

# Supplementary Information

## Processivity of dimeric kinesin-1 molecular motors

Si-Kao Guo<sup>1,2</sup>, Xiao-Xuan Shi<sup>1,2</sup>, Peng-Ye Wang<sup>1,2</sup>, Ping Xie<sup>1,2,\*</sup>

<sup>1</sup> *Key Laboratory of Soft Matter Physics, Beijing National Laboratory for Condensed Matter Physics, Institute of Physics, Chinese Academy of Science, Beijing 100190, China,*

<sup>2</sup> *School of Physical Sciences, University of Chinese Academy of Sciences, Beijing 100049, China*

\*Corresponding author:

**E-mail address:** [pxie@aphy.iphy.ac.cn](mailto:pxie@aphy.iphy.ac.cn)

### Appendix S1. Extended Material and Methods

#### S1. Potential of interaction between one kinesin head and MT in a mechanochemical coupling cycle

Based on argument (i) (see main text), we take the interaction potential of one kinesin head with MT as described as follows. In nucleotide-free state the kinesin head binds strongly to MT, with the interaction potential being written as  $V_S(x, y, z, \alpha, \theta, \phi) = V_{Sx}(x)V_y(y)V_z(z)V_\alpha(\alpha)V_\theta(\theta)V_\phi(\phi)$ , where coordinate  $oxyz$  is defined in Fig. 1,  $\alpha$ ,  $\theta$  and  $\phi$  are angles characterizing respectively the nutation, rotation and precession motions (when the kinesin head is in the MT-binding site,  $\alpha$ ,  $\theta$  and  $\phi$  correspond to the angles of rotations in  $xoz$ ,  $xoy$  and  $yoz$  planes, respectively). Term  $V_{Sx}(x) < 0$  (with the maxima equal to zero) represents the interaction potential between the kinesin head and MT along a MT protofilament and is approximately shown in the inset of Fig. 1 (upper panel). The period of  $V_{Sx}(x)$ ,  $d = 8.2$  nm, is equal to the distance between two successive binding sites on MT filaments. To be consistent with that for the case of the monomeric KIF1A [1], we take  $V_{Sx}(x)$  in one periodicity having an asymmetric form here, with asymmetric ratio  $d_1/d_2 = 3/5$ . It should be mentioned that taking other forms for  $V_{Sx}(x)$  (including the symmetric one) has little effect on the results for the dimer [2]. Terms  $V_y(y) \equiv \exp[-(y - y_0)/A_y]$  and  $V_z(z) \equiv \exp(-|z - z_0|/A_z)$  denote the potential changes in the vertical and horizontal

directions, respectively, with  $A_y$  and  $A_z$  characterizing the interaction distances. Note that, due to the steric restriction of MT, the position of the kinesin head is confined to the region  $y \geq y_0$ . Terms  $V_\alpha(\alpha) \equiv \exp(-|\alpha - \alpha_0|/A_\alpha)$ ,  $V_\theta(\theta) \equiv \exp(-|\theta - \theta_0|/A_\theta)$  and  $V_\phi(\phi) \equiv \exp(-|\phi - \phi_0|/A_\phi)$  denote the potential changes arising from the head rotations, with  $A_\alpha$ ,  $A_\theta$  and  $A_\phi$  characterizing the interaction distances. Here, we define  $y_0 = z_0 = \alpha_0 = \theta_0 = \phi_0 = 0$  in the MT-binding state. These potential changes  $V_y(y)$ ,  $V_z(z)$ ,  $V_\alpha(\alpha)$ ,  $V_\theta(\theta)$  and  $V_\phi(\phi)$  are similar to the Morse potential form that describes the van der Waals interaction. To be consistent with the Debye length that is in the order of 1 nm in solution, we take  $A_y = A_z = 1$  nm and  $r_{head}A_\alpha = r_{head}A_\theta = r_{head}A_\phi = 1$  nm, where the kinesin head is approximately a sphere of radius  $r_{head} = 2.5$  nm. After ATP binding and then hydrolysis to ADP.Pi the kinesin head remains bound strongly to MT, with the interaction potential still being approximately described by  $V_S(x, y, z, \alpha, \theta, \phi)$ .

Immediately after Pi release, the interaction potential becomes one that can be written as  $V_W(x, y, z, \alpha, \theta) = V_{Wx1}(x)V_y(y)V_z(z)V_\alpha(\alpha)V_\theta(\theta)V_\phi(\phi)$ , with  $V_{Wx1}(x) < 0$  being approximately shown in the inset of Fig. 1 (middle panel) and  $V_y(y)$ ,  $V_z(z)$ ,  $V_\alpha(\alpha)$ ,  $V_\theta(\theta)$  and  $V_\phi(\phi)$  being the same as those defined above. Note that immediately after Pi release the binding affinity of kinesin for the local MT-binding site at which the ADP.Pi-kinesin has just bound,  $E_{w1}$ , is weaker than at other MT-binding sites,  $E_{w2}$ . After a period of time,  $t_r$ , the affinity of the local MT-binding site for ADP-head relaxes to the normal value and the interaction potential becomes  $V_W(x, y, z, \alpha, \theta) = V_{Wx2}(x)V_y(y)V_z(z)V_\alpha(\alpha)V_\theta(\theta)V_\phi(\phi)$ , with  $V_{Wx2}(x)$  being shown approximately in the inset of Fig. 1 (lower panel). Note that the weak binding affinity of ADP-kinesin for MT,  $E_{w2}$ , is smaller than the strong binding affinity of nucleotide-free, ATP- or ADP.Pi-kinesin for MT,  $E_S$ .

