Article

Fold-Change Detection of NF-κB at Target Genes with Different Transcript Outputs

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ABSTRACT The transcription factor nuclear factor (NF)-κB promotes inflammatory and stress-responsive gene transcription across a range of cell types in response to the cytokine tumor necrosis factor (TNF). Although NF-κB signaling exhibits significant variability across single cells, some target genes supporting high levels of TNF-inducible transcription exhibit fold-change detection of NF-κB, which may buffer against stochastic variation in signaling molecules. It is unknown whether fold-change detection is maintained at NF-κB target genes with low levels of TNF-inducible transcription, for which stochastic promoter events may be more pronounced. Here, we used a microfluidic cell-trapping device to measure how TNF-induced activation of NF-κB controls transcription in single Jurkat T cells at the promoters of integrated *HIV* and the endogenous cytokine gene *IL6*, which produce only a few transcripts per cell. We tracked TNF-stimulated NF-κB RelA nuclear translocation by live-cell imaging and then quantified transcript number by RNA FISH in the same cell. We found that TNF-induced transcript abundance at 2 h for low- and high-abundance target genes correlates with similar strength with the fold change in nuclear NF-κB. A computational model of TNF-NF-κB signaling, which implements fold-change detection from competition for binding to κB motifs, could reproduce fold-change detection across the experimentally measured range of transcript outputs. However, multiple model parameters affecting transcription had to be simultaneously varied across promoters to maintain fold-change detection while also matching other trends in the single-cell data for low-abundance transcripts. Our results suggest that cells use multiple biological mechanisms to tune transcriptional output while maintaining robustness of NF-κB fold-change detection.

INTRODUCTION

Tumor necrosis factor (TNF) acts on a wide range of cell types and is a critical mediator of inflammatory and stress responses (1) and of the development of certain immune cells, including T lymphocytes (2,3). TNF stimulation activates a signaling cascade that disrupts the interaction between the transcription factor nuclear factor-κB (NF-κB) and the inhibitor of NF-κB α (IκBα), thereby releasing NF-κB and allowing it to accumulate in the nucleus. NF-κB can then regulate the expression of hundreds of genes, including those encoding its own negative regulators IκBα (*NFKBIA*) and A20 (*TNFAIP3*) and inflammatory cytokines TNF (*TNFA*) and IL-6 (*IL6*) (4). Given its central role in development and immunity, understanding how cells decode responses to TNF signals is of fundamental interest.

Dynamic signaling and response measurements from single cells provide direct information about input-output signal-response functions (5,6). By measuring dynamic nuclear translocation of the NF-κB RelA subunit and transcription in the same single cells, we previously demonstrated that the maximal fold change in nuclear RelA predicts transcript abundance of *NFKBIA*, *TNFAIP3*, and *IL8* after TNF treatment in HeLa cells, a cell line of epithelial origin (7). This observation had significant implications for our understanding of RelA-mediated signaling in these cells because only two signaling circuits commonly observed in biological systems allow for fold-change detection (8). One is an incoherent type 1 feed-forward loop (I1-FFL), in which a molecular species increases with the input and also inhibits the output (9). By adapting a mathematical model of TNF-stimulated NF-κB RelA signaling (10), we showed that we could accurately reproduce fold-change detection for the measured RelA target genes by incorporating an I1-FFL

mechanism via competition for binding to κB motifs (7). However, the generality of this mechanism across cell types and promoters has not been explored.

NF-κB is also a positive transcriptional regulator of human immunodeficiency virus-1 (HIV), which infects CD4+ T cells (11). We recently observed that TNF-activated NF-κB deterministically controls activation of an HIV reporter, even for latent viruses with very low TNF-inducible transcription (12). Interestingly, we observed significant differences in TNF-induced recruitment of RNA polymerase II at the promoters of these low-abundance HIV target genes in Jurkat cells as compared to the high-abundance target *NFKBIA* (12). Therefore, we were interested to see whether the transcription of low-abundance target genes also exhibited fold-change detection and whether the I1-FFL model of NF-κB-mediated transcription could accurately describe the HIV transcription patterns we observed in T cells.

These questions are challenging to address in T cells with a single-cell approach because T cells do not adhere to surfaces and are therefore difficult to track when perturbed. Consequently, we developed a workflow whereby we immobilized Jurkat T cells within a microfluidic cell trap array (13) and then tracked NF-κB RelA nuclear translocation by live-cell imaging and quantified transcript number by fluorescence in situ hybridization of single messenger RNAs (smFISH) in the same cell. Using this workflow, we measured how TNF-induced activation of NF-κB controls transcription in single Jurkat T cells across diverse NF-κB target promoters, including HIV and endogenous regulatory and cytokine genes, exhibiting a range of TNF-inducible transcript levels.

We found that all measured NF-κB target promoters responded to TNF-stimulated fold change in nuclear RelA, even for transcripts induced at an average messenger RNA (mRNA) level of six or fewer transcripts per cell after 2 h of TNF treatment. Our computational model of RelA signaling, with I1-FFL topology downstream of RelA, accurately recapitulated fold-change detection at low-abundance genes but only if multiple model parameters affecting transcription were varied simultaneously. Different trends in the single-cell data served to constrain the model parameter space. Our results suggest that cells use multiple biological mechanisms to tune transcriptional output while maintaining robustness of NF-κB fold-change detection.

MATERIALS AND METHODS

Cell culture and pharmacological treatments

Jurkat T cell clones J65c 4.4 and 6.6 were created as previously described (12). Each cell line contains the same retroviral integration of a full-length human RelA fused at its N-terminus to mCherry (Ch-RelA) and a unique integration of a full-length, non-replication-competent reporter virus construct (psLTR-Tat-GFP) in which Nef has been replaced with green fluorescent protein (GFP) and the open reading frames of all other viral proteins

except Tat are disrupted with premature stop codons. J65c cells were cultured in Roswell Park Memorial Institute 1640 (RPMI) medium (Thermo Fisher Scientific, Waltham, MA). All media were supplemented with 10% fetal bovine serum (Atlanta Biologicals, Flowery Branch, GA), 100 U/mL penicillin, and 100 μg/mL streptomycin (Thermo Fisher Scientific). Cells were maintained in 5% CO_2 at 37°C and were never cultured beyond passage 12. J65c cells were grown to 5×10^5 cells/mL before treatment with recombinant human TNF (Peprotech, Rocky Hill, NJ). As in a previous study, we used 160 ng/mL cycloheximide (CHX; Sigma, St. Louis, MO) to block HIV Tat protein production and the resulting amplification of HIV gene expression (12) and to restrict our analysis to RelA-mediated transcription. This level of CHX is very low and does not change TNF-stimulated RelA translocation dynamics (Fig. S1 A), nor does it affect viability under our imaging conditions (no increased cell death was observed for CHX-treated cells versus untreated cells in our time-lapse images). For consistency, we used these same conditions throughout this study, irrespective of which transcript was assayed.

Microfluidic device fabrication

The silicon master was etched as previously described (13). After silanization (see (13) for conditions), a mixture of polydimethylsiloxane (PDMS) base and curing agent (Sylgard 184 Elastomer kit; Dow Corning, Midland, MI) was mixed 10:1 by weight and poured over the master. This was degassed and cured for 2 h at 75°C. The cured PDMS mold was peeled from the master and cut to fit a #1 glass coverslip. A 7 mm Harris Uni-Core punch (Ted Pella, Redding, CA) was used to punch holes for reservoirs at the inlet and outlet ports. A #1 25 × 75 mm microscope coverslip was rinsed with isopropanol and dried and cleared of dust with filtered air before being placed inside a PE-25 benchtop plasma cleaner (Plasma Etch) with the mold. The coverslip and PDMS mold were exposed to O_2 plasma at 150 W, 200 mTorr for 2 min and adhered immediately upon removal from the plasma chamber. The channel and the inlet and outlet reservoirs were filled with deionized water to maintain hydrophilic surfaces.

Cell loading protocol

For each experiment, 5×10^6 cells were suspended in 1 mL of fresh RPMI medium before being loaded into the microfluidic device. Cell clumps were dispersed immediately before loading by pipetting the cell suspension vigorously and filtering cells through a 35 μm nylon mesh strainer cap tube (BD Falcon; BD Biosciences, Bedford, MA). 50 μL of cells was loaded into the inlet and allowed to flow through the channel for 10 min. Flow-through medium in the outlet was first removed to prevent backflow that can dislodge cells. The cell suspension was then removed from the inlet by gently scraping the bottom of the inlet reservoir with a pipette while withdrawing the medium. 100 μL of medium was added to the inlet to wash the cells for 3 min to remove any free-floating cells from the main channel and the inlet and outlet reservoirs; this wash step was repeated three times. 50 μL medium was added only to the inlet after final wash to ensure continuous flow and the device was moved onto the microscope stage for imaging and stimulation (see below). The continuous flow was maintained throughout imaging to prevent cells from dislodging from the traps.

Live-cell imaging

Cells were imaged on a Nikon Eclipse Ti spinning disk confocal microscope (Yokogawa CSU-W1 spinning disk) with a plan apochromatic 60× oil objective (numerical aperture [NA] 1.4; Nikon, Tokyo, Japan). Ch-RelA was excited with a 561 nm laser at 20–30% power, and images were collected with an Andor iXon Ultra888 EMCCD camera (Andor Technology, Belfast, Northern Ireland). Live-cell imaging was performed on an

TABLE 1 smFISH Probe Sets

	Probe (5′-3′) env-GFP		Probe (5′-3′) NFKBIA		Probe (5′-3′) TNFAIP3		Probe (5′-3′) IL6
1	aggatccgttcactaatcga	1	agtagccgctccttcttcag	1	atacaaagcctgaggaagga	1	ggggttgagactctaatatt
2	cagatcgtcccagataagtg	2	tcgtctttcatggagtccag	2	acagctttccgcatattgct	2	atctccagtcctatatttat
3	tagctgaagaggcacaggct	3	cttgaccatctgctcgtact	3	gtgtatcggtgcatggtttt	3	gagggcagaatgagcctcag
4	agagtaagtctctcaagcgg	4	atgatggccaagtgcaggaa	4	ggcaagttctgaacatttcc	4	ttctctttcgttcccggtgg
5	tccacaatcctcgttacaat	5	ggtcagtgccttttcttcat	5	tcccgaaactgaggacaaaa	5	gctcctggaggggagataga
6	caccaatatttgagggcttc	6	ttcacctggcggatcacttc	6	ttttctgtcgatgagggcttt	6	tggagaaggagttcatagct
7	tcctgactccaatactgtag	7	agttgaggaaggccaggtct	7	agtttcttctggctttccag	7	agaaggcaactggaccgaag
8	tatggctgtggcattgagca	8	agtctgctgcaggttgttct	8	tactgagaagtggcatgcat	8	aaggcagcaggcaacaccag
9	cttctataaccctatctgtc	9	tcagcaatttctggctggtt	9	taccaagtctgtgtcctgaa	9	cggctacatctttggaatct
10	agctctataagctgcttgta	10	atttcctcgaaagtctcgga	10	ttgcgtgtgtctgtttcctt	10	aagaggtgagtggctgtctg
11	tattcttctaggtatgtggc	11	ttggtagccttcaggatgga	11	cagttgccagcggaatttaa	11	atttgtttgtcaattctgtt
12	gcaccggtcttatagcaaaa	12	tagacacgtgtggccattgt	12	cccgtttcaacacaattcctg	12	agatgccgtcgaggatgtac
13	tcctcgcccttgctcaccat	13	tagccatggatagaggctaa	13	cagttccgagtatcatagca	13	atgtctcctttctcagggc
14	gggcaccacccggtgaaca	14	attttgcaggtccactgcga	14	gtctgtggaagccattttga	14	tcacacatgttactcttgtt
15	cgccgtccagctcgaccagg	15	acacttcaacaggagtgaca	15	ttgtactgaagtccacttcg	15	ttctgccagtgcctctttgc
16	ctgaacttgtggccgtttac	16	taactctgttgacatcagcc	16	gaggatgttgcaaaggacaa	16	tctttggaaggttcaggttg
17	gccctcgccctcgccggaca	17	tagggagaatagccctggta	17	ggaacctgattccaaacttc	17	aagcatccatcttttttcagc
18	tcagcttgccgtaggtggca	18	ttttctagtgtcagctggcc	18	attccacccactttcaaagg	18	ctcctcattgaatccagatt
19	gtggtgcagatgaacttcag	19	actctctggcagcatctgaa	19	atggggtatctgtagcattc	19	tgatgatttttcaccaggcaa
20	ccagggcacgggcagcttgc	20	tgtgtcatagctctcctcat	20	aaatgatggctgtcatagcc	20	acctcaaactccaaaagacc
21	tcagggtggtcacgagggtg	21	tgaactccgtgaactctgac	21	aagtggaacagctcggattt	21	tgttctggaggtactctagg
22	ctgaagcactgcacgccgta	22	aacacacagtcatcataggg	22	aagtcttcaaatcttccccg	22	tgttcctcactactctcaaa
23	cttcatgtggtcggggtagc	23	ataacgtcagacgctggcct	23	cggggatttctatcaccatt	23	tactcatctgcacagctctg
24	cggacttgaagaagtcgtgc	24	atgttctttcagcccctttg	24	atgagatgagttgtgccatg	24	caggaactggatcaggactt
25	tggacgtagccttcgggcat	25	gtgtgtggatataagtacaccc	25	ttcatccaactttgcggcat	25	gggtggttattgcatctaga
26	cttgaagaagatggtgcgct	26	aataagacgttttgggccag	26	gccatttcttgtactcatgc	26	gctggcatttgtggttgggt
27	gggtcttgtagttgccgtcg	27	aaaatgagggctgatcctac	27	ttcacagacatgaagaaggg	27	tggttctgtgcctgcagctt
28	ccctcgaacttcacctcggc	28	gtcccctacaaaaagttcac	28	tgagcactcatggcataaag	28	tgagatgagttgtcatgtcc
29	gatgcggttcaccagggtgt	29	ggtgaggtttaaaagaagtt	29	tttgattcttttgccgcctc	29	aactccttaaagctgcgcag
30	ttgaagtcgatgcccttcag	30	aaccttctccaaaaacccca	30	gagttcagctttgggagttt	30	catgctacatttgccgaaga
31	ccccaggatgttgccgtcct	31	gtggtccttccatgaaattt	31	tcactgaacagaaaagggct	31	aacaacaacaatctgaggtg
32	tgtagttgtactccagcttg	32	cagtcactcgaagcacaata	32	tgctgcacattcagtgtgaa	32	acaggtttctgaccagaaga
33	catgatatagacgttgtggc	33	atgtcacaggataccactgg	33	gcaacgttcacaaaatccgt	33	aacataagttctgtgcccag
34	tgccgttcttctgcttgtcg	34	gcttaacactcctggctgtt	34	aatgtcctggtaacatcctg	34	cgctcatactttttagttctc
35	cggatcttgaagttcacctt	35	ttttcaccccacatcactga	35	tgaagcaagtactgcagatc	35	cttacataaattaactcagc
f36	gctgccgtcctcgatgttgt	36	cacaaaccttgacaggtagt	36	tctggagtcccaaaatacac	36	caaactgcatagccactttc
37	tggtagtggtcggcgagctg	37	tacaccatttacaggagggt	37	aaacacagtgtgcaaaagcc	37	ccaagaaatgatctggctct
38	gtcgccgatggggggtgttct	38	gtaccaaaataattaccaac	38	tcaaacatggtgcttccaag	38	atttgaggtaagcctacact
39	ttgtcgggcagcagcacggg	–	–	39	gaaacacttctggcagtatc	39	aaaatatgtataagttagcc
40	ggactgggtgctcaggtagt	–	–	40	ggcctcatgaaatctctgat	–	–
41	cgttggggtctttgctcagg	–	–	41	tcagttgctcttctgtcctt	–	–
42	aggaccatgtgatcgcgctt	–	–	42	ttgaggtgctttgtgtggtt	–	–
43	ggcggcggtcacgaactcca	–	–	43	ttgccaaaatgatcacaggc	–	–
44	tcgtccatgccgagagtgat	–	–	44	aaagcattcgttgcagtagc	–	–

