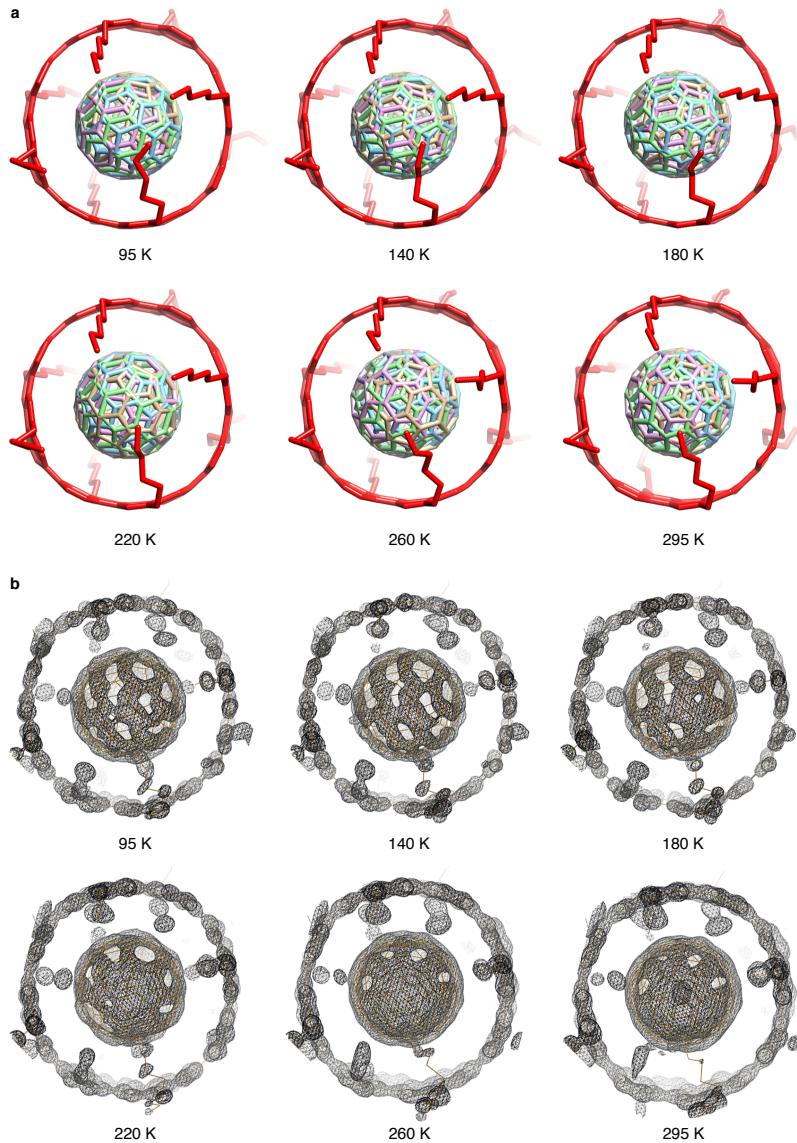


Supplementary Information

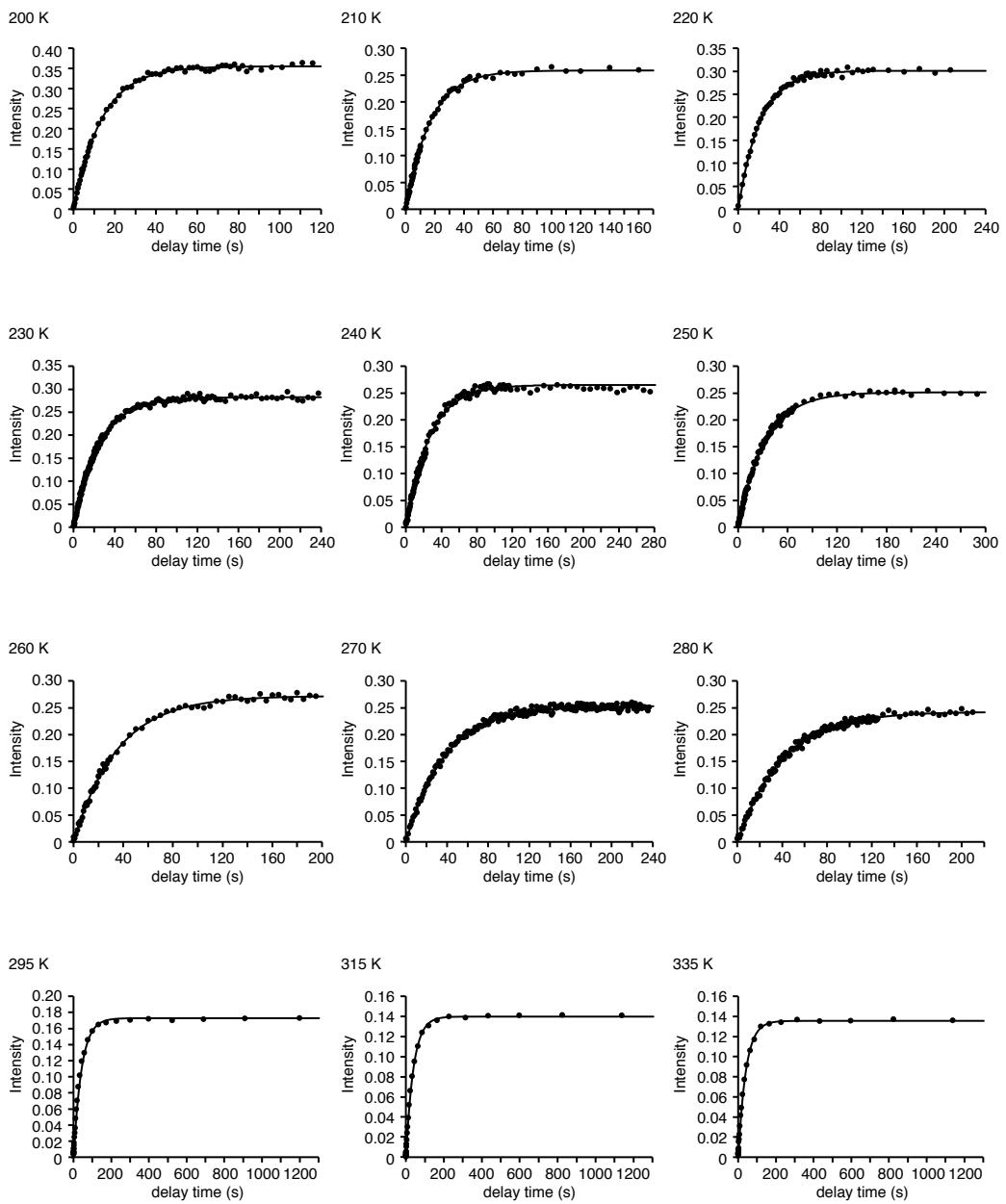
Ratchet-free solid-state inertial rotation of a guest ball in a tight tubular host