## **S2. Potential of the effect of neck linker docking to the motor domain of the MT-bound head on the movement of the other ADP-head**

Structural studies showed that the N-terminal strand of motor domain,  $\beta_0$ , contributes to the docking of the strand  $\beta_9$  of the neck linker (NL) by forming a cover-neck bundle (CNB) [3]. Thus, it is assumed that only when  $\beta_0$  and  $\beta_9$  are

in proximity can CNB form. As a result, the effect of the NL docking to the MT-bound head on the motion of the detached head relative to the MT-bound head can be approximately characterized by a potential  $V_{NL}(x)$ , which has the form

$$V_{NL}(x) = E_{NL}, \quad x \leq 0, \quad (\text{S1})$$

$$V_{NL}(x) = -E_{NL}(x-1), \quad 0 < x \leq 1, \quad (\text{S2})$$

$$V_{NL}(x) = 0, \quad x > 1, \quad (\text{S3})$$

where it is considered that the MT-bound head is at position  $(x, y, z) = (0, 0, 0)$ , and  $E_{NL}$  is the free energy change of the NL docking. This form of  $V_{NL}(x)$  implies that when the detached head is in the range of  $x \leq 0$  relative to the MT-bound head,  $\beta_9$  is far away from  $\beta_0$  and CNB is unable to form, when  $x > 0$ ,  $\beta_0$  and  $\beta_9$  are in proximity and CNB can form, and when  $x > 1$ , CNB is formed and thus the NL docking is completed, allowing the detached head to move forward freely but preventing it from moving backward.

### S3. Potential of interaction between two kinesin heads

We take the potential of interaction between two kinesin heads with the NL of the MT-bound head being undocked having the following form

$$V_I(x, y, z, \alpha, \theta, \phi) = -E_{I1} \exp\left(-\frac{\sqrt{(x-x_1)^2 + (y-y_1)^2 + (z-z_1)^2}}{A_r}\right), \quad (\text{S4})$$

$$\times \exp\left(-\frac{|\alpha-\alpha_1|}{A_\alpha}\right) \exp\left(-\frac{|\theta-\theta_1|}{A_\theta}\right) \exp\left(-\frac{|\phi-\phi_1|}{A_\phi}\right)$$

where  $(x, y, z)$  is the center-of-mass coordinate of the detached ADP-head relative to that of the MT-bound head (which is taken as the origin of the coordinate) during one stepping period,  $(x_1, y_1, z_1)$  is the position of the detached ADP-head in the intermediate state,  $\alpha_1$ ,  $\theta_1$  and  $\phi_1$  are the nutation, rotation and precession angles of the detached ADP-head in the intermediate state,  $E_{I1} > 0$  is the strong interaction strength and  $A_r = 1$  nm characterizes the interaction distance. Based on the available structural data [4], we take  $\alpha_1 = 180^\circ$ ,  $\theta_1 = -80^\circ$  and  $\phi_1 = 0$  in the calculation, thus

giving  $(x_1, y_1, z_1) = 2r_{head} \times (\cos 80^\circ, \sin 80^\circ, 0)$ . Note that taking other values of  $\alpha_1$ ,  $\theta_1$  and  $\phi_1$  has nearly no effect on our results given in this work. When the NL of the MT-bound head is docked, the potential is still described by Eq. (S4), but with  $E_{I1}$  being replaced with  $E_{I2}$  ( $E_{I2} < E_{I1}$ ).

#### **S4. Interaction between the neck linker and kinesin head**

To determine the interaction between the NL and kinesin head, we should determine the elasticity of the NL by using all-atom MD simulations (see Section S5), as used elsewhere [5,6]. Here, we take the NL of wild-type *Drosophila* kinesin as an example to describe the simulation procedure. We take residues 324 through 338 from the structural data (PDB 3KIN), where residues 325 – 338 constitute the NL. We adjust the line connecting the alpha carbon (CA) atom of residue 324 and that of residue 338 along a given direction. We fix the CA atom of the residue 324 and impose a series of constant forces on the CA atom of the residue 338 along the given direction, as done before [7]. We then calculate the distance,  $r_{NL}$ , between the two terminal CAs of the NL after reaching the equilibrium for 20 ns. In the literature, the calculated data of the force–extension relation of a flexible peptide were usually fitted by using the worm-like-chain (WLC) model. However, it is noted that the simulated data of the force–extension relation of the kinesin’s NL are better fitted by using the exponential function than WLC model, especially at small values of pulling force (see Fig. S1). Thus, here we use the exponential function to fit the simulated data

$$F_{NL}(r_{NL}) = a \exp(br_{NL}), \quad (\text{S5})$$

where  $a$  and  $b$  are constants. Then the force on the detached head, which results from the stretched NL, can be calculated by using Eq. (S5).

