

## Supplementary file

# Photopatternable PEDOT:PSS/PEG hybrid thin film with moisture stability and sensitivity

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### THEORETICAL CALCULATION OF BENDING RADIUS AND INDUCED STRAIN

As shown in Supplementary Figure S2, the computer-controlled step motor can control the end-to-end length ( $L-dL$ ) of the hybrid film. Therefore, we can use the experimentally measured distant change to calculate the bending radius ( $r$ ) and its induced strain ( $\epsilon$ ), using the classic bending theory as outlined below<sup>1</sup>:

$$r = \frac{L}{2\pi \sqrt{\frac{dL}{L} - \frac{\pi^2 h^2}{12L^2}}}$$

$$\epsilon = \frac{h}{2r}$$

where  $L$  is the initial film length,  $dL$  is the compressed distance, and  $h$  is the thickness of the hybrid film. Using the equations above, the strain experienced by PEDOT:PSS film is estimated at 1.25% given a bending radius of 10 mm.

### THEORETICAL CALCULATION OF DEVICE SENSITIVITY

PEG has a strong capacity to absorb water from humid environment, and the amount of water that can be absorbed is determined by the open pores volume, radius size, and pore distribution. To estimate change of capacitance under different humidity level in theory, different PEGDA concentration of water solutions were prepared and PEG hydrogel films with different pore sizes were formed under UV exposure. After fully dried in 80 °C oven for 1 h, PEG films were put into humidity control tank, which is controlled by nitrogen gas and Air-O-Swiss 7144 humidifier. All PEG films were maintained under each relative humidity environment for 30 min and then weighed the change of mass. The fractional volume of water absorbed in each PEG films under different relative humidity was plotted in Supplementary Figure S3a. Since water has relatively high dielectric constant (~80) compared with PEG (~10), dielectric constant of PEG film will increase after water sorption, which can be expressed as:

$$\epsilon_{\text{wet}} = \left[ \gamma \left( \epsilon_{\text{water}}^{\frac{1}{3}} \epsilon_{\text{dry}}^{\frac{2}{3}} \right) + \epsilon_{\text{dry}}^{\frac{1}{3}} \right]^3$$

And then

$$\frac{\Delta\epsilon}{\epsilon_0} = \frac{\epsilon_{\text{wet}} - \epsilon_{\text{dry}}}{\epsilon_{\text{dry}}}$$

where  $\gamma$  is the fractional volume of water that absorbed in the PEG film,  $\epsilon_{\text{wet}}$  and  $\epsilon_{\text{dry}}$  are dielectric constants of wet and dry PEG film,

respectively<sup>2</sup>. According to the relationship between dielectric constant and water uptake fraction, the change of dielectric constant of PEG versus relative humidity was plotted in Supplementary Figure S4b.

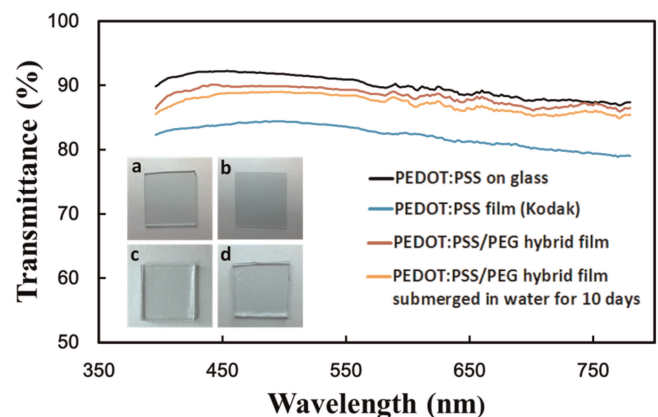
Considering dielectric constant differences between different components and edge effects, the capacitance of the fringe capacitive humidity sensor can be expressed as<sup>2</sup>:

$$C = (N - 3) \frac{C_I}{2} + \frac{2C_I C_E}{C_I + C_E}, \quad N > 3$$

$$C_I = \epsilon_0 L \left( \epsilon_{\text{air}} C'(\infty) \left( \frac{1}{\epsilon_p C'(h)} + \frac{1}{\epsilon_s} \left( \frac{1}{C'(h)} - \frac{1}{C'(\infty)} \right) \right) \right)^{-1}$$

