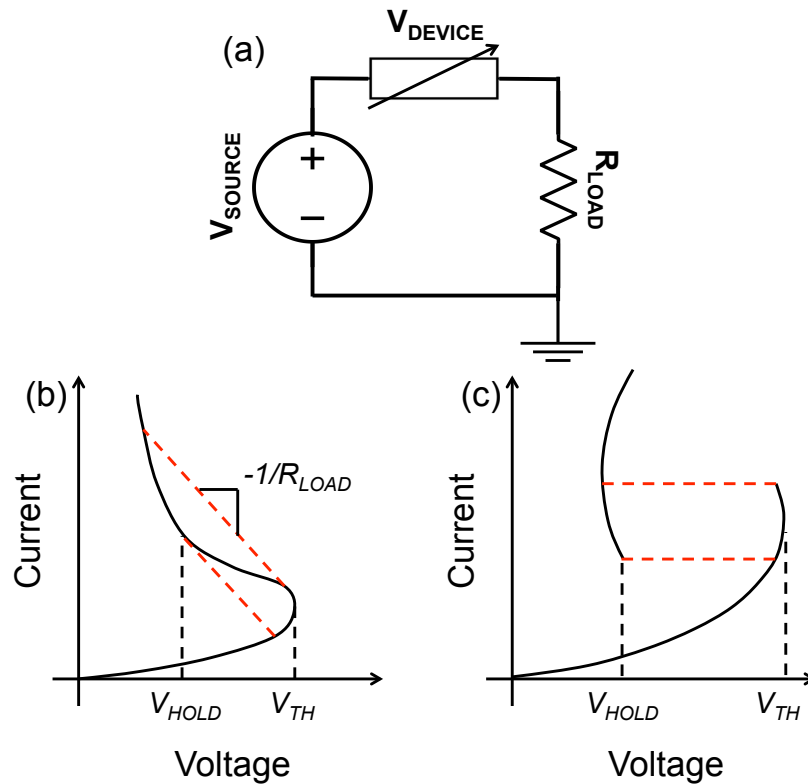


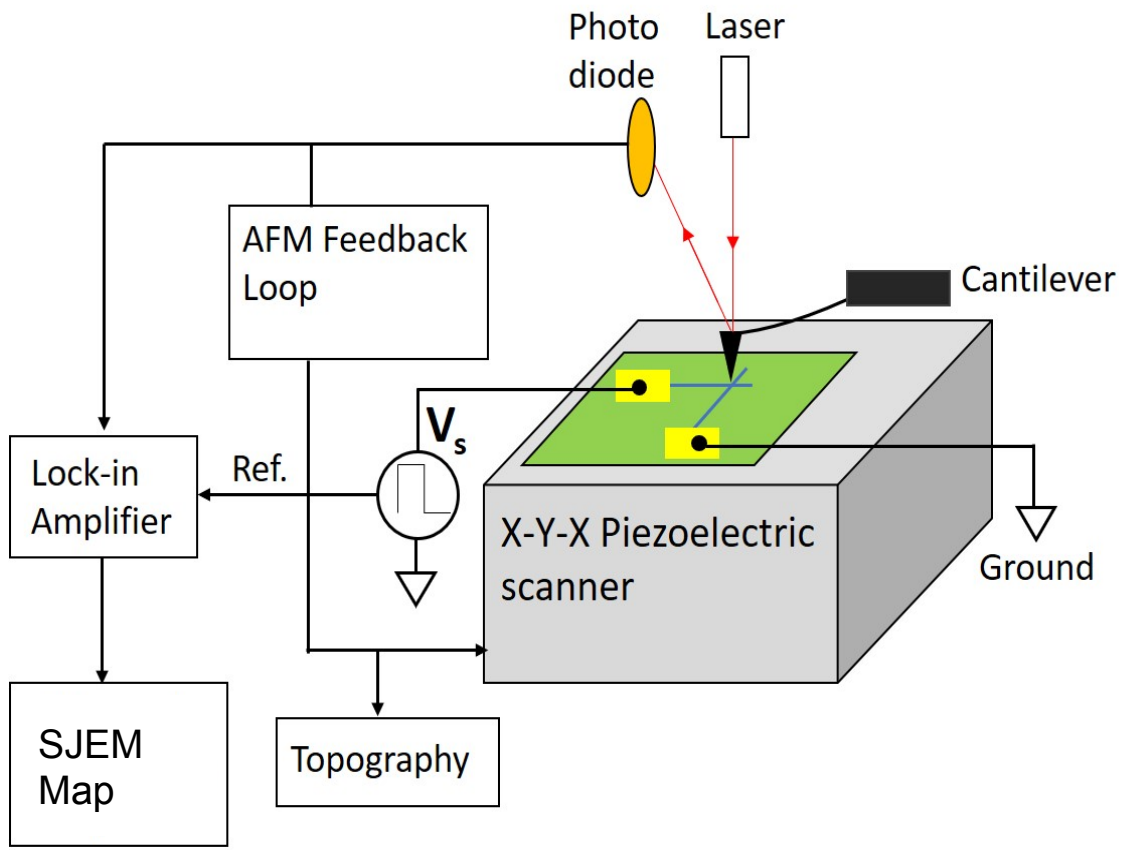
Spontaneous current constriction in threshold switching devices