Taisuke Matsuno, Yusuke Nakai, Sota Sato, Yutaka Maniwa & Hiroyuki Isobe

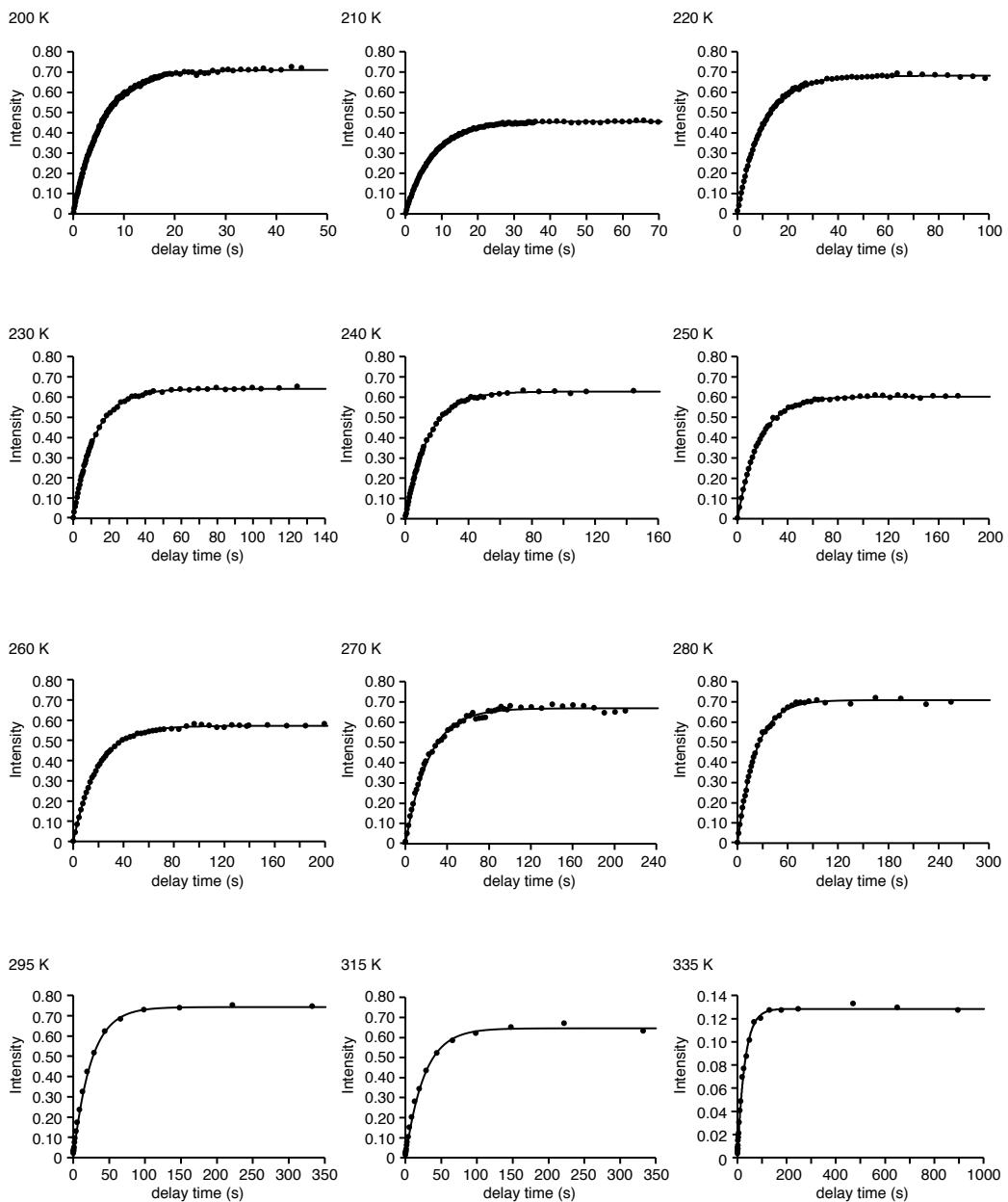
Supplementary Figures



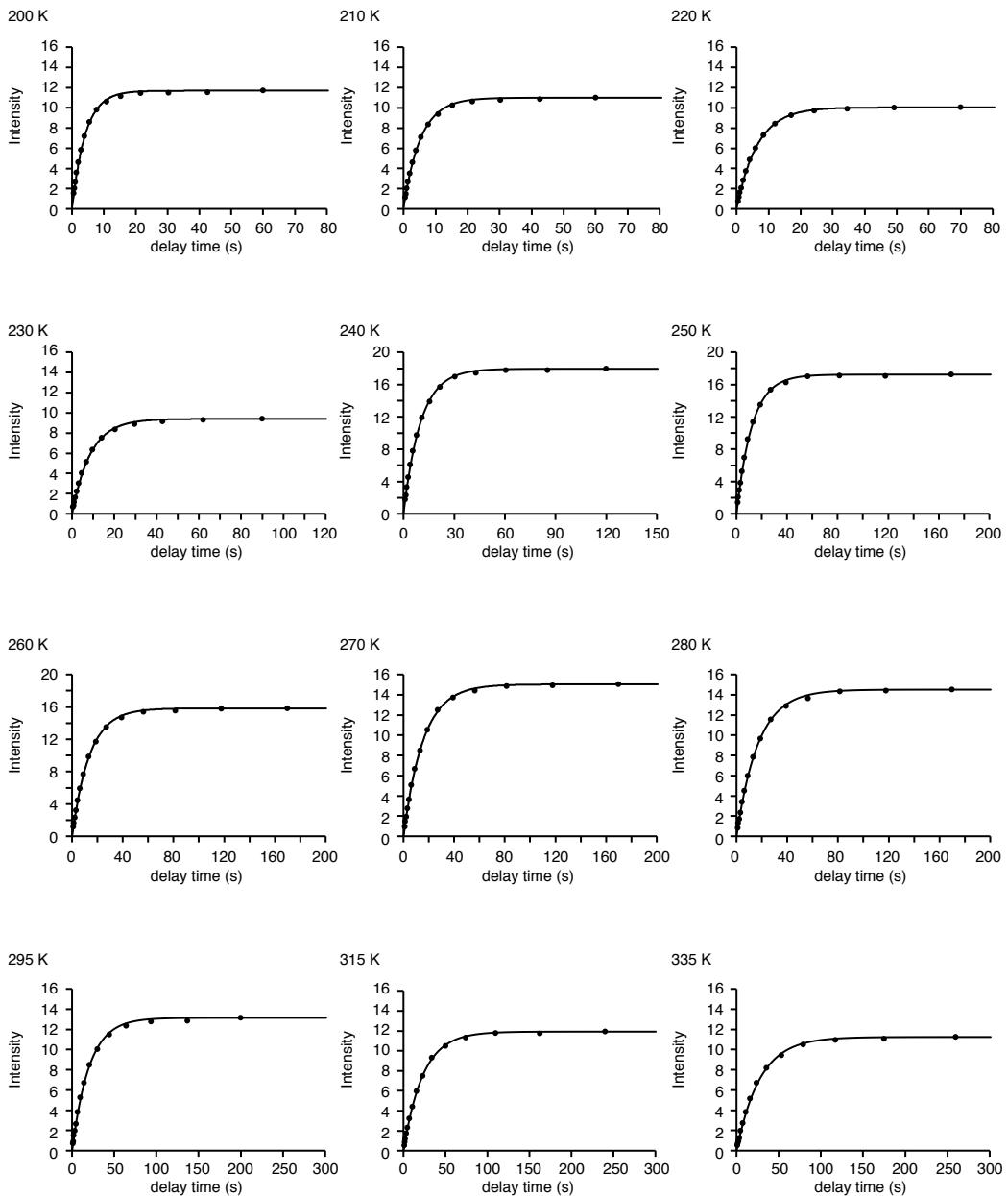
Supplementary Fig. 1 Crystallographic analyses of (P)-(12,8)-[4]CC \supset C₆₀ at 95, 140, 180, 220, 260 and 295 K. **a**, Crystal structures shown in tube models. Four different orientations of C₆₀ were shown in different colors. Disordered alkyl chains and hydrogen atoms are omitted for clarity. **b**, Electron density mappings with 2F_o - F_c (RMSD: 1.5 σ).



