## **Switchable plasmonic routers controlled by external magnetic fields by using magneto-plasmonic waveguides**

**Kum-Song Ho**<sup>1</sup> **, Song-Jin Im**1,\***, Ji-Song Pae**<sup>1</sup> **, Chol-Song Ri**<sup>1</sup> **, Yong-Ha Han**<sup>1</sup> **, and J. Herrmann**2,+

<sup>1</sup>Department of Physics, Kim II Sung University, Pyongyang, Democratic People's Republic of Korea <sup>2</sup>Max-Born-Institute for Nonlinear Optics and Short Pulse Spectroscopy, Max-Born-Str. 2a, D-12489 Berlin, **Germany** 

\* ryongnam31@yahoo.com + jherrman@mbi-berlin.de

## **ABSTRACT**

## **Supplementary information**

## Derivation of Eq. (4)

Let's remind the dispersion relation Eq. (3).

$$
e^{-2k_m t} = \frac{q_m + q_{-g}}{q_m - q_{-g}} \frac{q_m + q_g}{q_m - q_g},\tag{0.1}
$$

where  $q_m = k_m/\varepsilon_m$ ,  $q_g = (\varepsilon_d k_d + g\beta)/( \varepsilon_d^2 - g^2)$ ,  $k_m^2 = \beta^2 - k_0^2 \varepsilon_m$ ,  $k_d^2 = \beta^2 - k_0^2(\varepsilon_d^2 - g^2)/\varepsilon_d$ , t: thickness of the metal film,  $\beta$ : propagation constant,  $\varepsilon_m$  and  $\varepsilon_d$ : permittivity of the metal and the ferromagnetic dielectric, respectively.

For a metal film thickness larger than the skin depth  $\delta = 1/2k_m$ , in first approximation of  $|\Delta \beta / \beta_0|$ , following equations can be obtained.

<span id="page-0-1"></span>
$$
e^{-t/\delta} = \frac{(q_m + q_d)^2 - (g\beta_0/\varepsilon_d^2)^2}{(q_m - q_d)^2 - (g\beta_0/\varepsilon_d^2)^2},
$$
\n(0.2)

<span id="page-0-0"></span>
$$
q_m = -q_0 \left( 1 + \frac{\beta_0 \Delta \beta}{q_0^2 \varepsilon_m^2} \right),
$$
  
\n
$$
q_d = q_0 \left( 1 + \frac{\beta_0 \Delta \beta}{q_0^2 \varepsilon_d^2} \right),
$$
\n(0.3)

where  $q_d = k_d/\varepsilon_d$ ,  $\beta = \beta_0 + \Delta\beta$ ,  $\beta_0 = k_0[\varepsilon_d\varepsilon_m/(\varepsilon_d + \varepsilon_m)]^{1/2}$ ,  $q_0 = k_0(-\varepsilon_d - \varepsilon_m)^{-1/2}$ .

By substituting Eq.  $(0.3)$  to Eq.  $(0.2)$ , we can get the following analytical equation.

<span id="page-0-2"></span>
$$
\Delta \beta^2 = \beta_0^2 \left[ \frac{4 \left(\varepsilon_d / \varepsilon_m\right)^2 e^{-t/ \delta}}{\left(1 - \varepsilon_d^2 / \varepsilon_m^2\right)^2} + \frac{g^2}{\left(1 - \varepsilon_d^2 / \varepsilon_m^2\right)^2 \left(-\varepsilon_m \varepsilon_d\right)} \right].
$$
\n(0.4)

From Eq.  $(0.4)$ , we obtain Eq.  $(4)$ .

$$
\beta^{e(o)} = \beta_0 + (-)\sqrt{(\Delta\beta_0)^2 + (\Delta\beta_g)^2},
$$
  

$$
\Delta\beta_0 = \frac{2(-\varepsilon_d/\varepsilon_m)\exp(-t/2\delta)}{1 - \varepsilon_d^2/\varepsilon_m^2}\beta_0, \qquad \Delta\beta_g = \frac{g}{(1 - \varepsilon_d^2/\varepsilon_m^2)\sqrt{-\varepsilon_m\varepsilon_d}}\beta_0,
$$
(0.5)

where the superscripts *o* and *e* represent the odd and the even modes, respectively.