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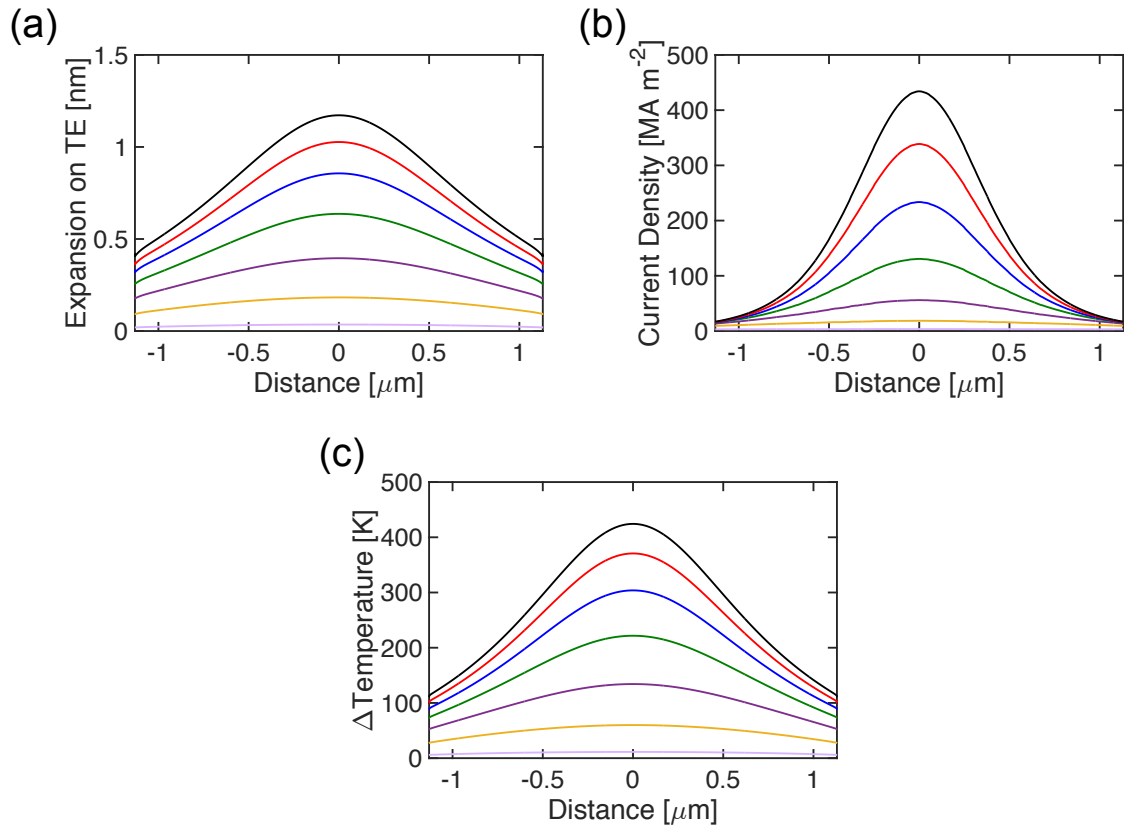
Supplementary Information



