)            | 353<br>(102-1221)       | 74<br>(23-232)          | 2.6<br>(1.1-6.2)     | 404<br>(185-882)     | 21<br>(14-32)        |

Table S9: Comparison of PD model parameters estimated during leave-one-out validation and final PD model parameters for patient 7.

| Training Data | Test Data | Accept? | $C_{E50}$       | $E_{max}$           | $F_{01}$            | $k_{12} \cdot 10^{-4}$ | $k_{a1} \cdot 10^{-4}$ | $k_{a2} \cdot 10^{-4}$ | $k_{a3} \cdot 10^{-4}$ | $S_D \cdot 10^{-4}$ | $S_E \cdot 10^{-4}$ | $S_T \cdot 10^{-4}$ |
|---------------|-----------|---------|-----------------|---------------------|---------------------|------------------------|------------------------|------------------------|------------------------|---------------------|---------------------|---------------------|
| BCD           | A         | N       | 281             | 91.4                | 14.5                | 250                    | 34                     | 558                    | 32                     | 2.0                 | 321                 | 15                  |
| ACD           | B         | N       | 293             | 81.9                | 16.2                | 268                    | 189                    | 607                    | 283                    | 2.0                 | 104                 | 15                  |
| ABD           | C         | Y       | 151             | 86.9                | 12.1                | 309                    | 253                    | 791                    | 218                    | 4.7                 | 194                 | 20                  |
| ABC           | D         | Y       | 146             | 82.8                | 15.0                | 357                    | 58                     | 616                    | 113                    | 4.4                 | 143                 | 20                  |
| ABCD          | ABCD      | 4/4     | 141<br>(96-187) | 78.0<br>(68.9-87.1) | 14.2<br>(12.2-16.1) | 358<br>(252-509)       | 49<br>(23-105)         | 624<br>(319-1221)      | 178<br>(69-459)        | 4.4<br>(3.2-6.0)    | 140<br>(99-199)     | 21<br>(16-29)       |

Table S10: Comparison of PD model parameters estimated during leave-one-out validation and final PD model parameters for patient 8.

| Training Data | Test Data | Accept? | $C_{E50}$        | $E_{max}$           | $F_{0I}$            | $k_{I2} \cdot 10^{-4}$ | $k_{aI} \cdot 10^{-4}$ | $k_{a2} \cdot 10^{-4}$ | $k_{a3} \cdot 10^{-4}$ | $S_D \cdot 10^{-4}$ | $S_E \cdot 10^{-4}$ | $S_T \cdot 10^{-4}$ |
|---------------|-----------|---------|------------------|---------------------|---------------------|------------------------|------------------------|------------------------|------------------------|---------------------|---------------------|---------------------|
| BCD           | A         | Y       | 362              | 39.7                | 16.8                | 429                    | 273                    | 546                    | 280                    | 0.6                 | 125                 | 36                  |
| ACD           | B         | N       | 390              | 40.4                | 17.8                | 369                    | 323                    | 538                    | 286                    | 0.3                 | 92                  | 27                  |
| ABD           | C         | N       | 344              | 36.1                | 16.2                | 451                    | 83                     | 549                    | 264                    | 0.8                 | 197                 | 45                  |
| ABC           | D         | N       | 307              | 75.3                | 13.4                | 289                    | 37                     | 518                    | 154                    | 4.2                 | 463                 | 29                  |
| BC            | A         | N       | 328              | 85.5                | 9.0                 | 367                    | 58                     | 184                    | 94                     | 13.6                | 279                 | 38                  |
| AC            | B         | N       | 378              | 59.1                | 16.7                | 276                    | 73                     | 554                    | 269                    | 1.3                 | 262                 | 26                  |
| AB            | C         | N       | 359              | 71.5                | 13.9                | 306                    | 30                     | 379                    | 191                    | 3.5                 | 197                 | 27                  |
| ABC           | ABC       | 3/3     | 307<br>(228-386) | 75.3<br>(61.5-89.1) | 13.4<br>(11.4-15.4) | 289<br>(197-424)       | 37<br>(18-75)          | 518<br>(203-1324)      | 154<br>(68-348)        | 4.2<br>(2.8-6.5)    | 463<br>(377-569)    | 29<br>(20-42)       |

