

Biophysical Journal, Volume 117

Supplemental Information

**Na-K-2Cl Cotransporter and Store-Operated Ca²⁺ Entry in Pacemaking
by Interstitial Cells of Cajal**

Jae Boum Youm, Haifeng Zheng, Sang Don Koh, and Kenton M. Sanders

Supplement equations

A1. Membrane potential

$$\frac{dV}{dt} = \frac{-(I_{\text{total}} + I_{\text{ext}})}{C_m} \#(1)$$

$$I_{\text{total}} = I_{\text{CaL}} + I_{\text{CaT}} + I_{\text{K1}} + I_{\text{NaLCN}} + I_{\text{ClCa}} + I_{\text{Clb}} + I_{\text{Orai}} + I_{\text{NaCa}} + I_{\text{NaK}} \#(2)$$

A2. Constant field equation

$$CF_X = z_X \cdot \frac{F \cdot V}{R \cdot T} \cdot \frac{[X]_i - [X]_o \cdot e^{-z_X \frac{F \cdot V}{R \cdot T}}}{1 - e^{-z_X \frac{F \cdot V}{R \cdot T}}} \#(3)$$

$$CF_{X,\text{md}} = z_X \cdot \frac{F \cdot V}{R \cdot T} \cdot \frac{[X]_{\text{md}} - [X]_o \cdot e^{-z_X \frac{F \cdot V}{R \cdot T}}}{1 - e^{-z_X \frac{F \cdot V}{R \cdot T}}} \#(4)$$

A3. L-type Ca^{2+} current (I_{CaL})

$$I_{\text{CaL}} = I_{\text{CaLCa}} + I_{\text{CaLNa}} + I_{\text{CaLK}} \#(5)$$

$$I_{\text{CaLCa}} = P_{\text{CaL}} \cdot CF_{\text{Ca}} \cdot m \cdot h \#(6)$$

$$I_{\text{CaLNa}} = 0.00005 \cdot P_{\text{CaL}} \cdot CF_{\text{Na}} \cdot m \cdot h \#(7)$$

$$I_{\text{CaLK}} = 0.001 \cdot P_{\text{CaL}} \cdot CF_{\text{K}} \cdot m \cdot h \#(8)$$

$$P_{\text{CaL}} = 57.6 \#(9)$$

$$\alpha_m = 0.002175 \cdot \frac{V + 30}{1 - e^{-\frac{V+30}{2.5}}} \#(10)$$

$$\beta_m = 0.0006315 \cdot \frac{V}{e^{2.5} - 1} \#(11)$$

$$\alpha_h = 1.775 \cdot 10^{-6} \cdot \frac{V + 34}{e^{5.633} - 1} \#(12)$$

$$\beta_h = 0.427 \cdot [\text{Ca}^{2+}]_i \cdot \frac{V + 64}{1 + e^{-\frac{V+44}{4.16}}} \#(13)$$

A4. T-type Ca^{2+} current (I_{CaT})

$$I_{\text{CaT}} = P_{\text{CaT}} \cdot CF_{\text{Ca}} \cdot d \cdot f \#(14)$$

$$P_{\text{CaT}} = 7.92 \#(15)$$

$$d_{\infty} = \frac{1}{1 + e^{-\frac{V+26}{6}}} \#(16)$$

$$\tau_d = 0.6 + \frac{5.4}{1 + e^{0.03 \cdot (V+100)}} \#(17)$$

$$\alpha_d = \frac{d_{\infty}}{\tau_d} \#(18)$$

$$\beta_d = \frac{1 - d_{\infty}}{\tau_d} \#(19)$$

$$f_{\infty} = \frac{1}{1 + e^{-\frac{V+66}{6}}} \#(20)$$

$$\tau_f = 10 + \frac{400}{1 + e^{0.02 \cdot (V+65)}} \#(21)$$

$$\alpha_f = \frac{f_{\infty}}{\tau_f} \#(22)$$

$$\beta_f = \frac{1 - f_{\infty}}{\tau_f} \#(23)$$

A5. Inward rectifier K⁺ current (I_{K1})

$$I_{K1} = G_{K1} \cdot \left(\frac{[K^+]_o}{5.4} \right)^{0.4} \cdot \frac{(V - E_K - 1.73)}{1 + e^{\frac{1.613 \cdot F}{R \cdot T} \cdot (V - E_K - 1.73)}} + a_{K1} \cdot b_{K1} \#(24)$$

$$G_{K1} = 18.0 \#(25)$$

$$E_K = \frac{R \cdot T}{F} \cdot \log \frac{[K^+]_o}{[K^+]_i} \#(26)$$

$$a_{K1} = 10 + \frac{48}{e^{\frac{V+37}{25}} + e^{-\frac{V+37}{25}}} \#(27)$$

$$b_{K1} = \frac{0.0001}{1 + e^{-\frac{V - E_K - 76.77}{17}}} \#(28)$$

A6. Na⁺-leak current (I_{NaLCN})

$$I_{NaLCN} = I_{NaLCN}Na + I_{NaLCN}K \#(29)$$

$$I_{NaLCN}Na = P_{NaLCN} \cdot CF_{Na} \#(30)$$

$$I_{NaLCN}K = 0.9 \cdot P_{NaLCN} \cdot CF_K \#(31)$$

$$P_{\text{NaLCN}} = 0.1485 \#(32)$$

A7. Ca^{2+} -activated Cl current (I_{ClCa})