environmentally controlled stage at 37°C and 5% CO_2 (Tokai Hit, Fujino-miya, Japan). Once the loaded device was secured to the stage insert, five regions of interest were identified, and their positions relative to fiducial markers on the outside of the channel were recorded. 12 μm Z-stacks with 1 μm slices were recorded for each position as a reference image. Fluid was removed from the outlet and then inlet, and 50 μL of RPMI medium containing TNF was added to the inlet and imaging immediately started. Based on our previous study, we estimated that TNF flows through the entire length of the channel within 30 s and that 50 μL of media was sufficient to maintain a nearly constant flow velocity of ∼300 μm/s for 2 h (13). 12 μm Z-stacks of each region of interest were recorded every 3 min for 110 min after stimulation; using Z-stacks ensured that we captured the nuclear signal near the cell equator even as cells moved in the z axis during imaging. Nikon Perfect Focus autofocus system was used to identify the same Z slice for every time point. After 110 min of imaging, cells were fixed by removing fluid from the outlet and then inlet and replacing with 50 μL of 4% formaldehyde in phosphate-buffered saline (PBS) for fixation before in situ hybridization.

smFISH

Stellaris RNA FISH probe sets (Biosearch Technologies, Novato, CA) targeting NFKBIA/IκBα, TNFAIP3/A20, env-GFP/HIV, and GAS6 were previously described (7,12,14). The IL6/IL-6 probe set was designed using online software (https://www.biosearchtech.com/) and previously described strategies (7,15). Probes for env-GFP, NFKBIA, and IL6 were conjugated to carboxyfluorescein; probes for TNFAIP3 and GAS6 were conjugated to Quasar 670. Probe sets for the main targets are included in Table 1.

After fixation in the passive-flow device, cells were washed three times with PBS, allowing the buffer to flow through the device for 3 min for each wash. Cells were permeabilized by adding 150 μL of 70% ethanol

to the inlet and 50 μL of 70% ethanol to the outlet and placing the device for 16 h at 4°C. After permeabilization, cells were washed three times with PBS and then incubated with 10% formamide (Thermo Fisher Scientific) in 2× saline sodium citrate (SSC; Thermo Fisher Scientific) for 30 min at 37°C. Cells were hybridized by adding 50 μL of indicated probes (concentrations discussed below) in buffer containing 2× SSC, 10% formamide, and 100 mg/mL dextran sulfate (M_W > 500,000; Millipore, Burlington, MA) at 37°C in the dark for 12 h. Cells were washed twice with 10% formamide in 2× SSC. Finally, cells were counterlabeled with 1 μg/mL Hoechst 33342 (Thermo Fisher Scientific) and imaged in either PBS or VectaShield mounting media (Vector Labs, Peterborough, UK).

We note here that a key practice to minimize the loss of flow and cells during the smFISH protocol was to implement a simple stepwise procedure that would minimize the loss of hydrostatic pressure in the microfluidic system during fluid replacement. At every buffer exchange step, the outlet was emptied first, and then the inlet was emptied and immediately refilled with the new buffer to reestablish flow. All solutions, including the viscous hybridization buffer, passed through the channel and could be displaced within 60 s by addition of a subsequent solution (Fig. S1 B). We confirmed that the multiple incubation and wash steps did not result in significant cell loss (Fig. S1 C).

Labeled cells were imaged on a Nikon Eclipse Ti spinning disk confocal microscope with a plan apochromatic 100× oil objective (NA 1.45; Nikon). Regions of interest imaged in the live-cell imaging step were reidentified using the fiducial markers. For each field, we acquired Z-stacks of 30–60 images with 0.3 μm intervals.

Implementing the smFISH protocol in the device, we found that moderate probe concentrations (100–200 nM) yielded labeling comparable to that achieved with cells on a dish; higher probe concentrations (500 nM) resulted in high background and the loss of distinct spots (Fig. S1 D). In addition, both in conventional culture and in the device, we found very low nonspecific probe binding when performing labeling for transcripts of GAS6, a gene not normally expressed in Jurkat cells (16) (200 nM probes; Fig. S1 E). Finally, validating the specificity of the env-GFP probe set, we found very few foci in parental Jurkat cells (averaging to <0.3 per cell; Fig. S1 F).

Image analysis

The Z-center for each cell was manually identified, and the mean fluorescence intensity (MFI) for nuclear Ch-RelA in this slice was quantified at every time point. Background was determined by measuring the MFI of an area equivalent to the cell nucleus but in an area of the channel with no objects in the same slice. The background MFI was then subtracted from the nuclear MFI. Cells that were displaced from the traps or divided during imaging were not analyzed. The features for Ch-RelA nuclear translocation were extracted from live-cell time courses as previously reported (7,12). Fixed cells with labeled transcripts were registered to live cells based on fiducial markers. Cell outlines were traced manually, and transcripts were identified and counted using FISH-Quant software (17) as previously described (12).

Chromatin immunoprecipitation

EZ ChIP Kit (Upstate) reagents and protocols were used as described previously (12). 15×10^6 cells were fixed in 1% formaldehyde for 10 min. Unreacted formaldehyde was quenched with 125 mM glycine for 5 min. Cells were washed three times with PBS and lysed with 1% sodium dodecyl sulfate lysis buffer in the presence of cOmplete protease inhibitor cocktail (Roche, Basel, Switzerland). Lysed cells were sonicated with a Diagenode Bioruptor (settings: seven cycles of 5 min per cycle with 30 s pulses followed by 30 s of incubation at a high power). Samples were precleared with Protein G agarose (Millipore), and 1% of each sample was used as a percent input. Samples were incubated with antibody for 16 h at 4°C. Protein G agarose was then added to the samples and incubated for 1 h at 4°C. Beads were washed once each with low salt, high salt, and LiCl immune

complex wash buffers included in the kit, and then washed twice with 10 mM Tris, 1 mM EDTA (pH 8.0). DNA-protein complexes were eluted from agarose beads with 1% sodium dodecyl sulfate and 100 nM NaHCO$_3$. Crosslinks were reversed by incubating samples with 5 M NaCl overnight at 65°C. DNA was purified with DNA spin filters and eluted with 10 mM Tris, 1 mM EDTA (pH 8.0). DNA was quantified by quantitative PCR (iCycler, iQ5; BioRad, Hercules, CA) using SYBR Green Supermix (BioRad). qPCR was performed in triplicate, and melt curves were run to ensure product specificity. Antibodies and primers are listed in Table 2.

Computational modeling

To make predictions about fold-change detection, RelA promoter binding, and transcript variance across a range of target transcriptional outputs, we used a previously reported computational model of TNF-RelA signaling (7) (Fig. S2; Table S1). Ensemble simulations that included sampling to mimic cell-to-cell variability were run using the ode15s solver in MATLAB (The MathWorks, Natick, MA). Sensitivity analyses and the five-dimensional parameter scan were run using a Fortran encoding of the same model and the DLSODE solver, with outputs plotted in MATLAB.

Briefly, the transcription rate of the RelA inducible target promoter is given by the following ordinary differential equation:

$$\frac{d[tIndTarget]}{dt} = FB \times c1t - c3t[tIndTarget], \quad (1)$$

in which the transcript synthesis rate $c1t$ is modified by the fractional binding (FB) of nuclear RelA ($nNF\kappa B$) to the target promoter and the target transcript ($tIndTarget$) is degraded at a rate $c3t$. Fractional binding of $nNF\kappa B$ depends on the affinity of RelA for the target promoter (k), the concentration of the competitor protein ($Comp$), the affinity of the competitor for the target promoter ($k3$), and the Hill coefficient (ht), which effectively varies the steepness of the change in transcriptional response over a range of $nNF\kappa B$ concentrations:

$$FB = \frac{\left(\frac{[nNF\kappa B]}{k}\right)^{ht}}{\left(\frac{[nNF\kappa B]}{k}\right)^{ht} + \left(\frac{[Comp]}{k3}\right)^{ht} + 1}. \quad (2)$$

For the sensitivity analysis, the normalized local sensitivity index was calculated for features of both nuclear RelA ($nNF\kappa B$; initial, F_{init}, maximal, F_{max}, and fold change, F_{max}/F_{init}) and the target transcript ($tIndTarget$; initial, $mRNA_{init}$, maximal, $mRNA_{max}$, at $t = 2$ h, $mRNA_{t = 2h}$, and fold change, $mRNA_{max}/mRNA_{init}$) using the following:

$$\widetilde{S}_i = \left(\frac{\partial Feature}{\partial k_i}\right)_{k_{jnom}} \times \frac{k_{inom}}{Feature_{nom}}. \quad (3)$$

TABLE 2 Antibody and Primers Used in ChIP Assays

Antibody	Source	Catalog #
anti-NF-κB p65 rabbit monoclonal	Cell Signaling	8242

Primers	Sequence (5′-3′)
5′ HIV LTR forward	TGCATCCGGAGTACTTCAAGAACTGC
5′ HIV LTR reverse	CTAACCAGAGAGACCCAGTACAGGC
IL6 forward	CTAGCCTCAATGACGACCTAAGC
IL6 reverse	GAATGAGCCTCAGACATCTCCAG
TNFAIP3 forward	GTGACTTTGGAAAGTCCCGTGG
TNFAIP3 reverse	TTGGCCCGCCACGAAGACTG
NFKBIA forward	TGACCCTAGTGGCTCATCGC
NFKBIA reverse	GGACTGCTGTGGGCTCTG

Here, k_i is the parameter whose relative influence on the selected *Feature* is calculated by varying the value of k_i 10-fold around its nominal value while all other parameters are unchanged (using $k_{j_{nom}}$, as given in Table S1). The first term of the sensitivity index in Eq. 3 is the slope of the *Feature*-versus-k_i curve at $k_{i_{nom}}$. The second term allows for normalization by the nominal value $k_{i_{nom}}$ and the value of *Feature* at $k_{i_{nom}}$. The slope was calculated by polynomial approximation and differentiation routines in MATLAB; a second-order polynomial function yielded a satisfactory approximation of the *Feature*-versus-k_i curve. We note that total *NFκB* (NF) and *ka* were kept constant and were chosen to represent an "average" cell with values of 0.24 μM and 10^{-4}, respectively.

To predict behavior across a range of RelA target promoters with different transcriptional outputs, we first scanned across a range of relative affinities of competitor versus RelA for the target promoter (changing competitor affinity *k3* while maintaining the same RelA affinity *k*) sufficient to produce the approximate absolute change in transcription output observed between *NFKBIA* and *IL6* (scanning over two orders of magnitude centered over the nominal parameter value). For each value of *k3*, we simulated 450 "cells" by varying total *NFκB* (RelA) abundance and *ka* (a proxy for the strength of activation of pathways leading to IKK) but keeping other parameters at their default value, as described previously (7). After setting total *NFκB* abundance, the system is allowed to reach an unstimulated steady state with *ka* = 0, setting basal cell conditions, including basal (or "initial") transcript numbers. Then, the stimulation is initiated by switching *ka* to its value for this "cell." For each set of 450 "cells," we estimated the predicted correlation of number of target transcripts at 120 min versus maximal fold change in *nNFκB* over this 120 min period. As a measure of the change in transcript distribution after stimulation, we also estimated a "relative variance" by dividing the variance of target transcripts at $t = 120$ min in the presence of TNF by the variance in transcripts in the basal state. Finally, we estimated the average fractional binding (*FB*) on the target promoter for each combination of scanned parameter values around the peak of *nNFκB* concentration using the time points 0, 30, and 60 min; *FB* was calculated based on Eq. 2.

For a two-dimensional parameter scan, we varied transcriptional output by scanning across both a range of competitor affinity to the inducible target promoter (*k3*), as well as a range of competitor affinity for the competitor promoter (*k4*, to modulate the relative abundance of RelA versus Comp, which is less well determined). As for the initial one-dimensional scan, we simulated ensembles of 450 "cells," varying total *NFκB* and *ka* and scanned over a range of 10-fold below to 10-fold above the nominal parameter values.

Finally, we explored model behavior over a five-dimensional parameter space, varying *k3* and *k4* as well as *c1t*, *c3t*, and *ht* (see Eqs. 1 and 2). Each of the five parameters were varied in all possible combinations over a range of two orders of magnitude, centered near its default value (using multipliers 0.1000, 0.1359, 0.1848, 0.2511, 0.3414, 0.4640, 0.6307, 0.8572, 1.1652, 1.5838, 2.1528, 2.9262, 5.4063, and 9.9885, chosen among the 16 equally spaced points in $\log_{10}$ space). The other model parameters were maintained at their original value. For a selection of combinations at the extremes or "corners" of the parameter space, for boundary regions of the parameter spaces that yielded appropriate transcript numbers, and for regions that qualitatively fitted HIV LTR promoter behavior, we also ran ensemble simulations of 450 "cells" to obtain estimates of the correlation of induced target transcript number with fold change, average *FB*, and/or relative variance.