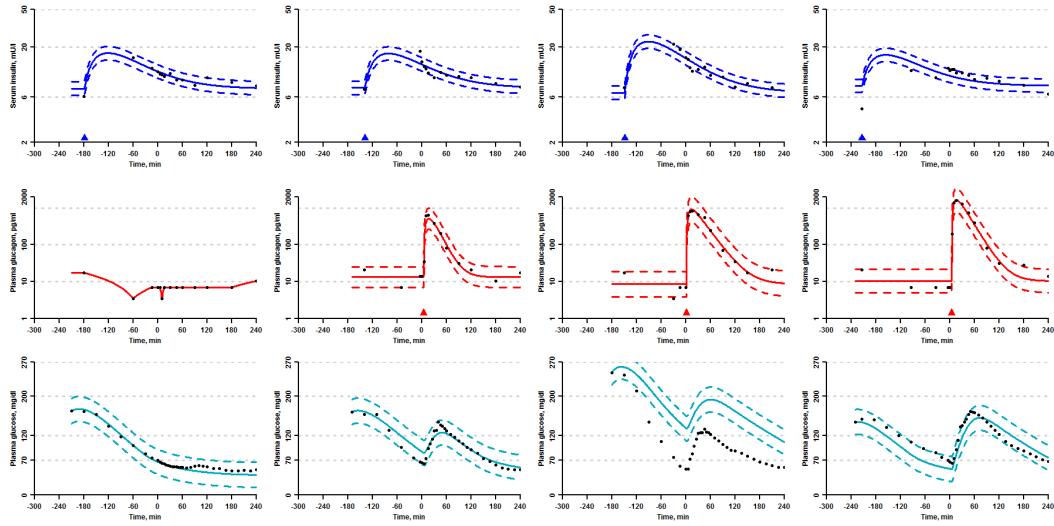


Figure S1: Data from all patient 1's visits (left to right: visit A to D) with insulin PK model fits (top row, logarithmic y-axes) and glucagon linear interpolation or PK model fits (middle row, logarithmic y-axes) both used as inputs to the glucose PD model for simulation built with data from visits A, B and D (bottom row). **The dynamics during visit C are clearly different from the three other visits.** The triangles indicate dose time of the insulin and glucagon boluses, respectively.