$$I_{\text{ClCa}} = g_{\text{ClCa}} \cdot O_{\text{ClCa}} \cdot (V - E_{\text{Cl}}) \#(33)$$

$$g_{\text{ClCa}} = 20.0 \#(34)$$

$$E_{\text{Cl}} = \frac{R \cdot T}{F} \cdot \log \frac{[\text{Cl}^-]_{\text{cld}}}{[\text{Cl}^-]_{\text{o}}} \#(35)$$

$$O_{\text{ClCa}\infty} = \left[(1 + e^{(V_h - V)/0.0156}) \left(1 + \left(\frac{\text{EC}_{50}}{[\text{Ca}^{2+}]_{\text{Ano1}}} \right)^2 \right) \right]^{-1} \#(36)$$

$$V_h = -100 \text{ mV} \#(37)$$

$$\tau = t_1 + t_2 \cdot e^{V/t_3} \#(38)$$

$$t_1 = 48.978 \cdot e^{-0.57[\text{Ca}^{2+}]_{\text{Ano1}}} \#(39)$$

$$t_2 = 45.702 \cdot e^{-0.05374[\text{Ca}^{2+}]_{\text{Ano1}}} \#(40)$$

$$t_3 = 133.57 \cdot e^{0.153[\text{Ca}^{2+}]_{\text{Ano1}}} \#(41)$$

$$\text{EC}_{50(0\text{mV})} = 1.39 \cdot 10^{-3} \text{ mM} \#(42)$$

$$\text{EC}_{50} = \text{EC}_{50(0\text{mV})} \cdot e^{-k_c \cdot V} \text{ mM} \#(43)$$

$$k_c = 5.4912 \cdot 10^{-3} \#(44)$$

$$[\text{Ca}^{2+}]_{\text{Ano1}} = \frac{\left(-D_c \cdot K_m + \frac{\sigma}{2\pi r} + C_2 + \sqrt{\left(D_c \cdot K_m + \frac{\sigma}{2\pi r} + C_2 \right)^2 + 4D_c \cdot D_m \cdot B_m \cdot K_m} \right)}{2D_c} \#(45)$$

$$D_c = 250 \cdot 10^{-3} \mu\text{m}^2 \cdot \text{ms}^{-1} \#(46)$$

$$D_m = 75 \cdot 10^{-3} \mu\text{m}^2 \cdot \text{ms}^{-1} \#(47)$$

$$B_m = 50 \cdot 10^{-3} \text{ mM} \#(48)$$

$$K_m = 0.1 \cdot 10^{-3} \text{ mM} \#(49)$$

$$r = 0.05 \mu\text{m} \#(50)$$

$$n_{\text{Orai}} = 250 \#(51)$$

$$C_2 = D_c \cdot [Ca^{2+}]_i - \frac{D_m \cdot B_m \cdot K_m}{K_m + [Ca^{2+}]_i} \#(52)$$

$$\sigma = \frac{J_{Orai} \cdot Vol_{cyt}}{n_{Orai}} \#(53)$$

$$J_{Orai} = \frac{-I_{Orai}}{F \cdot Vol_{cyt}} \#(54)$$

A8. Background Cl⁻ current (I_{Clb})

$$I_{Clb} = P_{Clb} \cdot CF_{Cl} \#(55)$$

$$P_{Clb} = 0.1 \#(56)$$

A9. Current carried by store-operated Ca²⁺ entry (I_{Orai})

$$I_{Orai} = g_{Orai} \cdot O_{Orai} \cdot (V - E_{Ca}) \#(57)$$

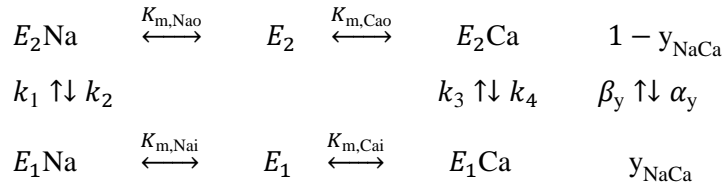
$$E_{Ca} = \frac{R \cdot T}{2 \cdot F} \cdot \log \frac{[Ca^{2+}]_o}{[Ca^{2+}]_i} \#(58)$$

$$g_{Orai} = 0.028 \#(59)$$

$$O_{Orai} = \frac{(K_{m,Ca})^8}{(K_{m,Ca})^8 + (0.021 \cdot [Ca]_{rel})^8} \#(60)$$

$$K_{m,Ca} = 0.2 \text{ mM} \#(61)$$

A10. Na⁺/Ca²⁺ exchange current (I_{NaCa})



$$I_{NaCa} = P_{NaCa} \cdot (k_1 \cdot E_1Na \cdot y_{NaCa} - k_2 \cdot E_2Na \cdot (1 - y_{NaCa})) \#(62)$$