#### **S5. All-atom MD simulations**

The all-atom MD simulations are carried out by using GROMACS5.1 [8] with OPLS-AA/L all-atom force field [9]. To avoid the edge effect, the distance between the peptide of the NL and the boundary of the box is at least 1.5 nm and much longer along the direction of the pulling force to stretch the NL. We add solvent and necessary ions with favorable concentration. Counter-ions are also added to neutralize

the system. All MD simulations are run at 300K and 1 bar. The time step is set as 2 fs, and the output data is updated every ps. All chemical bonds are constrained using LINCS algorithm [10]. The short-range electrostatics interaction and the cutoff for van der Waals interaction is set as 1 nm. Velocity-rescaling temperature coupling [11] and Berendsen pressure coupling [12] are used. The energy minimization is performed using the steepest descent method. Before the dynamic simulations, the systems are equilibrated successfully for 2 ns at 300 K and 1 bar pressure in the NVT ensemble and NPT ensemble, respectively. For calculations of the force–extension relation of the NL, after a 20-ns constant force–extension simulation, the distance between the two terminal CAs of the NL is extracted from the output trace files using the VMD1.9.2 [13].

### S6. Equation for kinesin dimer under an external force acting on the bead attached to one head

Consider a micro-meter-sized bead with diameter of  $2R_{bead}$  attached to one head of the dimer and an external force acting on the bead. For this case, the equations for the translation and rotation of the ADP-head, which is attached by the bead, relative to the other head binding fixedly to MT at position (0,0,0) can be described by following Langevin equations

$$\Gamma_x \frac{\partial x}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta)}{\partial x} - \frac{\partial V_I(x, y, z, \alpha, \theta)}{\partial x} - F_{NL} \left( \frac{r}{2} \right) \frac{x}{r} - \frac{\partial V_{NL}(x)}{\partial x} - C(x - x_{bead}) + \xi_x(t), \quad (S6)$$

$$\Gamma_y \frac{\partial y}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta)}{\partial y} - \frac{\partial V_I(x, y, z, \alpha, \theta)}{\partial y} - F_{NL} \left( \frac{r}{2} \right) \frac{y}{r} - C(y - y_{bead}) + \xi_y(t), \quad (S7)$$

$$\Gamma_x^{(bead)} \frac{\partial x_{bead}}{\partial t} = C(x - x_{bead}) + F_x + \xi_X(t), \quad (S8)$$

$$\Gamma_y^{(bead)} \frac{\partial y_{bead}}{\partial t} = C(y - y_{bead}) + F_y + \xi_Y(t), \quad (S9)$$

$$\Gamma_z \frac{\partial z}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial z} - \frac{\partial V_I(x, y, z, \alpha, \theta, \phi)}{\partial z} - F_{NL} \left( \frac{r}{2} \right) \frac{z}{r} + \xi_z(t), \quad (S10)$$

$$\Gamma_\alpha \frac{\partial \alpha}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial \alpha} - \frac{\partial V_I(x, y, z, \alpha, \theta, \phi)}{\partial \alpha} + \xi_\alpha(t), \quad (S11)$$

$$\Gamma_\theta \frac{\partial \theta}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial \theta} - \frac{\partial V_I(x, y, z, \alpha, \theta, \phi)}{\partial \theta} + \xi_\theta(t), \quad (S12)$$

$$\Gamma_\phi \frac{\partial \phi}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial \phi} - \frac{\partial V_I(x, y, z, \alpha, \theta, \phi)}{\partial \phi} + \xi_\phi(t). \quad (\text{S13})$$

where for simplicity but without loss of generality, the motion of the bead in the  $z$ -coordinate is not considered, as done in Eqs. (1) – (12). The initial conditions for Eqs. (S6) – (S13) are:  $(x_0, y_0, z_0, \alpha_0, \theta_0, \phi_0) = (-d, 0, 0, 0, 0, 0)$ ,  $x_{bead0} = -d + F_x/C$  and  $y_{bead0} = F_y/C$ . For the ADP-head that is not attached by the bead, its translation motion relative to the other head binding fixedly to MT at position (0,0,0) can still be described by Eqs. (S6), (S7) and (S10) but with  $C = 0$  and its rotation can still be described by Eqs. (S11) – (S13). Here, we still consider the linker connecting the head and bead has a length  $l = l_{kinesin} = 54$  nm. Thus, For the longitudinal or  $x$ -component of the external force,  $F_x$ , the vertical or  $y$ -component is still calculated by  $F_y = |F_x| \tan \Theta_0$  and  $\sin \Theta_0 = R_{bead} / (R_{bead} + l_{kinesin})$ , with  $2R_{bead} = 0.44 \mu\text{m}$ .