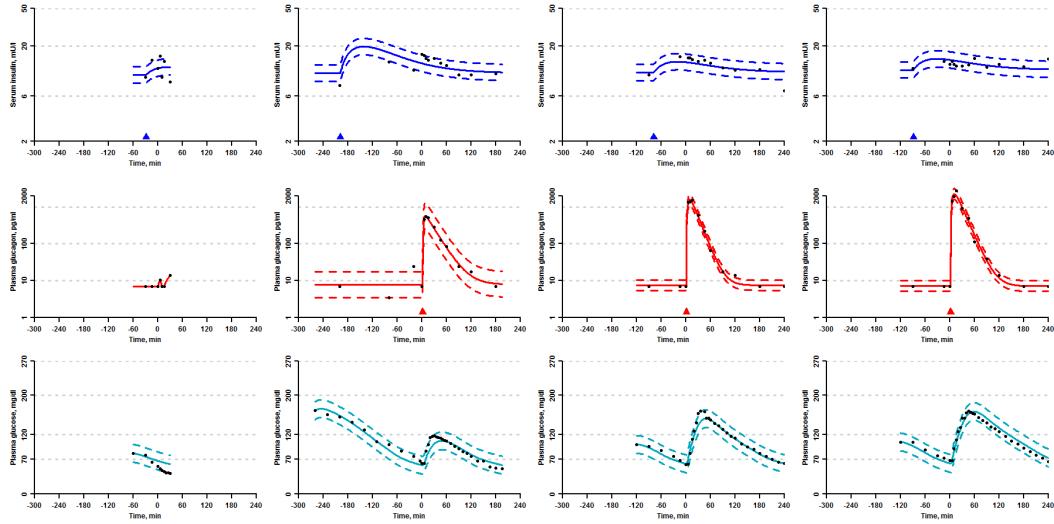


Figure S2: Data from all patient 2's visits (left to right: visit A to D) with insulin PK model fits (top row, logarithmic y-axes) and glucagon linear interpolation or PK model fits (middle row, logarithmic y-axes) both used as inputs to the glucose PD model for simulation **built with data from all four visits** (bottom row). The triangles indicate dose time of the insulin and glucagon boluses, respectively.

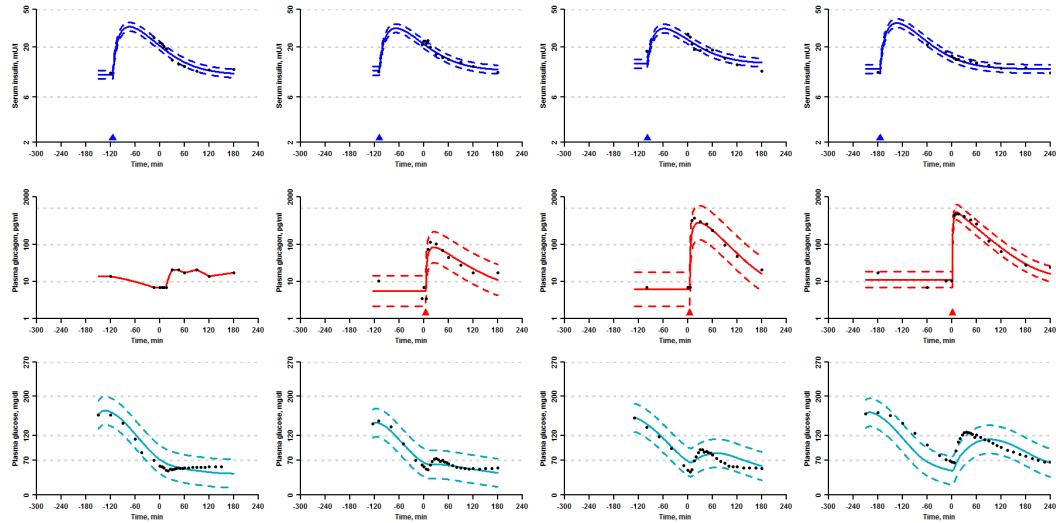


Figure S3: Data from all patient 3's visits (left to right: visit A to D) with insulin PK model fits (top row, logarithmic y-axes) and glucagon linear interpolation or PK model fits (middle row, logarithmic y-axes) both used as inputs to the glucose PD model for simulation **built with data from all four visits** (bottom row). The triangles indicate dose time of the insulin and glucagon boluses, respectively.