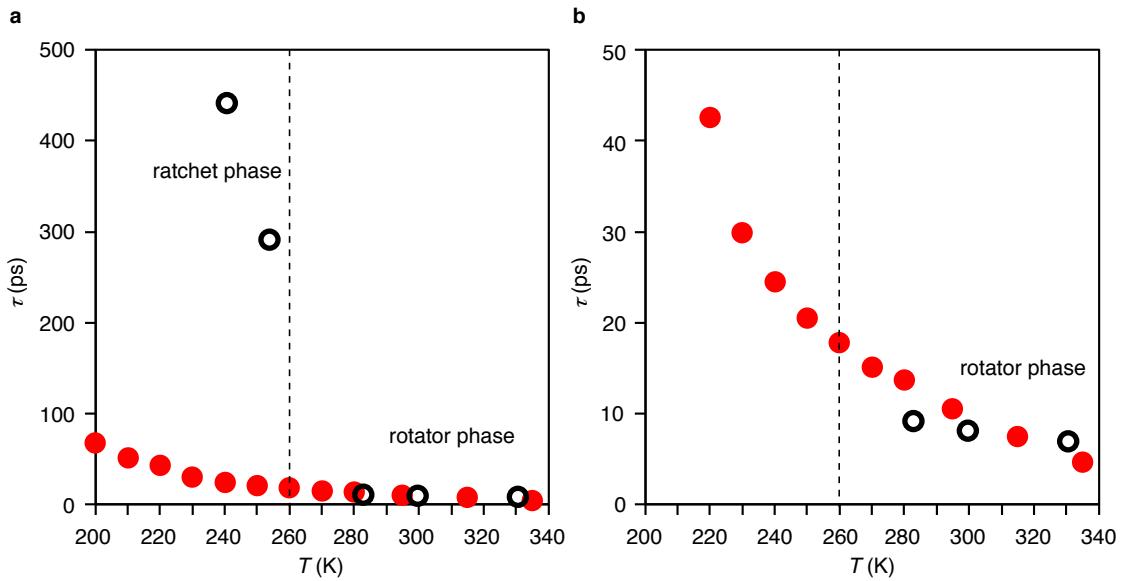
Supplementary Fig. 2 Raw data of VT T_1 measurements with (P) -(12,8)-[4]CC \supset C₆₀ under 4.01 T.



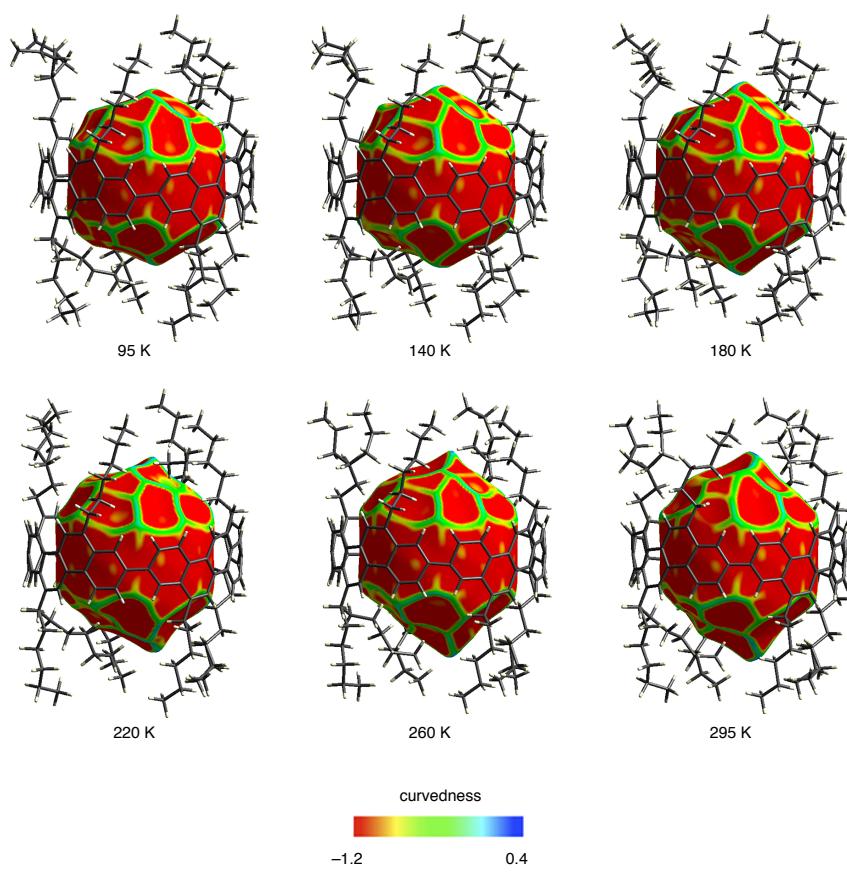
Supplementary Fig. 3 Raw data of VT T_1 measurements with (P) -(12,8)-[4]CC \supset C₆₀ under 9.40 T.