$$P_{NaCa} = 8.458 \text{ pA} \#(63)$$

$$k_1 = e^{\frac{0.32 \cdot F \cdot V}{R \cdot T}} \#(64)$$

$$k_2 = e^{\frac{(0.32-1) \cdot F \cdot V}{R \cdot T}} \#(65)$$

$$k_3 = 1 \#(66)$$

$$k_4 = 1 \#(67)$$

$$K_{m,Na_o} = 87.5 \text{ mM} \#(68)$$

$$K_{m,Ca_o} = 1.38 \text{ mM} \#(69)$$

$$K_{m,Na_i} = 4.375 \text{ mM} \#(70)$$

$$K_{m,Ca_i} = 0.00138 \text{ mM} \#(71)$$

$$\alpha_y = k_2 \cdot E_2Na + k_4 \cdot E_2Ca \#(72)$$

$$\beta_y = k_1 \cdot E_1Na + k_3 \cdot E_1Ca \#(73)$$

$$E_1Na = \left(1 + \frac{1 + [Ca^{2+}]_{cld}/K_{m,Ca_i}}{([Na^+]_{cld}/K_{m,Na_i})^3} \right)^{-1} \#(74)$$

$$E_2Na = \left(1 + \frac{1 + [Ca^{2+}]_o/K_{m,Ca_o}}{([Na^+]_o/K_{m,Na_o})^3} \right)^{-1} \#(75)$$

$$E_1Ca = \left(1 + \frac{1 + ([Na^+]_{cld}/K_{m,Na_i})^3}{[Ca^{2+}]_{cld}/K_{m,Ca_i}} \right)^{-1} \#(76)$$

$$E_2Ca = \left(1 + \frac{1 + ([Na^+]_o/K_{m,Na_o})^3}{[Ca^{2+}]_o/K_{m,Ca_o}} \right)^{-1} \#(77)$$

A11. Na⁺/K⁺ pump current (I_{NaK})

$$I_{NaK} = I_{NaK}A + I_{NaK}B \#(78)$$

$$I_{NaK}A = P_{NaK} \cdot \frac{0.7}{1 + (K_{m,Na_i}/[Na^+]_i)^{1.36}} \cdot \frac{1 - ((V + 50)/250)^2}{1 + K_{m,Ko}/[K^+]_o} \#(79)$$

$$I_{NaK}B = P_{NaK} \cdot \frac{7}{1 + (K_{m2,Na_i}/[Na^+]_i)^3} \cdot \frac{1 - ((V + 50)/250)^2}{1 + K_{m,Ko}/[K^+]_o} \#(80)$$

$$P_{NaK} = 27.65 \#(81)$$

$$K_{m,Na_i} = 3.5 \text{ mM} \#(82)$$

$$K_{m2,Na_i} = 18 \text{ mM} \#(83)$$

$$K_{m,Ko} = 0.27 \text{ mM} \#(84)$$

A12. Na-K-2Cl cotransporter (NKCC1)

$$J_{\text{NKCC,Na}} = P_{\text{NKCC}} \cdot (J_{\text{NKCC,Na influx}} - J_{\text{NKCC,Na efflux}}) \#(85)$$

$$J_{\text{NKCC,K}} = J_{\text{NKCC,Na}} \#(86)$$

$$J_{\text{NKCC,Cl}} = 2 \cdot J_{\text{NKCC,Na}} \#(87)$$

$$P_{\text{NKCC}} = 0.168 \#(88)$$

$$J_{E_1 \rightarrow E_1 \text{NaCl}} = \frac{v_1 \cdot v_2}{v_2 + v_{-1}} \#(89)$$

$$J_{E_1 \leftarrow E_1 \text{NaCl}} = \frac{v_{-2} \cdot v_{-1}}{v_2 + v_{-1}} \#(90)$$

$$J_{E_1 \rightarrow E_1 \text{NaClK}} = \frac{(J_{E_1 \rightarrow E_1 \text{NaCl}}) \cdot v_3}{v_3 + (J_{E_1 \leftarrow E_1 \text{NaCl}})} \#(91)$$

$$J_{E_1 \leftarrow E_1 \text{NaClK}} = \frac{(J_{E_1 \leftarrow E_1 \text{NaCl}}) \cdot v_{-3}}{v_3 + (J_{E_1 \leftarrow E_1 \text{NaCl}})} \#(92)$$

$$J_{E_1 \rightarrow E_1 \text{NaClKCl}} = \frac{(J_{E_1 \rightarrow E_1 \text{NaClK}}) \cdot v_4}{v_4 + (J_{E_1 \leftarrow E_1 \text{NaClK}})} \#(93)$$

$$J_{E_1 \leftarrow E_1 \text{NaClKCl}} = \frac{(J_{E_1 \leftarrow E_1 \text{NaClK}}) \cdot v_{-4}}{v_4 + (J_{E_1 \leftarrow E_1 \text{NaClK}})} \#(94)$$

$$J_{E_1 \rightarrow E_2 \text{NaClKCl}} = \frac{(J_{E_1 \rightarrow E_1 \text{NaClKCl}}) \cdot v_5}{v_5 + (J_{E_1 \leftarrow E_1 \text{NaClKCl}})} \#(95)$$

$$J_{E_1 \leftarrow E_2 \text{NaClKCl}} = \frac{(J_{E_1 \leftarrow E_1 \text{NaClKCl}}) \cdot v_{-5}}{v_5 + (J_{E_1 \leftarrow E_1 \text{NaClKCl}})} \#(96)$$

$$J_{\text{NKCC,Na influx}} = J_{E_1 \rightarrow E_2 \text{ClKCl}} = \frac{(J_{E_1 \rightarrow E_2 \text{NaClKCl}}) \cdot v_6}{v_6 + (J_{E_1 \leftarrow E_2 \text{NaClKCl}})} \#(97)$$