Statistical analysis

Differences between distributions of transcripts or time-course features were determined by Kolmogorov-Smirnov (K-S) test ($p < 0.05$). 95% confidence intervals (CIs) on descriptive statistics of RNA distributions were estimated from the 2.5 to 97.5% quantiles of copy numbers per cell bootstrapped by sampling 1000 times with replacement. Differences in the central tendency between pairs of distributions were determined using a Mann-Whitney U test ($p < 0.05$) to compare their median. To compare dy-

namics between Ch-RelA time courses, differences between distributions of t_{max} (defined as time to reach F_{max}) and $t_{duration}$ (defined as the time between 50% F_{max} rising and 50% F_{max} falling) were determined by K-S test ($p < 0.05$). All statistical tests and regression and correlation analyses were performed in Prism (Graphpad) unless otherwise indicated.

RESULTS

Implementation of smFISH for suspension T cells in a passive-flow microfluidic device

We previously developed a user-friendly microfluidic device that immobilizes suspension cells in an array of traps using passive gravity-driven flow between two reservoirs to implement long-term live-cell imaging of suspension cells (13). Our goal here was to collect paired data, tracking NF-κB RelA nuclear translocation dynamics by live-cell imaging and RelA-driven transcriptional output by smFISH in the same cells (Fig. 1 A), to gain insight into how NF-κB signaling dynamics are converted to transcriptional outputs in Jurkat T cells. A challenge posed by fixed-cell response assays such as smFISH is that they require multiple fluid exchanges within the device to allow for incubations with different reagents and multiple wash steps. After optimization of the workflow to implement smFISH in the device (see Materials and Methods), imaging Z-stacks on the device produced well-defined puncta, which were suitable for downstream analyses (Fig. 1 B). Previous studies have shown that these puncta represent individual mRNAs and thus allow accurate quantification of mRNA number in individual cells (15,18,19).

To validate the smFISH implementation in the device, we quantified *NFKBIA* transcripts in J65c cells, a clonal population of Jurkat T lymphocytes stably expressing an NF-κB mCherry-RelA (Ch-RelA) reporter protein. We compared measurements collected in the device to our previously published measurements of *NFKBIA* transcripts collected in a dish (12). We found that mean *NFKBIA* transcript numbers and the distribution of *NFKBIA* transcripts before and 1 h after TNF stimulation were indistinguishable between the two formats (Fig. 1, C and D). A similar comparison for TNF-stimulated HIV transcripts from clonal J65c Jurkat cell populations containing a latent-but-inducible HIV integration with very low transcript abundance also showed no evidence of changes in transcriptional output between formats (12) (Fig. 1, E and F). Overall, our data show that smFISH for both high- and low-abundance inducible transcripts in T cells can be implemented in our passive-flow device, allowing for a live-cell-to-fixed-cell imaging workflow for nonadherent cells.

Jurkat cells exhibit fold-change detection of RelA at promoters with high-inducible transcription

We proceeded to image TNF-induced NF-κB RelA translocation dynamics followed by smFISH in J65c cells to explore NF-κB RelA signal input-transcriptional output
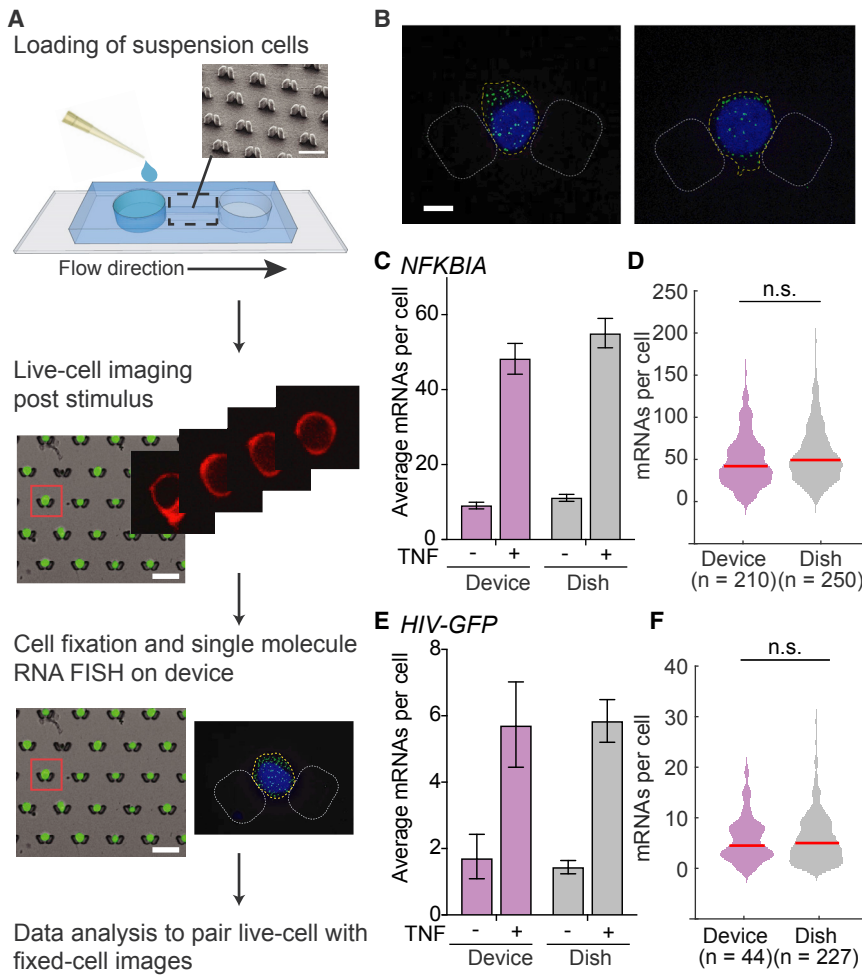
FIGURE 1 Optimization of a microfluidic-device-enabled protocol to connect signaling dynamics to smFISH measurements in single suspension cells. (*A*) A schematic of the live-cell-to-fixed-cell protocol. A cell suspension is pipetted into the inlet of a microfluidic device and flows into the channel containing traps that catch cells via gravity. Upon stimulation with a medium exchange, live cells are imaged in the traps for a desired amount of time. Then, cells are fixed and assayed by single-molecule RNA fluorescence in situ hybridization (smFISH). Data are then processed, and the live-cell and fixed-cell images are analyzed together for the same single cells. (*B*) Representative images of Jurkat J65c cells treated with 20 ng/mL TNF for 1 h, fixed in traps, and labeled for single *NFKBIA* mRNAs with carboxyfluorescein-conjugated probes (*green*). Nuclei stained with Hoechst (*blue*); scale bars, 5 μm. (*C*) A bar graph of mean *NFKBIA* transcript counts, as measured by smFISH for unstimulated cells and cells stimulated with 20 ng/mL TNF for 1 h measured in the passive-flow device (*purple*) and in a tissue culture dish (*gray*). Data are presented as the mean $\pm$ 95% CIs obtained by bootstrapping. (*D*) Violin plots of TNF-stimulated *NFKBIA* transcript distributions measured by smFISH at 1 h in the passive-flow device (*purple*) or tissue culture dish (*gray*). The median is indicated by the red line. There are no significant differences between the distributions ($p > 0.05$ by Kolmogorov-Smirnov (K-S) test). (*E* and *F*) A bar graph of mean *HIV-GFP* transcript count (*E*) and violin plots of *HIV-GFP* transcript distributions (*F*) measured by smFISH after 2 h of TNF stimulation. All other details are as in (*C*) and (*D*).

relationships. Ch-RelA translocation was imaged for 2 h after stimulation with 20 ng/mL TNF (Fig. 2 *A*, *left*). Cells were then fixed in the traps, and transcripts of the RelA target gene (here *NFKBIA*) were labeled by smFISH in the device to produce a set of live-cell signaling traces paired with transcriptional output (Fig. 2 *A*, *right*).

We first explored input-output relationships for the high-abundance targets *NFKBIA* and *TNFAIP3*. After 2 h of TNF stimulation, the average number of transcripts increased to 40 and 16 (observed maximum of 124 and 73) transcripts per cell, respectively, for *NFKBIA* and *TNFAIP3* (Fig. 2 *B*). Ch-RelA nuclear translocation dynamics over that period were not significantly different between the two experiments (Fig. 2 *C*). We note that TNF-stimulated Ch-RelA translocation dynamics differed between the device and a tissue culture dish; nuclear Ch-RelA peaked 5–10 min later and was sustained over a longer period (monitored for 2 h) in the device versus in a dish (Fig. S3 *A*). This slower and more sustained pattern of nuclear Ch-RelA translocation was not due to a delay in TNF stimulation between the inlet and outlet because the average response of the cells near the inlet of the device

was indistinguishable from the response of cells closer to the outlet (Fig. S3 *B*). Despite the slower and more sustained signaling dynamics observed in the device, transcript number distributions remained unchanged (Fig. 1, *C–F*), suggesting that T cells respond to a feature of the signaling dynamics that is conserved across formats.

We previously showed that maximal fold change in nuclear RelA is predictive of *NFKBIA* and *TNFAIP3* early transcriptional output in HeLa cells ($t = 60$ min (7)) and of the fluorescent protein production from an HIV activation reporter construct in Jurkat T cells (12). To evaluate which aspects of RelA signaling are most predictive of *NFKBIA* and *TNFAIP3* transcriptional output in Jurkat cells, we extracted features from individual TNF-stimulated Ch-RelA nuclear intensity time courses (Fig. 2 *D*) and matched them to the number of transcripts observed in the same cell. We included absolute nuclear RelA intensity (initial, maximal, and final), features describing relative changes in nuclear intensity (maximal and final intensity normalized to initial intensity), a feature that integrated nuclear intensity over time (area under the curve, *AUC*), and a feature that described pathway flux (the maximal rate of change). We
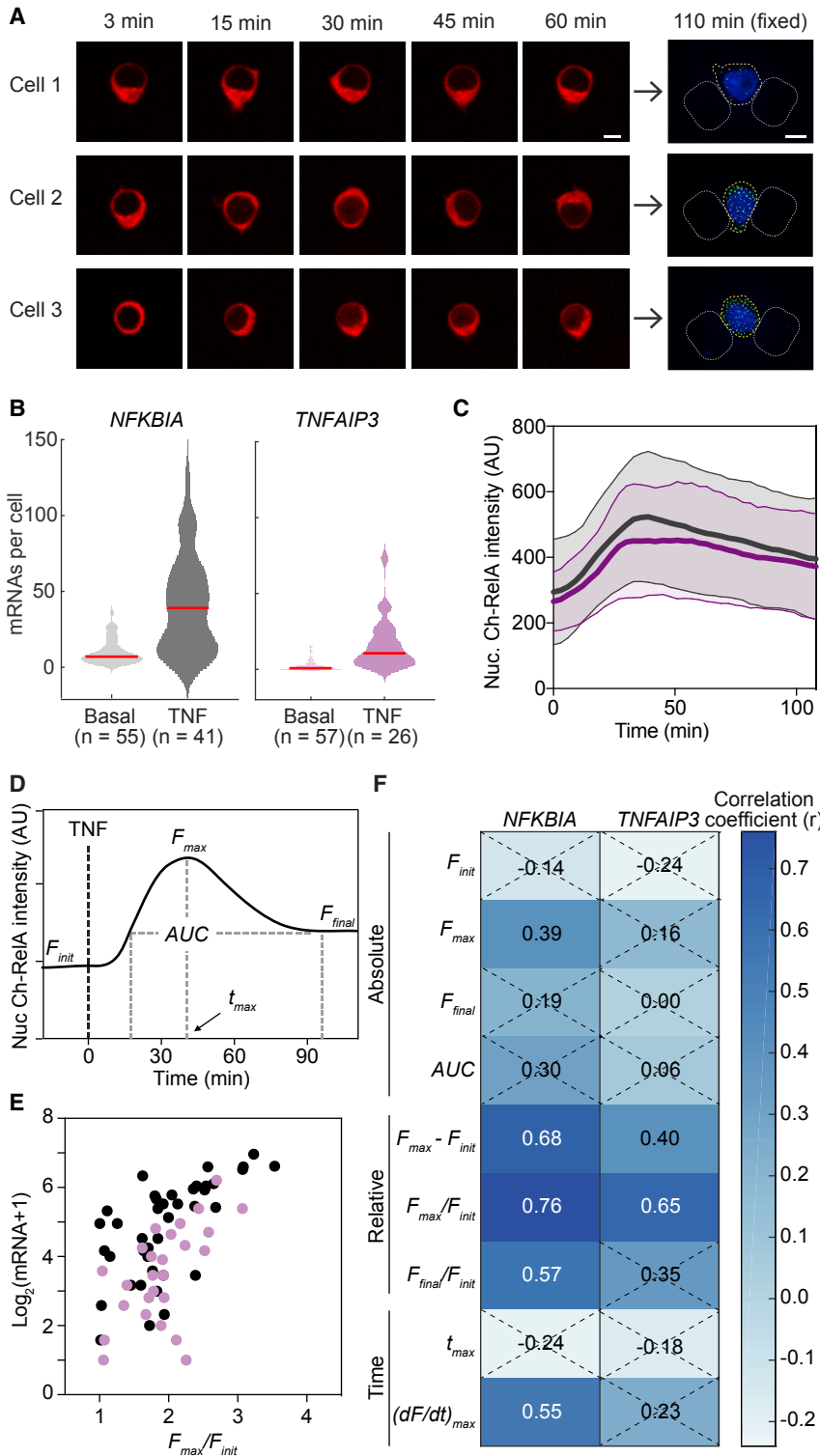
FIGURE 2 Fold-change detection of nuclear RelA is observed in Jurkat T cells at promoters exhibiting high levels of TNF-inducible transcription. (*A*) Time-lapse images of Ch-RelA paired with smFISH images of *NFKBIA* transcripts at 2 h after 20 ng/mL TNF treatment from the same cells. Scale bars, 5 μm. (*B*) Violin plots of transcript number distributions for *NFKBIA* (*gray*) and *TNFAIP3* (*purple*) measured by smFISH before and 2 h after TNF stimulation in the device. The median is indicated by the red line. (*C*) Time-course traces of nuclear Ch-RelA from J65c cells collected in the passive-flow device after 20 ng/mL TNF treatment for two independent experiments. Data are presented as the mean $\pm$ SD of individual cell traces ($n = 41$, traces linked to *NFKBIA*, *gray*; $n = 26$, traces linked to *TNFAIP3*, *purple*). Lack of statistical significance of differences in dynamics was determined by comparing distributions of t_{max} and $t_{duration}$ of nuclear RelA peak intensity between the data sets ($p > 0.05$ by K-S test). AU, arbitrary units. (*D*) A schematic indicating features calculated from individual nuclear Ch-RelA time courses including initial, maximal, and final fluorescence (F_{init}, F_{max}, and F_{final}); time at which F_{max} is reached (t_{max}); and area under the curve (AUC). (*E*) A scatter plot of smFISH-measured transcript number (2 h post-TNF addition) versus the maximal fold change in nuclear Ch-RelA (F_{max}/F_{init}) for *NFKBIA* (*gray*) and *TNFAIP3* (*purple*). (*F*) A heat map of Pearson correlation coefficients (*r*) with smFISH-measured transcript number for all extracted metrics describing same-cell nuclear Ch-RelA time courses. Nonsignificant correlations ($p > 0.05$) are indicated by a dashed X.

verified that the distributions of feature values were not significantly different between *NFKBIA* and *TNFAIP3* experiments (Fig. 2 *C*; Materials and Methods), confirming that Ch-RelA nuclear translocation was similar in both sets of sampled cells.