Supplementary Fig. 4 Raw data of VT T_1 measurements with (P) -(12,8)-[4]CC \supset C₆₀ under 11.7 T.



Supplementary Fig. 5 Comparisons of τ values of $(P)-(12,8)-[4]CC \supset C_60$ with those of intact C_60 . The data for the intact C_60 was taken from the literature². The data of $(P)-(12,8)-[4]CC \supset C_60$ are shown with red filled circles, and the data of C_60 are shown in open black circles. **a**, Whole-range data to show the presence of the phase transition (ratchet/rotator) with C_60 . **b**, A close-up view to show the absence of phase transition (ratchet/rotator) with $(P)-(12,8)-[4]CC \supset C_60$.



Supplementary Fig. 6 Hirshfeld surfaces of C_{60} in $(P)-(12,8)-[4]CC$ mapped with curvedness. No inflection lines were observed (see also ref. 15).

Supplementary Tables

Supplementary Table 1 Crystal data and structure refinement at 95 K (CCDC 1821725)

Empirical formula	$C_{182.50} H_{141} Cl_5$	
Formula weight	2511.19	
Temperature	95(2) K	
Wavelength	0.80000 Å	
Crystal system	Trigonal	
Space group	$P\bar{3}_1$	
Unit cell dimensions	$a = 28.980(4)$ Å	$\alpha = 90^\circ.$
	$b = 28.980(4)$ Å	$\beta = 90^\circ.$
	$c = 13.230(3)$ Å	$\gamma = 120^\circ.$
Volume	9622(3) Å ³	
Z	3	
Density (calculated)	1.300 Mg/m ³	
Absorption coefficient	0.233 mm ⁻¹	
$F(000)$	3963	
Crystal size	0.100 × 0.100 × 0.050 mm ³	
Theta range for data collection	1.582 to 28.840°.	
Index ranges	$-34 \leq h \leq 34, -34 \leq k \leq 34, -15 \leq l \leq 15$	
Reflections collected	113344	
Independent reflections	23472 [$R(\text{int}) = 0.0403$]	
Completeness to theta = 28.685°	100.0 %	
Absorption correction	Semi-empirical from equivalents	
Max. and min. transmission	1.000 and 0.686	
Refinement method	Full-matrix least-squares on F^2	
Data / restraints / parameters	23472 / 3225 / 2770	
Goodness-of-fit on F^2	2.396	
Final R indices [$I > 2\sigma(I)$]	$R_1 = 0.1213, wR_2 = 0.2931$	
R indices (all data)	$R_1 = 0.1397, wR_2 = 0.3081$	
Absolute structure parameter	0.024(13)	
Extinction coefficient	n/a	
Largest diff. peak and hole	0.370 and -0.461 e.Å ⁻³	

Supplementary Table 2 Crystal data and structure refinement at 140 K (CCDC 1821727)