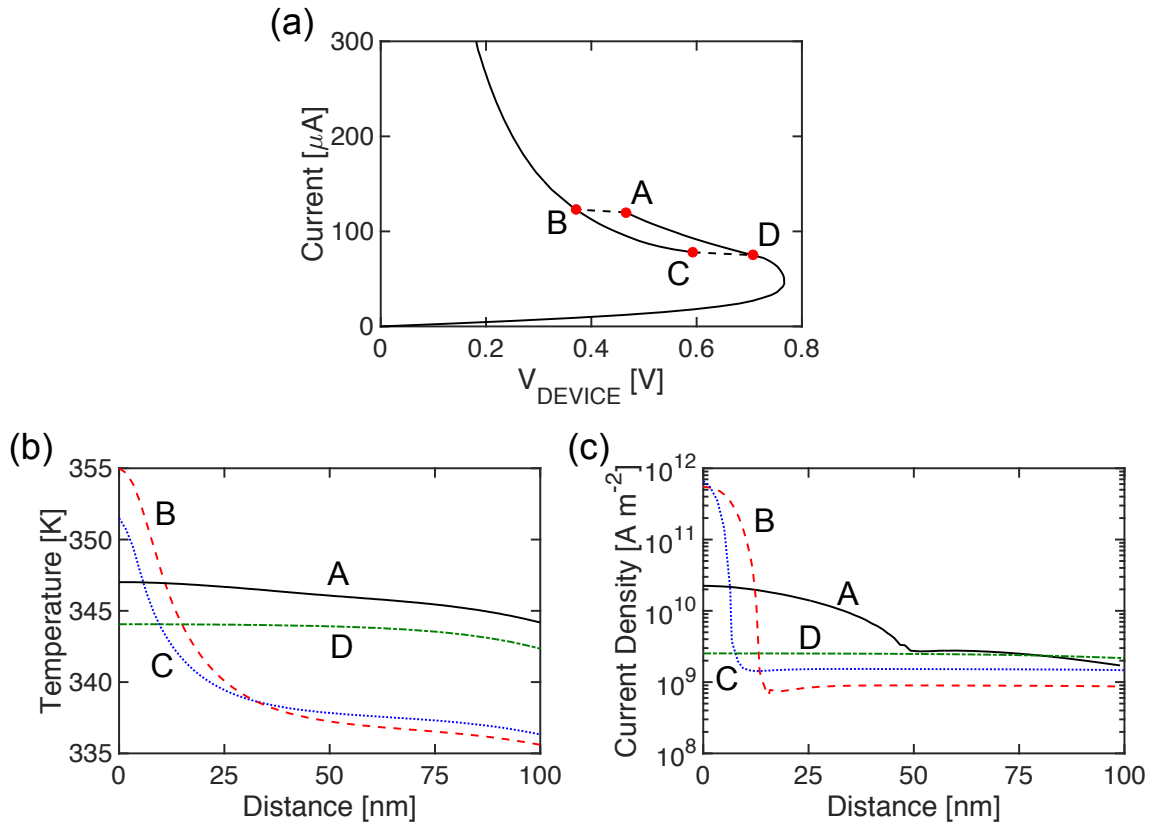
Supplementary Figure 1. Schematic of testing set-up and observed TaO_x $I-V$ characteristics. (a) Electrical testing circuit layout for $I-V$ characterization and SJEM. Schematic of (b) S-NDR $I-V$ and (c) multivalued $I-V$.