$$J_{\text{NKCC,Na efflux}} = J_{E_1 \leftarrow E_2 \text{ClKCl}} = \frac{(J_{E_1 \leftarrow E_2 \text{NaClKCl}}) \cdot v_{-6}}{v_6 + (J_{E_1 \leftarrow E_2 \text{NaClKCl}})} \#(98)$$

$$v_1 = k_{\text{on}}^{\text{ion}} \cdot [\text{Na}^+]_{\text{o}} \cdot [E_1] \#(99)$$

$$v_{-1} = (k_{\text{on}}^{\text{ion}} / K_{\text{Na}}) \cdot [E_1 \text{Na}] \#(100)$$

$$v_2 = k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_{\text{o}} \cdot [E_1 \text{Na}] \#(101)$$

$$v_{-2} = (k_{\text{on}}^{\text{ion}} / K_{\text{Cl}}) \cdot [E_1 \text{NaCl}] \#(102)$$

$$v_3 = k_{\text{on}}^{\text{ion}} \cdot [\text{K}^+]_{\text{o}} \cdot [\text{E}_1\text{NaCl}] \#(103)$$

$$v_{.3} = (k_{\text{on}}^{\text{ion}}/K_{\text{K}}) \cdot [\text{E}_1\text{NaClK}] \#(104)$$

$$v_4 = k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_{\text{o}} \cdot [\text{E}_1\text{NaClK}] \#(105)$$

$$v_{.4} = (k_{\text{on}}^{\text{ion}}/K_{\text{Cl}}) \cdot [\text{E}_1\text{NaClKCl}] \#(106)$$

$$v_5 = k_{\text{f}}^{\text{full}} \cdot [\text{E}_1\text{NaClKCl}] \#(107)$$

$$v_{.5} = k_{\text{b}}^{\text{full}} \cdot [\text{E}_2\text{NaClKCl}] \#(108)$$

$$v_6 = (k_{\text{on}}^{\text{ion}}/K_{\text{Na}}) \cdot [\text{E}_2\text{NaClKCl}] \#(109)$$

$$v_{.6} = k_{\text{on}}^{\text{ion}} \cdot [\text{Na}^+]_{\text{cld}} \cdot [\text{E}_2\text{ClKCl}] \#(110)$$

$$v_7 = (k_{\text{on}}^{\text{ion}}/K_{\text{Cl}}) \cdot [\text{E}_2\text{ClKCl}] \#(111)$$

$$v_{.7} = k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_{\text{cld}} \cdot [\text{E}_2\text{KCl}] \#(112)$$

$$v_8 = (k_{\text{on}}^{\text{ion}}/K_{\text{K}}) \cdot [\text{E}_2\text{KCl}] \#(113)$$

$$v_{.8} = k_{\text{on}}^{\text{ion}} \cdot [\text{K}^+]_{\text{i}} \cdot [\text{E}_2\text{Cl}] \#(114)$$

$$v_9 = (k_{\text{on}}^{\text{ion}}/K_{\text{Cl}}) \cdot [\text{E}_2\text{Cl}] \#(115)$$

$$v_{.9} = k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_{\text{cld}} \cdot [\text{E}_2] \#(116)$$

$$v_{10} = k_{\text{f}}^{\text{empty}} \cdot [\text{E}_2\text{Cl}] \#(117)$$

$$v_{.10} = k_{\text{b}}^{\text{empty}} \cdot [\text{E}_1] \#(118)$$

$$\begin{bmatrix} a_1 & a_2 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_3 \\ b_1 & b_2 & b_3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & c_1 & c_2 & c_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & d_1 & d_2 & d_3 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & e_1 & e_2 & e_3 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & f_1 & f_2 & f_3 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & g_1 & g_2 & g_3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & h_1 & h_2 & h_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & i_1 & i_2 & i_3 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \cdot \begin{bmatrix} [\text{E}_1] \\ [\text{E}_1\text{Na}] \\ [\text{E}_1\text{NaCl}] \\ [\text{E}_1\text{NaClK}] \\ [\text{E}_1\text{NaClKCl}] \\ [\text{E}_2\text{NaClKCl}] \\ [\text{E}_2\text{ClKCl}] \\ [\text{E}_2\text{KCl}] \\ [\text{E}_2\text{Cl}] \\ [\text{E}_2] \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} \#(119)$$