When we compared correlations of each Ch-RelA feature with transcript number, we found that the maximal fold change in RelA nuclear intensity (F_{max}/F_{init}) was the strongest predictor for *NFKBIA* and *TNFAIP3* early transcription levels across all features considered (for $t = 2$ h; Fig. 2, *E*

and *F*), consistent with our observations in HeLa cells. Interestingly, we found that the distributions of F_{max}/F_{init} for nuclear RelA were the same for translocation time courses collected in the tissue culture dish versus the device (Fig. S3 *C*), which may explain why the observed differences in translocation dynamics between the two formats did not significantly affect transcriptional output. Overall, we conclude that fold-change detection of nuclear RelA in response to TNF stimulation is maintained in Jurkat T cells for the high-abundance RelA target genes *NFKBIA* and *TNFAIP3*.

Fold-change detection is conserved at promoters exhibiting low inducible transcription

We recently studied RelA-mediated activation of latent HIV using J65c cells harboring unique integrations of an HIV lentiviral construct driving expression of GFP and the viral protein Tat. We specifically studied two clones, referred to as J65c 4.4 and 6.6 (12), which do not express virus in the basal state but are activated by TNF. 2 h of TNF treatment while blocking viral positive feedback induced similar, very low mean transcription at these two viral integration sites (Fig. 3 *A*; ∼6 transcripts per cell). We also observed a low TNF-induced transcript mean for the cytokine *IL6*

(Fig. 3 *A*), consistent with the expectation that *IL6* is not strongly activated by TNF in immune cells (20); however, the increase in response to TNF was nonetheless significant (Fig. 3 *B*). Therefore, we wanted to explore whether fold-change detection between nuclear RelA and transcript number would be observed at these promoters, which support very low amounts of inducible transcription.

In addition to differences in TNF-induced average transcript numbers, the TNF-induced transcript number distributions also varied across promoters. J65c 6.6 exhibited a highly skewed distribution of HIV transcript numbers in response to TNF stimulation that was more similar to *TNFAIP3*, but J65c 4.4 HIV transcript number distribution and distributions for *IL6* both exhibited much less skew (Fig. 3 *B*; Table 3). We previously observed such differences in transcript distributions and showed that they are associated with differences in the underlying mechanisms of RelA-mediated transcription (12), bringing into question whether the fold change in nuclear RelA will remain strongly correlated with transcript number at both promoters.

When we compared correlations of each Ch-RelA feature with early transcript number for these low-abundance targets, we found that the maximal Ch-RelA nuclear intensity and *AUC* of Ch-RelA intensity were again only weak
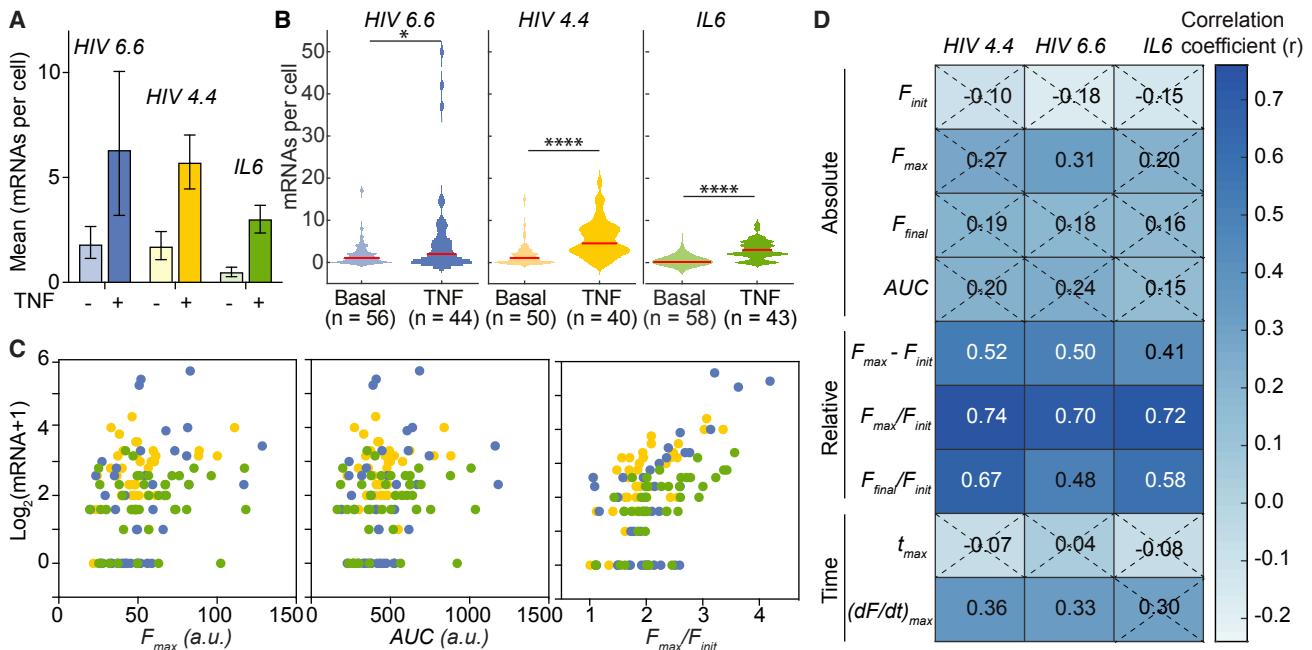
FIGURE 3 Maximal fold change in nuclear RelA correlates with transcript output for gene promoters exhibiting low levels of TNF-inducible transcription. (*A*) A bar graph of mean smFISH-measured transcript counts of *HIV 6.6* (*blue*), *HIV 4.4* (*yellow*), and *IL6* (*green*) before and 2 h after 20 ng/mL TNF stimulation. Data are presented as the mean ± 95% CIs obtained by bootstrapping. (*B*) Violin plots of transcript number distributions for *HIV 6.6*, *HIV 4.4*, and *IL6* measured by smFISH, before and 2 h after TNF stimulation. The median is indicated by the red line. Statistical significance for differences in the medians of two distributions is indicated (*P < 0.05; ****P < 0.0001; Mann-Whitney U test). (*C*) Scatter plots of smFISH-measured transcript number (2 h post-TNF) for *HIV 6.6* (*blue*), *HIV 4.4* (*yellow*), and *IL6* (*green*) versus maximal nuclear Ch-RelA abundance (F_{max}; *left*), *AUC* (*middle*), and maximal fold change in nuclear Ch-RelA (F_{max}/F_{init}; *right*). (*D*) A heat map of Pearson correlation coefficients (*r*) with smFISH-measured transcript numbers for all extracted metrics describing same-cell nuclear Ch-RelA time courses. Nonsignificant correlations (*p* > 0.05) indicated by a dashed X.

TABLE 3 Statistical Moments for Experimentally Measured Transcript Distributions

	Mean		Variance		Skewness	
Target	Basal	+TNF	Basal	+TNF	Basal	+TNF
NFKBIA	10.1 (8.0, 12.3)	40.6 (31.1, 50.4)	64.5 (36.6, 93.8)	984.9 (596, 1377)	1.3 (0.7, 1.9)	0.7 (0.2, 1.2)
TNFAIP3	2.0 (1.3, 2.8)	16.2 (10.6, 22.7)	8.6 (2.8, 16.0)	267.9 (78.7, 515.3)	2.5 (1.3, 3.4)	1.8 (0.4, 2.7)
HIV 6.6	1.8 (1.1, 2.7)	6.3 (3.2, 10.0)	8.0 (1.8, 17.5)	129.5 (17.0, 250.3)	3.5 (0.8, 4.4)	2.7 (1.3, 4.4)
HIV 4.4	1.7 (1.1, 2.4)	5.7 (4.4, 7.0)	6.8 (1.9, 14.1)	19.1 (10.2, 28.4)	3.0 (1.1, 4.1)	1.0 (0.3, 1.6)
IL6	0.5 (0.3, 0.7)	3.0 (2.3, 3.7)	0.8 (0.4, 1.3)	5.0 (3.0, 7.1)	2.0 (1.1, 2.8)	0.5 (−0.1, 1.0)

Values for the upper and lower bounds of the 95% CIs obtained by bootstrapping are listed in parentheses.

predictors of TNF-induced transcript number at 2 h (Fig. 3 *C*). In contrast, the maximal fold change in RelA nuclear intensity (F_{max}/F_{init}) was a strong predictor for *HIV* and *IL6* transcription (Fig. 3 *C*). For *IL6*, the correlation with maximal nuclear RelA fold change held despite the fact that transcript number ranged only from 0 to 10 transcripts per cell. As with high-abundance genes, we observed that only features describing relative changes in Ch-RelA nuclear intensity were strong predictors of output, with maximal fold change in nuclear RelA being the strongest predictor of all the features considered (Fig. 3 *D*). Surprisingly, this trend in the correlations was similar for all promoters despite the differences in their transcript distributions (Fig. 3 *B*; Table 3). We tested whether integrating the relative change in nuclear Ch-RelA over time (i.e., area under the curve of F/F_{init} or AUC_{FC}) would improve the correlation over using only its maximum. However, consistent with the observation that there is a strong correlation between these two features (Fig. S3 *D*), we found no improvement in correlations. Overall, we conclude that RelA fold-change detection is conserved at genes supporting low TNF-inducible mean transcription and with different TNF-induced transcript distributions.

Mathematical model of I1-FFL RelA signaling reveals that varying relative RelA binding affinity alone is insufficient to recapitulate single-cell experimental data

Fold-change detection of signals can be executed with an I1-FFL signaling motif (8). We previously implemented an I1-FFL in a mathematical model of TNF-stimulated NF-κB RelA activation and target gene transcription by incorporating a competitor protein that is induced by RelA and competes for binding to promoter κB sites, thereby inhibiting RelA-mediated transcription (7) (Fig. 4 *A*; Fig. S2). NF-κB p50, NF-κB p52, and BCL3 are potential candidates for this competitor protein because they are all induced by RelA (21), and they form complexes that suppress transcription of κB-site-containing genes, including *IL6* and the HIV long terminal repeat (e.g., p52:p52 or p50:p50, which is stabilized by BCL3 (22,23)). This model accurately described our observations in HeLa cells for RelA target genes with high early TNF-inducible transcrip-

tion (7). We now sought to explore whether this model could account for our new experimental observations in Jurkat cells extending to RelA target genes with low early TNF-inducible transcription.

We previously showed that it is possible to tune transcriptional output of high-abundance RelA targets in the model while maintaining fold-change detection by simply varying the strength of competitor binding affinity relative to RelA binding affinity at its promoter (7). This is biologically plausible because the relative affinities of RelA and the candidate competitor proteins vary across promoter κB site sequences (24). To determine if this finding still held at low-abundance targets, we performed a model parameter scan (changing competitor affinity *k3* while maintaining the same RelA affinity *k*) to find a range of competitor affinities for target promoters that reproduced the approximate absolute change in transcript abundance for *NFKBIA*, *TNFAIP3*, *HIV*, and *IL6* observed in our experiments 2 h after addition of 20 ng/mL TNF (Fig. 4 *B*). At each competitor affinity value, we simulated cell-to-cell variability by sampling over a range of total RelA-containing *NFκB* abundance (NF) and *ka* (a proxy for the strength of activation of pathways leading to IKK), two parameters chosen based on the sensitivity of fold change of nuclear RelA (Fig. S5). All other parameters remained the same as previously reported (7) (Table S1).

We found that moderate to strong correlations between maximal fold change in nuclear RelA and transcript number were maintained as competitor affinity increased and TNF-induced transcript abundance decreased, consistent with experimental observations (Fig. 4 *C*). We also previously reported that the variance of TNF-mediated transcript number distributions relative to transcript variance in the basal state (referred to as relative transcript variance) increased with decreasing TNF-induced transcript abundance (7). Consistent with this, reducing average TNF-stimulated mRNA levels from 58 to 1 resulted in the model prediction that relative transcript variance would increase ∼8-fold (Fig. 4 *D*). However, our single-cell measurements show that for very low-abundance targets, relative transcript variance decreases, in contrast to model predictions (Fig. 4 *D*, *right*) and to our observations at high-abundance targets (7).

