

## Supplementary Information

### Influence of the lignin content on the properties of poly(lactic acid)/lignin-containing cellulose nanofibrils composite films

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#### Surface energy calculation

The theory of the contact angle of pure liquids on a solid responds to the widely applied Young's equation (Eq. S1):

$$\gamma_L \cos \theta = \gamma_S - \gamma_{SL} \quad (\text{S1})$$

where  $\gamma_L$  is the experimentally determined surface energy of the liquid,  $\theta$  is the contact angle,  $\gamma_S$  is the surface energy of the solid and  $\gamma_{SL}$  is the solid/liquid interfacial energy.

Surface energy values were calculated according to the acid-base theory, which also allowed to obtain the disperse, acid and base components. Acid-base theory introduces a combining rule that factors molecular consideration and theories of intermolecular forces and eliminates  $\gamma_{SL}$  from Young's equation. The total surface energy of a solid ( $\gamma_S$ ) is calculated from the sum of one disperse component, associated with polar component ( $\gamma_S^p$ ) and dispersion component ( $\gamma_S^d$ ) (Eq. S2).

$$\gamma_S = \gamma_S^p + \gamma_S^d \quad (\text{S2})$$

In addition, we derived the relations between polar component and dispersion component of liquids and solids (Eq. S3).

$$\gamma(1 + \cos \theta) = 2\sqrt{\gamma_S^d \gamma_L^d} + 2\sqrt{\gamma_S^p \gamma_L^p} \quad (\text{S3})$$

Where  $\gamma_L^p$  is the polar component of test liquids,  $\gamma_L^d$  is the dispersion component of test liquids. The  $\gamma_S^p$  and  $\gamma_S^d$  can be obtained by taking the  $\gamma_L^p$  and  $\gamma_L^d$  of each two test liquids in to equation S3.