Empirical formula	$C_{182.50} H_{141} Cl_5$	
Formula weight	2511.19	
Temperature	140(2) K	
Wavelength	0.80000 Å	
Crystal system	Trigonal	
Space group	$P\bar{3}_1$	
Unit cell dimensions	$a = 29.080(4)$ Å	$\alpha = 90^\circ$.
	$b = 29.080(4)$ Å	$\beta = 90^\circ$.
	$c = 13.330(3)$ Å	$\gamma = 120^\circ$.
Volume	9762(3) Å ³	
Z	3	
Density (calculated)	1.281 Mg/m ³	
Absorption coefficient	0.230 mm ⁻¹	
$F(000)$	3963	
Crystal size	0.200 × 0.100 × 0.100 mm ³	
Theta range for data collection	1.576 to 28.826°.	
Index ranges	$-34 \leq h \leq 35, -35 \leq k \leq 35, -16 \leq l \leq 16$	
Reflections collected	111900	
Independent reflections	23817 [$R(\text{int}) = 0.0403$]	
Completeness to theta = 28.685°	100.0 %	
Absorption correction	Semi-empirical from equivalents	
Max. and min. transmission	1.000 and 0.512	
Refinement method	Full-matrix least-squares on F^2	
Data / restraints / parameters	23817 / 3231 / 2770	
Goodness-of-fit on F^2	2.924	
Final R indices [$I > 2\sigma(I)$]	$R_1 = 0.1394, wR_2 = 0.3425$	
R indices (all data)	$R_1 = 0.1505, wR_2 = 0.3524$	
Absolute structure parameter	0.020(13)	
Extinction coefficient	n/a	
Largest diff. peak and hole	0.510 and -0.523 e.Å ⁻³	

Supplementary Table 3 Crystal data and structure refinement at 180 K (CCDC 1821730)

Empirical formula	$C_{182.50} H_{141} Cl_5$
Formula weight	2511.19
Temperature	180(2) K
Wavelength	0.80000 Å
Crystal system	Trigonal
Space group	$P\bar{3}_1$
Unit cell dimensions	$a = 29.130(4)$ Å $\alpha = 90^\circ$. $b = 29.130(4)$ Å $\beta = 90^\circ$. $c = 13.410(3)$ Å $\gamma = 120^\circ$.
Volume	9855(3) Å ³
Z	3
Density (calculated)	1.269 Mg/m ³
Absorption coefficient	0.227 mm ⁻¹
$F(000)$	3963
Crystal size	0.200 × 0.200 × 0.100 mm ³
Theta range for data collection	1.574 to 28.825°.
Index ranges	$-35 \leq h \leq 35, -35 \leq k \leq 35, -16 \leq l \leq 16$
Reflections collected	111365
Independent reflections	23996 [$R(\text{int}) = 0.0436$]
Completeness to theta = 28.685°	100.0 %
Absorption correction	Semi-empirical from equivalents
Max. and min. transmission	1.000 and 0.447
Refinement method	Full-matrix least-squares on F^2
Data / restraints / parameters	23996 / 3239 / 2770
Goodness-of-fit on F^2	2.927
Final R indices [$I > 2\sigma(I)$]	$R_1 = 0.1396, wR_2 = 0.3455$
R indices (all data)	$R_1 = 0.1487, wR_2 = 0.3535$
Absolute structure parameter	0.028(17)
Extinction coefficient	n/a
Largest diff. peak and hole	0.491 and -0.512 e.Å ⁻³

Supplementary Table 4 Crystal data and structure refinement at 220 K (CCDC 1821728)

Empirical formula	$C_{182.50} H_{141} Cl_5$	
Formula weight	2511.19	
Temperature	220(2) K	
Wavelength	0.80000 Å	
Crystal system	Trigonal	
Space group	$P\bar{3}_1$	
Unit cell dimensions	$a = 29.240(4)$ Å	$\alpha = 90^\circ$.
	$b = 29.240(4)$ Å	$\beta = 90^\circ$.
	$c = 13.500(3)$ Å	$\gamma = 120^\circ$.
Volume	9996(3) Å ³	
Z	3	
Density (calculated)	1.252 Mg/m ³	
Absorption coefficient	0.224 mm ⁻¹	
$F(000)$	3963	
Crystal size	0.200 × 0.100 × 0.100 mm ³	
Theta range for data collection	1.568 to 28.844°.	
Index ranges	$-35 \leq h \leq 35, -35 \leq k \leq 35, -16 \leq l \leq 16$	
Reflections collected	115877	
Independent reflections	24398 [$R(\text{int}) = 0.0507$]	
Completeness to theta = 28.685°	100.0 %	
Absorption correction	Semi-empirical from equivalents	
Max. and min. transmission	1.000 and 0.705	
Refinement method	Full-matrix least-squares on F^2	
Data / restraints / parameters	24398 / 3240 / 2770	
Goodness-of-fit on F^2	2.700	
Final R indices [$I > 2\sigma(I)$]	$R_1 = 0.1428, wR_2 = 0.3322$	
R indices (all data)	$R_1 = 0.1535, wR_2 = 0.3391$	
Absolute structure parameter	0.07(3)	
Extinction coefficient	n/a	
Largest diff. peak and hole	0.359 and -0.396 e.Å ⁻³	