To explore this discrepancy, we noted that if we reduced transcript output solely by varying competitor affinity, the
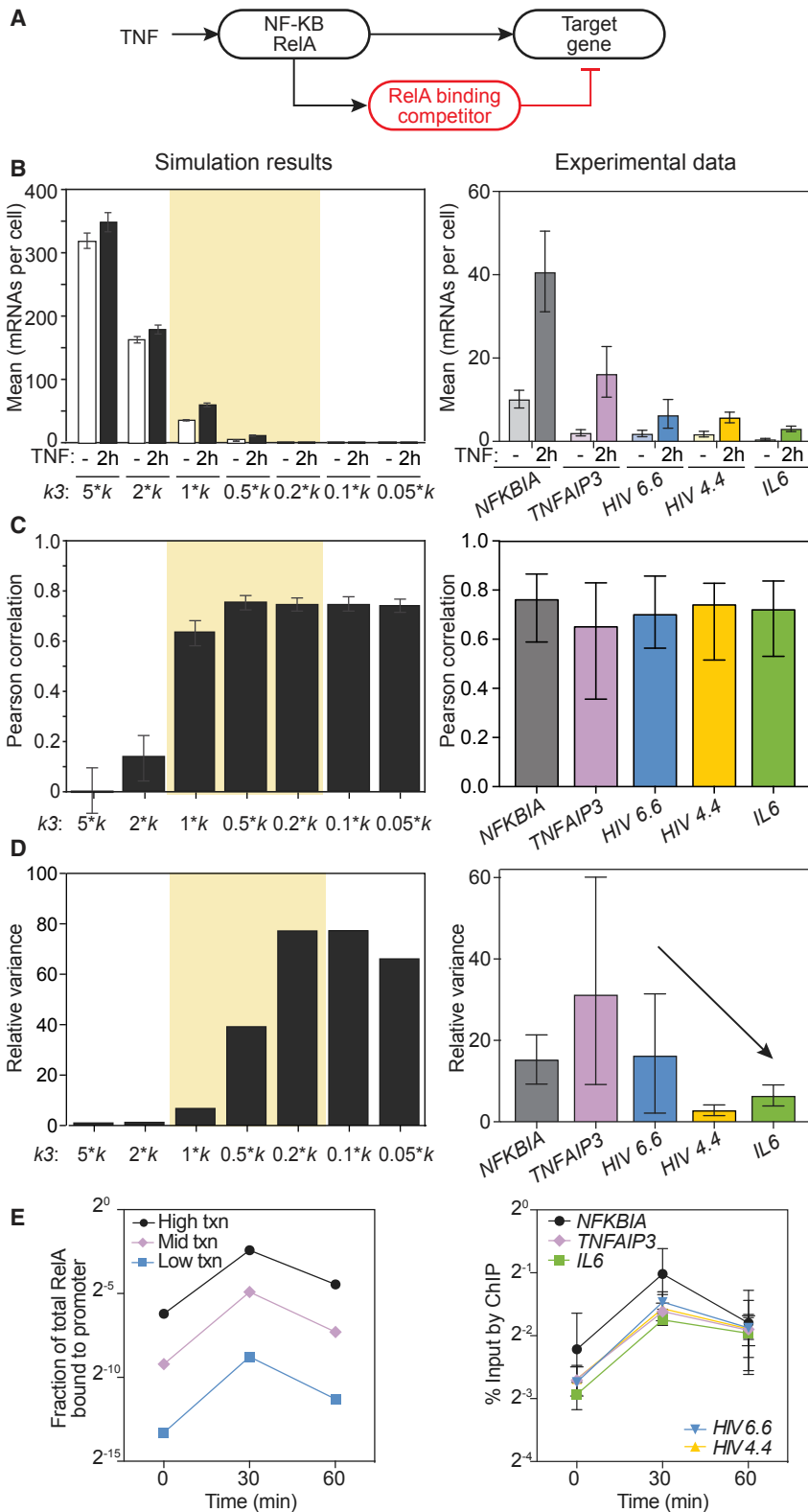
FIGURE 4 Decreasing transcriptional output by decreasing relative RelA binding maintains fold-change detection but is inconsistent with experimental RelA binding data. (A) A schematic of how the I1-FFL motif was implemented in a computational model of NF-κB RelA signaling. (B) A bar graph of mean transcriptional output simulated by the model (left) and measured experimentally by smFISH (right) before and 2 h after TNF stimulation. Simulations were run for $k4 = 1 \times k$ and the indicated $k3$ values, where $k4$ is the affinity of competitor for the competitor promoter and k and $k3$ are the respective affinities of nNFκB and competitor for the induced target promoter; cell-to-cell variability was modeled by sampling for total RelA-containing NF-κB (NF) and TNF-induced IKK activity (ka). Values that reproduced the experimentally observed transcript range are shaded in yellow. Error bars represent the ±95% CIs obtained by bootstrapping. Experimental data are similarly presented as the mean ± 95% CIs obtained by bootstrapping. (C) A bar graph of Pearson correlations between F_{max}/F_{init} and transcript abundance 2 h after TNF stimulation for simulated results (left) and experimental data (right). Simulations were run as described in (B). Error bars again represent 95% CIs. (D) A bar graph of relative variance in transcript distributions post- versus pre-TNF treatment ($t = 2$ h, 20 ng/mL) for simulation results (left) and experimental data (right). Relative variance is defined as variance at $t = 2$ h over the variance at $t = 0$; error bars represent 95% CIs. (E) Time courses of simulated RelA binding (left) and measured enrichment of RelA (% input measured by ChIP; right) after TNF addition. Simulations were run as described in (B) (error bars for 95% CIs are smaller than the markers). ChIP data are presented as mean ± standard error of independent biological duplicate (HIV 4.4 and HIV 6.6) or triplicate (endogenous promoters). There are no significant differences in measured time courses ($p > 0.05$, calculated by two-way ANOVA).

model predicted that the average fraction of RelA bound at 30 min after TNF treatment would need to be reduced nearly 80-fold (Fig. 4 E, left). We tested this prediction by using chromatin immunoprecipitation (ChIP) to measure average RelA binding at the promoters at 0, 30, and 60 min after TNF treatment. In contrast to the model prediction, we

found no significant differences in RelA binding across all promoters after TNF treatment (Fig. 4 E, right). Because the relative abundances of RelA versus competitor proteins (determined by varying *k4*) is a less well-determined parameter and may differ between promoters, we also scanned across a range of *k4* values to assess whether different trends in RelA binding and relative transcript variance could be found, but we found that all trends remained similar (Fig. S4). Thus, varying competitor affinity can reproduce the difference in transcript abundance at low- versus high-output targets and observations of fold-change detection, but it is inconsistent with experimental measurements of relative transcript variance and average RelA binding. We conclude that other mechanisms must be used to reduce transcript abundance to very low levels while maintaining fold-change detection.

Tuning multiple model parameters for individual target genes reproduces observed TNF-RelA-mediated behavior

To systematically determine other model parameters that strongly affect target transcript abundance, we performed a parameter sensitivity analysis (Fig. S5). We found that in addition to competitor binding affinity (*k3*) and relative abundance of RelA versus competitor (*k4*), target gene transcription in the model is most affected by target transcript synthesis rate (*c1t*), target transcript degradation rate (*c3t*), and a Hill coefficient determining the steepness of the transcription response with respect to the concentration of nuclear RelA (*ht*). We performed a five-way parameter scan across a range of values for the parameters identified above and examined the distributions of transcript abundance outputted by the model that fell within our experimentally observed ranges (Fig. 5 A; *yellow-red* heat map). Cell-to-cell heterogeneity in the model was again produced by varying the initial concentrations of total RelA (*NF*) and the TNF-induced IKK activity (*ka*). Within this broad parameter space, it was possible to simulate a range of TNF-mediated increases in transcript abundance that are associated with different patterns of fold-change detection, relative transcript variance, and fractional RelA binding (Fig. S6 A).

We next explored how the predicted transcript distributions compared to our experimental measurements across a range of transcriptional outputs. To do this, we identified parameter sets that reproduced the approximate absolute transcript abundance pre- and post-TNF addition for each target observed experimentally (with *t* = 2 h, 20 ng/mL; defined by the interquartile range of single-cell measurements; Fig. S6 B). We further refined these sets by requiring that the fold-change correlation be recapitulated, resulting in a reduced range of possible parameters for each promoter (Fig. 5 B). Fractional RelA binding, *FB*, was constant for all simulations with the same pair of *k3* and *k4* values and neighboring regions in the *k3-k4* space had similar RelA

binding values. By comparing across similar *k3-k4* regions, it was possible to find regions within this space in which transcript abundance changed without significant changes in RelA binding (Fig. 5 B; Fig. S6 A). Based on these simulation results, we conclude that to maintain fold-change detection for all low-abundance targets, it becomes necessary to vary a combination of model parameters, rather than a single parameter as we previously reported (7).

Finally, we explored whether we could combine experimentally observed trends in relative transcript variance with prior biological knowledge to further constrain the parameter space. In particular, TNF-stimulated transcript number distributions and their relative variance trends are different for the two integrations of HIV, despite the fact that the promoter is identical and supports a similar average TNF-stimulated transcription. Therefore, we fixed RelA competitor affinity (*k3*) and competitor abundance (*k4*), as well as transcript degradation rate (*c3t*), for HIV, based on the assumption that these values would be the same for the same HIV promoter and transcript, respectively. We then varied transcript synthesis rate (*c1t*) and the Hill coefficient (*ht*) and searched for parameterizations that could reproduce the observed trends in relative transcript variance while still maintaining fold-change detection (Fig. 6, A–C). We found that by individually varying these two parameters for a specific set of *k3*, *k4*, and *c3t*, it was possible to obtain a similar increase in transcript abundance with different relative variances while maintaining fold-change detection (Fig. 6, D and E). Furthermore, it was possible to approximately reproduce all experimentally observed trends across the full range of transcript abundances with identical RelA binding (i.e., fixed values of *k3* and *k4*). We note that these are not the only parameterizations that could reproduce the trends and that the assumption that *k3*, *k4* and *c3t* are invariant is unlikely to hold for *NFKBIA*, *TNFAIP3*, and *IL6*, although the space is substantially constrained (Fig. 5 B). By using experimental measurements to fix additional model parameters (e.g., *c3t* for *NFKBIA*, *TNFAIP3*, and *IL6*), it may be possible to find, for each promoter, a well-constrained parameter set that could reproduce experimental trends.

Overall, our quantitative single-cell data set of NF-κB signal-response relationships for low-abundance transcripts provided additional constraints for testing TNF-RelA model predictions. We conclude that to maintain fold-change detection across promoters with widely varying transcriptional outputs requires changes in multiple determinants of transcriptional outputs and that to accurately model NF-κB-driven gene transcription for a wide range of targets, measuring single-cell input-output relationship can help constrain model parameter values.

DISCUSSION

Signal-response relationships measured in single cells provide insights into regulatory mechanisms. We previously
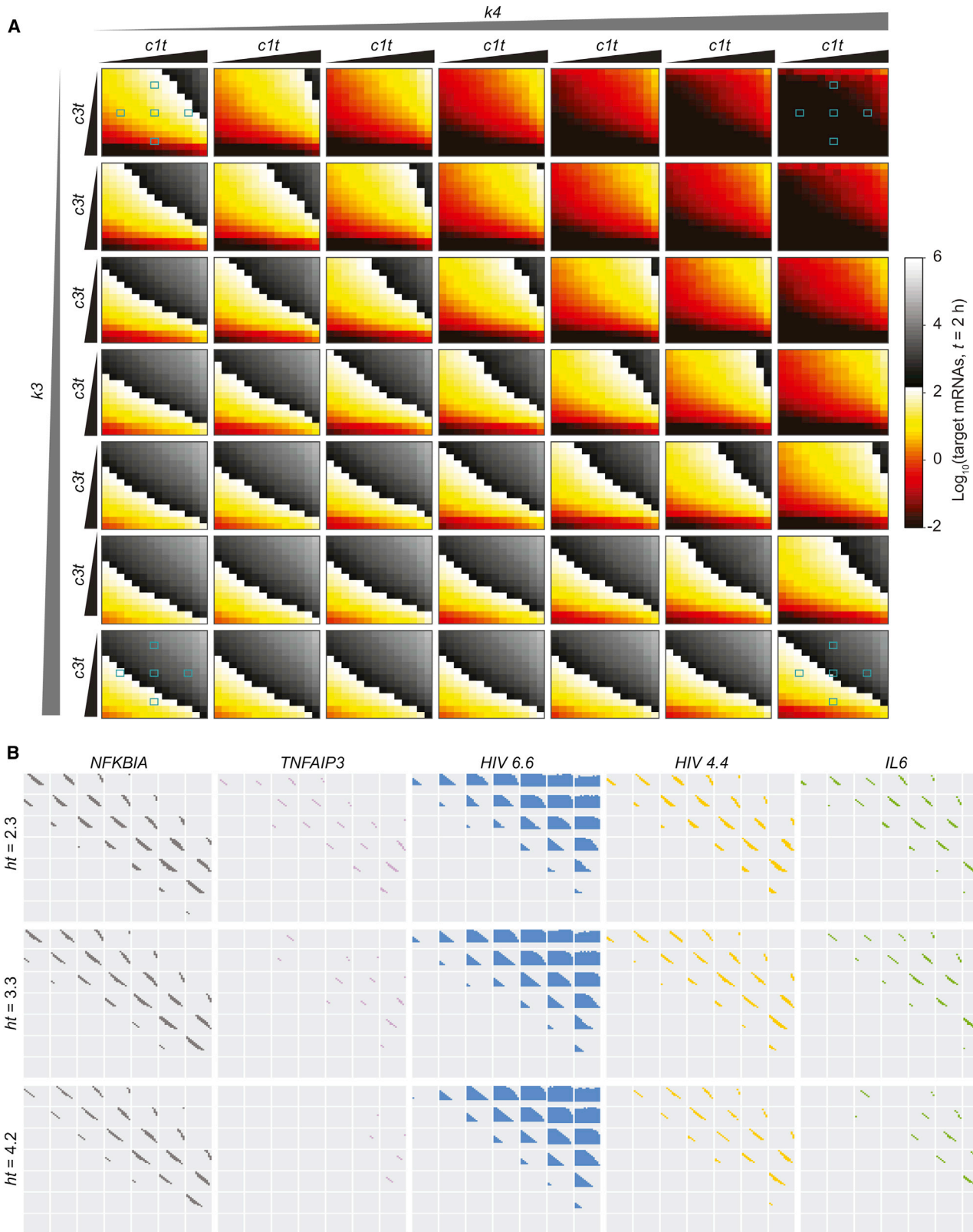
FIGURE 5 Tuning multiple model parameters for each target promoter can reproduce experimentally observed behaviors. (A) A heat map of transcript output 2 h after TNF stimulation for a range of RelA target binding affinities ($k3$) and relative competitor abundance ($k4$) values (varied across *small rectangles*, subsampling our simulation results to multipliers 0.1000, 0.1848, 0.3414, 0.6307, 1.1652, 2.1528, and 5.4063) and target transcript synthesis ($c1t$) and degradation ($c3t$) rates (varied within *small rectangles* using the full set of simulations described in Materials and Methods). The heat map color scale is set to the

discovered that RelA target promoters exhibit fold-change detection of TNF-stimulated signaling; here, we extended this finding to show that fold-change detection is conserved across cell types and even at promoters with low TNF-induced transcription. Acquiring signal-response relationships in single Jurkat T cells required development of a microfluidic-device-enabled imaging protocol to measure paired live-cell signaling dynamics and fixed-cell transcriptional output in the same suspension cells.