In the intermediate state, where the two ADP-heads bind together strongly, the equations for the translation and rotation of the MT-bound ADP-head relative to MT can be described by following Langevin equations

$$\Gamma_x \frac{\partial x}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial x} - C(x - x_{bead}) + \xi_x(t), \quad (\text{S14})$$

$$\Gamma_y \frac{\partial y}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial y} - C(y - y_{bead}) + \xi_y(t), \quad (\text{S15})$$

$$\Gamma_x^{(bead)} \frac{\partial x_{bead}}{\partial t} = C(x - x_{bead}) + F_x + \xi_X(t), \quad (\text{S16})$$

$$\Gamma_y^{(bead)} \frac{\partial y_{bead}}{\partial t} = C(y - y_{bead}) + F_y + \xi_Y(t), \quad (\text{S17})$$

$$\Gamma_z \frac{\partial z}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial z} + \xi_z(t), \quad (\text{S18})$$

$$\Gamma_\alpha \frac{\partial \alpha}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial \alpha} + \xi_\alpha(t), \quad (\text{S19})$$

$$\Gamma_\theta \frac{\partial \theta}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial \theta} + \xi_\theta(t), \quad (\text{S20})$$

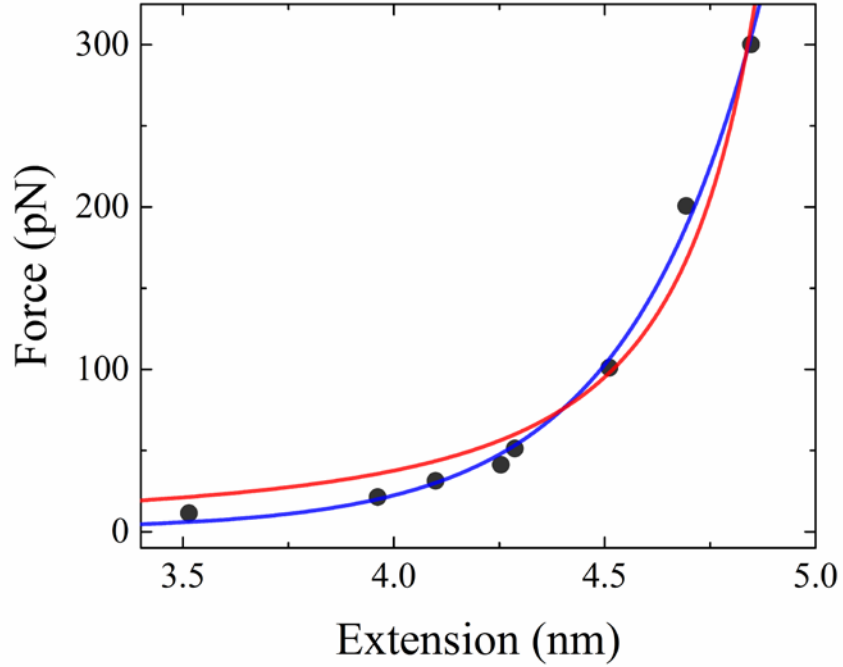
$$\Gamma_\phi \frac{\partial \phi}{\partial t} = -\frac{\partial V_W(x, y, z, \alpha, \theta, \phi)}{\partial \phi} + \xi_\phi(t), \quad (\text{S21})$$

where, for simplicity of treatment, the head and bead are implicitly considered to be

rigidly connected. The initial conditions for Eqs. (S14) – (S21) are:  
 $(x_0, y_0, z_0, \alpha_0, \theta_0, \phi_0) = (0, 0, 0, 0, 0, 0)$ ,  $x_{bead0} = F_x/C$  and  $y_{bead0} = F_y/C$ .