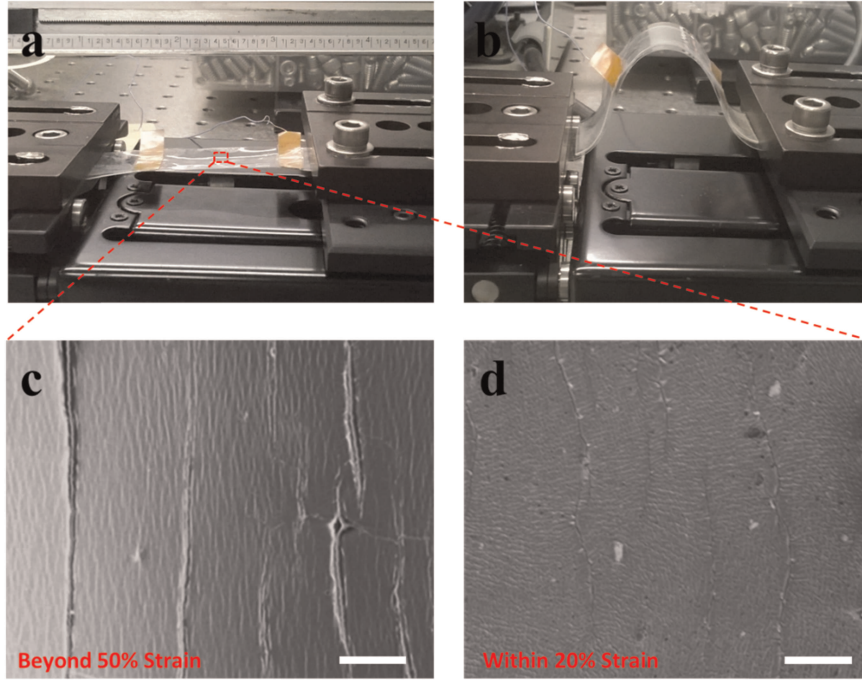
$$C_E = \epsilon_0 L \left( \epsilon_{\text{air}} C'(\infty) \left( \frac{1}{\epsilon_p C'(h)} + \frac{1}{\epsilon_s} \left( \frac{1}{C'(h)} - \frac{1}{C'(\infty)} \right) \right) \right)^{-1}$$

where  $C_I$  is the half capacitance between one interior electrode and ground,  $C_E$  is the capacitance between one outer electrode and ground, and  $N$  is the number of electrodes.  $\epsilon_{\text{air}}$ ,  $\epsilon_p$ , and  $\epsilon_s$  are relative dielectric constant of air, PEG layer, and PDMS substrate layer, respectively.  $C(\infty)$  is the geometric capacitance of an infinite layer and  $C(h)$  is the geometric capacitance of the PEG layer with

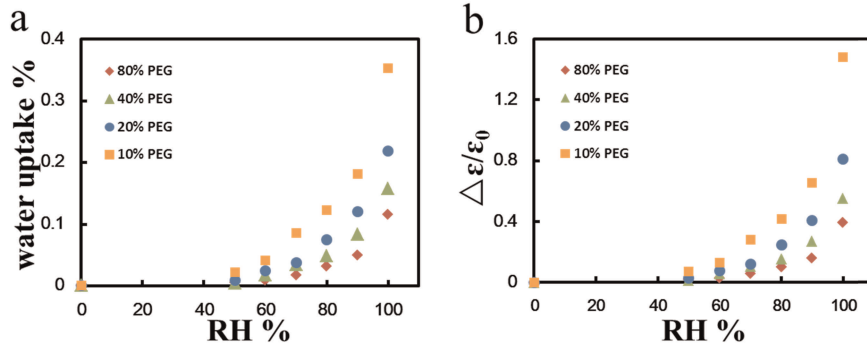


**Figure S1** Transmittance measurement. Optical transmittance and photos of (a) PEDOT:PSS film spin-coated on glass. (b) Commercial PEDOT:PSS film on PET (Kodak). (c) PEDOT:PSS/PEG hybrid film on PDMS before water treatment. (d) PEDOT:PSS/PEG hybrid film on PDMS after 10-day water treatment.