Our findings suggest that fold-change detection may be a general mechanism of TNF-induced NF-κB signal detection. Fold-change detection has also been observed in the extracellular regulated kinase pathway (25) and for cyclic adenosine 3′,5′-monophosphate in social amoebae (26), indicating that fold-change detection may confer broadly useful biological functionality. For example, fold-change detection has been proposed as a mechanism by which cells buffer against stochastic variation in signaling molecules by allowing transcriptional output to correlate with signal strength instead of absolute abundance of the signal-driving protein (7,8). Our results show that this buffering is observed for low-abundance transcripts, even though gene expression noise has been observed to increase as mean expression decreases (27,28).

Our results demonstrate some advantages of measuring transcript number for low-abundance transcripts rather than tracking a transcriptional reporter that requires protein expression. We previously quantified how TNF-stimulated RelA signaling features correlated to levels of HIV activation in J65c 4.4 and 6.6 using a GFP gene expression reporter that is subject to positive feedback amplification by the HIV-encoded protein Tat (12). A weakness of that approach was that only a minor fraction of the J65c 4.4 cells (25%) exhibited detectable reporter expression, even though most cells increased HIV transcription (12). Although we did find that the maximal fold change in RelA was the strongest predictor of the Tat-mediated GFP protein expression for both viral integrations, we observed that this correlation was significantly weaker for J65c 4.4 versus J65c 6.6 ($r = 0.55$ vs. $r = 0.78$). By directly measuring transcriptional output using smFISH, we now conclude that the RelA signal-to-transcript relationship is identical for both clones, and inefficient Tat-mediated positive feedback degrades the correlation for J65c 4.4. We note, however, that smFISH is a static, end-point measurement, whereas transcriptional reporters provide a way to track transcriptional dynamics, which may provide additional useful information in other biological scenarios.

To gain mechanistic insight, we compared our experimental measurements across a range of transcript abundances to simulations of a mathematical model of TNF-mediated NF-κB signaling (7). Tuning RelA binding affinity at the target promoters was sufficient to recapitulate our observation of fold-change detection across cells for low-abundance transcripts as previously reported (7) but was inconsistent with our experimental observation that average RelA binding did not change at the low-abundance targets. Instead, we were able to qualitatively reproduce experimental observations by varying multiple parameters independently for each target promoter.

Why might there be limited transcription at some promoters despite similar transcription factor occupancy? One potential simple explanation is that these different targets have different transcript stability, a parameter that has previously been shown to also strikingly affect the dynamics of transcript accumulation of NF-κB and p53 targets (29–31). However, a difference in transcript stability could not explain the differences in transcript count distributions between the two HIV LTR integrations that we studied because their outputs are the same transcripts. Here, an explanation might be differing local chromatin environments. Indeed, genome-wide studies of transcriptional reporters integrated at different genomic locations, including the HIV LTR, show that transcriptional activity is affected by features of the local chromatin environment (32,33) and the stability of nucleosomes, which compact DNA and may inhibit access of transcriptional machinery (34). In our abstracted model of NF-κB-driven transcription, such effects can be reflected in differences in target transcription rates ($c1t$). Additionally, transcription factor (TF)-induced chromatin and nucleosome remodeling appears to be a rate-limiting step for transcriptional activation (35,36). Because rates of chromatin and nucleosome remodeling are slower than TF binding (37), they may further impose an apparent threshold of TF binding required for transcription (38). In our model, such behavior can be captured by varying the Hill coefficient (ht) characterizing the transcriptional response at a target promoter.

There are several molecular mechanisms that underlie this chromatin remodeling that may limit the rate of RelA-mediated transcription. Although RelA cannot directly remodel chromatin, RelA has been shown to recruit the histone acetyltransferase p300, which acetylates histones to enhance transcriptional activity (23,39). Moreover, the candidate competitor proteins in the incoherent feedforward loop of NF-κB-driven transcription, p50, p52, and BCL3, have been reported to mediate their repressive transcriptional activity at the HIV LTR and other RelA target promoters by recruiting histone deacetylases (40–42). Thus, RelA has the potential to mediate chromatin

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experimentally observed range of transcript output for all transcripts combined. Areas in gray color scale are outside of the experimentally observed range. Simulations were done for a Hill coefficient of $ht = 3.2$. Small blue squares highlight areas further explored in Fig. S6. (*B*) Possible parameter sets for each target transcript are highlighted in color over the same $k3$-$k4$-$c1t$-$c3t$ space as in (*A*) and for the indicated Hill coefficient (ht), if they reproduce experimentally observed baseline and TNF-induced transcript levels at 2 h and have a Pearson correlation coefficient of $r > 0.6$ for fold-change detection.
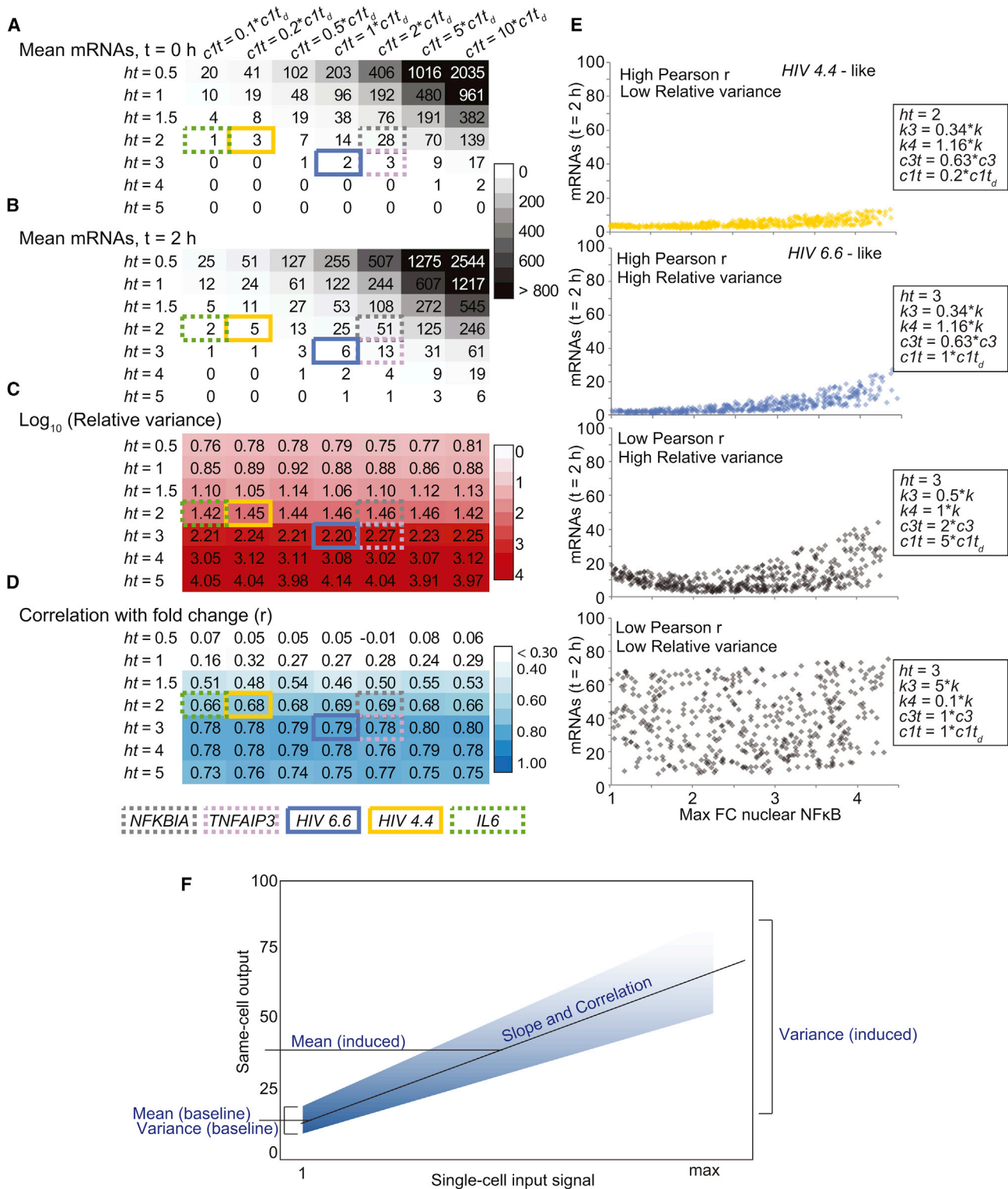
FIGURE 6 Parametrizations of an I1-FFL model of NF-κB-driven transcription can capture features of TNF-induced increases in HIV transcription as well as that of low-abundance endogenous genes. (*A–D*) Heat maps are shown of baseline (*A*) and post-TNF ($t = 2$ h; *B*) mean transcript number, relative variance (expressed as $\log_{10}$ ($\mathrm{Var}_t = 2$ h$/\mathrm{Var}_t = 0$ h) (*C*), and Pearson correlation of transcript number with fold change in nuclear RelA (*r*; *D*) for a range of target transcript transcription rates (*c1t* versus its default value $c1t_d$) and Hill coefficients (*ht*). Parametrizations with good fit for *NFKBIA* (*gray*), *TNFAIP3* (*lilac*), *HIV 6.6* (*blue*), *HIV 4.4* (*yellow*), and *IL6* (*green*) are outlined. All simulations were run using fixed values of *k3* (0.3414 × *k*), *k4* (1.1652 × *k*), and *c3t* (0.6307 × *c3*) chosen from a region that showed good fit to mean transcript numbers for *HIV 6.6* and *HIV 4.4* (Fig. 5 *B*). Cell-to-cell variability was generated by sampling over *ka* and total RelA-containing NF-κB (parameter *NF*; Table S1) as described in Materials and Methods. (*E*) Two-dimensional scatter plots

(legend continued on next page)

remodeling and change transcriptional output on a timescale that is different from the lifetime of the RelA-bound promoter complex, effectively yielding target genes with different transcript abundances while under the control of the same RelA-DNA-binding activity.

Going forward, quantitative models of transcription activated by the NF-κB pathway or other gene regulatory pathways will need to incorporate many contributing factors (i.e., signal decoding, promoter architecture, and chromatin environment) to accurately predict input-output relationships for specific genes in individual cells of different types. This will require the integration of both cell-population "average" and same-cell single-cell experimental measurements as described here (Fig. 6 F). The recruitment of cofactor complexes and changes in chromatin environment at the promoter has been addressed mathematically by modeling promoters as switching between discrete states (43–47). Incorporating this multistate promoter structure into the TNF-RelA signaling model may more accurately capture how RelA activates its transcript targets as compared to varying Hill coefficients for a single-state promoter. A recent study demonstrated how a transcription factor that affects the frequency of transitions between promoter states can cause strong transcriptional responses even with weak binding (48). We recently showed that TNF likely affects both the frequency of transitions between promoter states and the size of the transcriptional bursts in the active promoter state, depending on the chromatin environment at the promoter (12). Accurately modeling how transcription factors influence switching between these states will require additional direct observations of signaling input-output relationships across cell types, signaling pathways, and other gene targets, as well as coupling with measurements and manipulations of additional regulatory factors such as chromatin environment and transcriptional cofactor binding.

SUPPORTING MATERIAL

Six figures and one table are available at http://www.biophysj.org/biophysj/supplemental/S0006-3495(19)30027-X.

AUTHOR CONTRIBUTIONS

V.C.W., S.G., and K.M.-J. conceived of the study. V.C.W. performed experiments. V.C.W., S.M., S.G., and K.M.-J. performed data analysis. S.M. and S.G. performed computational modeling. R.R. contributed to microfluidic protocol design. V.C.W., S.M., S.G., and K.M.-J. prepared figures. S.G. and K.M.-J. wrote the manuscript with contributions from all authors. S.G. and K.M.-J. supervised the research.

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showing the relationship between target mRNA abundance and maximal fold change in nuclear NFκB (for $t = 2$ h) for model simulations with parametrizations chosen in (A)–(D) to recapitulate *HIV 4.4* and *HIV 6.6* data (*top, yellow* and *blue*, respectively) or simulations that show quantitatively and qualitatively different mRNAs versus maximal fold change distributions (*bottom, gray*). Selected parameter values are indicated (*right*); cell-to-cell variability was obtained by sampling total NFκB and *ka* values, and all other parameters were held at their default value in the model. (*F*) A schematic diagram showing some of the informative features of same-cell single-cell data measuring both an input and an output of a signaling pathway.

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Supplemental Information

Fold-Change Detection of NF-*κ*B at Target Genes with Different Transcript Outputs

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Table S1. **List of reactions and parameters in the D2FC model of NF-κB-induced transcription.** For transcriptional reactions: h = hill function exponent, $k1$ is the activation coefficient and kr is the repressive coefficient such that $1/k1$ is the affinity of NF-κB for the promoter and $1/kr$ is the affinity of competitor for the promoter. Parameters for which the value was scanned in a figure panel are indicated. Throughout, "NFκB" refers to a RelA-containing NF-κB dimer.