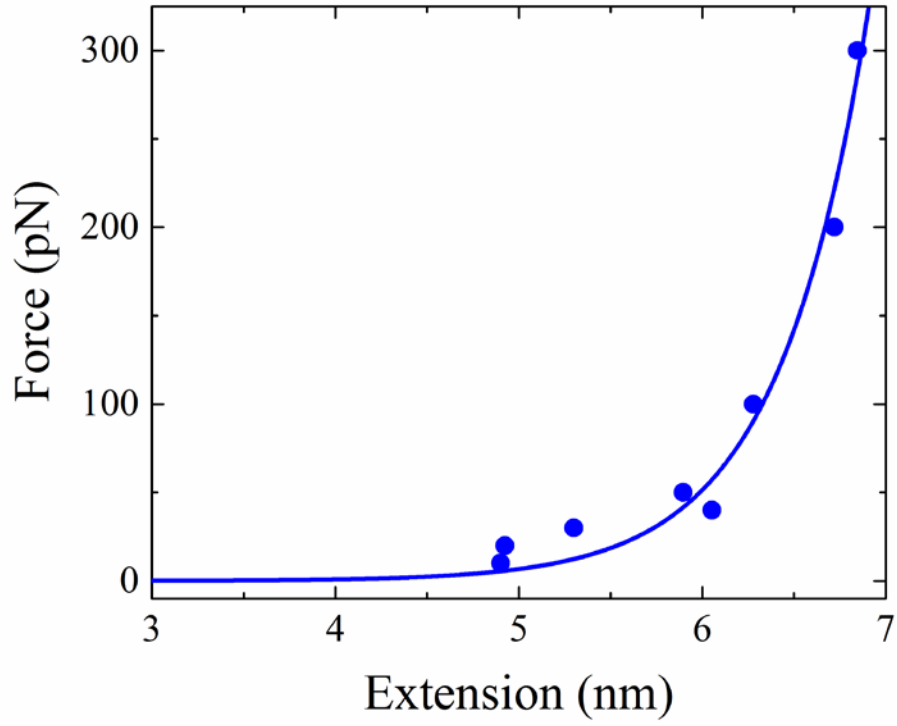
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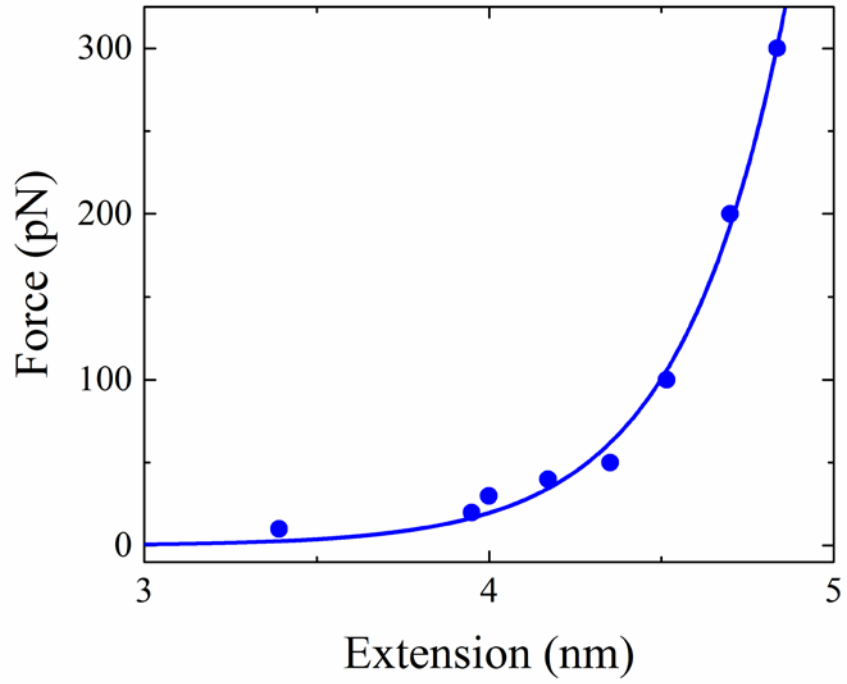


**Fig. S1. Force–extension relation of the neck linker of DmK-WT head.** Dots represent the results obtained by using all-atom MD simulations. Red lines is the fit curve with WLC model,  $f(x) = k_B T / (4L_p) \left[ (1 - x/L_c)^{-2} - 1 + 4x/L_c \right]$ , where the contour length  $L_c = 5.26$  nm and the persistence length  $L_p = 0.56$  nm. Blue line is the fit curve with Eq. (S5),  $F_{NL}(r_{NL}) = a \exp(br_{NL})$ , with  $a = 7.064 \times 10^{-5}$  pN and  $b = 3.148 \text{ nm}^{-1}$ .