$$\begin{bmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \\ d_1 & d_2 & d_3 \\ e_1 & e_2 & e_3 \\ f_1 & f_2 & f_3 \\ g_1 & g_2 & g_3 \\ h_1 & h_2 & h_3 \\ i_1 & i_2 & i_3 \end{bmatrix} = \begin{bmatrix} -k_b^{\text{empty}} - k_{\text{on}}^{\text{ion}} \cdot [\text{Na}^+]_o & k_{\text{off}}^{\text{Na}} & k_f^{\text{empty}} \\ k_{\text{on}}^{\text{ion}} \cdot [\text{Na}^+]_o & -k_{\text{off}}^{\text{Na}} - k_{\text{ion}}^{\text{on}} \cdot [\text{Cl}^-]_o & k_{\text{off}}^{\text{Cl}} \\ k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_o & -k_{\text{off}}^{\text{Cl}} - k_{\text{on}}^{\text{ion}} \cdot [\text{K}^+]_o & k_{\text{off}}^{\text{K}} \\ k_{\text{on}}^{\text{ion}} \cdot [\text{K}^+]_o & -k_{\text{off}}^{\text{K}} - k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_o & k_{\text{off}}^{\text{Cl}} \\ k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_o & -k_{\text{off}}^{\text{Cl}} - k_f^{\text{full}} & k_b^{\text{full}} \\ k_f^{\text{full}} & -k_b^{\text{full}} - k_{\text{off}}^{\text{Na}} & k_{\text{on}}^{\text{ion}} \cdot [\text{Na}^+]_{\text{cld}} \\ k_{\text{off}}^{\text{Na}} & -k_{\text{on}}^{\text{ion}} \cdot [\text{Na}^+]_{\text{cld}} - k_{\text{off}}^{\text{Cl}} & k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_{\text{cld}} \\ k_{\text{off}}^{\text{Cl}} & -k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_{\text{cld}} - k_{\text{off}}^{\text{K}} & k_{\text{on}}^{\text{ion}} \cdot [\text{K}^+]_{\text{cld}} \\ k_{\text{off}}^{\text{K}} & -k_{\text{on}}^{\text{ion}} \cdot [\text{K}^+]_{\text{cld}} - k_{\text{off}}^{\text{Cl}} & k_{\text{on}}^{\text{ion}} \cdot [\text{Cl}^-]_{\text{cld}} \end{bmatrix} \quad \#(120)$$

$$\begin{bmatrix} [E_1] \\ [E_1\text{Na}] \\ [E_1\text{NaCl}] \\ [E_1\text{NaClK}] \\ [E_1\text{NaClKCl}] \\ [E_2\text{NaClKCl}] \\ [E_2\text{ClKCl}] \\ [E_2\text{KCl}] \\ [E_2\text{Cl}] \\ [E_2] \end{bmatrix} = \begin{bmatrix} a_1 & a_2 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_3 \\ b_1 & b_2 & b_3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & c_1 & c_2 & c_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & d_1 & d_2 & d_3 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & e_1 & e_2 & e_3 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & f_1 & f_2 & f_3 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & g_1 & g_2 & g_3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & h_1 & h_2 & h_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & i_1 & i_2 & i_3 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix}^{-1} \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} \quad \#(121)$$

$$K_{\text{Na}} = 15.8 \cdot 10^{-3} \text{ L} \cdot \text{mmol}^{-1} \#(122)$$

$$K_{\text{Cl}} = 216.9 \cdot 10^{-3} \text{ L} \cdot \text{mmol}^{-1} \#(123)$$

$$K_{\text{K}} = 9.22 \cdot 10^{-3} \text{ L} \cdot \text{mmol}^{-1} \#(124)$$

$$k_f^{\text{full}} = 1002.0 \cdot 10^{-3} \text{ ms}^{-1} \#(125)$$

$$k_b^{\text{full}} = 2255.0 \cdot 10^{-3} \text{ ms}^{-1} \#(126)$$

$$k_f^{\text{empty}} = 37767 \cdot 10^{-3} \text{ ms}^{-1} \#(127)$$

$$k_b^{\text{empty}} = \frac{K_{\text{Na}} \cdot K_{\text{Cl}} \cdot K_{\text{K}} \cdot K_{\text{Cl}} \cdot k_f^{\text{full}} \cdot k_f^{\text{empty}}}{K_{\text{Na}} \cdot K_{\text{Cl}} \cdot K_{\text{K}} \cdot K_{\text{Cl}} \cdot k_b^{\text{full}}} \text{ ms}^{-1} \#(128)$$

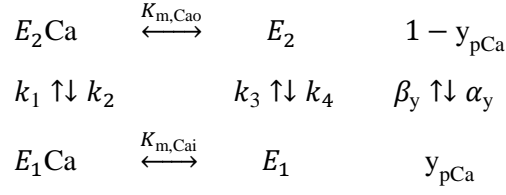
$$k_{\text{on}}^{\text{ion}} = 100 \text{ L} \cdot \text{mmol}^{-1} \#(129)$$

$$k_{\text{off}}^{\text{Na}} = k_{\text{on}}^{\text{ion}} / K_{\text{Na}} \#(130)$$

$$k_{\text{off}}^{\text{K}} = k_{\text{on}}^{\text{ion}} / K_{\text{K}} \#(131)$$

$$k_{\text{off}}^{\text{Cl}} = k_{\text{on}}^{\text{ion}} / K_{\text{Cl}} \#(132)$$

A13. ER Ca²⁺ pump current (I_{pCa})



$$I_{pCa} = P_{pCa} \cdot (k_2 \cdot E_2Ca \cdot (1 - y_{pCa}) - k_1 \cdot E_1Ca \cdot y_{pCa}) \#(133)$$

$$P_{pCa} = 772.8 \#(134)$$

$$k_1 = 0.01 \#(135)$$

$$k_2 = 1 \#(136)$$

$$k_3 = 1 \#(137)$$

$$k_4 = 0.01 \#(138)$$

$$\alpha_y = k_2 \cdot E_2Ca + k_4 \cdot E_2 \#(139)$$

$$\beta_y = k_1 \cdot E_1Ca + k_3 \cdot E_1 \#(140)$$

$$E_1Ca = \left(1 + \frac{K_{m,Cai}}{[Ca^{2+}]_{up}}\right)^{-1} \#(141)$$

$$E_2Ca = \left(1 + \frac{K_{m,Cao}}{[Ca^{2+}]_i}\right)^{-1} \#(142)$$

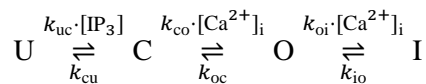
$$E_1 = \left(1 + \frac{[Ca^{2+}]_{up}}{K_{m,Cai}}\right)^{-1} \#(143)$$