Phenomena and pertinent reactions	Parameter	Parameter value(s)	Source
TNF stimulation			
TNF	*TR*	1/0 = on/off	*(1)*
TNF + IKKn → IKKa(active) + TNF	*ka*	Sampled, dependent on total NF-κB	*(2)*
Complex formation & dissociation			
Total NFκB	*NF*	Sampled, between 0.04 - 0.4 μM	*(2)*
IkBa + NFκB → IkB:NFκB	*ka1a*	0.5 (μM*s)$^{-1}$	*(1, 3)*
nIkBa + nNFκB → nIkB:NFκB	*ka1a*	0.5 (μM*s)$^{-1}$	*(1, 3)*
IkBa:NFκB → IkBa + NFκB	*kd1a*	0.05 s-1	*(2)*
nIkBa:NFκB → nIkBa + nNFκB	*kd1a*	0.05 s-1	*(2)*
IKK parameters			
TNF + IKKn → IKKa(active) + TNF	*ka*	Sampled, dependent on total NFκB	*(2)*
IKKa → IKKi	*ki*	0.003 s^{-1}	*(1)*
IKKi → IKKN	*kp*	0.0006 s^{-1}	*(1)*
* IKKi → IKKN is sensitive to A20 inhibition rate constant	*kbA20*	0.0018 μM	*(1)*
IKK interactions			
IKKa + IkBa → pIkBa	*kc1a*	0.074 s^{-1}	*(1)*
IKKa + IkBa:NFκB → pIkBa:NFκB	*kc2a*	0.370 s^{-1}	*(1)*
pIkBa → degradation	*kt1a*	0.1 s^{-1}	*(1)*
pIkBa:NFκB → degradation + NFκB	*kt2a*	0.1 s^{-1}	*(1)*
Transport			
NFκB → nNFκB	*ki1*	0.0026 s^{-1}	*(1)*
nNFκB → NFκB	*ke1*	0.000052 s^{-1}	*(1)*
nIkB:NFκB → IkB:NFκB	*ke2a*	0.01 s^{-1}	*(1)*
IkB → nIkB	*ki3a*	0.00067 s^{-1}	*(1)*
nIkB → IkB	*ke3a*	0.000335 s^{-1}	*(1)*
IkB protein synthesis and degradation			
nNFκB → nNFκB + tIkB $h = 2, k1 = k^h, kr = 0;$ with $k = 0.065$	*c1a*	1.4x10^{-7}(μM*s)$^{-1}$	*(1)*
tIkB → tIkB + IkB	*c2a*	0.5 s^{-1}	*(1)*
tIkB → Degradation	*c3a*	0.0003 s^{-1}	*(1)*
IkB → Degradation	*c4a*	0.0005 s^{-1}	*(1)*
IkB:NFκB → NFκB	*c5a*	0.000022 s^{-1}	*(1)*
nIkB:NFκB → nNFκB	-	0 s^{-1}	*(1)*
A20 protein synthesis and degradation			
nNFκB + Competitor → nNFκB + Competitor + tA20 $h = 3, k1 = k^h, kr = k2^h;$ with $k = 0.065, k2 = 0.065$	*c1*	2x10^{-7}(μM*s)$^{-1}$	*(2)*
tA20 → tA20 + A20	*c2*	0.5 s^{-1}	*(1)*
tA20 → Degradation	*c3*	0.0004 s^{-1}	*(2)*
A20 → Degradation	*c4*	0.0045 s^{-1}	(1)
Prototypical inducible target transcript			
nNFκB + Competitor → nNFκB + Competitor + tIndTarget $h = 3, k1 = k^h, kr = k3^h;$ with $k = 0.065, k3 = 0.0325$ or scanned	*c1t*	2x10^{-7}(μM*s)$^{-1}$ or scanned	*(2)*
tIndTarget → Degradation	*c3t*	0.0004 s^{-1} or scanned	*(2)*
Competitor protein synthesis and degradation			
nNFκB + Competitor → nNFκB + Competitor + tCompetitor $h = 3, k1 = k^h, kr = k4^h;$ with $k = 0.065, k4 = 0.065$ or scanned	*c1a*	1.4x10^{-7}(μM*s)$^{-1}$	*(2)*
tCompetitor → tCompetitor + Competitor	*c2a*	0.5 s^{-1}	*(2)*
tCompetitor → Degradation	*c6a*	0.00004 s^{-1}	*(2)*
Competitor→ Degradation	*c4a*	0.0005 s^{-1}	*(2)*

Sources

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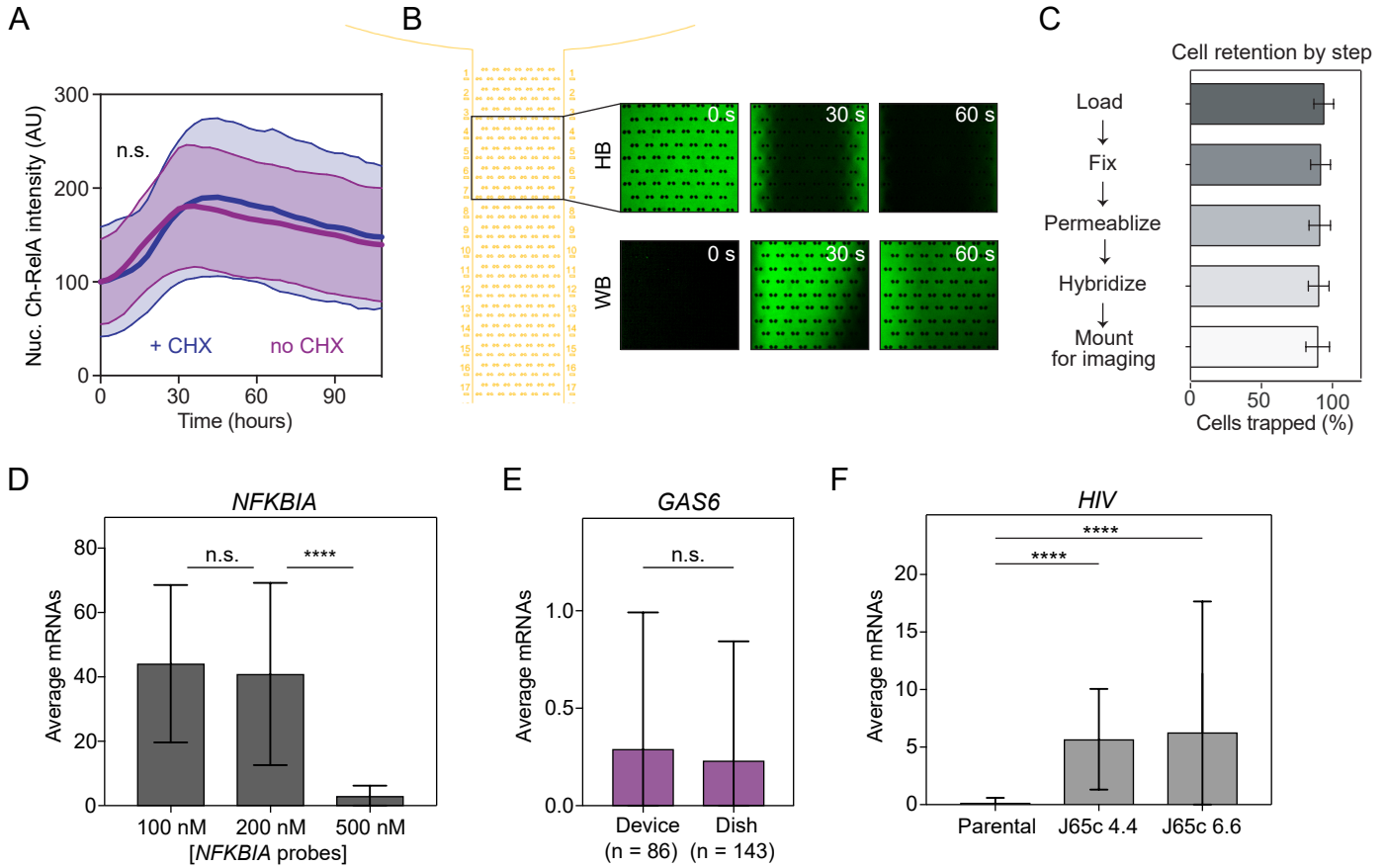
Figure S1 (related to Methods). Optimization of imaging and single-molecule RNA FISH in passive-flow device. (**A**) Time courses of nuclear Ch-RelA in J65c cells infected with latent HIV 6.6 collected in the passive-flow device following stimulation with 20 ng/mL TNF with 160 ng/mL CHX (*blue*) and without CHX (*purple*). Data presented as the mean ± standard deviation (SD; *shaded*) of individual cell traces (n = 30, no CHX; n = 44, + CHX). No changes in cell viability were observed. Lack of statistical significance of differences in dynamics was determined by comparing distributions of t_{max} and $t_{duration}$ of the nuclear RelA intensity peak (n.s., p > 0.05 by Kolmogorov-Smirnov, or K-S, test). (**B**) Time-lapses images taken near the outlet of the passive-flow device during buffer exchanges. Buffer containing BSA conjugated with Alexa Fluor 488 is displaced from the passive-flow device channel by hybridization buffer (HB, *top*) within 60 seconds of adding hybridization buffer to the inlet. Similarly, the hybridization buffer is displaced from the channel by wash buffer (WB, *bottom*) containing BSA conjugated with Alexa Fluor 488 within 60 seconds of adding the wash buffer to the inlet. (**C**) Bar graph quantifying cell retention in the flow device after each step in the smFISH protocol. Fraction of cells remaining trapped after each step was determined by counting the number of trapped cells and dividing it by the total number of traps per device. Data are presented as the mean ± SD for three devices. (**D**) Bar graph of mean *NFKBIA* transcripts for cells stimulated with 20 ng/mL TNF for 1 hour in the device and labelled with increasing *NFKBIA*-specific probes concentrations. Data are presented as the mean ± SD of mRNA molecules per cell. Cell numbers: n = 67, 100 nM; n = 62, 200 nM; n = 61, 500 nM. (**E**) Bar graph of mean *GAS6* transcripts for basal cells in a tissue culture dish and in the passive-flow device. Data are presented as the mean ± SD of mRNA molecules per cell. Cell numbers: n = 143, dish; n = 86, device. (**F**) Bar graph of mean HIV transcripts for HIV-infected cells and parental Jurkat cells (negative control) stimulated with 20 ng/mL TNF for 2 hours. Data are presented as the mean ± SD of mRNA molecules per cell. Cell numbers: n = 74, parental; n = 227, J65c 4.4; n = 211, J65c 6.6. Statistics in (**D-F**) n.s. = not significant, ****p < 0.0001, as determined by K-S, test.

Figure S2. The D2FC model for NF-κB-dependent transcription incorporates an I1-FFL through competition on target genes promoters. Process diagram of the D2FC model. Different arrow types represent different processes or regulatory influences, reaction (binding and unbinding), transport, transcription, translation, activation or inhibition, as indicated below the diagram. Molecular species are indicated in *blue*, and the parameters for each reaction in *green* type. The model allows transport between two compartments, the cytosol and the nucleus.

Figure S3 (related to Fig. 2). Nuclear Ch-RelA translocation dynamics show subtle differences between dish and device but max fold change in nuclear Ch-RelA does not. (**A**) Measured time courses of nuclear Ch-RelA from J65c cells collected in the passive-flow device (*purple*) versus in a tissue culture dish (*gray*) after 20 ng/mL TNF treatment. Data presented as the mean ± SD of individual cell time courses (n = 30, device; n = 68, dish). (**B**) Measured time courses of nuclear Ch-RelA collected in the passive-flow device after 20 ng/mL TNF treatment for cells positioned in the rows 0-2 by the inlet (*gray*) versus rows 10+ closer to the outlet. Data presented as the mean ± SD of individual cell time courses combined from several experiments (n = 40, *gray*; n = 26, *red*). In A-B, significant differences in dynamics were evaluated by comparing distributions of t_{max} and $t_{duration}$ of the nuclear RelA intensity peak between the two data sets (***, p < 0.001; n.s., p > 0.05 by K-S test; see Methods for more details). (**C**) One-dimensional scatter plots of the maximum fold change in nuclear Ch-RelA in individual cells for J65c cells in a tissue culture dish (*left*) or in the passive-flow device (*center, right*). Each dot represents an individual cell (Dish, n = 68, Device, Expt #1 n = 30 and Expt #2 n = 39); bars show the mean ± SD. The distributions are not significantly different (n.s., p > 0.05 by K-S test). (**D**) Matrix of correlations between RelA signaling features extracted from the time-course data. AUC_{norm} is the area under the curve for the time course of nuclear Ch-RelA after substraction of its initial value (time course of $F-F_{init}$). Yellow outlines mark pairwise correlations > 0.95. Ellipses are shaped and shaded according to the direction and strength of correlation.

A Mean transcript number

Baseline

	k4 = 0.1*k	k4 = 0.2*k	k4 = 0.5*k	k4 = 1*k	k4 = 2*k	k4 = 5*k	k4 = 10*k
k3 = 0.05*k	1	0	0	0	0	0	0
k3 = 0.1*k	1	1	0	0	0	0	0
k3 = 0.2*k	45	11	1	0	0	0	0
k3 = 0.5*k	243	114	21	5	1	0	0
k3 = 1*k	338	285	116	35	8	1	0
k3 = 2*k	354	345	287	165	57	10	3
k3 = 5*k	352	354	354	333	270	109	37

2-hour TNF

	k4 = 0.1*k	k4 = 0.2*k	k4 = 0.5*k	k4 = 1*k	k4 = 2*k	k4 = 5*k	k4 = 10*k
k3 = 0.05*k	1	0	0	0	0	0	0
k3 = 0.1*k	2	2	0	0	0	0	0
k3 = 0.2*k	57	17	2	1	0	0	0
k3 = 0.5*k	210	117	32	8	2	1	0
k3 = 1*k	324	248	122	51	16	4	1
k3 = 2*k	359	342	257	166	80	21	7
k3 = 5*k	366	370	362	334	265	136	61

(scale: 0 – 400)

B r_P - transcript number vs. max nRelA fold change

	k4 = 0.1*k	k4 = 0.2*k	k4 = 0.5*k	k4 = 1*k	k4 = 2*k	k4 = 5*k	k4 = 10*k
k3 = 0.05*k	0.76	0.77	0.80	0.74	0.76	0.75	0.77
k3 = 0.1*k	0.74	0.73	0.76	0.75	0.75	0.75	0.76
k3 = 0.2*k	0.53	0.73	0.76	0.75	0.75	0.74	0.77
k3 = 0.5*k	-0.06	0.17	0.69	0.76	0.74	0.75	0.78
k3 = 1*k	-0.05	-0.19	0.24	0.63	0.74	0.77	0.78
k3 = 2*k	0.04	-0.02	-0.07	0.14	0.57	0.77	0.78
k3 = 5*k	0.12	0.13	-0.05	-0.00	0.07	0.44	0.69

(scale: < 0.30 – 1.00)
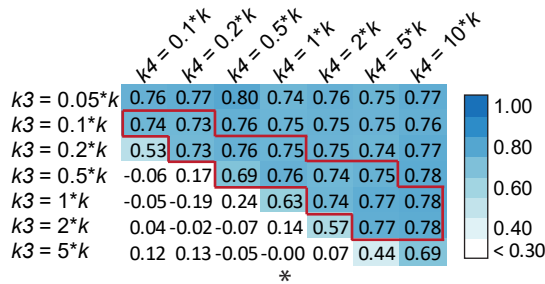
C Log_{10}(Relative variance)

	k4 = 0.1*k	k4 = 0.2*k	k4 = 0.5*k	k4 = 1*k	k4 = 2*k	k4 = 5*k	k4 = 10*k
k3 = 0.05*k	1.31	1.48	1.75	1.82	2.03	2.07	2.39
k3 = 0.1*k	1.37	1.45	1.75	1.89	1.97	2.11	2.43
k3 = 0.2*k	0.54	1.11	1.57	1.89	2.07	2.31	2.14
k3 = 0.5*k	-0.11	0.13	0.92	1.59	1.98	2.32	2.28
k3 = 1*k	-0.11	-0.11	0.15	0.84	1.62	2.23	2.39
k3 = 2*k	0.04	-0.01	-0.18	0.12	0.85	1.85	2.23
k3 = 5*k	0.10	0.11	0.16	-0.01	0.20	0.62	1.40