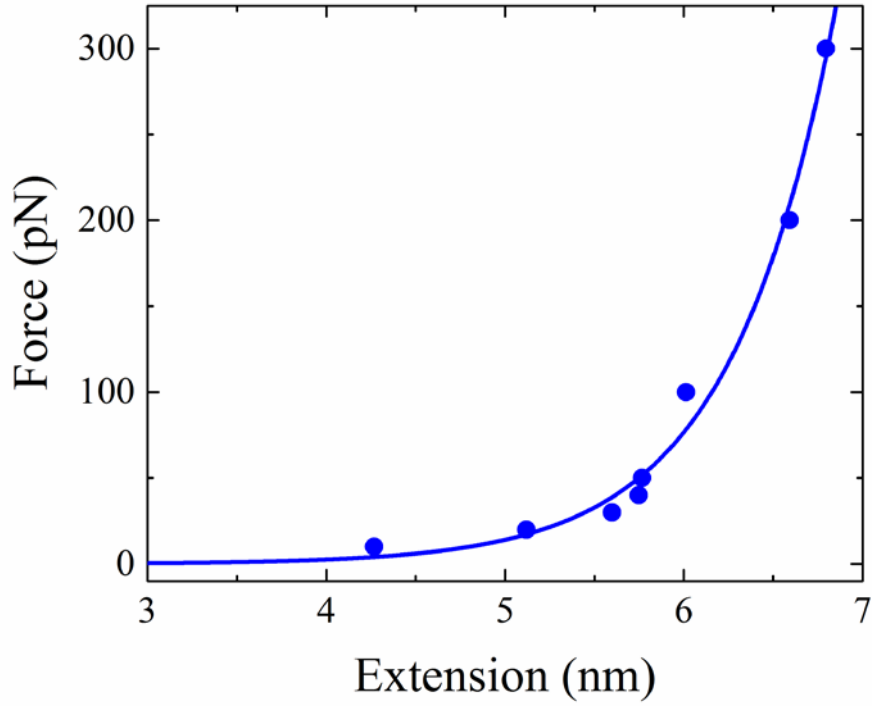




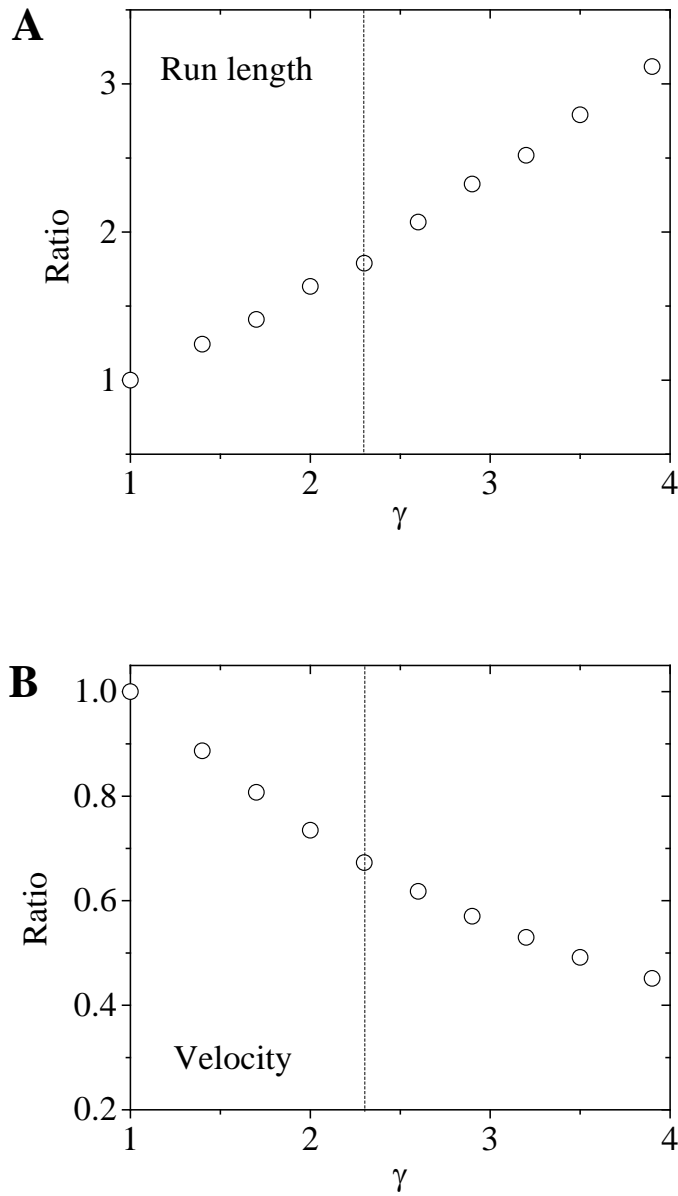
**Fig. S2. Force–extension relation of the neck linker of DmK-6AA head.** Dots represent the results obtained by using all-atom MD simulations. Line is the fit curve with Eq. (S5),  $F_{NL}(r_{NL}) = a \exp(br_{NL})$ , with  $a = 2.623 \times 10^{-4}$  pN and  $b = 2.031 \text{ nm}^{-1}$ .



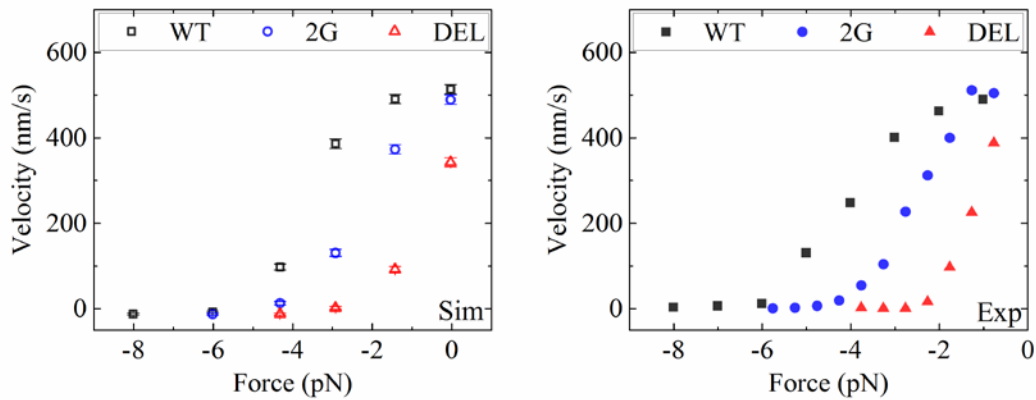
**Fig. S3. Force–extension relation of the neck linker of HsK-CL head.** Dots represent the results obtained by using all-atom MD simulations. Line is the fit curve with Eq. (S5),  $F_{NL}(r_{NL}) = a \exp(br_{NL})$ , with  $a = 4.226 \times 10^{-5}$  pN and  $b = 3.263 \text{ nm}^{-1}$ .