$$E_2 = \left(1 + \frac{[Ca^{2+}]_i}{K_{m,Cao}}\right)^{-1} \#(144)$$

$$K_{m,Cao} = 0.00258 \text{ mM} \#(145)$$

$$K_{m,Cai} = 0.08 \text{ mM} \#(146)$$

A14. IP₃-mediated Ca²⁺ release current from the ER (I_{IP3R})



$$I_{IP3R} = P_{IP3R} \cdot ([Ca^{2+}]_{rel} - [Ca^{2+}]_i) \cdot P_{o(IP3R)} \#(147)$$

$$P_{IP3R} = 217.2\#(148)$$

$$P_{O(IP3R)} = O^3\#(149)$$

$$k_{uc} = 400 \text{ mM}^{-1} \cdot \text{ms}^{-1}\#(150)$$

$$k_{cu} = 0.37736 \text{ ms}^{-1}\#(151)$$

$$k_{co} = 20 \text{ mM}^{-1} \cdot \text{ms}^{-1}\#(152)$$

$$k_{oc} = 0.0016468 \text{ ms}^{-1}\#(153)$$

$$k_{oi} = 0.2 \text{ mM}^{-1} \cdot \text{ms}^{-1}\#(154)$$

$$k_{io} = 0.0002098 \text{ ms}^{-1}\#(155)$$

A15. Ca²⁺ leak from ER uptake pool (I_{leak})

$$I_{leak} = P_{leak} \cdot ([Ca^{2+}]_{up} - [Ca^{2+}]_i)\#(156)$$

$$P_{leak} = 1.9125\#(157)$$

A16. Ca²⁺ transfer between ER uptake and release pool (I_{tr})

$$I_{tr} = P_{tr} \cdot ([Ca^{2+}]_{up} - [Ca^{2+}]_{rel})\#(158)$$

$$P_{tr} = 205\#(159)$$

A17. Ca²⁺ concentration in ER uptake pool

$$\frac{d[Ca^{2+}]_{up}}{dt} = \frac{I_{pCa} - I_{tr} - I_{leak}}{2F \cdot Vol_{up}}\#(160)$$

A18. Ca²⁺ concentration in ER release pool

$$[Ca^{2+}]_{rel} = 0.5 \cdot \left(-b_{CSQN} + \sqrt{b_{CSQN}^2 + 4 \cdot c_{CSQN}} \right)\#(161)$$

$$b_{CSQN} = [CSQN]_{total} - [Ca]_{rel} + K_m\#(162)$$

$$c_{CSQN} = K_m \cdot [Ca]_{rel}\#(163)$$

$$K_m = 0.8 \text{ mM}\#(164)$$

$$[CSQN]_{total} = 10 \text{ mM}\#(165)$$

$$\frac{d[Ca]_{rel}}{dt} = \frac{I_{tr} - I_{IP3R}}{2F \cdot Vol_{rel}} \#(166)$$

A19. Ion concentrations in cytosol

$$\frac{d[Na^+]_i}{dt} = \frac{-I_{netNa}}{F \cdot Vol_{cyt}} + D_{Na} \cdot ([Na^+]_{cld} - [Na^+]_i) \#(167)$$

$$I_{netNa} = I_{CaLNa} + I_{NaLCNNa} + 3 \cdot I_{NaK} \#(168)$$

$$D_{Na} = 0.3 \text{ ms}^{-1} \#(169)$$

$$\frac{d[K^+]_i}{dt} = \frac{-I_{netK}}{F \cdot Vol_{cyt}} + D_K \cdot ([K^+]_{cld} - [K^+]_i) \#(170)$$

$$I_{netK} = I_{K1} + I_{CaLK} + I_{NaLCNK} - 2 \cdot I_{NaK} \#(171)$$

$$D_K = 0.3 \text{ ms}^{-1} \#(172)$$

$$\frac{d[Ca]_i}{dt} = \frac{-I_{netCa}}{2F \cdot Vol_{cyt}} + D_{Ca} \cdot ([Ca^{2+}]_{cld} - [Ca^{2+}]_i) \#(173)$$

$$D_{Ca} = 0.2 \text{ ms}^{-1} \#(174)$$

$$I_{netCa} = I_{Orai} + I_{CaLCa} + I_{CaT} + I_{pCa} - I_{IP3R} - I_{leak} \#(175)$$

$$[Ca^{2+}]_i = 0.5 \cdot \left(-b_{CMDN} + \sqrt{b_{CMDN}^2 + 4 \cdot c_{CMDN}} \right) \#(176)$$

$$b_{CMDN} = [CMDN]_{total} - [Ca]_i + K_m \#(177)$$

$$c_{CMDN} = K_m \cdot [Ca]_i \#(178)$$

$$K_m = 0.00238 \text{ mM} \#(179)$$

$$[CMDN]_{total} = 0.0005 \text{ mM} \#(180)$$

$$\frac{d[Cl^-]_i}{dt} = \frac{I_{Clb}}{F \cdot Vol_{cyt}} + D_{Cl} \cdot ([Cl^-]_{cld} - [Cl^-]_i) \#(181)$$

