

Table S1. List of parameters used in the model, related to **Figure 2A**.

Parameter	Meaning	Value
g_L	Leak conductance	0.0025 1/s
V_L	Rest potential	-90 mV
g_{C1}	Initial cation channel conductance	0.0125 1/s
g_{C2}	Final cation channel conductance	0.003125 1/s
δ_C	Cation channel decay rate	0.025 1/s
V_0	Cation Nernst potential when $C = C_e$	1 mV
C_e	Extracellular cation concentration	2 mM
α_{in}	Import rate	0.075 1/s
α_{out}	Export rate	0.075 1/s
F	Conductance coefficient	0.0067 mM/mV
β_T	ThT input rate	0.01 mM/s
δ_{hyp}	ThT export rate under hyperpolarization	0.00025 1/s
δ_{dep}	ThT export rate under depolarization	0.005 1/s
V_S	Steepness of the ThT response function	0.1 mV

Table S2. Proteins enriched uniquely in the L22* mutant, related to **Figure 5**.

Proteins marked in bold are ion transporters. The table lists a description of overexpressed proteins and its expression level in wild-type in the presence of spectinomycin (Spec), Δ yhdP, Δ L34, and L22* mutant normalized to wild-type (WT) expression level.

Protein	Description	WT	Spec	ΔyhdP	ΔL34	L22*
YodF	Uncharacterized symporter, similar to amino acid permease	1	0.83	0.69	0.87	1.94
MgtE	Magnesium transporter MgtE	1	0.94	0.57	0.99	1.87
YybJ	Uncharacterized ABC transporter ATP-binding protein	1	0.91	1.04	0.92	1.77
YoaB	2-oxoglutarate permease (proton symporter)	1	0.77	0.73	0.87	1.68
YhdP	Magnesium efflux pump	1	0.93	0.27	1.09	1.57
YbeC	Probable amino acid-proton symporter	1	1.06	0.72	0.97	1.56
NtdC	Glucose-6-phosphate 3-dehydrogenase	1	0.68	0.51	0.67	6.25
NtdA	3-oxo-glucose-6-phosphate:glutamate aminotransferase	1	0.69	0.55	0.66	5.02
NtdB	Kanosamine-6-phosphate phosphatase	1	0.70	0.57	0.62	4.90
YqjL	General stress protein, putative hydrolase involved in oxidative stress resistance	1	0.92	1.09	1.00	2.31
YdiP	Similar to DNA-3-methyladenine glycosidase II	1	0.94	0.93	0.87	1.90
EpsN	UDP-2,6-dideoxy 2-acetamido 4-keto glucose aminotransferase	1	0.66	0.83	0.71	1.75
BioD	ATP-dependent dethiobiotin synthetase	1	0.87	1.00	0.94	1.71
YokE	SPBc2 prophage-derived uncharacterized protein	1	1.07	1.09	1.06	1.68
MtnK	Methylthioribose kinase	1	0.69	0.96	0.96	1.65
PxpC	5-oxoprolinase subunit C	1	1.05	0.98	0.87	1.65
YvyE	IMPACT family member	1	1.02	0.97	1.07	1.57
KipR	HTH-type transcriptional regulator KipR	1	0.91	0.85	0.71	1.56
RapG	Response regulator aspartate phosphatase G	1	0.99	0.97	1.05	1.54
MtnA	Methylthioribose-1-phosphate isomerase	1	0.95	1.03	0.90	1.51

Table S3. Summary values of parameters measured at the population level for the conditions listed, related to **Figure 7**.

The table lists mean ThT level with its standard deviation (ThT std), hyperpolarized cell fraction and its confidence interval (CI), and number of analyzed cells.

Condition	ThT mean (a.u.)	ThT std	Hyperpolarized cell fraction	CI	Number of cells
WT	211.39	20.15	3.68	0.03	1,459,602
WT Spec	229.56	42.41	28.54	0.07	1,404,264
WT Kan	219.89	34.24	15.76	0.06	1,298,188
WT Cm	219.44	41.03	23.41	0.07	1,415,308
WT+20 mM Mg ²⁺	191.36	31.98	2.94	0.04	781,747
L22*	197.35	15.35	0.29	0.01	896,718
L22* Spec	197.6	17.05	0.36	0.01	1,279,746
ΔL34	237.09	47.30	35.22	0.07	1,741,790
ΔL34+100 mM Mg ²⁺	184.42	21.53	2.3	0.03	1,249,549

Table S4. Summary values of parameters measured at the single-cell level for the conditions listed, related to **Figure 7**.

The table lists the elongation rate with its standard error (SE), mean number of surviving generations with its standard error (SE), and number of analyzed cells.

Condition	Elongation rate (h⁻¹)	SE	Surviving generations	SE	Number of cells
WT	0.19	0.01	2.85	0.18	102
WT Spec	0.06	0.01	1.22	0.08	174
WT Kan	0.19	0.01	1.56	0.12	134
WT Cm	0.04	0.01	1.31	0.13	35
WT+20 mM Mg ²⁺	0.19	0.02	3.58	0.10	50
L22*	0.26	0.01	4.02	0.31	51
L22* Spec	0.17	0.01	2.52	0.14	100
ΔL34	0.09	0.02	1.29	0.28	35
ΔL34+100 mM Mg ²⁺	0.23	0.02	2.56	0.34	35