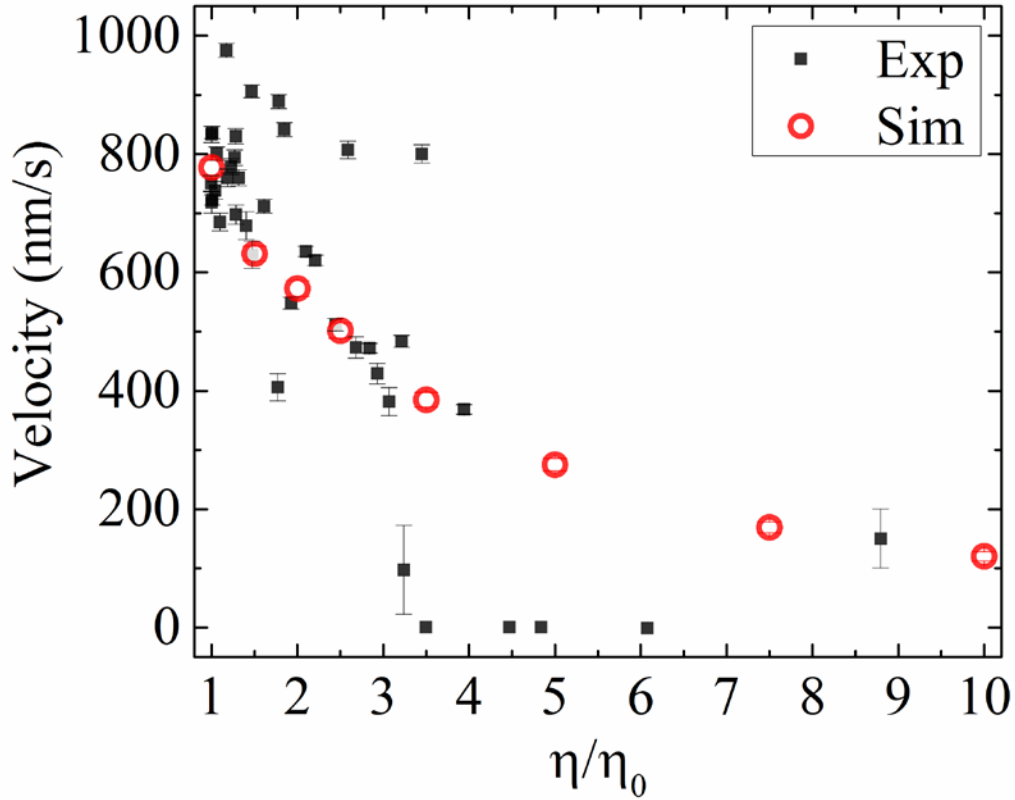
**Fig. S4. Force–extension relation of the neck linker of HsK-CL-6AA head.** Dots represent the results obtained by using all-atom MD simulations. Line is the fit curve with Eq. (S5),  $F_{NL}(r_{NL}) = a \exp(br_{NL})$ , with  $a = 2.936 \times 10^{-3}$  pN and  $b = 1.695 \text{ nm}^{-1}$ .



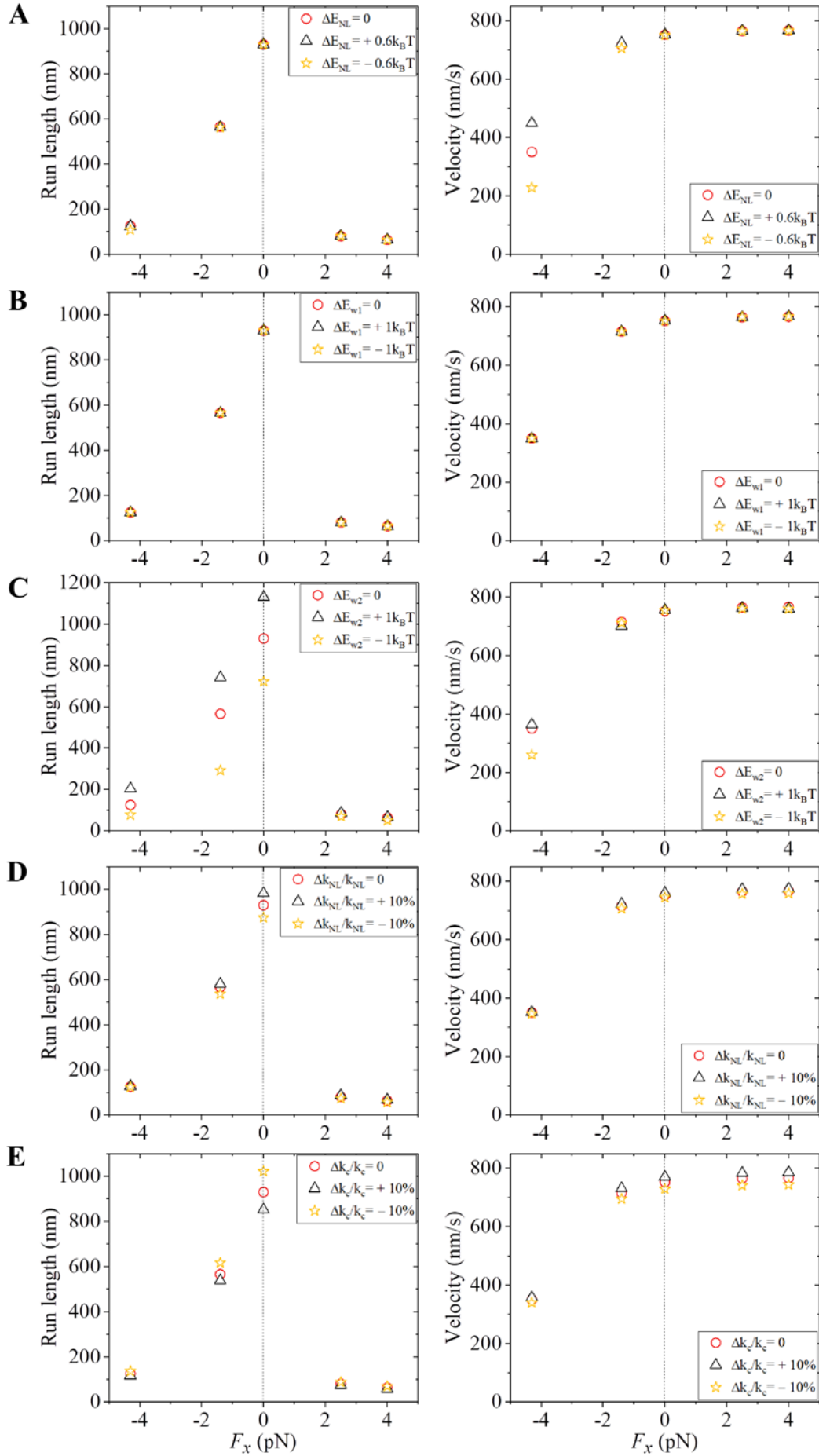
**Fig. S5. Effects of the presence of additional Pi in solution on run length and velocity of DmK-WT at saturating ATP. (A)** Ratio of the calculated run length in the presence of additional Pi to that without the additional Pi at  $F_x = 4$  pN as a function of  $\gamma$ . The vertical broken line corresponds to  $\gamma = 2.3$ . **(B)** Ratio of the calculated velocity in the presence of additional Pi to that without the additional Pi at  $F_x = 4$  pN as a function of  $\gamma$ . The vertical broken line corresponds to  $\gamma = 2.3$ .