$$D_{Cl} = 0.002 \text{ ms}^{-1} \#(182)$$

A20. Ion concentrations in Cl⁻ microdomain

$$\frac{d[Na^+]_{cld}}{dt} = \frac{-3 \cdot I_{NaCa}}{F \cdot Vol_{cld}} + J_{NKCC,Na} + D_{Na} \cdot ([Na^+]_i - [Na^+]_{cld}) \cdot \frac{Vol_{cyt}}{Vol_{cld}} \#(183)$$

$$\frac{d[K^+]_{\text{cld}}}{dt} = J_{\text{NKCC,K}} + D_K \cdot ([K^+]_i - [K^+]_{\text{cld}}) \cdot \frac{Vol_{\text{cyt}}}{Vol_{\text{cld}}} \#(184)$$

$$\frac{d[Ca]_{\text{cld}}}{dt} = \frac{2 \cdot I_{\text{NaCa}}}{2F \cdot Vol_{\text{cld}}} + D_{\text{Ca}} \cdot ([Ca^{2+}]_i - [Ca^{2+}]_{\text{cld}}) \cdot \frac{Vol_{\text{cyt}}}{Vol_{\text{cld}}} \#(185)$$

$$[Ca^{2+}]_{\text{cld}} = 0.5 \cdot \left(-b_{\text{CMDN}} + \sqrt{b_{\text{CMDN}}^2 + 4 \cdot c_{\text{CMDN}}} \right) \#(186)$$

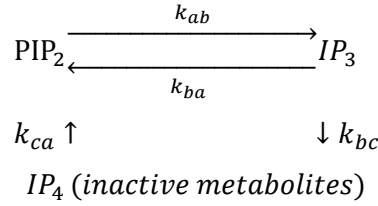
$$b_{\text{CMDN}} = [\text{CMDN}]_{\text{total}} - [Ca]_{\text{cld}} + K_m \#(187)$$

$$c_{\text{CMDN}} = K_m \cdot [Ca]_{\text{cld}} \#(188)$$

$$K_m = 0.00238 \text{ mM} \#(189)$$

$$\frac{d[Cl^-]_{\text{cld}}}{dt} = \frac{I_{\text{ClCa}}}{F \cdot Vol_{\text{cld}}} + J_{\text{NKCC,Cl}} + D_{\text{Cl}} \cdot ([Cl^-]_i - [Cl^-]_{\text{cld}}) \cdot \frac{Vol_{\text{cyt}}}{Vol_{\text{cld}}} \#(190)$$

A21. IP₃ concentration



$$\frac{d[\text{IP}_3]}{dt} = k_{ab} \cdot [\text{PIP}_2] - (k_{ba} + k_{bc}) \cdot [\text{IP}_3] \#(191)$$

$$\frac{d[\text{PIP}_2]}{dt} = k_{ba} \cdot [\text{IP}_3] + k_{ca} \cdot [\text{IP}_4] - k_{ab} \cdot [\text{PIP}_2] \#(192)$$

$$\frac{d[\text{IP}_4]}{dt} = k_{bc} \cdot [\text{IP}_3] - k_{ca} \cdot [\text{IP}_4] \#(193)$$

$$[\text{PI}_{\text{total}}] = [\text{PIP}_2] + [\text{IP}_3] + [\text{IP}_4] = 3.3 \cdot 10^{-3} \#(194)$$

$$k_{ab} = 0.2 \cdot e^{\frac{V+48.5}{18.1}} \cdot \frac{[Ca^{2+}]_i}{[Ca^{2+}]_i + K_{m,\text{Cai(PI)}}} \text{ ms}^{-1} \#(195)$$

$$k_{ba} = 0.5 \cdot e^{-\frac{V+100}{28.5}} \text{ ms}^{-1} \#(196)$$

$$k_{bc} = 0.004 \text{ ms}^{-1} \#(197)$$

$$k_{ca} = 0.0035 \cdot e^{-\frac{V+100}{25.5}} \text{ ms}^{-1} \#(198)$$

$$K_{m,\text{Cai(PI)}} = 0.00001 \text{ mM} \#(199)$$

Supplement tables

Table A1. Glossary

Parameter	Unit	Description
I_{total}	pA	Total current of ion channels, exchanger, and pump
I_{ext}	pA	Externally applied current
I_{CaL}	pA	L-type Ca^{2+} current
$I_{\text{CaL}X}$	pA	ion X component of L-type Ca^{2+} current
I_{CaT}	pA	T-type Ca^{2+} current
I_{K1}	pA	Inward rectifier K^{+} current
I_{NaLCN}	pA	Na^{+} -leak current
$I_{\text{NaLCN}X}$	pA	ion X component of Na^{+} -leak current
I_{ClCa}	pA	Ca^{2+} -activated Cl^{-} current
I_{Clb}	pA	Background Cl^{-} current
I_{Orai}	pA	Current carried by Orai (store-operated Ca^{2+} entry)
I_{NaCa}	pA	$\text{Na}^{+}/\text{Ca}^{2+}$ exchange current
I_{NaK}	pA	$\text{Na}^{+}/\text{K}^{+}$ exchange current
J_{NKCC}	$\text{mM} \cdot \text{ms}^{-1}$	Flux by Na-K-2Cl cotransporter (NKCC1)
$J_{\text{NKCC}X}$	$\text{mM} \cdot \text{ms}^{-1}$	ion X component of J_{NKCC}
I_{pCa}	pA	ER Ca^{2+} pump current
I_{IP3R}	pA	IP_3 -mediated Ca^{2+} release current from the ER
$P_{\text{o(IP3R)}}$	unitless	Probability of IP_3 receptor in conducting state
I_{leak}	pA	Ca^{2+} leak from ER uptake pool
I_{tr}	pA	Ca^{2+} transfer between ER uptake and release pool
α_X	ms^{-1}	Forward rate constant for gating variable X
β_X	ms^{-1}	Backward rate constant for gating variable X
τ_X	ms	Time constant of gating variable X
X_{∞}	unitless	Steady-state value of gating variable X
E_X	mV	Equilibrium potential for ion X
V	mV	Membrane potential
t	ms	Time
CF_X	mM	Constant field for intracellular and extracellular ion X
$\text{CF}_{X,\text{md}}$	mM	Constant field for microdomain and extracellular ion X
G_X	$\text{pA} \cdot \text{mV}^{-1}$	Maximum conductance of channel X
z_X	unitless	Valence of the ion X
$[\text{X}]_i$	mM	Intracellular concentration of ion X
$[\text{X}]_{\text{cld}}$	mM	Concentration of ion X in Cl^{-} microdomain

