

Supplementary Information

Establishing Cost-Effective Computational Models for the Prediction of Lanthanoid Binding in $[\text{Ln}(\text{NO}_3)]^{2+}$ (with Ln = La to Lu)

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Table S.1 contains the predicted Gibbs free energy of reaction for $[\text{Ln}(\text{NO}_3)]^{+2}$ calculated with CCSD(T)-FSI/cc-pVTZ-DK3, MP2-FSI/cc-pVTZ-DK3, CCSD(T)-FSII/cc-pwCVTZ-DK3, MP2-FSI/cc-pV ∞ Z, CCSD(T)-FSI/cc-pV ∞ Z-DK3, and CCSD(T)-FSII/cc-pCV ∞ Z-DK3.

Table S.2 contains the predicted Gibbs free energy of reaction for $[\text{Ln}(\text{NO}_3)]^{+2}$ calculated with the composite Method A and Method B, and the Target Method, CCSD(T)-FSII/cc-pwCV ∞ Z-DK3.

Table S.3 contains absolute and relative cost for target method and f-ccCA for $[\text{Ln}(\text{NO}_3)]^{+2}$ (with Ln = La, Ce, Sm, and Lu).

Table S.1: ΔG_{rxn} (kcal mol⁻¹) for [Ln(NO₃)₂]⁺ calculated with CCSD(T)-FSI/cc-pVTZ-DK3, MP2-FSI/cc-pVTZ-DK3, CCSD(T)-FSII/cc-pwCVTZ-DK3, MP2-FSI/cc-pV ∞ Z, CCSD(T)-FSI/cc-pV ∞ Z-DK3, and CCSD(T)-FSII/cc-pwCV ∞ Z-DK3.

| | CCSD(T)-FSI /cc-pVTZ-DK3 | MP2-FSI /cc-pVTZ- DK3 | CCSD(T)-FSII /cc-pwCVTZ- DK3 | MP2-FSI /cc-pV ∞ Z- DK3 | CCSD(T)-FSI /cc-pV ∞ Z- DK3 | CCSD(T)-FSII /cc-pwCV ∞ Z-DK3 |
|----|-----------------------------|-----------------------------|------------------------------------|--------------------------------------|------------------------------------------|-----------------------------------------|
| La | -485.96 | -483.15 | -485.98 | -474.77 | -477.37 | -478.62 |
| Ce | -493.08 | -490.13 | -493.36 | -482.78 | -485.66 | -485.78 |
| Pr | -520.85 | -534.33 | -528.79 | -526.40 | -515.14 | -522.59 |
| Nd | -514.39 | -554.46 | -550.55 | -546.08 | -519.60 | -544.21 |
| Sm | -511.78 | -509.87 | -511.65 | -503.00 | -505.33 | -505.80 |
| Eu | -460.41 | -453.94 | -460.52 | -446.69 | -452.91 | -452.52 |
| Gd | -514.80 | -512.99 | -515.75 | -506.32 | -508.22 | -508.19 |
| Tb | -521.42 | -520.16 | -522.13 | -513.82 | -515.28 | -514.87 |
| Dy | -519.91 | -519.69 | -520.80 | -513.25 | -513.55 | -514.33 |
| Ho | -581.07 | -594.73 | -587.95 | -586.20 | -577.17 | -581.12 |
| Er | -581.45 | -603.31 | -594.51 | -594.94 | -581.13 | -588.23 |
| Tm | -571.60 | -585.99 | -578.23 | -578.44 | -567.72 | -571.96 |
| Yb | -525.38 | -575.92 | -517.27 | -577.29 | -526.38 | -519.54 |
| Lu | -536.44 | -539.04 | -537.38 | -533.47 | -530.64 | -530.31 |

Table S.2: ΔG_{rxn} (kcal mol⁻¹) for [Ln(NO₃)₂]⁺ calculated with the composite Method A and Method B, and the Target Method, CCSD(T)-FSII/cc-pwCV ∞ Z-DK3

| | Method A $E_{\text{ref}}[\text{MP2}] + \Delta E_{\text{cc}} + \Delta E_{\text{cv}}$ | Method B $E_{\text{ref}}[\text{CCSD(T)}] + \Delta E_{\text{cv}}$ | Target method CCSD(T)-FSII/cc-pwCV ∞ Z-DK3 |
|----|----------------------------------------------------------------------------------------|---------------------------------------------------------------------|------------------------------------------------------|
| La | -478.52 | -478.31 | -478.62 |
| Ce | -486.30 | -486.23 | -485.78 |
| Pr | -522.84 | -525.06 | -522.59 |
| Nd | -535.61 | -549.20 | -544.21 |
| Sm | -504.59 | -505.01 | -505.80 |
| Eu | -452.81 | -452.57 | -452.52 |
| Gd | -508.40 | -508.49 | -508.19 |
| Tb | -514.96 | -515.16 | -514.87 |
| Dy | -513.67 | -513.76 | -514.33 |
| Ho | -577.88 | -582.51 | -581.12 |
| Er | -583.26 | -591.30 | -588.23 |
| Tm | -569.67 | -573.34 | -571.96 |
| Yb | -514.44 | -514.07 | -519.54 |
| Lu | -530.75 | -530.52 | -530.31 |

Table S.3: Relative computational cost calculated with f-ccCA and the target method for $[\text{Ln}(\text{NO}_3)]^{+2}$ (with Ln = La, Ce, Sm, and Lu). [Relative computational cost is shown as a percentage and it is calculated as relative cost = (CPU units with f-ccCA)/(CPU units with target method) x 100]. Values shown in CPU units.

| Ln | CCSD(T)-FSII /cc-pwCV∞Z-DK3+SO (target) | f-ccCA | Relative Cost |
|-----------|----------------------------------------------------------------------|---------------|--------------------------|
| La | 95.07 | 11.28 | 12% |
| Ce | 61.96 | 14.20 | 23% |
| Sm | 64.64 | 9.82 | 15% |
| Lu | 77.89 | 10.39 | 13% |