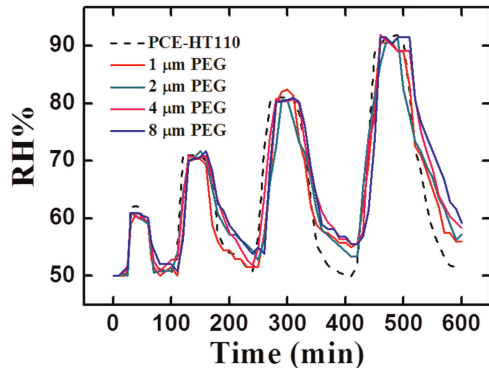
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**Figure S2** Tensile and bending tests. Measurement set-up for (a) tensile and (b) bending tests and SEM images of the surface of PEDOT:PSS/PEG hybrid film on PDMS after (c) stretched beyond 50% strain (scale bar: 50  $\mu\text{m}$ ), (d) stretched within 20% strain (scale bar: 10  $\mu\text{m}$ ).



**Figure S3** (a) Fractional volume of water absorbed in various PEG film under different humidity environment. (b) Theoretically calculation of PEG dielectric constant change under different humidity environment.



**Figure S4** PEG thickness effect on response time. Sensor responses to humidity change with different PEG thicknesses.

thickness  $h$ . To simplify calculation, edge effect was neglected and equations above can be expressed as:

$$C = \frac{(N+1)}{2} C_l$$

$$= \frac{(N+1)}{2} \epsilon_0 L \epsilon_{\text{air}} C(\infty) \left( \frac{1}{\epsilon_p C(h)} + \frac{1}{\epsilon_s} \left( \frac{1}{C(h)} - \frac{1}{C(\infty)} \right) \right)^{-1}$$

Since we only care about the change of dielectric constant in PEG and the change in air and substrate can be neglected, then the change of capacitance can be simplified as:

$$\frac{\Delta C}{C_0} = \frac{\frac{\epsilon_{\text{wet}}}{\epsilon_{\text{wet}} + \epsilon_s} - \frac{\epsilon_{\text{dry}}}{\epsilon_{\text{dry}} + \epsilon_s}}{\frac{\epsilon_{\text{dry}}}{\epsilon_{\text{dry}} + \epsilon_s}} \approx \frac{\frac{\Delta \epsilon}{\epsilon_0}}{1}$$

where  $\epsilon_s$  is dielectric of PDMS substrate ( $\sim 2.5$ ).

## THEORETICAL CALCULATION OF DEVICE SENSITIVITY

According to Montgomery's work<sup>3</sup>, the vertical gradient of water vapor can be expressed as:

$$\frac{dP}{d\ln z} = \frac{P_b - P_a}{\ln b/a}$$

And

$$\Gamma \equiv \frac{P_b - P_a}{P_s - P_a} \frac{1}{\ln b/a}$$

where  $P_b$ ,  $P_a$ , and  $P_s$  are vapor pressure at the height  $a$ ,  $b$ , and at the surface, respectively. For a smooth surface, assuming that the vertical transfer of water vapor is independent of height, the evaporation coefficient can be calculated by<sup>4</sup>:

$$\Gamma = \left( \frac{\lambda \nu k_0}{\kappa} + \ln \frac{k_0 \gamma_0 W_0 a}{\kappa} \right)^{-1}$$

where  $\lambda$  is a numerical factor,  $\kappa$  is the kinematic coefficient of diffusion of vapor in air,  $\nu$  is the kinematic viscosity of the air,  $k_0$  is von Karman's constant,  $\gamma_0$  is the resistance coefficient, and  $W_0$  is the wind velocity at the height  $a$ , in which way, the change of RH is directly proportional to  $-\ln(b/a)$ .

## REFERENCES

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