(scale: 0.00 – 2.40)
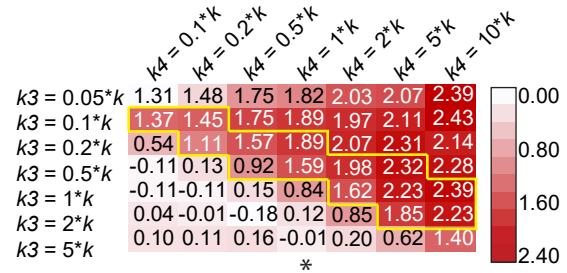
D Mean 'fraction bound' RelA

t = 0 min (basal)

	k4 = 0.1*k	k4 = 0.2*k	k4 = 0.5*k	k4 = 1*k	k4 = 2*k	k4 = 5*k	k4 = 10*k
k3 = 0.05*k	0.00	0.00	0.00	0.00	0.00	0.00	0.00
k3 = 0.1*k	0.00	0.00	0.00	0.00	0.00	0.00	0.00
k3 = 0.2*k	0.07	0.02	0.00	0.00	0.00	0.00	0.00
k3 = 0.5*k	0.37	0.18	0.03	0.01	0.00	0.00	0.00
k3 = 1*k	0.51	0.43	0.18	0.05	0.01	0.00	0.00
k3 = 2*k	0.53	0.52	0.43	0.25	0.09	0.02	0.00
k3 = 5*k	0.53	0.53	0.53	0.50	0.40	0.17	0.06

t = 30 min

	k4 = 0.1*k	k4 = 0.2*k	k4 = 0.5*k	k4 = 1*k	k4 = 2*k	k4 = 5*k	k4 = 10*k
k3 = 0.05*k	0.02	0.00	0.00	0.00	0.00	0.00	0.00
k3 = 0.1*k	0.04	0.04	0.01	0.00	0.00	0.00	0.00
k3 = 0.2*k	0.48	0.21	0.04	0.01	0.00	0.00	0.00
k3 = 0.5*k	0.83	0.67	0.33	0.12	0.03	0.01	0.00
k3 = 1*k	0.87	0.85	0.68	0.44	0.19	0.04	0.01
k3 = 2*k	0.88	0.88	0.84	0.76	0.54	0.23	0.09
k3 = 5*k	0.88	0.86	0.88	0.88	0.85	0.69	0.49

(scale: 0.00 – 1.00)

t = 60 min

	k4 = 0.1*k	k4 = 0.2*k	k4 = 0.5*k	k4 = 1*k	k4 = 2*k	k4 = 5*k	k4 = 10*k
k3 = 0.05*k	0.00	0.00	0.00	0.00	0.00	0.00	0.00
k3 = 0.1*k	0.02	0.00	0.00	0.00	0.00	0.00	0.00
k3 = 0.2*k	0.12	0.03	0.01	0.00	0.00	0.00	0.00
k3 = 0.5*k	0.53	0.29	0.08	0.02	0.01	0.00	0.00
k3 = 1*k	0.68	0.60	0.32	0.14	0.05	0.01	0.00
k3 = 2*k	0.70	0.70	0.60	0.44	0.22	0.07	0.02
k3 = 5*k	0.70	0.70	0.70	0.68	0.61	0.39	0.21

Figure S4 (related to Fig. 4). 2D parameter scan of the competitor affinity for target promoter vs. the parameter controlling competitor abundance predicts decreased RelA binding with decreasing transcript output. Heatmaps of the outputs of a parameter scan of competitor affinity ($k3$; *columns*) and the parameter tuning relative competitor abundance ($k4$; *rows*) producing a range of (**A**) median transcriptional output before and 2 hours after TNF stimulation (*gray*), (**B**) the corresponding Pearson correlation coefficients (r_p) of transcript abundance at 2 hours post-TNF with maximum fold change in nuclear RelA (*blue*), (**C**) the relative variance of transcripts before and two hours after TNF stimulation (calculated as $\log_{10}(\text{Var}_{t=120\,min}/\text{Var}_{t=0\,min})$) and (**D**) mean fraction of RelA bound at the target gene promoter (*FB*) at 0, 30, and 60 min after TNF stimulation. Both $k3$ and $k4$ are expressed as a function of affinity of RelA binding to a target promoter (k). The range of $k3$ and $k4$ combinations that correspond to our experimentally observed absolute change in transcript abundance induced by TNF at 2 hours is outlined in red in each heat map. The asterisk marks a column discussed in Fig. 4 ($k4 = 1*k$).

Parameter	total nuclear NFκB			target gene transcript				
	$\frac{F_{max}}{F_{init}}$	F_{init}	F_{max}	$\frac{mRNAs_{max}}{mRNAs_{init}}$	$mRNAs_{init}$	$mRNAs_{max}$	$mRNAs_{t=2h}$	
ka	0.62	0.00	0.64	0.90	0.00	0.66	0.44	ka
kv	0.56	0.26	0.86	0.92	0.04	0.72	0.38	kv
NF	0.54	0.73	1.38	0.61	0.39	0.95	0.96	NF
ka1a	0.52	-0.43	0.05	0.91	-0.24	0.34	0.08	ka1a
kc2a	0.50	0.00	0.52	0.74	0.00	0.54	0.36	kc2a
c2a	0.36	-0.80	-0.45	1.11	-1.02	-0.43	-0.82	c2a
c1a	0.34	-0.74	-0.44	0.81	-0.49	-0.03	-0.44	c1a
ki3a	0.23	-0.36	-0.13	0.57	-0.28	0.08	-0.20	ki3a
ke2a	0.20	-0.19	0.01	0.15	-0.02	0.09	0.04	ke2a
kc1a	0.15	0.00	0.16	0.23	0.00	0.17	0.11	kc1a
h	0.02	-0.10	-0.08	1.27	-0.41	0.37	-0.05	h
kt2a	0.00	0.00	0.00	0.00	0.00	0.00	0.00	kt2a
k4	0.00	0.00	0.00	0.97	-1.37	-0.99	-0.73	k4
kp	0.00	0.00	0.00	0.00	0.00	0.00	0.00	kp
kbA20	0.00	0.00	0.00	0.00	0.00	0.00	0.00	kbA20
c4	0.00	0.00	0.00	0.00	0.00	0.00	0.00	c4
c3	0.00	0.00	0.00	0.60	-0.69	-0.41	-1.07	c3
tv	0.00	0.00	0.00	0.00	0.00	0.00	0.00	tv
kt1a	0.00	0.00	0.00	0.00	0.00	0.00	0.00	kt1a
k3	0.00	0.00	0.00	-1.19	2.32	1.45	1.14	k3
c1t	0.00	0.00	0.00	0.00	1.00	1.03	1.00	c1t
ht	0.00	0.00	0.00	1.88	-1.71	-0.25	-0.44	ht
c3t	0.00	0.00	0.00	0.56	-0.90	-0.43	-1.38	c3t
c1	0.00	0.00	0.00	0.27	0.19	0.43	0.23	c1
c6a	0.00	0.00	0.00	-0.44	0.55	0.30	0.19	c6a
c2	0.00	0.00	0.00	0.00	0.00	0.00	0.00	c2
k2	0.00	0.00	0.00	0.00	0.00	0.00	0.00	k2
c5a	-0.02	0.02	0.01	-0.03	0.01	-0.01	0.00	c5a
ke1	-0.05	-0.01	-0.06	-0.07	-0.01	-0.06	-0.05	ke1
ke3a	-0.05	0.03	-0.02	-0.10	0.02	-0.05	-0.02	ke3a
ki1	-0.25	0.59	0.33	-0.51	0.31	-0.01	0.14	ki1
k	-0.40	0.72	0.31	-0.65	-0.09	-0.58	-0.32	k
kd1a	-0.45	0.46	-0.01	-0.79	0.25	-0.30	-0.04	kd1a
c3a	-0.46	0.96	0.45	-1.00	0.61	-0.11	0.44	c3a
ki	-0.54	0.00	-0.56	-0.86	0.00	-0.64	-0.47	ki
c4a	-0.64	0.95	0.22	-1.64	1.23	-0.04	0.37	c4a

Column minimum   0   Column maximum

Figure S5 (related to Fig. 5). Distinct sets of parameters affect nuclear RelA dynamics and target gene transcript numbers. Heat map of the outputs of a sensitivity analysis showing the normalized local sensitivity indices for total nuclear NF-κB (*left*) and target gene transcript (*right*) with respect to the parameters indicated for each row. For total nuclear NF-κB, sensitivity was calculated for fold change (F_{max}/F_{init}), initial concentration (F_{init}) and maximal concentration (F_{max}). For target gene transcript, sensitivity was calculated for fold change ($mRNAs_{max}/mRNAs_{init}$), and initial ($mRNAs_{init}$), maximal ($mRNAs_{max}$) and t = 2 h TNF ($mRNAs_{t=2h}$) abundances. On the left, parameters highlighted in yellow were varied to mimic cell-to-cell variability (*ka*, NF, Figures 4, 5, 6 and S6); on the right, parameters highlighted in yellow were varied in the five-dimensional parameter scan (*k4*, *k3*, *c1t*, *ht*, *c3t*; Figures 5 and S6).
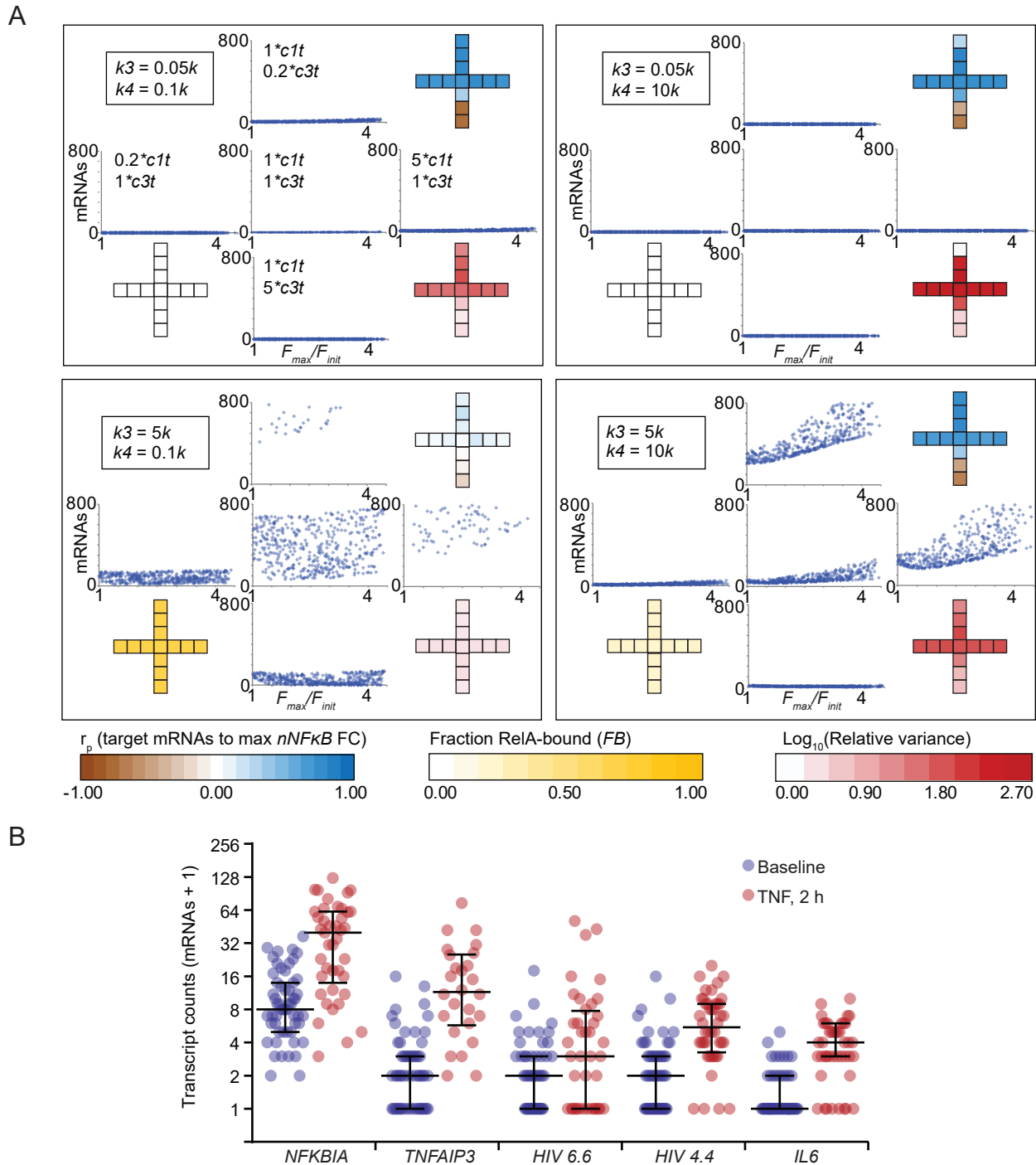
Figure S6 (related to Fig. 5). Refining parameter clouds to identify model simulations that reproduce transcript abundance, fold-change detection, and fractional RelA binding patterns observed in experiments. (**A**) Parameter spaces were explored for each corner of the parameter range presented in Fig. 5A (fixed $k3$ and $k4$ as indicated). Plots depict the simulated values of transcript number versus F_{max}/F_{init} for nuclear RelA ($nNF\kappa B$ in the model) for five pairs of fixed $c1t$ and $c3t$ values (as marked on the top right panel). Heat map crosses indicate the values for Pearson correlation of mRNAs at $t = 2$ h to fold change (r_p with FC = F_{max}/F_{init}; *brown-to-blue*), the fraction RelA bound (*FB*; *white-to-yellow*) and the relative variance (calculated as $\log_{10}(\text{Var}_{t=120\,min}/\text{Var}_{t=0\,min}$; *white-to-red*). (**B**) One-dimensional scatter plots showing the median and interquartile range (IQR) of experimental smFISH transcript numbers distributions at baseline (*blue*) and 2 hours after TNF stimulation (*red*). The IQRs were then used to identify plausible parameter sets associated with each target gene (Fig. 5B).