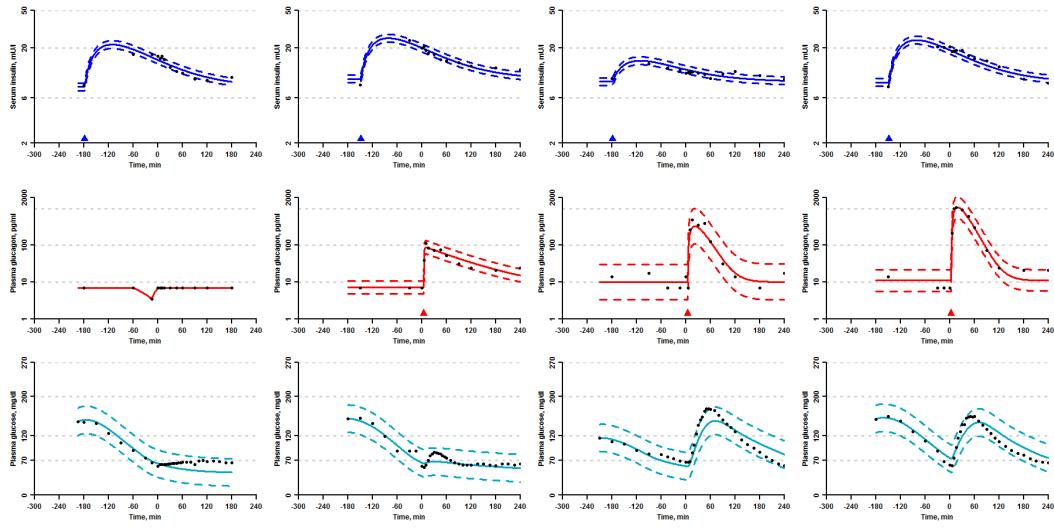


Figure S4: Data from all patient 4's visits (left to right: visit A to D) with insulin PK model fits (top row, logarithmic y-axes) and glucagon linear interpolation or PK model fits (middle row, logarithmic y-axes) both used as inputs to the glucose PD model for simulation **built with data from all four visits** (bottom row). The triangles indicate dose time of the insulin and glucagon boluses, respectively.

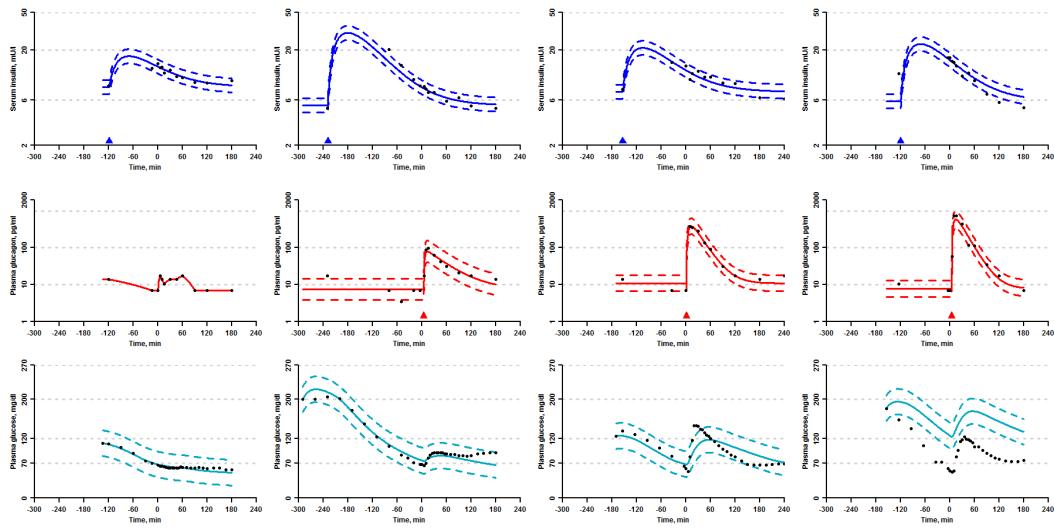


Figure S5: Data from all patient 5's visits (left to right: visit A to D) with insulin PK model fits (top row, logarithmic y-axes) and glucagon linear interpolation or PK model fits (middle row, logarithmic y-axes) both used as inputs to the glucose PD model for

simulation built with data from visits A, B and C (bottom row). The dynamics during visit D are clearly different from the three other visits. The triangles indicate dose time of the insulin and glucagon boluses, respectively.