Supplementary Table 5 Crystal data and structure refinement at 260 K (CCDC 1821726)

Empirical formula	$C_{182.50} H_{141} Cl_5$
Formula weight	2511.19
Temperature	260(2) K
Wavelength	0.80000 Å
Crystal system	Trigonal
Space group	$P\bar{3}_1$
Unit cell dimensions	$a = 29.320(4)$ Å $\alpha = 90^\circ$. $b = 29.320(4)$ Å $\beta = 90^\circ$. $c = 13.540(3)$ Å $\gamma = 120^\circ$.
Volume	10080(3) Å ³
Z	3
Density (calculated)	1.241 Mg/m ³
Absorption coefficient	0.222 mm ⁻¹
$F(000)$	3963
Crystal size	0.200 × 0.200 × 0.100 mm ³
Theta range for data collection	0.903 to 28.851°.
Index ranges	$-35 \leq h \leq 35, -35 \leq k \leq 35, -16 \leq l \leq 16$
Reflections collected	77552
Independent reflections	21210 [$R(\text{int}) = 0.0365$]
Completeness to theta = 28.685°	99.1 %
Absorption correction	Semi-empirical from equivalents
Max. and min. transmission	1.000 and 0.818
Refinement method	Full-matrix least-squares on F^2
Data / restraints / parameters	21210 / 3203 / 2770
Goodness-of-fit on F^2	1.145
Final R indices [$I > 2\sigma(I)$]	$R_1 = 0.1082, wR_2 = 0.2654$
R indices (all data)	$R_1 = 0.1145, wR_2 = 0.2805$
Absolute structure parameter	0.09(5)
Extinction coefficient	n/a
Largest diff. peak and hole	0.220 and -0.217 e.Å ⁻³

Supplementary Table 6 Crystal data and structure refinement at 295 K (CCDC 1821729)

Empirical formula	$C_{182.50} H_{141} Cl_5$	
Formula weight	2511.19	
Temperature	295(2) K	
Wavelength	0.80000 Å	
Crystal system	Trigonal	
Space group	$P\bar{3}_1$	
Unit cell dimensions	$a = 29.430(4)$ Å	$\alpha = 90^\circ$.
	$b = 29.430(4)$ Å	$\beta = 90^\circ$.
	$c = 13.520(3)$ Å	$\gamma = 120^\circ$.
Volume	$10141(4)$ Å ³	
Z	3	
Density (calculated)	1.234 Mg/m ³	
Absorption coefficient	0.221 mm ⁻¹	
$F(000)$	3963	
Crystal size	$0.100 \times 0.100 \times 0.050$ mm ³	
Theta range for data collection	1.558 to 28.875°.	
Index ranges	$-35 \leq h \leq 35, -35 \leq k \leq 35, -16 \leq l \leq 16$	
Reflections collected	119096	
Independent reflections	24764 [$R(\text{int}) = 0.0341$]	
Completeness to theta = 28.685°	99.9 %	
Absorption correction	Semi-empirical from equivalents	
Max. and min. transmission	1.000 and 0.741	
Refinement method	Full-matrix least-squares on F^2	
Data / restraints / parameters	24764 / 3246 / 2770	
Goodness-of-fit on F^2	1.985	
Final R indices [$I > 2\sigma(I)$]	$R_1 = 0.1209, wR_2 = 0.2711$	
R indices (all data)	$R_1 = 0.1498, wR_2 = 0.2924$	
Absolute structure parameter	0.07(2)	
Extinction coefficient	n/a	
Largest diff. peak and hole	0.359 and -0.262 e.Å ⁻³	