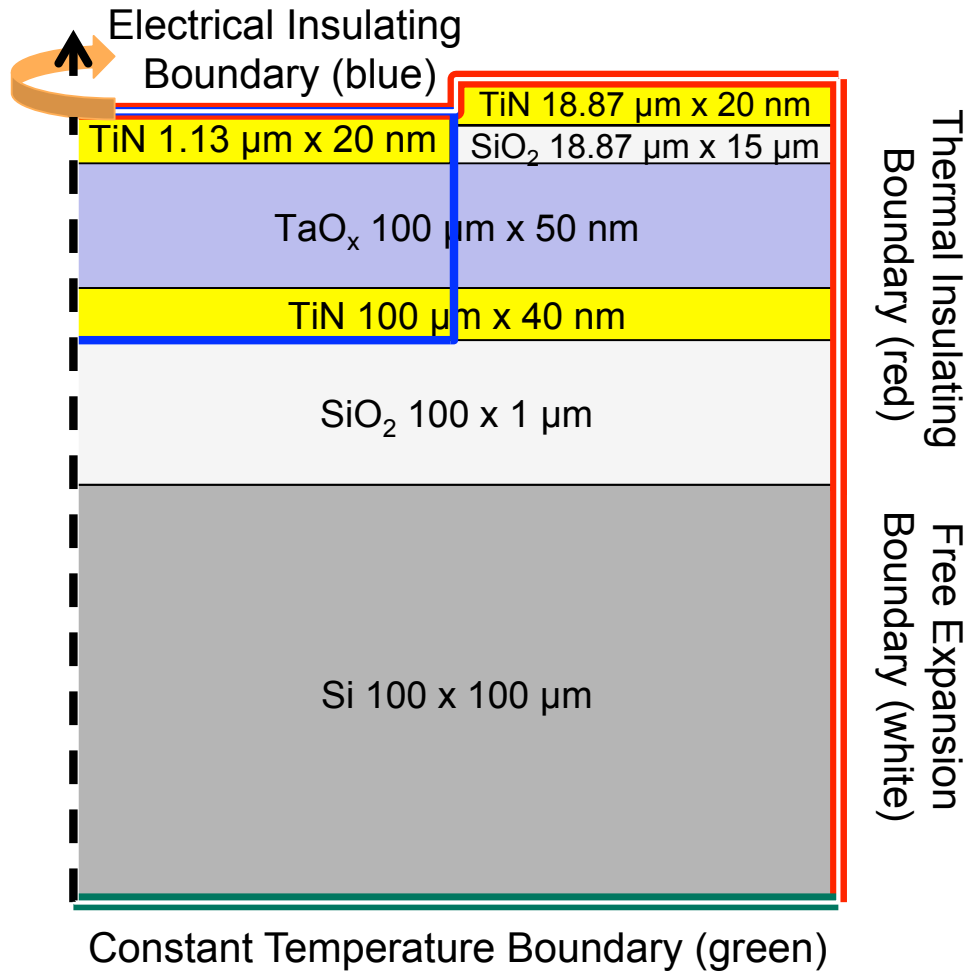
Supplementary Figure 2. Schematic of SJEM measurement setup.



Supplementary Figure 3. Simulated characteristics of a $2 \times 2 \mu\text{m}$ TaO_x device. Simulated line profiles of (a) expansion (b) current density and (c) temperature for all points of equal power dissipation along the I - V shown in Figure 2(b). Source data are provided as a Source Data file.



Supplementary Figure 4. Simulated characteristics of a 200 nm diameter VO₂ device. (a) Simulated I - V for VO₂-based device with current source, shown for reference from Figure 5. (b) Temperature and (c) current density line profiles in the device shown for points A-D along the I - V curve. Source data are provided as a Source Data file.



Supplementary Figure 5. Device structure and boundary conditions used in simulation. The dimensions shown for each layer are indicated as width \times height.

Supplementary Table 1. Material properties used in simulation.

	Si	SiO ₂	TiN ¹	TaO _x ¹
Density (kg·m ⁻³)	2329	2200	5210	8200
Thermal conductivity (W·m ⁻¹ ·K ⁻¹)	130	1.4	5	4
Electrical conductivity (S·m ⁻¹)	N/A	N/A	5×10 ⁶	User defined
Heat capacity (J·kg ⁻¹ ·K ⁻¹)	700	730	545	174
Relative permittivity	N/A	N/A	4	22
Thermal expansion coefficient (1/K)	2.6×10 ⁻⁶	0.5×10 ⁻⁶	1.0×10 ^{-5 2}	5.0×10 ^{-6 3}
Young's Modulus (GPa)	170	70	300 ²	179 ³
Poisson's Ratio	0.28	0.17	0.25 ²	0.27 ³

Supplementary References

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2. Cen, Z. H. *et al.* Temperature effect on titanium nitride nanometer thin film in air. *J. Phys. D. Appl. Phys.* **50**, (2017).
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