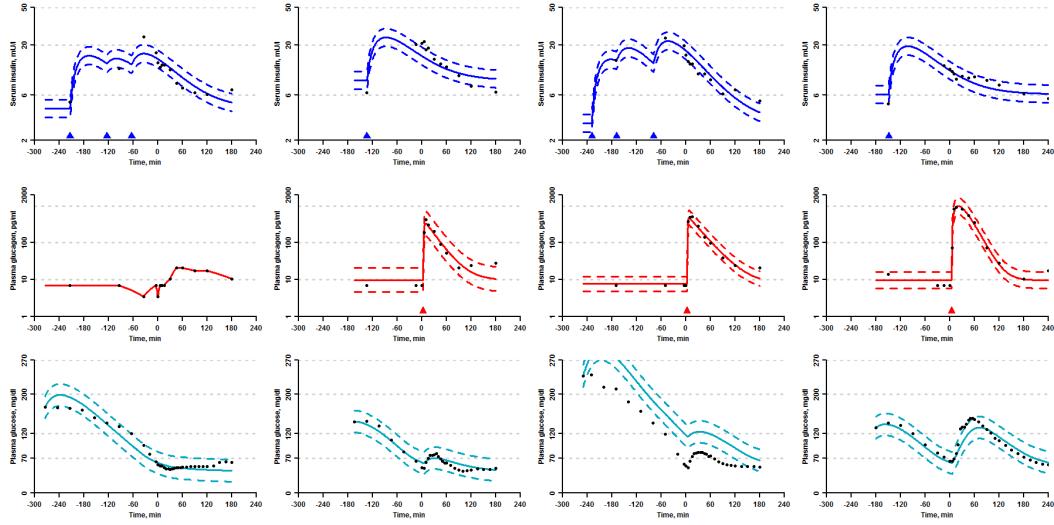


Figure S6: Data from all patient 6's visits (left to right: visit A to D) with insulin PK model fits (top row, logarithmic y-axes) and glucagon linear interpolation or PK model fits (middle row, logarithmic y-axes) both used as inputs to the glucose PD model for simulation built with data from visits A, B and D (bottom row). The dynamics during visit C are clearly different from the three other visits. The triangles indicate dose time of the insulin and glucagon boluses, respectively.

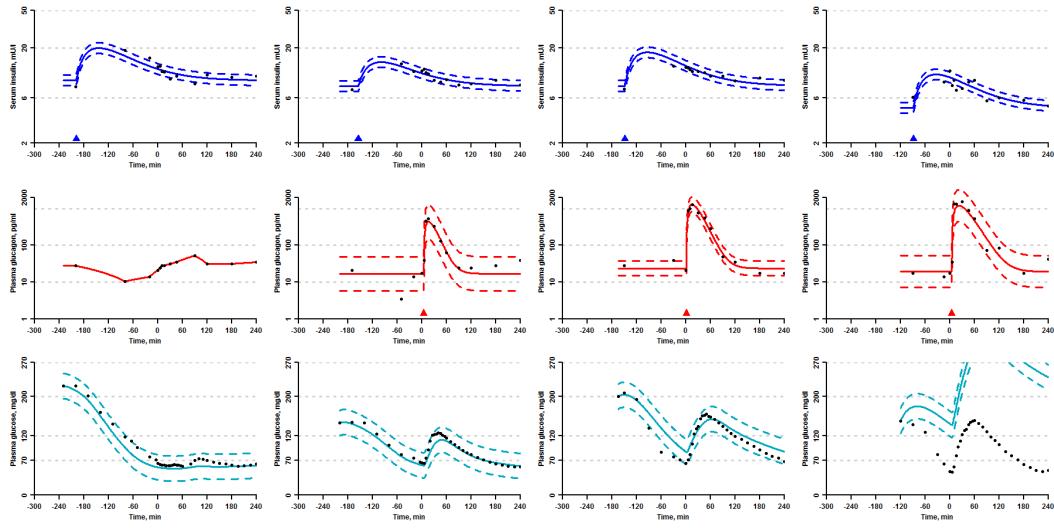


Figure S7: Data from all patient 8's visits (left to right: visit A to D) with insulin PK model fits (top row, logarithmic y-axes) and glucagon linear interpolation or PK model fits (middle row, logarithmic y-axes) both used as inputs to the glucose PD model for simulation **built with data from visits A, B and C** (bottom row). **The dynamics during visit D are clearly different from the three other visits.** The triangles indicate dose time of the insulin and glucagon boluses, respectively.