$[X]_o$	mM	Extracellular concentration of ion X
$[Ca]_{rel}$	mM	Total calcium concentration in ER release pool
$[Ca^{2+}]_{rel}$	mM	Free calcium concentration in ER release pool
$[Ca^{2+}]_{up}$	mM	Free calcium concentration in ER uptake pool

Table A2. General model constants

Parameter	Value	Unit	Description
C_m	25	pF	Membrane capacitance
Vol_{cyt}	715.5	μm^3	Cell volume accessible for ion diffusion
Vol_{up}	21.465	μm^3	Volume of ER uptake pool
Vol_{rel}	7.155	μm^3	Volume of ER release pool
Vol_{cld}	35.775	μm^3	Volume of Cl^- microdomain
F	96.4867	$\text{C}\cdot\text{mmol}^{-1}$	Faraday constant
R	8.314	$\text{C}\cdot\text{mV}\cdot\text{K}^{-1}\cdot\text{mmol}^{-1}$	Gas constant
T	309.15	K	Absolute temperature

Table A3. Initial values (gating variables)

Ion carriers	Parameter	Value
I_{CaL}	m	$8.980\cdot 10^{-8}$
	h	$0.680\cdot 10^{-1}$
I_{CaT}	d	$4.429\cdot 10^{-4}$
	f	$7.262\cdot 10^{-1}$
I_{ClCa}	O_{ClCa}	$3.249\cdot 10^{-3}$
I_{NaCa}	y_{NaCa}	$9.798\cdot 10^{-1}$
I_{NaK}	y_{NaK}	$5.983\cdot 10^{-1}$
I_{pCa}	y_{pCa}	$4.226\cdot 10^{-1}$
I_{IP3R}	$P_{o(IP3R)}$	$7.009\cdot 10^{-4}$

Table A4. Initial values (membrane potential and concentrations)

Parameter	Value	Unit
V	-72.332	mV
$[\text{Na}^+]_o$	140.0	mM
$[\text{Na}^+]_i$	6.321	mM
$[\text{Na}^+]_{\text{cld}}$	6.321	mM
$[\text{K}^+]_o$	5.4	mM
$[\text{K}^+]_i$	135.6	mM
$[\text{K}^+]_{\text{cld}}$	135.6	mM
$[\text{Cl}^-]_o$	140	mM
$[\text{Cl}^-]_i$	87.290	mM
$[\text{Cl}^-]_{\text{cld}}$	87.464	mM
$[\text{Ca}^{2+}]_o$	1.8	mM
$[\text{Ca}]_i$	$1.071 \cdot 10^{-4}$	mM
$[\text{Ca}^{2+}]_i$	$8.913 \cdot 10^{-5}$	mM
$[\text{Ca}]_{\text{cld}}$	$1.717 \cdot 10^{-4}$	mM
$[\text{Ca}^{2+}]_{\text{cld}}$	$1.433 \cdot 10^{-4}$	mM
$[\text{Ca}]_{\text{rel}}$	8.065	mM
$[\text{Ca}^{2+}]_{\text{rel}}$	1.517	mM
$[\text{Ca}^{2+}]_{\text{up}}$	1.783	mM
$[E_1]$	$1.579 \cdot 10^{-3}$	mM
$[E_1\text{Na}]$	$3.489 \cdot 10^{-3}$	mM
$[E_1\text{NaCl}]$	$1.059 \cdot 10^{-1}$	mM
$[E_1\text{NaClK}]$	$5.271 \cdot 10^{-3}$	mM
$[E_1\text{NaClKCl}]$	$1.600 \cdot 10^{-1}$	mM
$[E_2\text{NaClKCl}]$	$6.039 \cdot 10^{-2}$	mM
$[E_2\text{ClKCl}]$	$6.046 \cdot 10^{-1}$	mM
$[E_2\text{KCl}]$	$3.186 \cdot 10^{-2}$	mM
$[E_2\text{Cl}]$	$2.548 \cdot 10^{-2}$	mM
$[E_2]$	$1.340 \cdot 10^{-3}$	mM
$[\text{IP}_3]$	$3.396 \cdot 10^{-4}$	mM
$[\text{PIP}_2]$	$1.364 \cdot 10^{-3}$	mM