**Fig. S6. Effect of the neck linker docking on the velocity of kinesin-1.** The panels show the velocity versus longitudinal component ( $F_x$ ) of the external force for WT, 2G-mutant and DEL. WT refers to the wild-type kinesin-1, 2G-mutant refers to mutant kinesin-1 with A9G and S12G mutations in the N-terminal cover strand that is responsible for the NL docking, and DEL refers to mutant kinesin-1 lacking the entire N-terminal cover strand, as used in the single molecule experiments of Khalil et al. [14]. Here it is considered that the NL docking still occurs in the mutant heads, weakening the interaction between the two heads, but the mutations reduce the NL-docking energy  $E_{NL}$ . Values of parameters are taken as follows:  $E_{NL} = 4.5k_B T$  for WT,  $E_{NL} = 2.5k_B T$  for 2G-mutant and  $E_{NL} = 0$  for DEL; other parameters are the same as those for DmK-WT in Fig. 2 except  $k_c = 82 \text{ s}^{-1}$ . Left panel corresponds to our simulation results and the right panel corresponds to the experimental data taken from Khalil et al. [14].



**Fig. S7. Effect of the solution viscosity  $\eta$  on the velocity of kinesin-1.** The panel shows the velocity versus  $\eta/\eta_0$ , where  $\eta_0$  is the solution viscosity in the vicinity of MT. In the experiments of Sozański et al. [15], no bead is attached to the coiled-coil. This is equivalent to taking spring constant,  $C = 0$ , for the connection between the bead and C-terminus ends of the NLs in our calculations using Eqs. (1) – (12). Values of parameters are the same as those for HsK-CL in Fig. 4 except  $k_c = 240 \text{ s}^{-1}$ . Unfilled symbols are calculated data, and filled symbols are experimental data taken from Sozański et al. [15].



**Fig. S8. The sensitivity of the calculated run length and velocity to the relevant parameters for DmK-WT.** Left panels are results of run length versus longitudinal component ( $F_x$ ) of the external force, while right panels are results of velocity versus  $F_x$ . **(A)** Effects of changing  $E_{NL}$ . Circles are data calculated with parameter values given in Table 1. Triangles and stars are data calculated with value of  $E_{NL}$  increased and decreased by  $0.6k_B T$ , respectively, while other parameter values are kept unchanged. **(B)** Effects of changing  $E_{w1}$ . Circles are data calculated with parameter values given in Table 1. Triangles and stars are data calculated with value of  $E_{w1}$  increased and decreased by  $1k_B T$ , respectively, while other parameter values are kept unchanged. **(C)** Effects of changing  $E_{w2}$ . Circles are data calculated with parameter values given in Table 1. Triangles and stars are data calculated with value of  $E_{w2}$  increased and decreased by  $1k_B T$ , respectively, while other parameter values are kept unchanged. **(D)** Effects of changing  $k_{NL}$ . Circles are data calculated with parameter values given in Table 1. Triangles and stars are data calculated with value of  $k_{NL}$  increased and decreased by 10%, respectively, while other parameter values are kept unchanged. **(E)** Effects of changing  $k_c$ . Circles are data calculated with parameter values given in Table 1. Triangles and stars are data calculated with value of  $k_c$  increased and decreased by 10%, respectively, while other parameter values are kept unchanged.